

# Graph Neural Network Simulator Assignment

CE397 and CSE393: Scientific Machine Learning

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## 1 Implementing Loss Functions for Particle Simulation

The notebook `gnn.ipynb` implements a Graph Neural Network-based Simulator (GNS) to predict the motion of particles in a "WaterDrop" simulation. The model is trained to predict the normalized acceleration of each particle. The standard training loop uses a simple Mean Squared Error loss on this predicted acceleration.

In this assignment, you will implement and compare two different loss functions: one based on the predicted acceleration (the default) and a new one based on the predicted position after one step of simulation.

### a) Acceleration-based Loss (Default)

The default training procedure in the `train` function (cell 63) uses `torch.nn.MSELoss()`. This computes the mean squared error between the model's direct output (predicted normalized acceleration,  $\mathbf{y}_{\text{pred}}$ ) and the ground truth normalized acceleration ( $\mathbf{y}_{\text{true}}$ , available as `data.y`).

Write the mathematical formula for this loss,  $\mathcal{L}_{\text{accel}}$ , using  $N$  for the number of particles in the batch.

### b) Position-based Loss (New Implementation)

A loss function based on the predicted particle *position* at the next timestep,  $\mathbf{p}^{t+1}$ , may provide a more physically relevant training signal. To implement this, you must modify data processing and implement a position loss.

### c) Train and Compare

Modify the `train` function to use your new position-based loss function,  $\mathcal{L}_{\text{pos}}$ . Run the training for at least one epoch (`params["epoch"] = 1`) and report the final "One Step MSE" from the evaluation. How does this value compare to the "One Step MSE" obtained when training with the original  $\mathcal{L}_{\text{accel}}$ ?

(Note: The `oneStepMSE` function itself calculates MSE on acceleration, so you may need to either adapt it or compare the `eval_loss` values directly, ensuring your new loss function is also used during evaluation.)