

$$\textcircled{1} \quad Df(-1) = \lim_{x \rightarrow -1} \frac{f(x) - f(-1)}{x - (-1)} = \lim_{x \rightarrow -1} \frac{4x^2 - 4}{x + 1} = \frac{0}{0}$$

$$= \lim_{x \rightarrow -1} \frac{4(x^2 - 1)}{x + 1} = \lim_{x \rightarrow -1} \frac{4(x-1)(x+1)}{x+1} = \textcircled{-8}$$

$\textcircled{2}$ f is differentieerbaar in $\mathbb{R} \setminus \{1\}$

In $x=1$ heeft f een knikpunt, dus bestaat de afgeleide niet. Er kunnen in dit punt 2 raaklijnen getekend worden, de linkerafgeleide is verschillend v/d rechterafgeleiden

$$\textcircled{3} \quad a) \quad f(-1) = \textcircled{10}$$

$$b) \quad Df(-1) = \textcircled{-2}$$

$$c) \quad f(2) = 13$$

$$\frac{f(2) - f(-1)}{2 - (-1)} = \frac{13 - 10}{3} = \frac{3}{3} = \textcircled{1}$$

$$d) \quad t: y - f(-1) = -2(x - (-1))$$

$$y - 10 = -2(x + 1)$$

$$y = -2x - 2 + 10$$

$$\textcircled{y = -2x + 8}$$

e) $x=0$ want in de top is de raaklijn horizontaal, dus $Df(0) = 0$

$$\textcircled{4} a) \quad D(5x^6 - \sqrt{2}x^4 + 7x^2 + 6x - 9)$$

$$= 30x^5 - 4\sqrt{2}x^3 + 14x + 6$$

$$b) \quad D(x^5 \cdot \cos x) = \cos x \cdot D x^5 + x^5 \cdot D \cos x$$

$$= \cos x \cdot 5x^4 + x^5 \cdot (-\sin x)$$

$$= 5x^4 \cos x - x^5 \sin x$$

$$c) \quad D\left(\frac{4x^3 + 2x - 3}{7x^2 + 5x}\right)$$

$$= \frac{(7x^2 + 5x) \cdot D(4x^3 + 2x - 3) - (4x^3 + 2x - 3) \cdot D(7x^2 + 5x)}{(7x^2 + 5x)^2}$$

$$= \frac{(7x^2 + 5x) \cdot (12x^2 + 2) - (4x^3 + 2x - 3) \cdot (14x + 5)}{(7x^2 + 5x)^2}$$

$$= \frac{84x^4 + 60x^3 + 14x^2 + 10x - (56x^4 + 20x^3 + 28x^2 + 10x - 42x - 15)}{(7x^2 + 5x)^2}$$

$$= \frac{28x^4 + 40x^3 - 14x^2 + 42x + 15}{(7x^2 + 5x)^2}$$

$$d) \quad D \sin^2(8x) = 2 \sin(8x) \cdot D \sin 8x$$

$$= 2 \sin(8x) (\cos 8x) \cdot 8$$

$$= 16 \sin 8x \cdot \cos 8x$$

$$= 8 \cdot \sin 16x$$