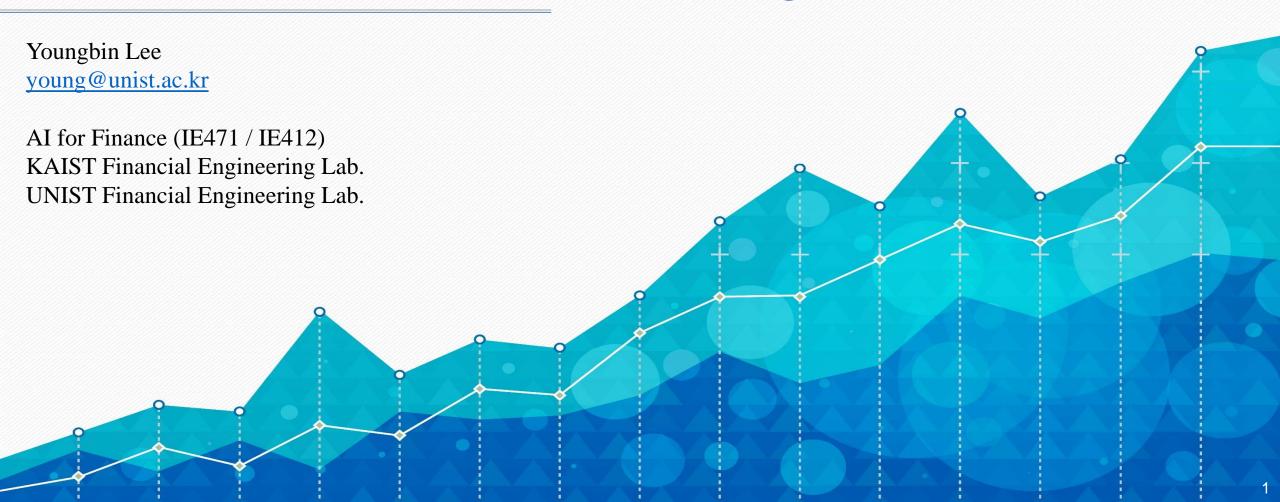


## Hands-on Practice on Financial AI Session

## **Session 2**

## Within Stock Classification via Clustering



## Contents

#### ■ 1. Introduction

- A. Problem statement
- B. Impact of asset classification schemes

### • 2. AI model

- A. Clustering
- B. k-means clustering
- C. Performance evaluation

### • 3. Implementation

- A. Data
- B-1. k-means with financial statements
- B-2. k-means with style factors
- B-3. Traditional method (Style classification)
- C. Analysis

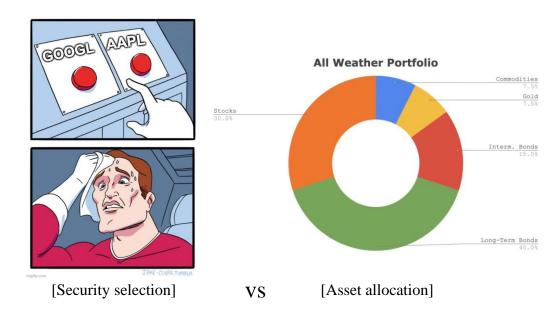
#### 4. Conclusion

- A. Summary
- B. Homework

## Introduction

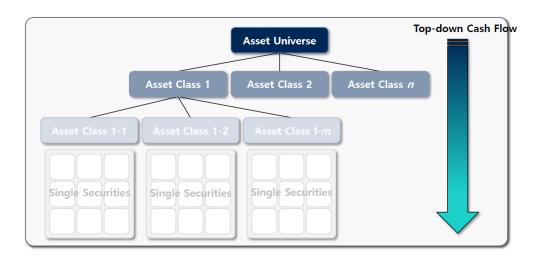
## Α

#### **Problem statement**





- Asset allocation decides how the investment should be distributed
  - Equities, bonds, cash, commodities, etc.
- Asset allocation decisions explain a majority of investment return variabilities [1]

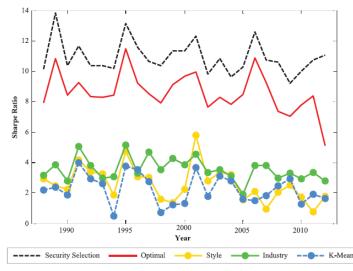


### ■ **How to define asset classes?** (for single-stock universe)

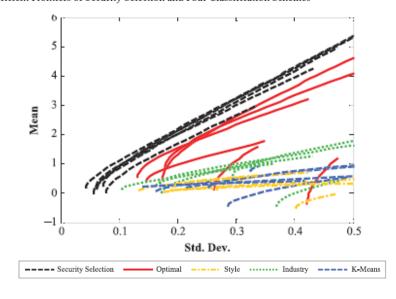
- Traditional methods
  - Style classification: large-cap, small-cap, growth, value, ...
  - Industry classification: Health care, Technology, Financials, ...
  - Market classification: US stocks, developed market stocks, emerging market stocks, ...
- AI methods (we will do)
  - Clustering

### Impact of asset classification schemes

E X H I B I T  $\;\;2$  Sharpe Ratios of Security Selection and Four Classification Schemes



E X H I B I T 3
Efficient Frontiers of Security Selection and Four Classification Schemes



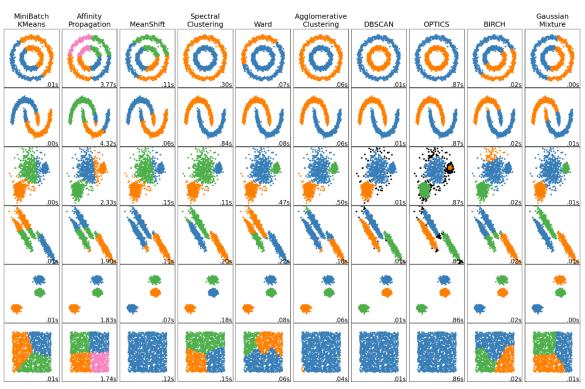
### Asset classification and investment performance

- Investment performance is significantly affected by the employed asset classification scheme [2]
  - In exhibits, each line represents different classification scheme
  - A poor classification scheme choice can result in poor portfolio return
- Assets in different classes are expected to have different characteristics in market (e.g., return, risk)



## Al model

## **A** Clustering



[A comparison of the clustering algorithms in scikit-learn]

### Unsupervised learning

- The goal is to understand data itself by learning patterns from unlabeled data
  - E.g., Dimensionality reduction, Clustering

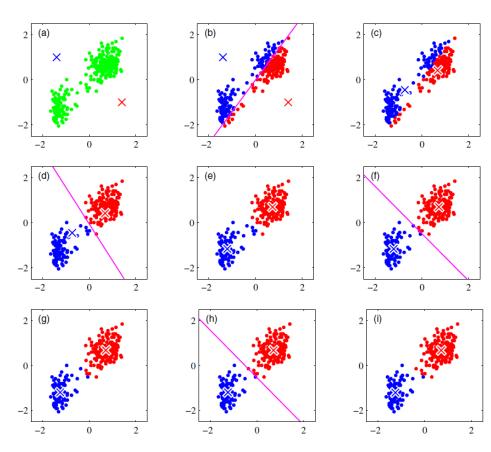
### Clustering

- The organization of unlabeled data into similarity groups called clusters
  - A cluster is a collection of data items which are similar between them, and dissimilar to data items in other clusters

#### Methods

- Conventional algorithms
  - k-means (we will do), DBSCAN, Gaussian Mixtures, Spectral clustering, ...
- Deep clustering
  - Usually combines representation learning with deep neural networks

### k-means clustering



[Illustration of the k-means algorithm]

## Algorithm

- Initialize k centroids
  - k is a user-defined parameter
- Iterate until convergence
  - Step 1. Assign each data point to its closest centroid
  - Step 2. Move each centroid to the center of data points assigned to it

#### k-means clustering

The goal is to find a set of vectors  $\{\mu_k\}$ , the centers of the clusters k = 1, ..., K, such that the cost function J is minimum.

*J*: the sum of squares of the distances of each data point to its closest vector  $\mu_k$ 

$$J = \sum_{n=1}^{N} \sum_{k=1}^{K} r_{nk} ||x_n - \mu_k||^2$$

where responsibilities  $r_{nk} \in \{0,1\}$  are binary indicator variables describing which of the K clusters the data point  $x_n$  is assigned to.

#### Step 1. Assign each data point to its closest centroid

This can be done by computing responsibilities.

$$r_{nk} \begin{cases} 1 & if \ k = argmin_j \left| \left| x_n - \mu_j \right| \right|^2 \\ 0 & otherwise \end{cases}$$

#### Step 2. Move each centroid to the center of data points assigned to it

This can be done by computing new sample means for every cluster.

$$\boldsymbol{\mu}_k = \frac{\sum_n r_{nk} x_n}{\sum_n r_{nk}}$$

### The two steps are repeated in turn until convergence

 Because each step reduces the value of the cost function J, convergence of the algorithm is assured

### **Performance evaluation**

### Silhouette coefficient

- A measure of cohesion compared to separation
- Range: [-1, 1]
  - Higher scores indicate dense and well separated clusters

For data point i in cluster  $C_I$ , the Silhouette coefficient

$$s_i = \frac{b_i - a_i}{\max(a_i, b_i)}$$

where

 $a_i$  is the mean distance between a sample i and all other points in the same cluster (cohesion)

$$a_i = \frac{1}{|C_I| - 1} \sum_{j \in C_I, i \neq j} d(i, j)$$

 $b_i$  is the mean distance between a sample i and all other points in the next nearest cluster (separation)

$$b_i = \min_{J \neq I} \frac{1}{|C_J|} \sum_{j \in C_J} d(i, j)$$

#### Davies-Bouldin index

- A measure of average similarity
- Lowest possible score: 0
  - Lower scores indicate better separated clusters

For cluster  $C_i$  for i = 1, ..., k, the **Davies-Bouldin index** 

$$DB = \frac{1}{k} \sum_{i=1}^{k} \max_{i \neq j} R_{ij}$$

where

 $R_{ij}$  is the similarity (the ratio of within-cluster distances to between-cluster distances)

$$R_{ij} = \frac{s_i + s_j}{d_{ij}}$$

 $s_i$  is the average distance between each point of cluster i and the centroid of that cluster

 $d_{ij}$  is the distance between cluster centroids i and j







WRDS hosts 350+TB of data, partnering with global vendors

Compustat Fundamentals provides standardized North American and global financial statement and market data

### financial\_statements.csv

- Quarterly financial statement of 2094 US stocks
- Date
  - Dec 31 2020 or Jan 4 2021

	datadate_x	tic	name	gsector	market_cap	PBR	PER	EPS	ROE	net_income	net_cash_flow	volatility
C	20210104	PNW	PINNACLE WEST CAPITAL CORP	utilities	8.905297e+09	1.099	18.112	5.63	0.082	550.559	49.685	0.016509
1	20210104	ABT	ABBOTT LABORATORIES	health_care	1.933824e+11	6.183	96.174	1.89	0.107	4473.000	2907.000	0.013776
2	20210104	ALK	ALASKA AIR GROUP INC	industrial	6.089215e+09	1.627	10.233	-5.64	-0.145	-1324.000	1154.000	0.035188
3	20210104	MATX	MATSON INC	industrial	2.442149e+09	1.944	20.084	2.86	0.107	193.100	-8.700	0.030216
4	20210104	Υ	ALLEGHANY CORP	financial	8.430382e+09	1.005	26.306	-1.75	-0.003	101.754	-411.621	0.021499
				***	***							
2089	20210104	NES	NUVERRA ENVIRONMENTAL SOLUTN	energy	3.280576e+07	0.243	-0.513	-4.73	-0.436	-44.143	9.990	0.062768
2090	20210104	MHH	MASTECH DIGITAL INC	industrial	1.752520e+08	3.142	32.530	0.91	0.206	9.861	4.883	0.036276
2091	20210104	ISDR	ISSUER DIRECT CORP	IT	6.473660e+07	2.384	58.476	0.50	0.070	2.106	3.785	0.031666
2092	20210104	AMPE	AMPIO PHARMACEUTICALS INC	health_care	2.738814e+08	27.435	-20.666	-0.07	-2.600	-15.894	10.814	0.100264
2093	20210104	ENSV	ENSERVCO CORP	energy	9.617410e+06	3.202	-1.591	-0.60	-3.031	-2.509	0.804	0.350034

### security\_daily.csv

- Daily close price of US stocks
- Period
  - Jan 4 2021 ~ Jul 4 2021

tadate tic conm proce	tic	datadate	
10104 AIR AAR CORP 34.3600	AIR	20210104	254
10105 AIR AAR CORP 36.0100	AIR	20210105	255
10106 AIR AAR CORP 38.4500	AIR	20210106	256
10107 AIR AAR CORP 38.6200	AIR	20210107	257
10108 AIR AAR CORP 37.9500	AIR	20210108	258
11227 DTRUY DAIMLER TRUCK HOLDING AG 18.2717	DTRUY	20211227	9692678
11228 DTRUY DAIMLER TRUCK HOLDING AG 18.1591	DTRUY	20211228	9692679
11229 DTRUY DAIMLER TRUCK HOLDING AG 18.4389	DTRUY	20211229	9692680
11230 DTRUY DAIMLER TRUCK HOLDING AG 18.2940	DTRUY	20211230	9692681
11231 DTRUY DAIMLER TRUCK HOLDING AG 18.3600	DTRUY	20211231	9692682

5078928 rows × 4 columns

2094 rows × 12 columns



#### k-means clustering with financial statements

	datadate_x	tic	name	gsector	market_cap	PBR	PER	EPS	ROE	net_income	net_cash_flow	volatility
0	20210104	PNW	PINNACLE WEST CAPITAL CORP	utilities	8.905297e+09	1.099	18.112	5.63	0.082	550.559	49.685	0.016509
1	20210104	ABT	ABBOTT LABORATORIES	health_care	1.933824e+11	6.183	96.174	1.89	0.107	4473.000	2907.000	0.013776
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3	20210104	MATX	MATSON INC	industrial	2.442149e+09	1.944	20.084	2.86	0.107	193.100	-8.700	0.030216
4	20210104	Υ	ALLEGHANY CORP	financial	8.430382e+09	1.005	26.306	-1.75	-0.003	101.754	-411.621	0.021499
			***									
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2090	20210104	МНН	MASTECH DIGITAL INC	industrial	1.752520e+08	3.142	32.530	0.91	0.206	9.861	4.883	0.036276
2091	20210104	ISDR	ISSUER DIRECT CORP	IT	6.473660e+07	2.384	58.476	0.50	0.070	2.106	3.785	0.031666
2092	20210104	AMPE	AMPIO PHARMACEUTICALS INC	health_care	2.738814e+08	27.435	-20.666	-0.07	-2.600	-15.894	10.814	0.100264
2093	20210104	ENSV	ENSERVCO CORP	energy	9.617410e+06	3.202	-1.591	-0.60	-3.031	-2.509	0.804	0.350034

2094 rows × 12 columns

## Identifying information

- Tic: Ticker symbol

- Name: Company name

gsector: GIC sectors

Global Industry Classification Standard

#### Cluster features

- Market cap: Total dollar market value of a company's outstanding shares of stock (size)
- **PER**: Price Earnings Ratio (value)
- **EPS**: Earnings Per Share
- **ROE**: Return on Equity (profitability)
- Net income: Revenues minus expenses, interest, and taxes
- Net cash flow: The sum of a company's cash inflows and outflows over a period of time
- Volatility: Standard deviation of daily log returns over the last 3 months



#### k-means clustering with financial statements



### Removing outliers

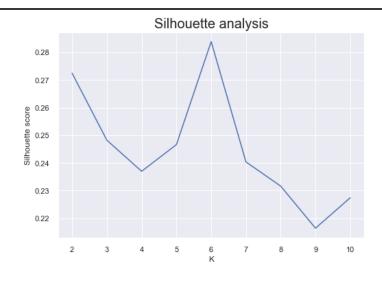
- EPS, net income, PER, ROE, net cash flow
  - 3% from each of both tails are removed to reduce the effect of outliers
  - Because even a small amount of outliers can significantly distort the clustering results

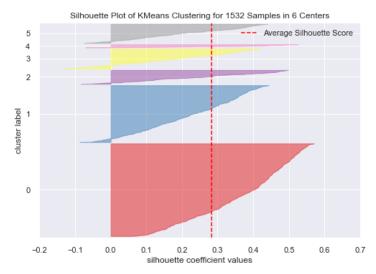
### Scaling features

- Market cap
  - A logarithmic transformation (base 10) is applied to make small values and large values closer
  - Because the distribution is highly skewed towards large values
- All features
  - A standard scaling is applied to make every feature have the same scales
  - Because you will measure Euclidean distance for k-means clustering

## B-1

### k-means clustering with financial statements





### Silhouette analysis

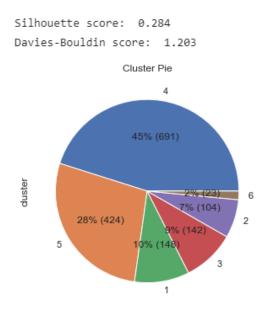
- The optimal number of clusters is determined to be 6
- Because the score is highest with k=6

## Silhouette plot

- Silhouette scores for each data point are visualized
- Cluster size is visualized from the thickness of the plot

## B-1

#### k-means clustering with financial statements

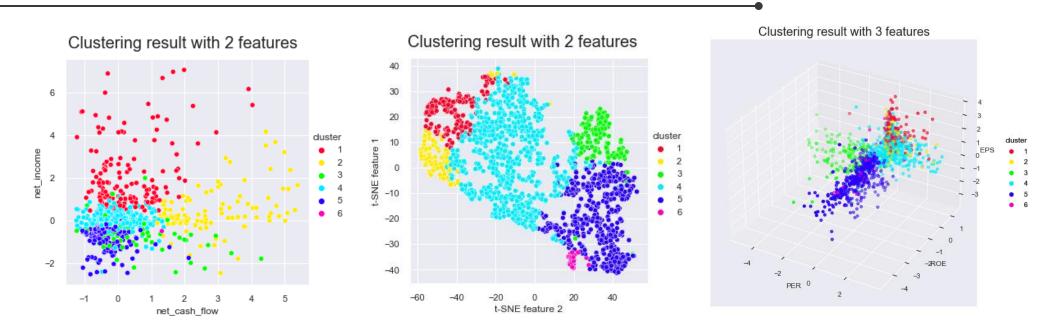


#### Run k-means

- Fitting scaled data into k-means model with k=6
  - The cluster size is visualized from pie chart
- The scores indicate goodness of fit based on similarity
  - However, they do not necessarily represent the actual performance of clustering as we are dealing with unlabeled data
  - The distributions of each feature will be investigated in later slides

B-1

#### k-means clustering with financial statements



## Clustering results

- Clustering was done with 7 features, but data points in each cluster are visualized with 2 or 3 features in standardized scale
- t-SNE (t-distributed Stochastic Neighbor Embedding) is used to visualize high-dimensional data
  - A dimensionality reduction technique that embeds the points from a higher dimension to a lower dimension with an objective of optimizing local distances (trying to preserve the neighborhood of that point)
    - > Unlike PCA, it is a non-linear method

### **B-2** k-means clustering with style factors

	datadate_x	tic	name	gsector	market_cap	PBR	PER	EPS	ROE	net_income	net_cash_flow	volatility
0	20210104	PNW	PINNACLE WEST CAPITAL CORP	utilities	8.905297e+09	1.099	18.112	5.63	0.082	550.559	49.685	0.016509
1	20210104	ABT	ABBOTT LABORATORIES	health_care	1.933824e+11	6.183	96.174	1.89	0.107	4473.000	2907.000	0.013776
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2094 rows × 12 columns

### Identifying information

Tic: Ticker symbol

- Name: Company name

gsector: GIC sectors

• Global Industry Classification Standard

#### Cluster features

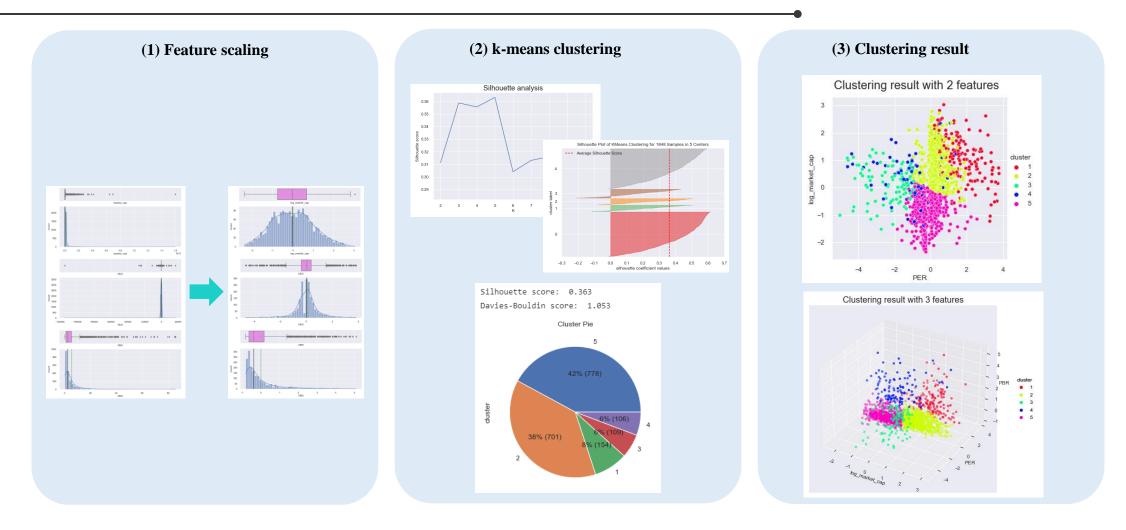
Market cap: Total dollar market value of a company's outstanding shares of stock

- PBR: Price-to-Book Ratio

- PER: Price Earnings Ratio

B-2

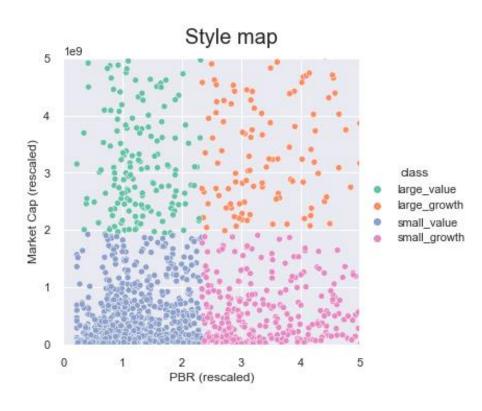
### k-means clustering with style factors



• Same process as B-1, with different number of clusters (k=5)

B-3

## **Traditional method (Style classification)**



### Style classification

- Size (Market cap)
  - Stocks in the top 40% were classified as large
  - Stocks in the bottom 60% were classified as small
- Value (PBR)
  - Stocks in the upper half were classified as value
  - Stocks in the lower half were classified as growth
- There are 4 classes
  - Large-Value, Large-Growth, Small-Value, Small-Growth



### **Analysis**

#### **B-1.** k-means with financial statements

	cluster_1	cluster_2	cluster_3	cluster_4	cluster_5	cluster_6
1	INTUITIVE SURGICAL INC	FIDELITY NATIONAL INFO SVCS	PINTEREST INC	DOMINION ENERGY INC	BRIDGEBIO PHARMA INC	ARCTURUS THERAPETCS HOLD INC
2	FISERV INC	KRAFT HEINZ CO	SEAGEN INC	ZIMMER BIOMET HOLDINGS INC	INVITAE CORP	ASSEMBLY BIOSCIENCES INC
3	DUKE ENERGY CORP	MARRIOTT INTL INC	ZENDESK INC	WILLIAMS COS INC	NOVAVAX INC	CHINA AUTOMOTIVE SYSTEMS INC
4	GLOBAL PAYMENTS INC	IQVIA HOLDINGS INC	AVALARA INC	ROLLINS INC	TG THERAPEUTICS INC	HEAT BIOLOGICS INC
5	NORFOLK SOUTHERN CORP	KINDER MORGAN INC	SAREPTA THERAPEUTICS INC	AES CORP (THE)	PTC THERAPEUTICS INC	WESTWATER RESOURCES INC

#### **B-2.** k-means with style factors

	cluster_1	cluster_2	cluster_3	cluster_4	cluster_5
1	META PLATFORMS INC	JPMORGAN CHASE & CO	EXACT SCIENCES CORP	LILLY (ELI) & CO	MATADOR RESOURCES CO
2	JOHNSON & JOHNSON	UNITEDHEALTH GROUP INC	BIOMARIN PHARMACEUTICAL INC	TEXAS INSTRUMENTS INC	SMILEDIRECTCLUB INC
3	PAYPAL HOLDINGS INC	BANK OF AMERICA CORP	LIVE NATION ENTERTAINMENT	LOCKHEED MARTIN CORP	MACROGENICS INC
4	COCA-COLA CO	VERIZON COMMUNICATIONS INC	GUARDANT HEALTH INC	ILLINOIS TOOL WORKS	COHERUS BIOSCIENCES INC
5	MERCK & CO	COMCAST CORP	HOWMET AEROSPACE INC	MODERNA INC	MAGNOLIA OIL & GAS CORP

#### **B-3.** Traditional method (Style classification)

	cluster_large_value	cluster_large_growth	cluster_small_value	cluster_small_growth
1	JPMORGAN CHASE & CO	AMAZON.COM INC	FULTON FINANCIAL CORP	SOUTHWESTERN ENERGY CO
2	BANK OF AMERICA CORP	TESLA INC	PDC ENERGY INC	MEDNAX INC
3	COMCAST CORP	META PLATFORMS INC	ALLEGHENY TECHNOLOGIES INC	PRECIGEN INC
4	AT&T INC	JOHNSON & JOHNSON	FIRST MERCHANTS CORP	NGM BIOPHARMACEUTICAL INC
5	EXXON MOBIL CORP	MASTERCARD INC	WESBANCO INC	TPI COMPOSITES INC



## 1. Do they have distinct characteristics?

Distribution of financial features

### 2. Do they move differently in the market?

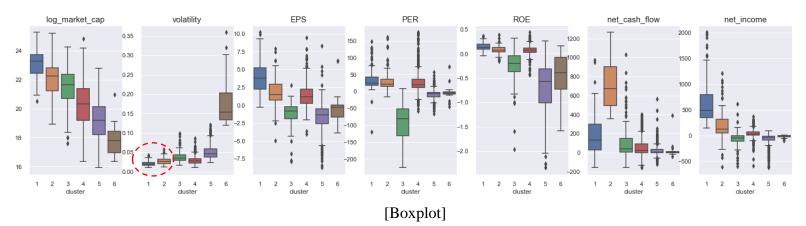
- Return correlations
- Return and risk characteristics





## Analysis

#### **B-1.** k-means with financial statements



	log_market_cap	volatility	EPS	PER	ROE	net_cash_flow	net_income
cluster							
1	23.143487	0.020301	4.041689	33.972872	0.149885	176.990230 <b>(</b>	655.284770
2	22.059823	0.026975	1.913433	31.048798	0.077894	717.509567	193.128269
3	21.408351	0.038003	-1.224718	-91.481338	-0.248669	113.574099	-71.282655
4	20.270595	0.029023	1.375094	28.247340	0.073624	57.531339	39.433779
5	19.140726	0.050010	-1.826705	-9.228061	-0.707828	21.716849	-79.047538
6	17.812397	0.182299	-0.408696	-4.603261	-0.472870	20.841652	-18.697435

[Mean table]

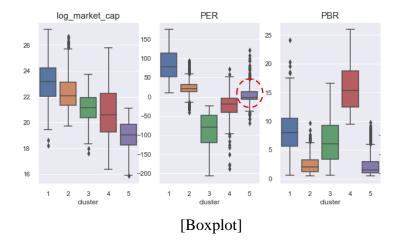
#### Distribution of financial features

- Clusters with higher market cap tend to have lower volatility
- Stocks in cluster 1 have highest mean value of net income
- Financial properties are similar within clusters, and distinct across clusters



### Analysis

#### **B-2.** k-means with style factors



	log_market_cap	PER	PBR
cluster			
1	23.124188	84.869597	8.337851
2	22.323108	23.294966	2.457762
3	21.105701	-85.737743	6.281294
4	20.724720	-28.471811(	15.999170
5	18.978872	3.100269	2.243172

### [Mean table]

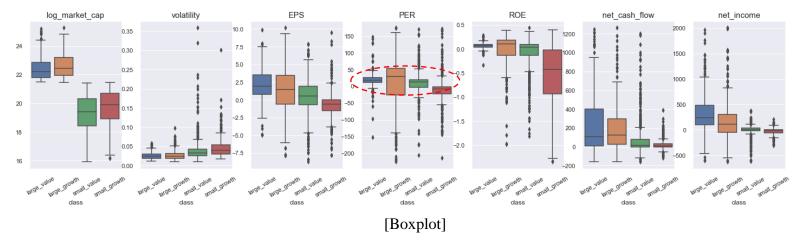
### Distribution of financial features

- Stocks in cluster 5 tend to have values of PER around zero
- Stocks in cluster 4 have highest mean value of PBR
- Financial properties are similar within clusters, and distinct across clusters

## С

### **Analysis**

#### **B-3.** Traditional method (Style classification)



	log_market_cap	volatility	EPS	PER	ROE	net_cash_flow	net_income
class							
large_growth	22.595455	0.026831	1.363923	11.311698	-0.022923	199.396682	177.956045
large_value	22.448989	0.025575	2.124186	20.730762	0.060035	259.638401	349.697320
small_growth	19.698659	0.046631	-0.642689	-7.868692	-0.542556	22.903694	-33.232794
small_value	19.297846	0.038938	0.394488	10.496966	-0.079792	77.808894	-3.053063

[Mean table]

#### Distribution of financial features

- Variations are higher
- Large stocks exhibit similar values of features to each other, and so do small stocks
- Financial properties are dissimilar within clusters, and indistinguishable across clusters



#### Average correlations within and between clusters



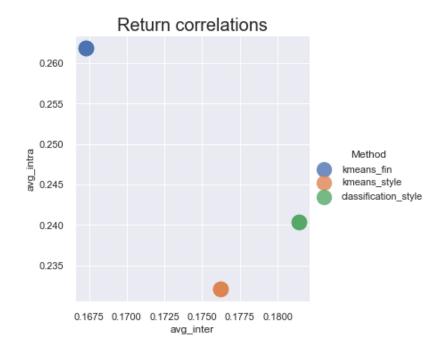
[B-1. k-means with financial statements]



[B-2. k-means with style factors]



[B-3. Traditional method (Style classification)]



- avg\_intra: Average correlations of daily log return within blusters
- avg\_inter: Average correlations of daily log return between clusters

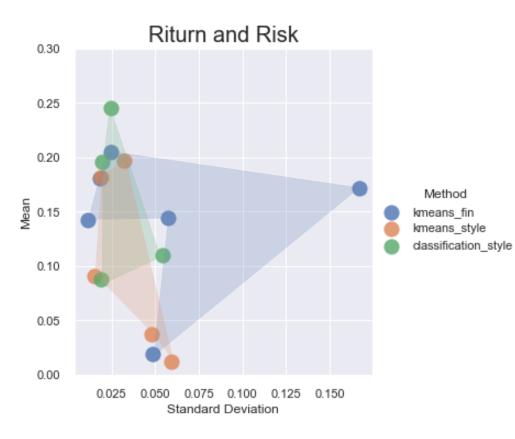
#### Return correlations

- We expect assets in the same cluster would move similarly, and assets in different clusters would move differently
- K-means clustering with financial statements (blue) have the most desired correlations between stocks
  - Higher intra-correlations and lower inter-correlations

Method

## **Implementation**

Analysis



- Each point stands for an asset class from three different methods
- Y-axis: Mean of average daily log returns in each class
- X-axis: Standard Deviation of average daily log returns in each class

### Return and Risk

- We expect assets in different clusters would have distinct return and risk characteristics (for the purpose of diversification)
- K-means clustering with financial statements (blue) have the most desired return and risk characteristics
  - Clusters have diverse mean and standard deviation of returns

## Conclusion

## A Summary

- A key determinant of portfolio returns is asset allocation, which requires proper asset classification
  - In this session, we focus on within-stock classification
- AI models allow you to classify assets in a different way than traditional methods
  - Existing asset classification methods include style-based and industry-based
- K-means clustering is one of the simplest and popular unsupervised machine learning algorithms
  - It is implemented by iterating two steps
    - Step 1. Assigning each data point to its closest centroid
    - Step 2. Updating centroids to the center of data points assigned to it
  - When clustering data without labels, we can evaluate performance with metrics such as Silhouette coefficient and Davies-Bouldin index
- As a result of **classifying stocks via clustering** with financial properties, stocks are grouped differently from the existing method
  - Financial features are distinct across classes
  - Stocks in different classes have different return and risk characteristics

## Conclusion

**B** Homework

"Implement stock classification via clustering on your own"

## Main

- K-means clustering
  - with your own number of clusters (k)

## Extension

- Another clustering method
  - E.g., DBSCAN, Gaussian mixtures, Spectral clustering, ...



# Thank You.