Introduction to Normal Distribution

your name

2024-10-3

Math 2265 Sec 4.1 Normal Distribution Part I

- · Work as a group!
- You will need to replace "ans" or your_answer in the source code or answer questions
- Update your name in L3
- Add your group members name below
- Make sure your save and knit your work (to html or pdf) before submitting it to Canvas

Question 0. Who are your group members? (List their first names should be sufficient)

Answer:

1. <name_1> 2. <name_2>

Load Packages

```
## Loading required package: airports
## Loading required package: cherryblossom
## Loading required package: usdata
## Registered S3 method overwritten by 'mosaic':
##
    method
                                      from
     fortify.SpatialPolygonsDataFrame ggplot2
##
##
## The 'mosaic' package masks several functions from core packages in order to add
## additional features. The original behavior of these functions should not be affected by this.
##
## Attaching package: 'mosaic'
##
  The following objects are masked from 'package:dplyr':
##
       count, do, tally
##
  The following object is masked from 'package:Matrix':
##
##
       mean
## The following object is masked from 'package:ggplot2':
##
##
       stat
## The following object is masked from 'package:openintro':
```

```
## dotPlot
## The following objects are masked from 'package:stats':
##
## binom.test, cor, cor.test, cov, fivenum, IQR, median, prop.test,
## quantile, sd, t.test, var
## The following objects are masked from 'package:base':
##
## max, mean, min, prod, range, sample, sum
```

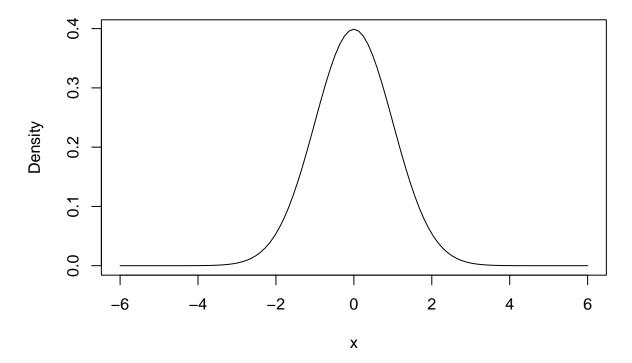
If you need more time to get used to Markdown, use the Visual mode.

The icon is located in the upper-left corner next to source.

Example 1: Plot normal distributions

```
curve(dnorm(x, mean = 0, sd = 1), from = -6, to = 6,
    main = "Normal Distribution (PDF, mean = 0, sd = 1)",
    xlab = "x", ylab = "Density")
```

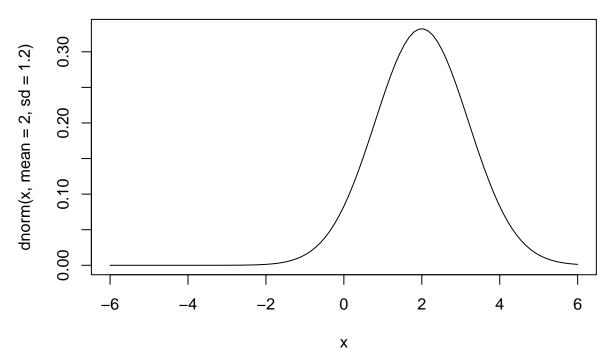
Normal Distribution (PDF, mean = 0, sd = 1)



Task 1: Plot some normal distributions with mean and standard deviation of your choice You may need to change from and to parameters too.

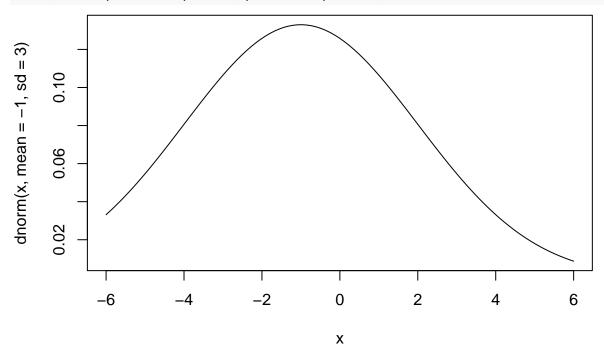
Your Example 1:

```
curve(dnorm(x, mean = 2, sd = 1.2), from = -6, to = 6)
```



Your Example 2:

```
curve(dnorm(x, mean = -1, sd = 3), from = -6, to = 6)
```

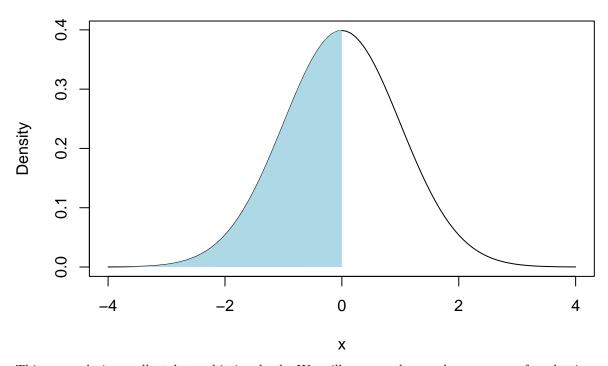


Example 2: Normal distribution with colors

```
# Plot the normal distribution curve
curve(dnorm(x, mean = 0, sd = 1), from = -4, to = 4,
    main = "Normal Distribution with Shaded Area (x <= 0)",
    xlab = "x", ylab = "Density")</pre>
```

```
# Shade the area under the curve for x <= 0
x_vals <- seq(-4, 0, length.out = 100) # Sequence of x values from -4 to 0
y_vals <- dnorm(x_vals, mean = 0, sd = 1) # Corresponding y values for the curve
polygon(c(x_vals, 0), c(y_vals, 0), col = "lightblue", border = NA) # Fill the area</pre>
```

Normal Distribution with Shaded Area $(x \le 0)$



This example is excellent but a bit involved. We will use another package mosaic for plotting normal distributions.

Example with the Mosaic pacakge

```
xpnorm(0) # if we skip mean and sd, the default values are mean = 0 and sd = 1

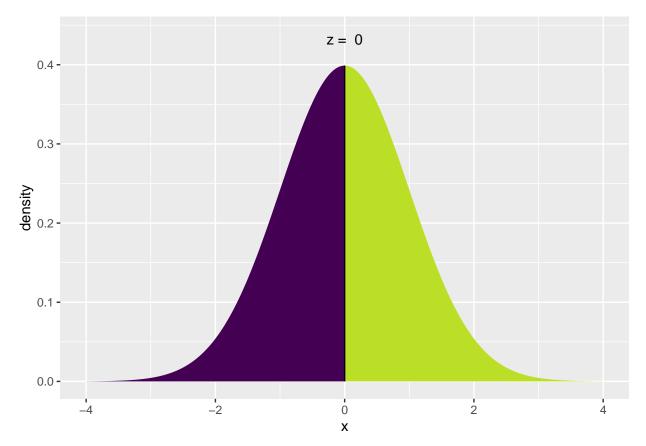
##

## If X ~ N(0, 1), then

## P(X <= 0) = P(Z <= 0) = 0.5

## P(X > 0) = P(Z > 0) = 0.5

##
```



[1] 0.5

So the following is the same as above.

$$xpnorm(0, mean = 0, sd = 1)$$

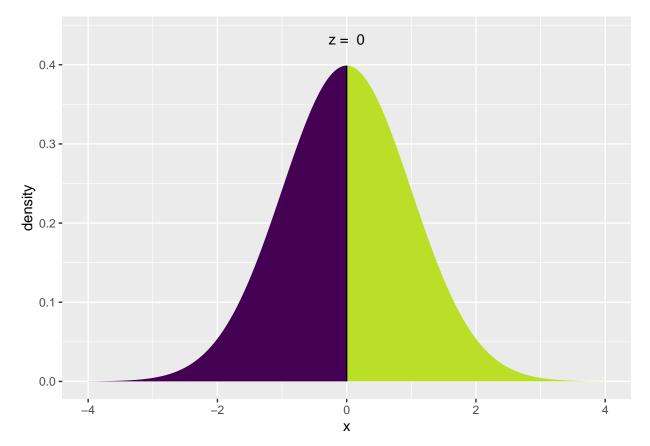
##

If X \sim N(0, 1), then

$P(X \le 0) = P(Z \le 0) = 0.5$

P(X > 0) = P(Z > 0) = 0.5

##



[1] 0.5

The first argument (0 in the example) is the x-value or Z-score when mean = 0 and sd = 1.

Z-Score

The possums example in the video follows the normal distribution with mean 92.6 and sd 3.6. Recall the Z-score formula.

$$Z = \frac{x - \mu}{\sigma},$$

where μ is the mean and σ is the standard deviation.

Task 2: Therefore, when x = 98, the Z-score is

$$(98 - 92.6)/3.6$$

[1] 1.5

Therefore, when x = 89, the Z-score is

[1] -1

Task 3: Compute the Z-Score and percentile (with table and pnorm)

The pnorm function will give you the percentile of the Z-score. Here is an example.

pnorm(0)

[1] 0.5

Use pnorm to compute the percentile for the two Z-score you computed for x = 98 and x = 89.

For x = 98,

pnorm(1.5)

[1] 0.9331928

For x = 89,

pnorm(-1)

[1] 0.1586553

Task 4: Sketch the normal distribution graphs using the function xpnorm

For x = 98,

xpnorm(1.5)

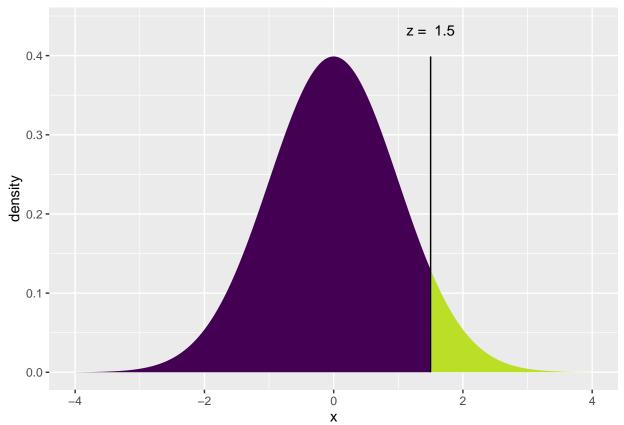
##

If X
$$\sim$$
 N(0, 1), then

$$P(X \le 1.5) = P(Z \le 1.5) = 0.9332$$

$$P(X > 1.5) = P(Z > 1.5) = 0.06681$$

##



[1] 0.9331928

For x = 89,

xpnorm(-1)

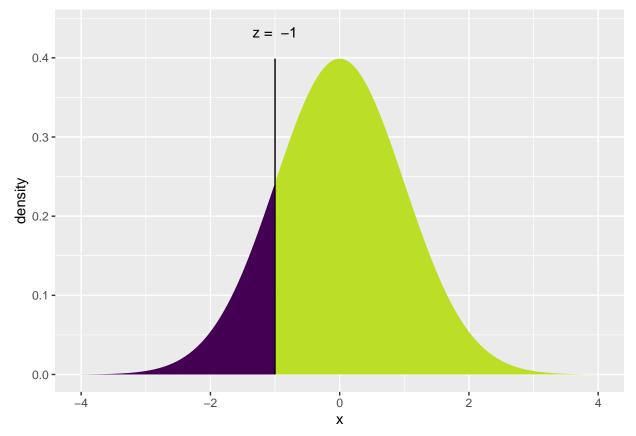
##

If X \sim N(0, 1), then

$$P(X \le -1) = P(Z \le -1) = 0.1587$$

$$P(X > -1) = P(Z > -1) = 0.8413$$

##



[1] 0.1586553

Task 5: Try the first HW problem.

Question 1:

3.1 Area under the curve, Part I: Find the probability of each of the following, if $Z \sim N(\mu = 0, \sigma = 1)$.

a)
$$P(Z<-1.35) =$$

[1] 0.08850799

b)
$$P(Z>1.48) =$$

```
q1_b <- 1-pnorm(1.48)
q1_b

## [1] 0.06943662
c) P(-0.4< Z< 1.5) =
q1_c <- pnorm(1.5) - pnorm(-0.4)
q1_c

## [1] 0.5886145
d) P(|Z|>2) =
q1_d <- 2*pnorm(-2)
q1_d

## [1] 0.04550026</pre>
```

Task 6. Knit your code and check your outcomes.

You are only allowed to upload pdf or html

Task 7. Check your answer

```
if(sum((c(q1_a, q1_b, q1_c, q1_d) - c(0.0885,0.0694,0.5886,0.0455))<0.001)==4) {
  print("Your answers are correct")
} else {
  print("Check your answers")
}</pre>
```

[1] "Your answers are correct"

Share your work and help your group members before uploading your work to Canvas