

Algorithms – Assignment 1

(Complexity)

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Due: 19th March

1) Show directly that $f(n) = n^2 + 3n^3 \in O(n^3)$ and $f(n) = n^2 + 3n^3 \in \Omega(n^3)$.

2) Using the definitions of O and Ω , show that

$$6n^2 + 20n \in O(n^3), \text{ but } 6n^2 + 20n \notin \Omega(n^3).$$

3) The function $f(n) = 3n^2 + 10n \log n + 1000n + 4 \log n + 9999$ belongs in which of the following complexity categories:

- (a) $\Theta(\lg n)$ (b) $\Theta(n^2 \log n)$ (c) $\Theta(n)$ (d) $\Theta(n \lg n)$ (e) $\Theta(n^2)$ (f) None of these

4) The function $f(n) = (\log n)^2 + 2n + 4n + \log n + 50$ belongs in which of the following complexity categories:

- (a) $\Theta(\lg n)$ (b) $\Theta((\log n)^2)$ (c) $\Theta(n)$ (d) $\Theta(n \lg n)$ (e) $\Theta(n(\lg n)^2)$ (f) None of these

5) The function $f(n) = n + n^2 + 2^n + n^4$ belongs in which of the following complexity categories:

- (a) $\Theta(n)$ (b) $\Theta(n^2)$ (c) $\Theta(n^3)$ (d) $\Theta(n \lg n)$ (e) $\Theta(n^4)$ (f) None of these

6) What is the runtime (time complexity) of the below code?

```
def printUnorderedPairs(array):  
    for i in range(0,len(array)):  
        for j in range(i+1,len(array)):  
            print(array[i] + "," + array[j])
```

7) What is the runtime of the below code?

```
def printUnorderedPairs(arrayA, arrayB):  
    for i in range(len(arrayA)):  
        for j in range(len(arrayB)):  
            for k in range(0,100000):  
                print(str(arrayA[i]) + "," + str(arrayB[j]))
```

8) What is the runtime of the below code?

```
def powersOf2(n):  
    # print("n:"+str(n))  
    if n < 1:  
        return 0  
    elif n == 1:  
        print(1)  
        return 1  
    else:  
        prev = powersOf2(int(n/2))  
        # print("prev:"+str(prev))  
        print(prev)  
        curr = prev*2  
        print(curr)  
        return curr
```