

# AI Classification

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# Why I dislike ML?

## Input parameters

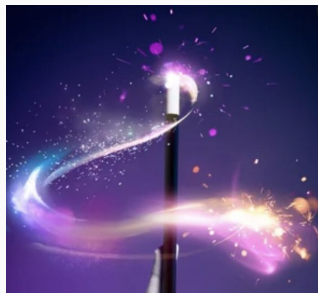
density = 1800 kg/m<sup>3</sup>

$n = 0.4$

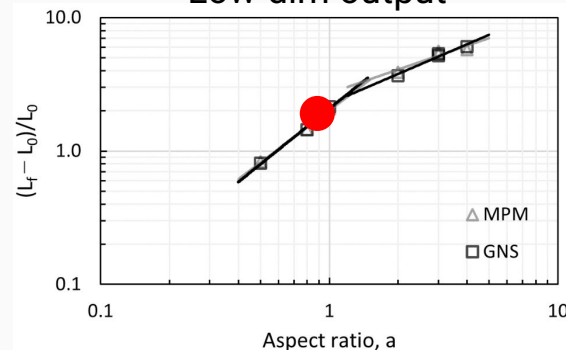
Aspect ratio = 0.8

Slope = 2.5°

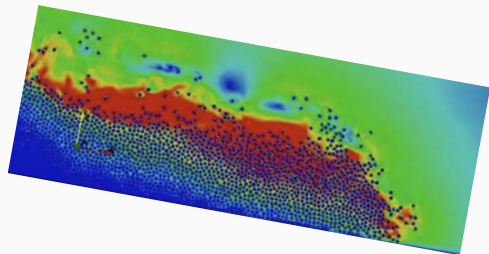
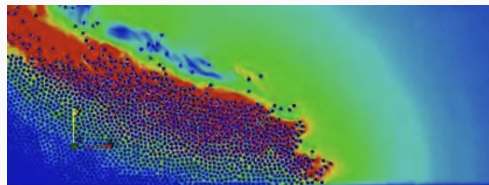
## Magical NN



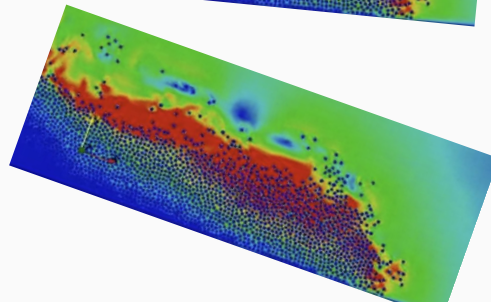
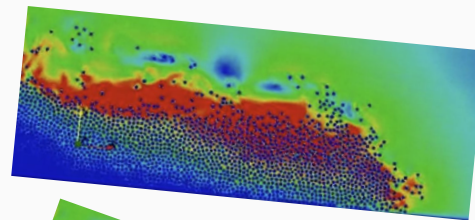
## Low-dim output



Training



Testing

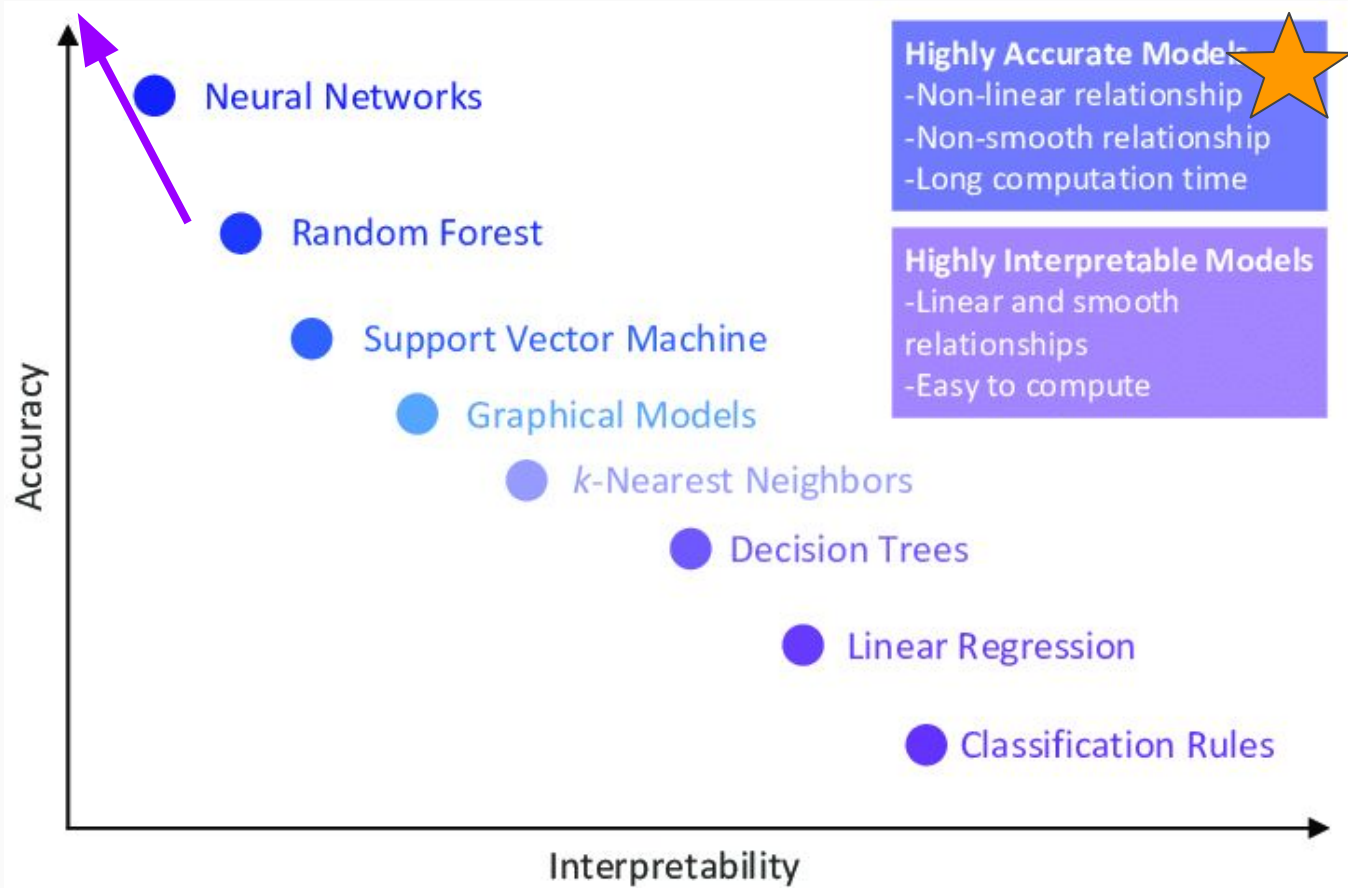


Interpolate



Extrapolate

# Interpretability vs accuracy



# Lateral Spreading

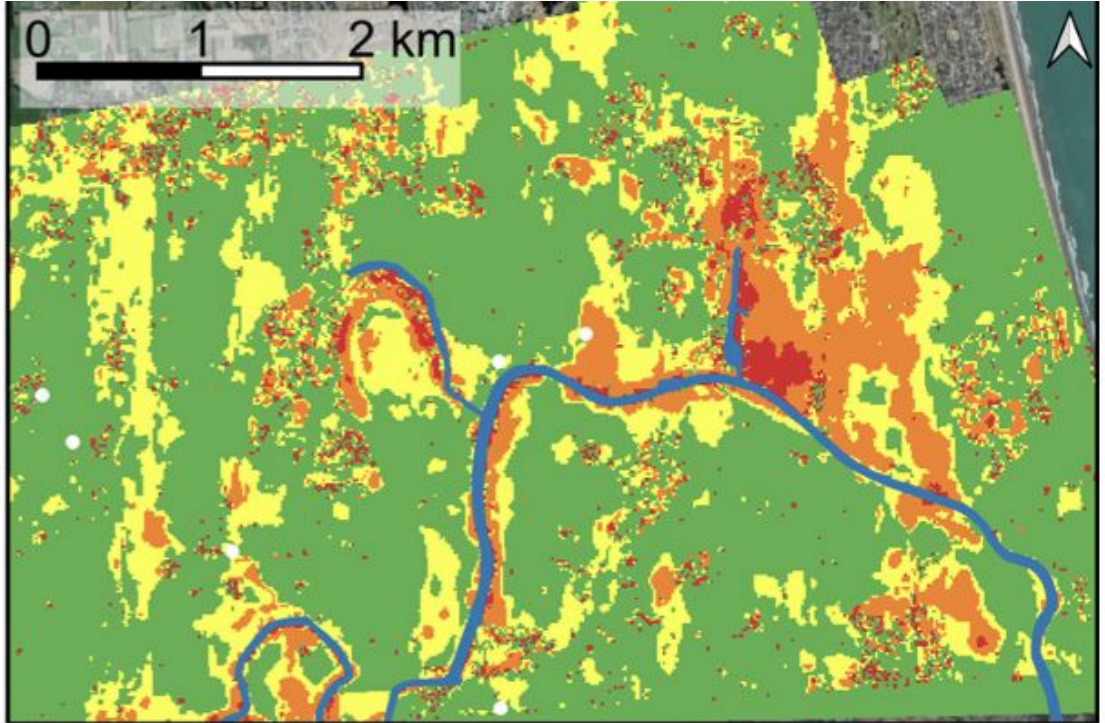
# Decision Trees & Random Forest



# Predicting lateral spreading in NZ

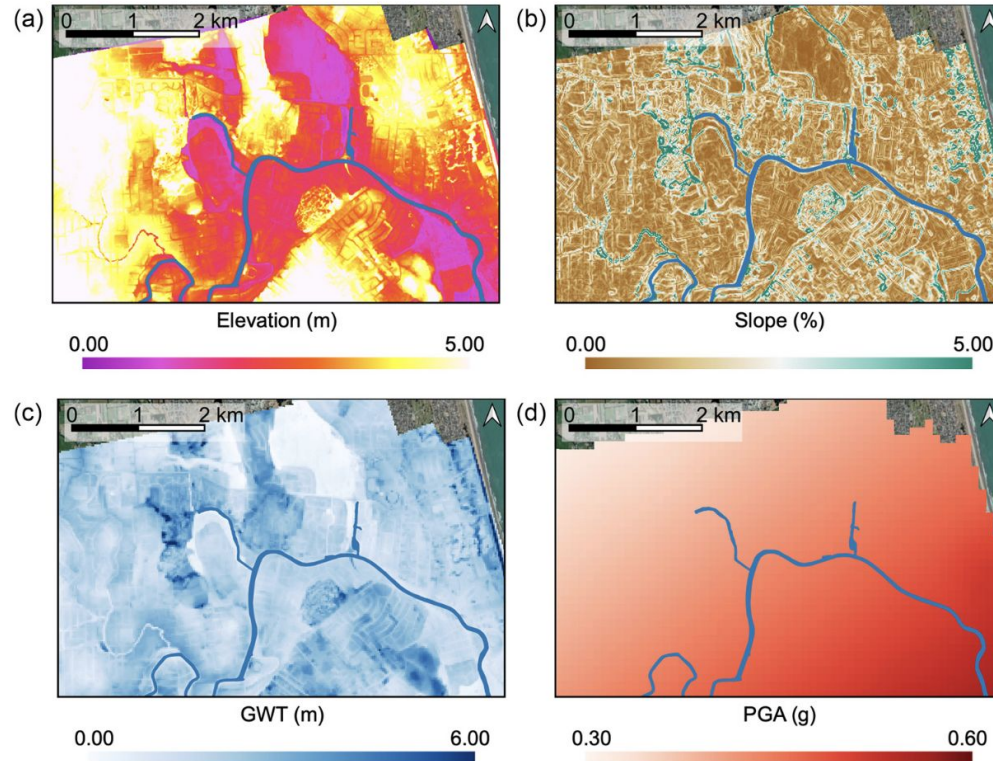
Observed  
displacement (m)

- None ( $< 0.30$ )
- 0.30 - 0.50
- 0.50 - 1.00
- $> 1.00$



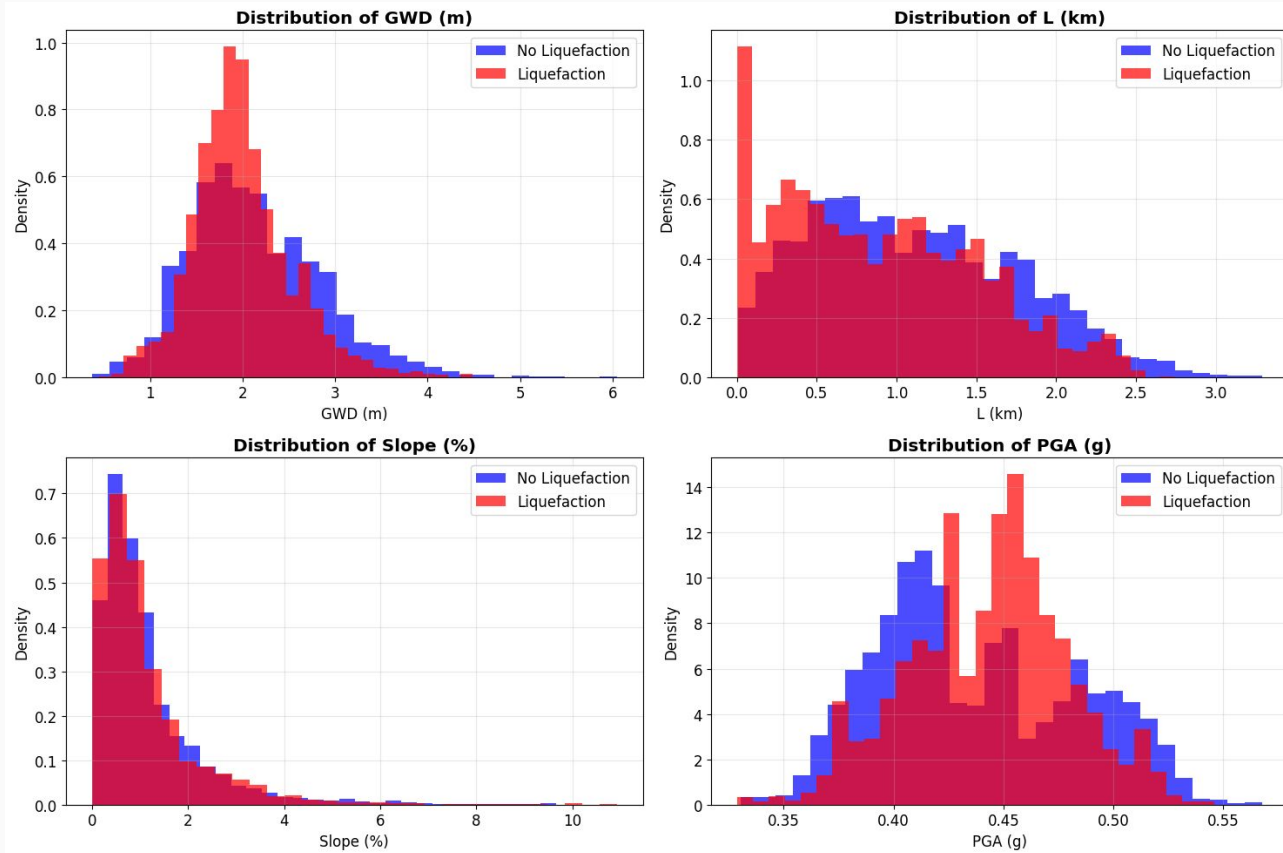
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# Predicting lateral spreading in NZ



**Figure 4.** Spatial distribution of geometric and event-specific input features considered in ML models: (a) ground elevation, (b) ground slope, (c) GWT depth, and (d) PGA.

# Distribution of data



# Random Forest model

**Table 3.** Summary of features used in each RF model analyzed

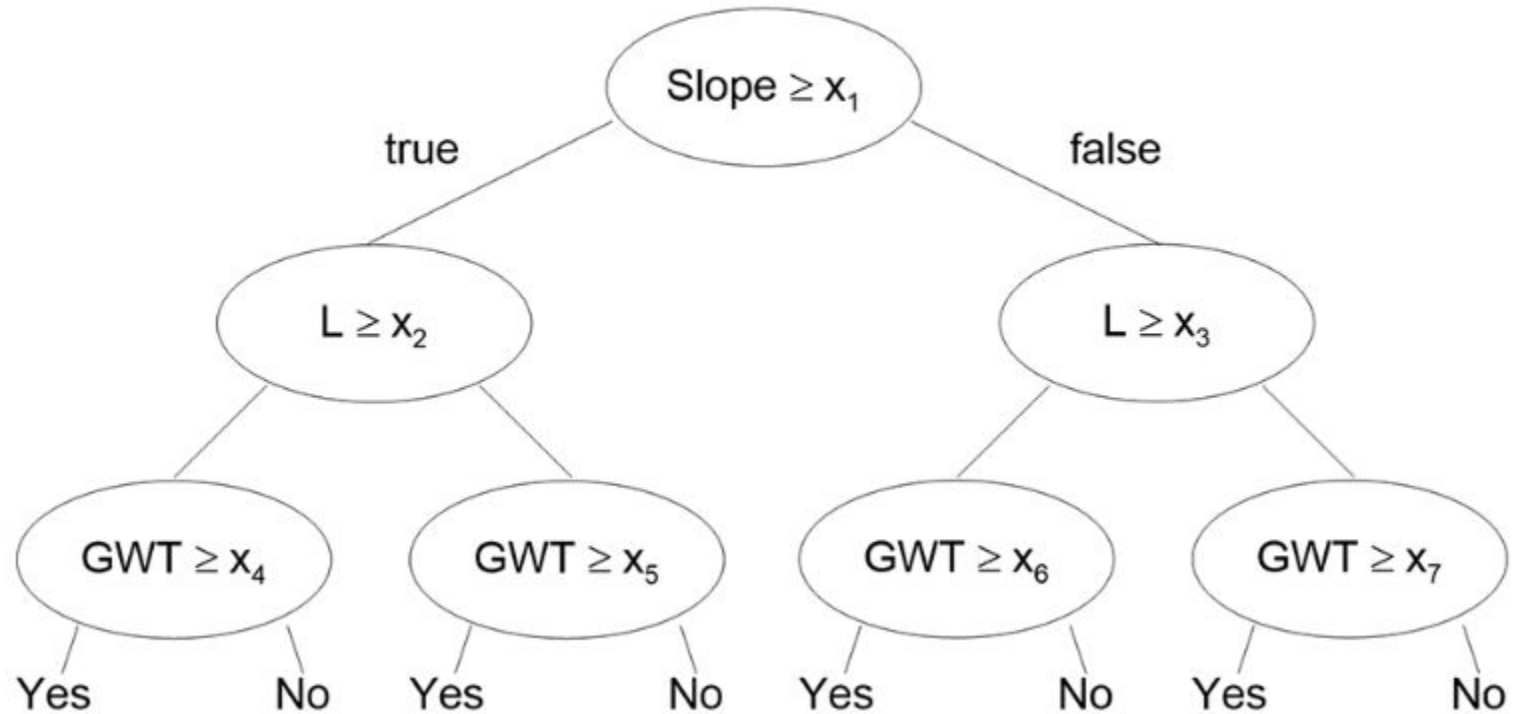
		Feature					
		L (m)	GWT (m)	Slope (%)	PGA (g)	Elevation (m)	CPT data
No CPT data	Model 0	✓	✓	✓	○	○	○
	Model 1	✓	✓	✓	✓	○	○
	Model 2	✓	✓	✓	○	✓	○
	Model 3	✓	✓	✓	✓	✓	○
CPT data	Model 4	✓	✓	✓	✓	○	✓
	Model 5	✓	✓	✓	✓	✓	✓

GWT: ground water table; PGA: peak ground acceleration; CPT: cone penetration tests.

Durante and Rathje, 2021

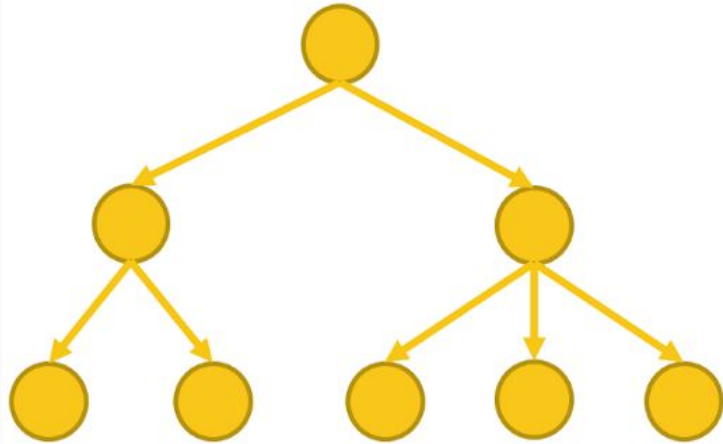


# Classification - Decision Tree

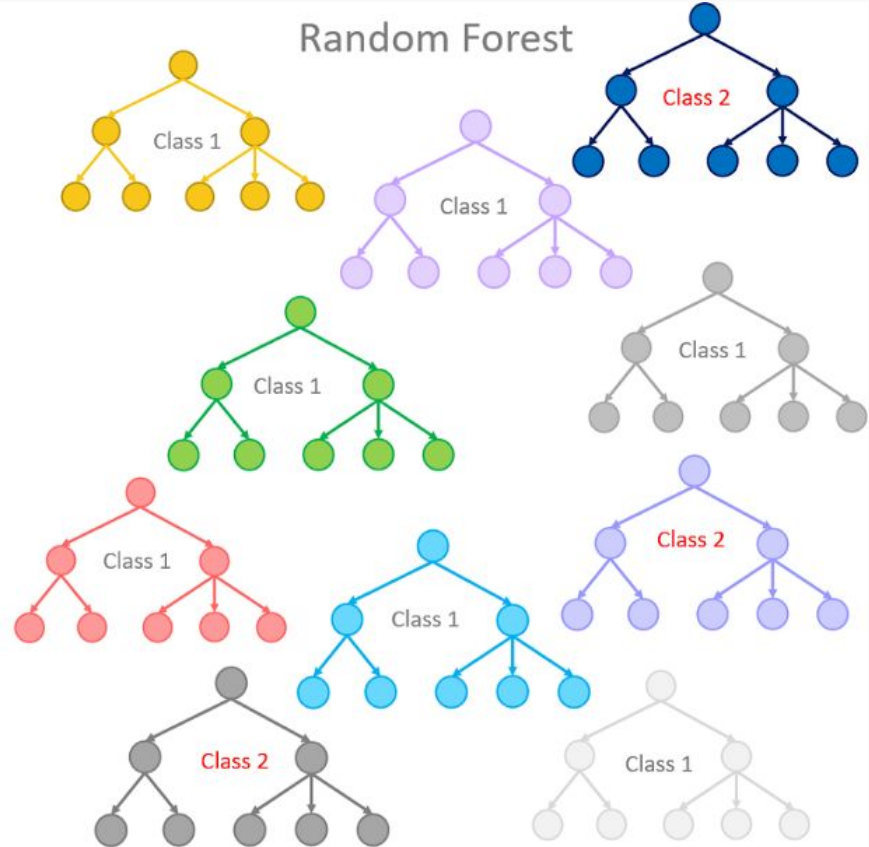


# Random Forest

Single Decision Tree



Random Forest



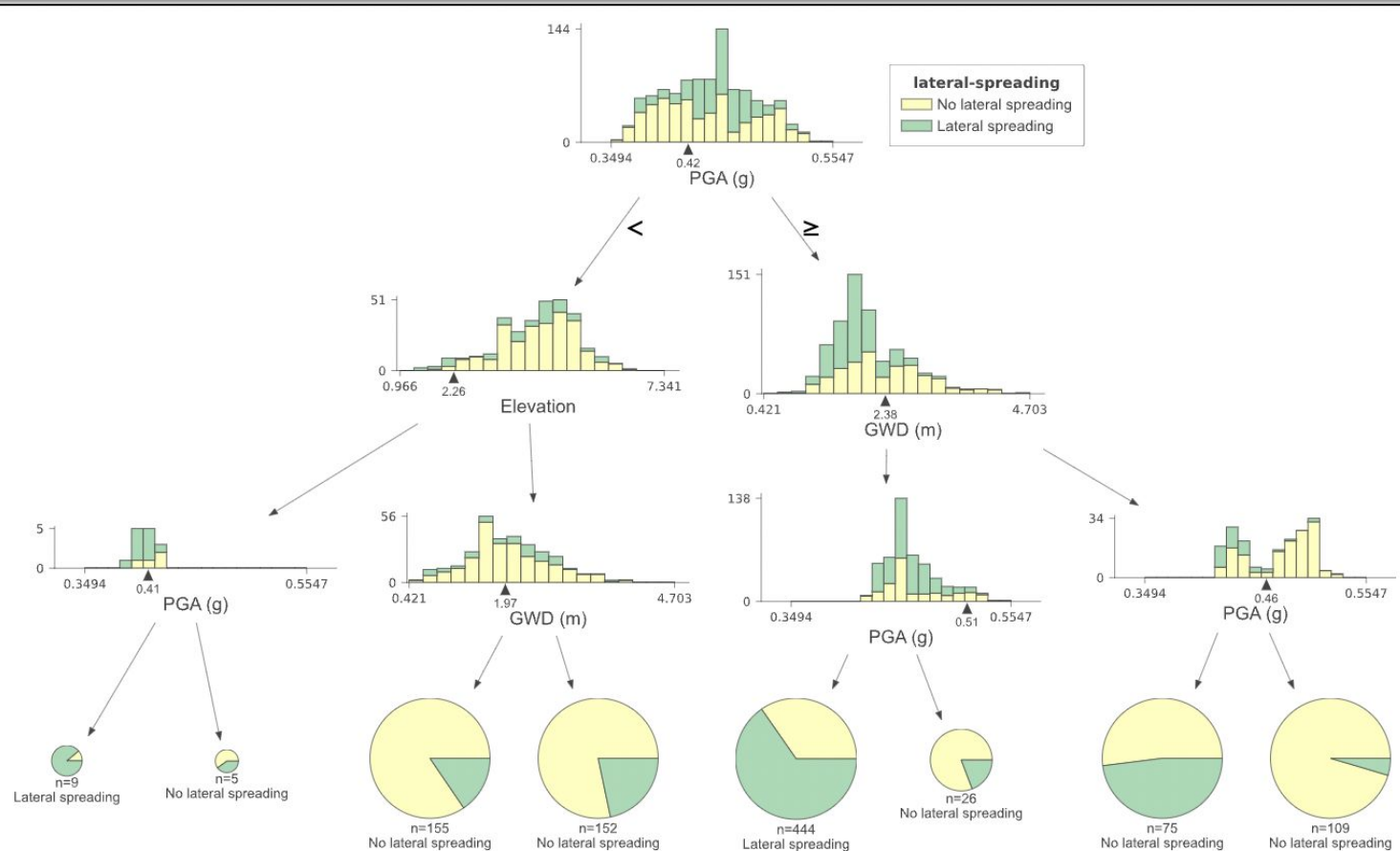
# Random Forest - Performance

**Table 4.** Evaluation metrics for RF models for Yes/No and displacement classification problems

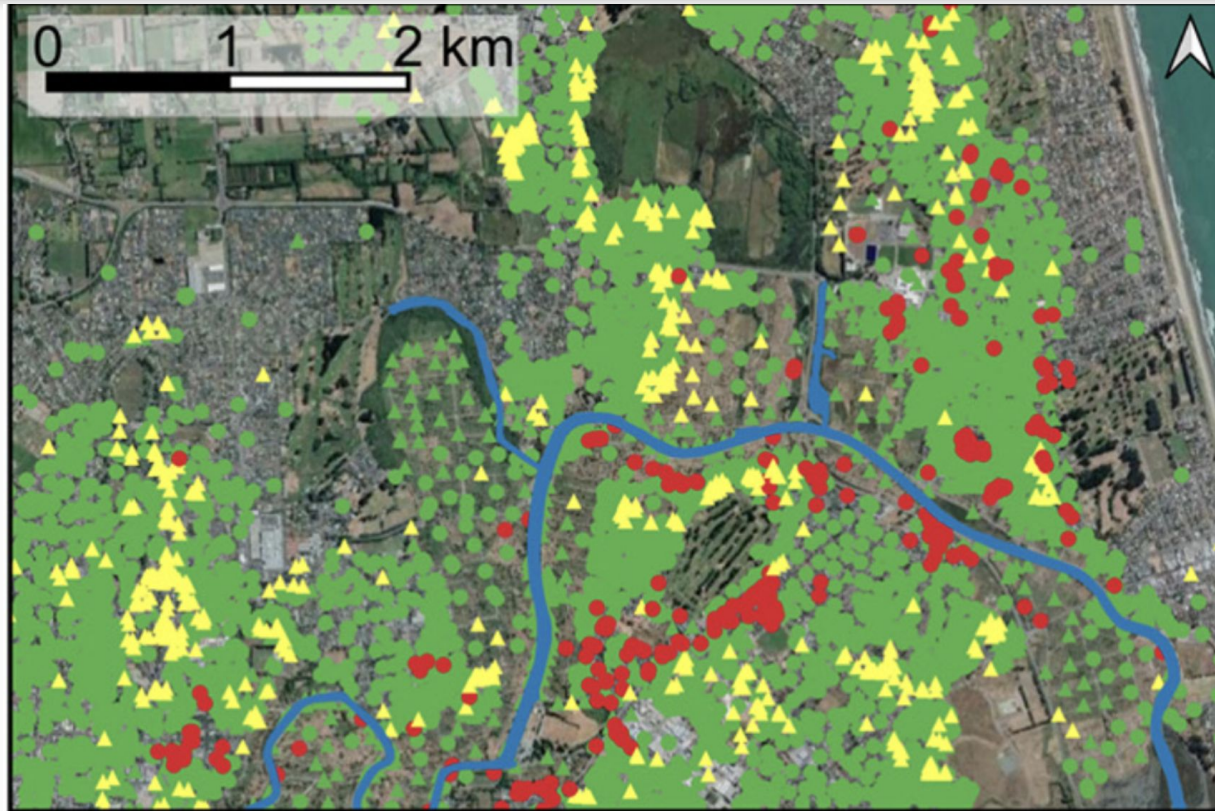
		No CPT data				CPT data	
		Model 0	Model 1	Model 2	Model 3	Model 4	Model 5
Y/N	Accuracy (Overall)	0.76	0.85	0.82	0.88	0.85	0.87
	Recall—Yes	0.58	0.75	0.74	0.82	0.76	0.78
	Recall—No	0.90	0.92	0.88	0.93	0.92	0.93
	Precision—Yes	0.80	0.88	0.82	0.89	0.87	0.89
	Precision—No	0.75	0.84	0.83	0.87	0.84	0.85
	ROC AUC	0.76	0.88	0.84	0.90	0.86	0.88
DISPL	Accuracy (Overall)	0.78	0.88	0.86	0.89	0.88	0.89
	Recall—Class 0	0.88	0.91	0.93	0.92	0.91	0.91
	Recall—Class 1	0.67	0.87	0.79	0.89	0.88	0.90
	Recall—Class 2	0.27	0.42	0.33	0.42	0.53	0.49
	Precision—Class 0	0.79	0.90	0.86	0.92	0.90	0.92
	Precision—Class 1	0.74	0.84	0.84	0.85	0.85	0.84
	Precision—Class 2	0.97	0.98	0.97	0.94	0.95	0.93
	ROC AUC	0.82	0.89	0.87	0.90	0.86	0.88

CPT: cone penetration tests; ROC: receiver operating characteristic; AUC: area under the ROC curve; Y/N: Yes/No Classification problem; DISPL: Class Displacement Classification problem.

# Visualizing the first tree in RF



# Random forest prediction of lateral spreading

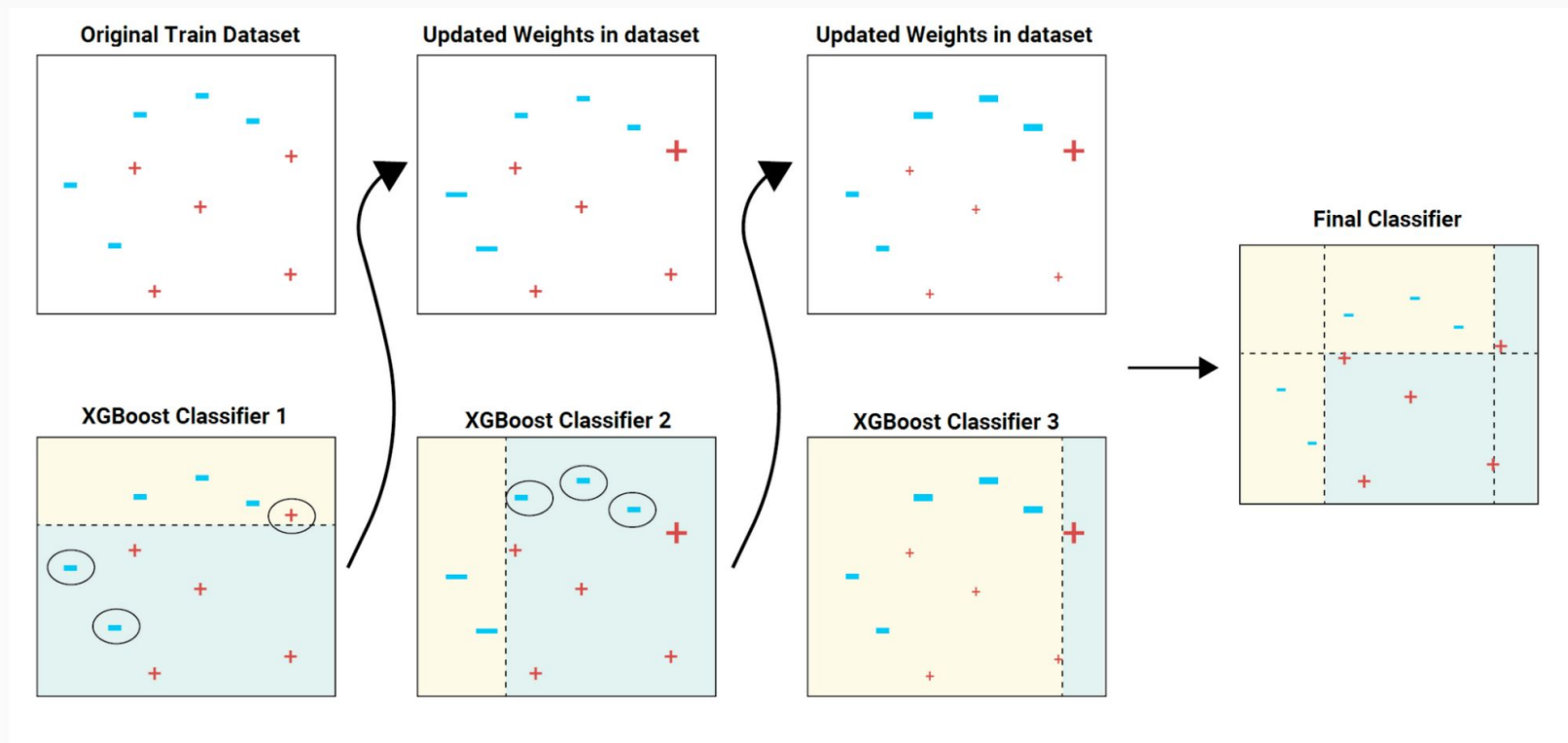


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▲ True Positive (TP) ● True Negative (TN) ● False Positive (FP) ▲ False Negative (FN)



# Extreme Gradient Boosting



# SHAP Value: Contribution of each variable



$$A: v(\{A\}) - v(\{\}) = 10 - 0 = 10$$

$$B: v(\{A, B\}) - v(\{A\}) = 60 - 10 = 50$$

$$C: v(\{A, B, C\}) - v(\{A, B\}) = 100 - 60 = 40$$

$$v(\{\}) = 0$$

$$v(\{A\}) = 10$$

$$v(\{B\}) = 20$$

$$v(\{C\}) = 30$$

$$v(\{A, B\}) = 60$$

$$v(\{B, C\}) = 70$$

$$v(\{A, C\}) = 90$$

$$v(\{A, B, C\}) = 100$$

$$\{\} \rightarrow \{A\} \rightarrow \{A, B\} \rightarrow \{A, B, C\} \parallel A = 10, B = 50, C = 40$$

$$\{\} \rightarrow \{A\} \rightarrow \{A, C\} \rightarrow \{A, B, C\} \parallel A = 10, B = 10, C = 80$$

$$\{\} \rightarrow \{B\} \rightarrow \{A, B\} \rightarrow \{A, B, C\} \parallel A = 40, B = 20, C = 40$$

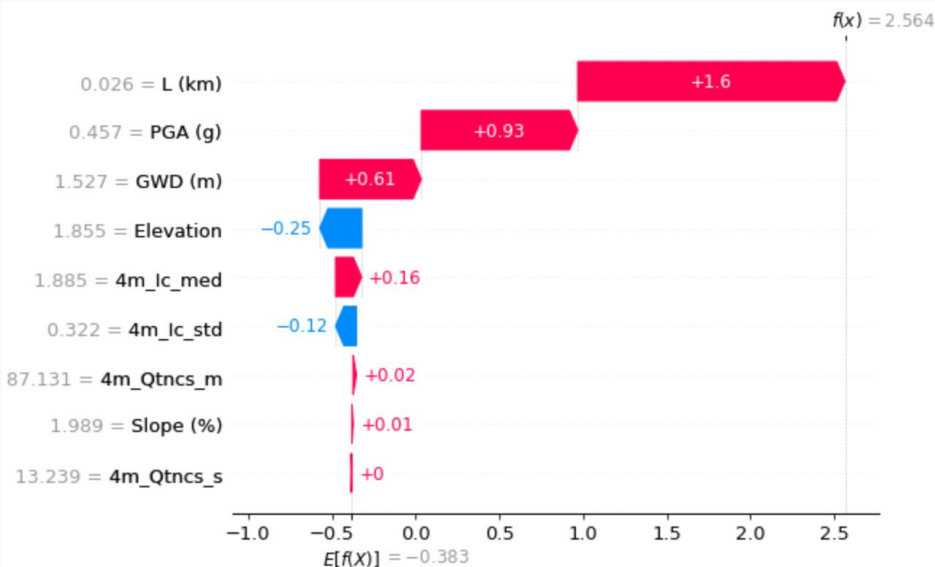
$$\{\} \rightarrow \{B\} \rightarrow \{B, C\} \rightarrow \{A, B, C\} \parallel A = 30, B = 20, C = 50$$

$$\{\} \rightarrow \{C\} \rightarrow \{B, C\} \rightarrow \{A, B, C\} \parallel A = 30, B = 40, C = 30$$

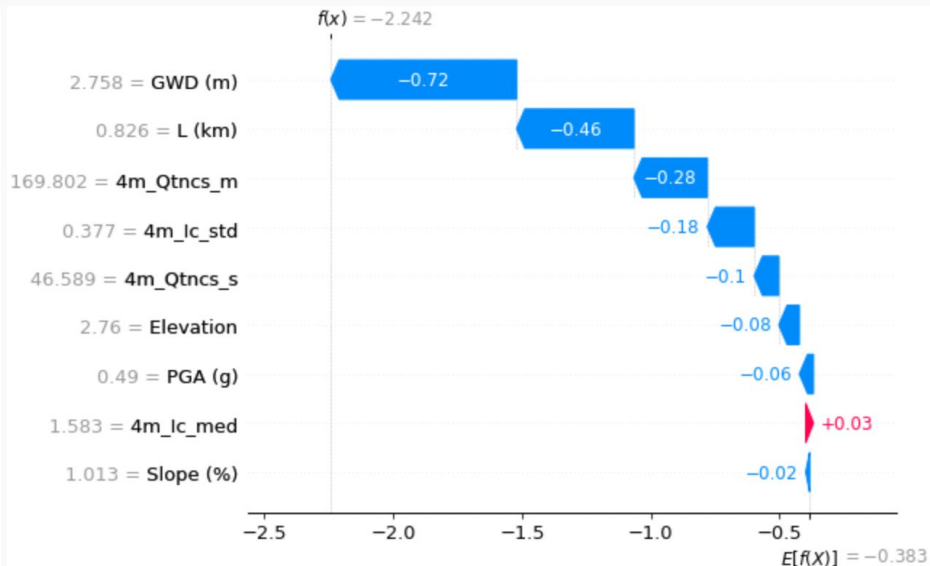
$$\{\} \rightarrow \{C\} \rightarrow \{A, C\} \rightarrow \{A, B, C\} \parallel A = 60, B = 10, C = 30$$

$$A_{avg} = 30, B_{avg} = 25, C_{avg} = 45$$

# Random Forest post-hoc explanation

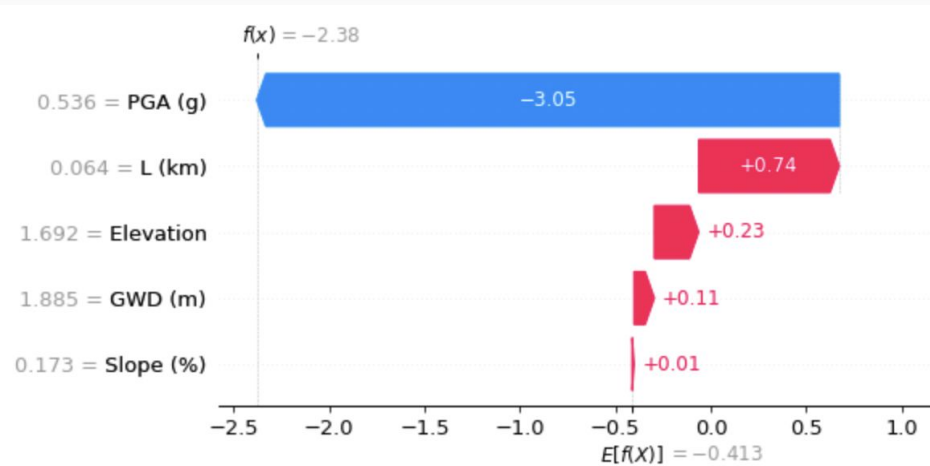


Lateral spreading - Prob (Lat spread) = 90%

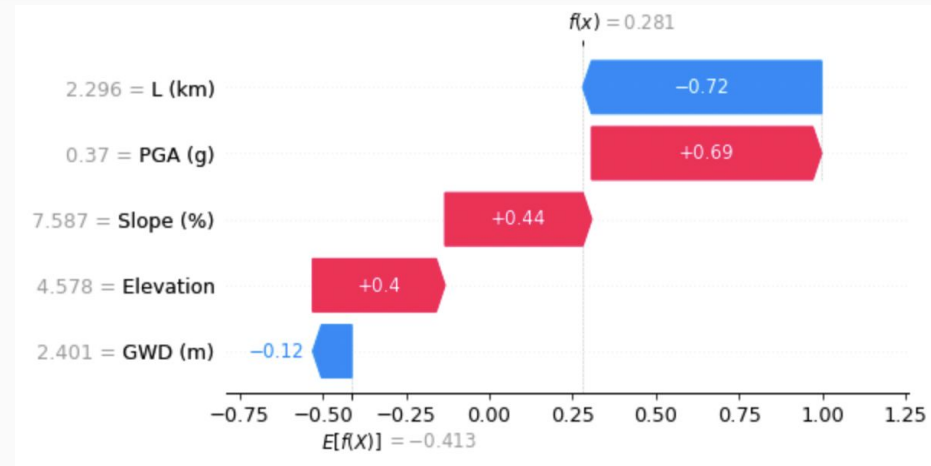


No lateral spreading - Prob (Lat spread) = 7%

# Incorrect learning

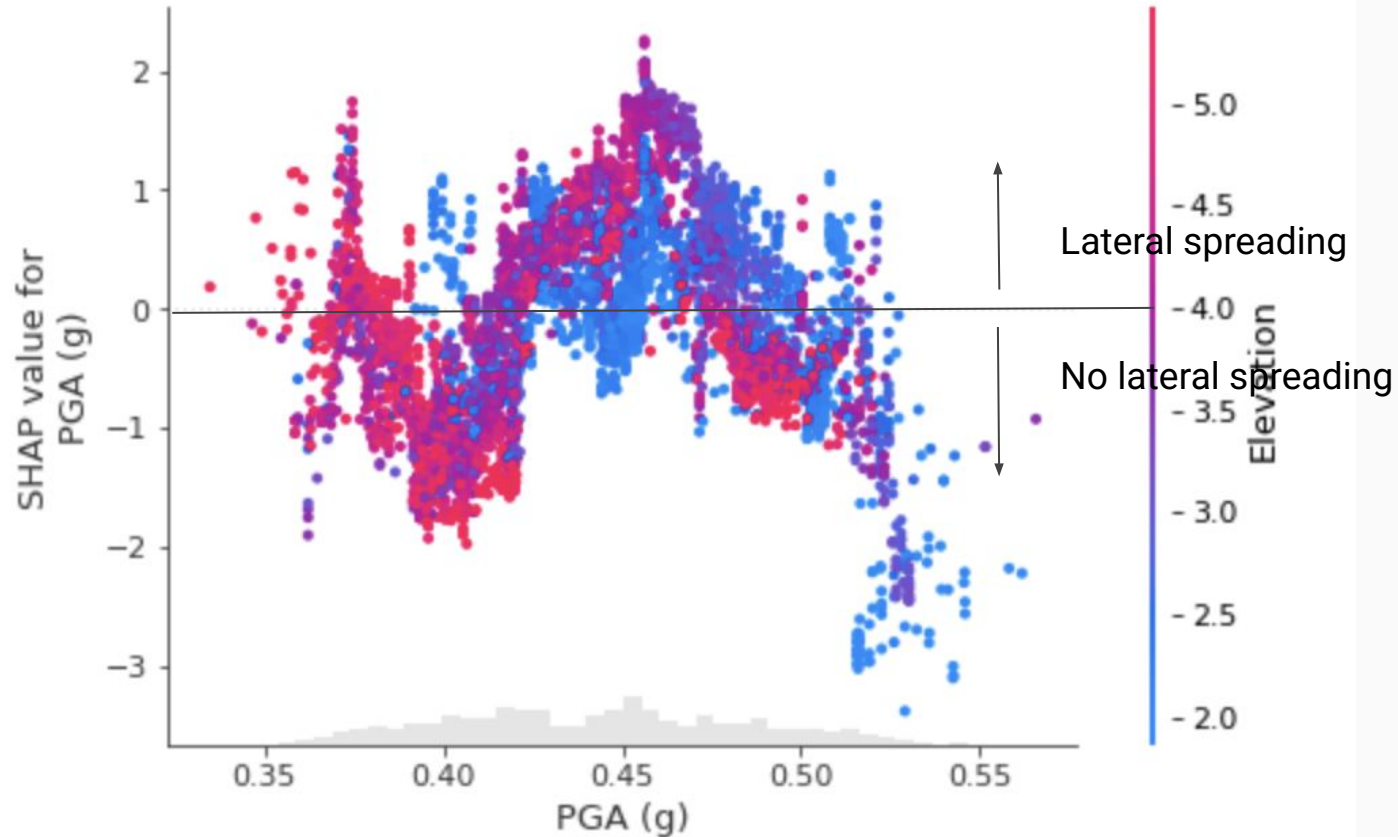


Incorrectly predicting no lateral spreading  
 Prob (Lat spread) = 8%



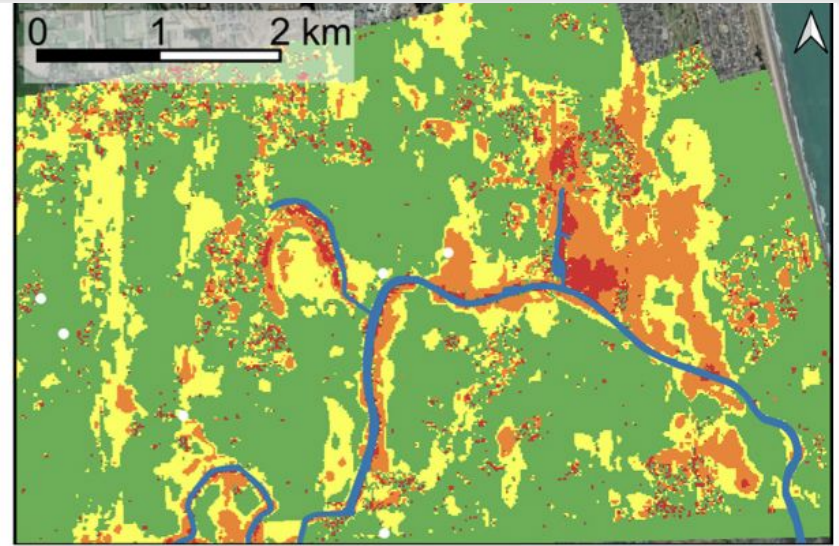
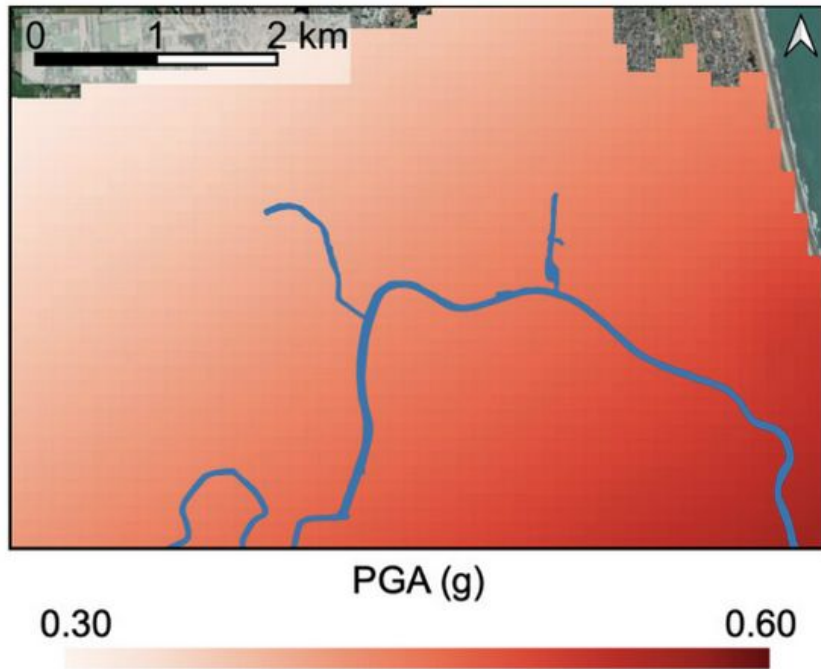
Incorrectly predicting lateral spreading  
 Prob (Lat spread) = 53%

# Why PGA has a bad influence?





# Bad learning of PGA relation



Observed  
displacement (m)

- None (< 0.30)
- 0.30 - 0.50
- 0.50 - 1.00
- > 1.00

# Multi-Layer Perceptron

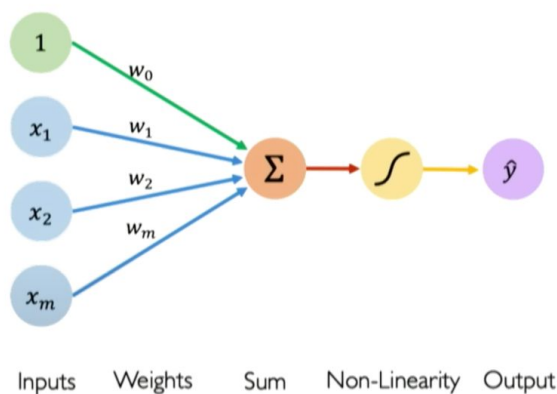
# Now let's try with MLP

A perceptron computes:

$$z = \mathbf{w}^T \mathbf{x} + b = \sum_{i=1}^n w_i x_i + b$$

$$\hat{y} = g(z)$$

where  $g$  is the activation function.



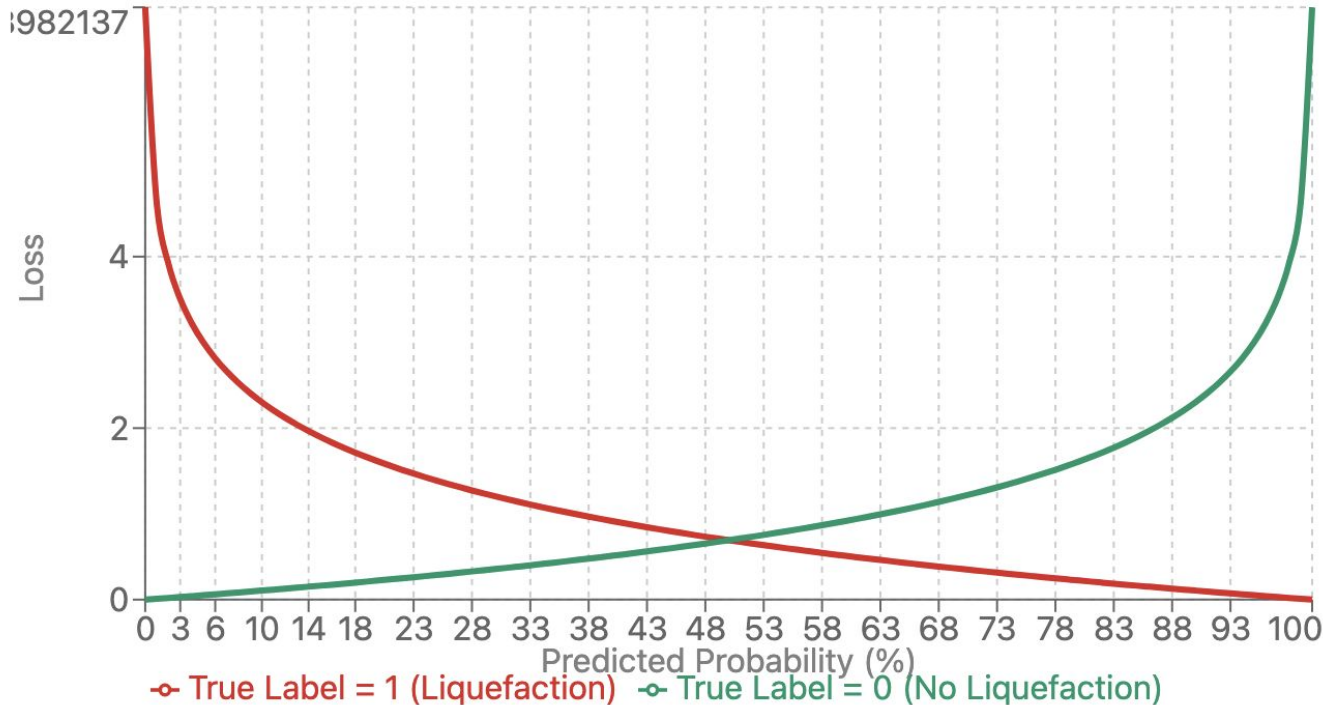
The diagram shows the mathematical equation for a perceptron's output, with color-coded arrows pointing to specific parts of the equation: 
$$\hat{y} = g \left( w_0 + \sum_{i=1}^m x_i w_i \right)$$
 The labels and their corresponding arrows are: 'Output' (purple arrow pointing to  $\hat{y}$ ), 'Linear combination of inputs' (red arrow pointing to the summation term  $\sum_{i=1}^m x_i w_i$ ), 'Non-linear activation function' (yellow arrow pointing to  $g$ ), and 'Bias' (green arrow pointing to  $w_0$ ).

Perceptron architecture

# Define a misfit (loss)

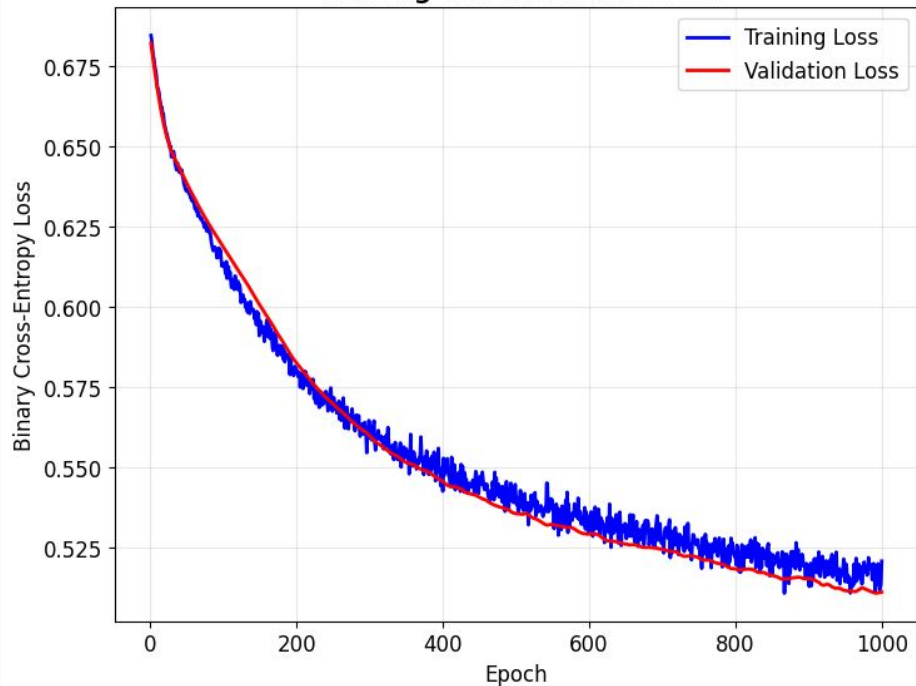
## Loss vs Predicted Probability

$$\text{BCE} = -[y \times \log(p) + (1-y) \times \log(1-p)]$$

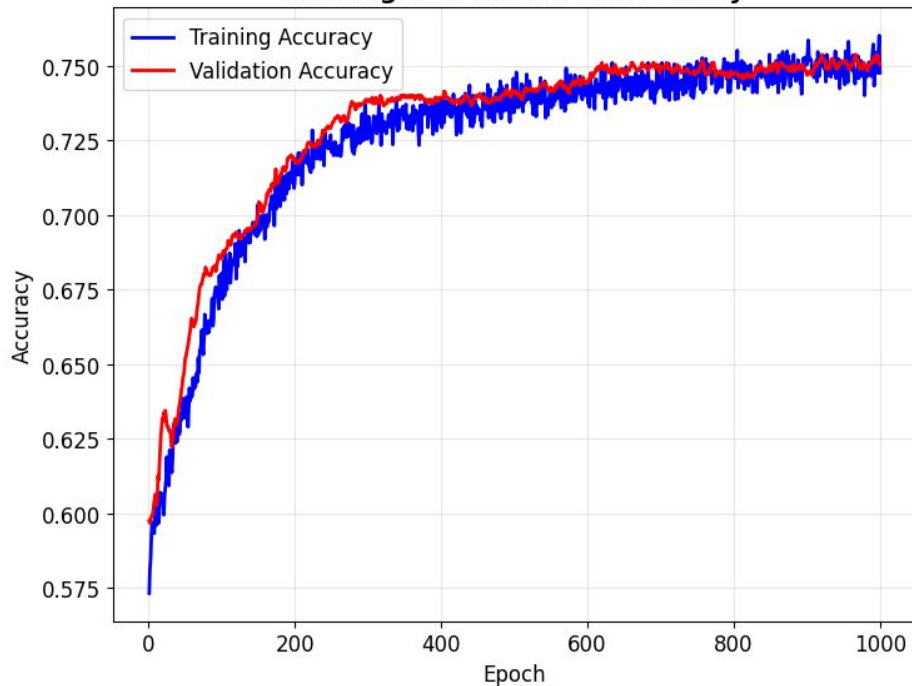


# Training vs validation

Training and Validation Loss

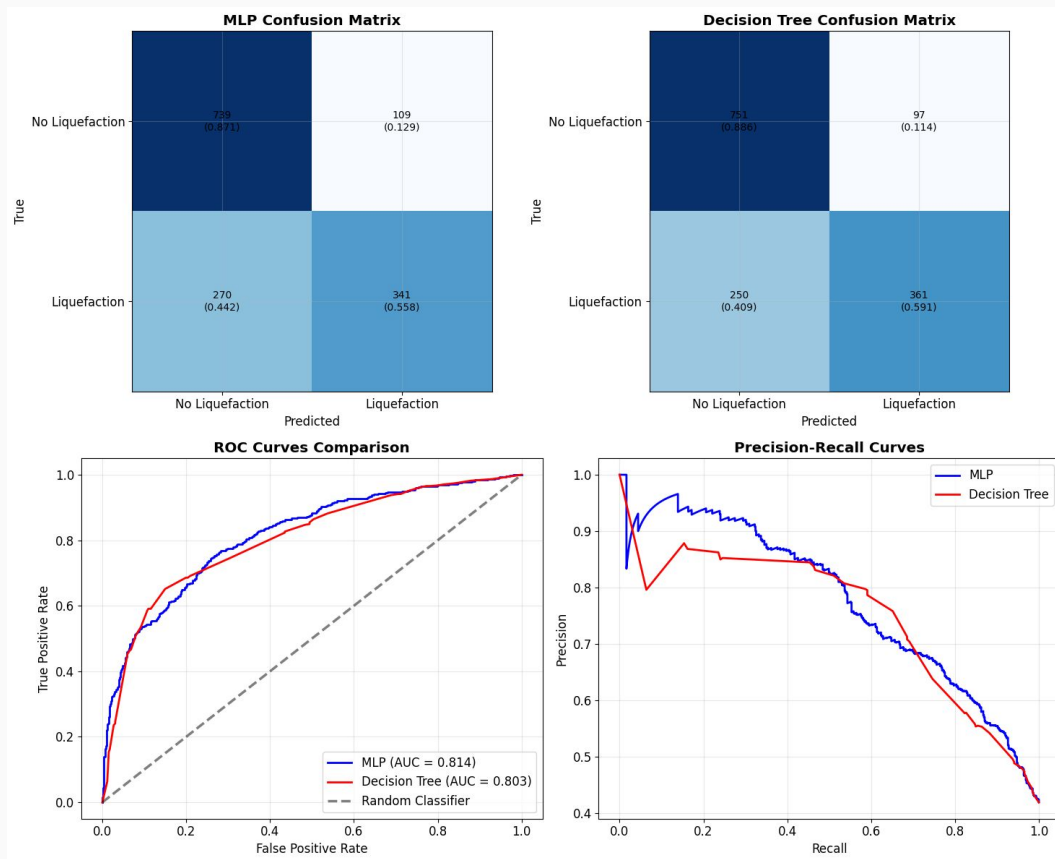


Training and Validation Accuracy





# MLP results



# Deeper/Larger Networks are better!

