

$$i) \begin{cases} x + y - 2z = -4 \\ 2x + y - 5z = 9 \\ -x + y + 4z = -30 \\ x - 2y - 5z = 47 \end{cases}$$

$$\begin{pmatrix} 1 & 1 & -2 & -4 \\ 2 & 1 & -5 & 9 \\ -1 & 1 & 4 & -30 \\ 1 & -2 & -5 & 47 \end{pmatrix} \xrightarrow{\substack{R_2 - 2R_1 \\ R_3 + R_1 \\ R_4 - R_1}} \begin{pmatrix} 1 & 1 & -2 & -4 \\ 0 & -1 & -1 & 17 \\ 0 & 2 & 2 & -34 \\ 0 & -3 & -3 & 51 \end{pmatrix}$$

$$\xrightarrow{\substack{-R_2 \\ \frac{1}{2}R_3 \\ -\frac{1}{3}R_4}} \begin{pmatrix} 1 & 1 & -2 & -4 \\ 0 & 1 & 1 & -17 \\ 0 & 1 & 1 & -17 \\ 0 & 1 & 1 & -17 \end{pmatrix} \xrightarrow{\substack{R_1 - R_2 \\ R_3 - R_2 \\ R_4 - R_2}} \begin{pmatrix} 1 & 0 & -3 & 13 \\ 0 & 1 & 1 & -17 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\begin{cases} x - 3z = 13 \\ y + z = -17 \end{cases} \Leftrightarrow \begin{cases} x = 13 + 3z \\ y = -17 - z \end{cases}$$

$$V = \{(13 + 3t, -17 - t, t) \mid t \in \mathbb{R}\}$$

$$\text{rk}(A_b) = 2$$

$$\text{R}(A) = 2$$

3 onbekenden