

Set: distinguishable collection.  
 Element: distinguishable object in the set

Element x is in set A:  
 $x \in A$

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Cardinality is the number of element which the set has

$$A = \{1, 2, 3\}$$

$$|A| = \text{card}(A) = 3$$

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Union of two sets A and B  
 $A \cup B$

Intersection of two sets A and B  
 $A \cap B$

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If set A is sub set of set B:  
 $A \subset B$

$$A \subset A \text{ is true}$$

If cardinality of A is smaller than B,  
 A is proper subset of B

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Difference set  
 $A - B$

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Complement set against entire set  $\Omega$   
 $A^C$

$$A^C = \Omega - A$$

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Null set  $\phi$  has none element

$$\phi \subset \text{all sets}$$

Following is true  
 $A \cap \phi = \phi$   
 $A \cup \phi = A$

$$A \cap A^C = \phi$$

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$A = \{1, 2\}$  has 4 number of sub sets

$$\begin{aligned} A_1 &= \phi \\ A_2 &= \{1\} \\ A_3 &= \{2\} \\ A_4 &= \{1, 2\} \end{aligned}$$

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If set A has N number of elements,  
A has  $2^N$  number of sub sets

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Following is true as distribution law  
 $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$   
 $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$

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afafaf Probabilistic sample(or random sample, sample):  
 One realizable phenomenon from the probabilistic problem you want to solve  
 Or one sampled case

Sample space  $\Omega$ :  
 Set which contains all possible samples

Task of defining sample sapce:  
 Define which phenomenon is possible to occur  
 and which phenomenon is impossible to occur

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Sample space when you toss the coin  
 $\Omega = \{H, T\}$

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Some cases has set of entire real numbers as sample space  
 $\Omega = \mathbf{R}$

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Possible events: possible sub sets of sample space  $\Omega$

Sample space  $\Omega = \{H, T\}$   
 Possible events:  $\phi, \{H\}, \{T\}, \{H, T\}$

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 Probability is function which takes all events  
 and which outputs number

$P(A) = 0.1$   
 $P()$  is function P  
 A is event  
 0.1 is probability value

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 Kolmogorov's axioms

1.  $P(\text{all events}) \geq 0$
2.  $P(\Omega) = 1$
3. If  $A \cap B = \phi$ , then  $P(A \cup B) = P(A) + P(B)$

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 Interpretation about probability value:

1. Frequentist
  2. Bayesian
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