

AREC422 Notes

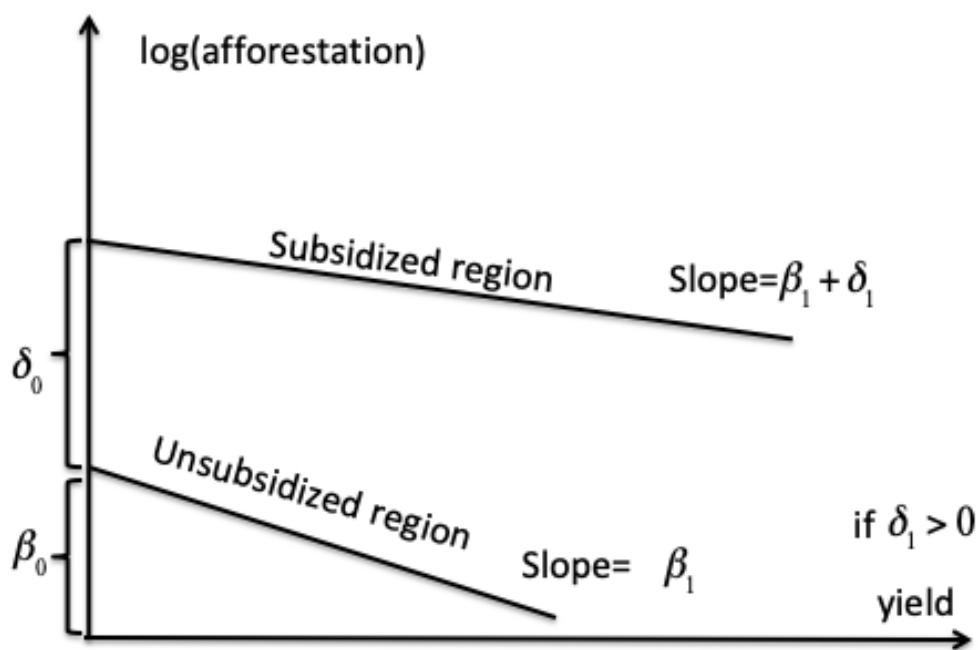
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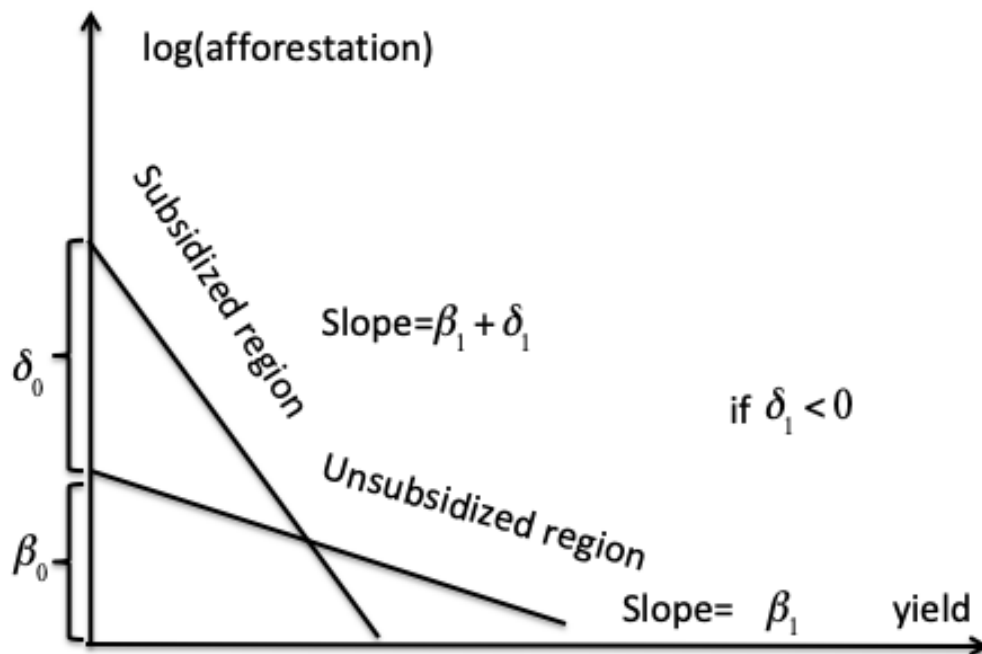
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e.g.2: $\log(\text{afforestation}) = \beta_0 + \delta_0 \text{subsidy} + \beta_1 \text{yield} + \delta_1 \text{subsidy} \cdot \text{yield} + u$ with only *subsidy* the dummy.

If *subsidy* = 0, $\log(\text{afforestation}) = \beta_0 + \beta_1 \text{yield} + u$

If *subsidy* = 1, $\log(\text{afforestation}) = (\beta_0 + \delta_0) + (\beta_1 + \delta_1) \text{yield} + u$





* Testing between groups: Chow Test

The change in the structure of the regression can be due to the intercept, the slopes, or both.

When we have two groups of observations:

group 1: $y_i = \alpha_1 + \alpha_2 X_i + u_{1i}$, with n_1 observations.

group 2: $y_i = \beta_1 + \beta_2 X_i + u_{2i}$, with n_2 observations.

It is possible that X have different impacts to y : $\alpha_2 \neq \beta_2, \alpha_1 \neq \beta_1$. Or, it is possible that there is no difference between the two groups:

$y_i = \lambda + \lambda X_i + u_i$ with $n = n_1 + n_2$ observations.

i.e., we can fit n points into one model: $\alpha_2 = \beta_2 = \lambda_2, \alpha_1 = \beta_1 = \lambda_1$

e.g.: $\text{pollution} = \lambda_0 + \lambda_1 \text{production} + \lambda_2 \text{abatement} + \lambda_3 \text{residential density} + u$, $n = n_1 + n_2$. There are n_1 firms inside an inspection zone, n_2 firms outside the zone.

How to test if they perform the same?

Unrestricted (UR) model (group of equations):

$\text{pollution} = \alpha_0 + \alpha_1 \text{production} + \alpha_2 \text{abatement} + \alpha_3 \text{residential density} + u$, with n_1 obs.

$\text{pollution} = \beta_0 + \beta_1 \text{production} + \beta_2 \text{abatement} + \beta_3 \text{residential density} + u$, with n_2 obs.

$H_0 : \alpha_0 = \beta_0, \alpha_1 = \beta_1, \alpha_2 = \beta_2, \alpha_3 = \beta_3$ vs. $H_1 : H_0$ is not true.

Apparently, this is an F-test. (Named Chow Test in this case)

Restrictions = $q = k + 1 = 4 = df_r - df_{ur}$

$$df_{ur} = (n_1 + n_2) - 2(k + 1) = n - 2(k + 1)$$

Recall the SSR-form of the F-value:

$$F = \frac{(SSR_r - SSR_{ur})/q}{SSR_{ur}/df_{ur}}$$

$$F = \frac{[SSR_r - (SSR_1 + SSR_2)]/(k + 1)}{(SSR_1 + SSR_2)/[n - 2(k + 1)]}$$

What if we have m categories?

UR model:

$$y_1 = \beta_{01} + \beta_{11}x_1 + \beta_{21}x_2 + \dots \beta_{k1}x_k + u, \text{ with } n_1 \text{ obs.}$$

$$y_2 = \beta_{02} + \beta_{12}x_1 + \beta_{22}x_2 + \dots \beta_{k2}x_k + u, \text{ with } n_2 \text{ obs.}$$

...

$$y_m = \beta_{0m} + \beta_{1m}x_1 + \beta_{2m}x_2 + \dots \beta_{km}x_k + u, \text{ with } n_m \text{ obs.}$$

R model:

$$y = \beta_0 + \beta_1x_1 + \beta_2x_2 + \dots + \beta_kx_k + u, \text{ with } n = n_1 + n_2 + \dots + n_m \text{ obs.}$$

Restrictions = $q = (m - 1)(k + 1)$ with slopes and intercept restrictions.

Restrictions = $q = (m - 1)k$ with just slopes restrictions.

$$df_{ur} = (n_1 + n_2 + \dots + n_k) - m(k + 1)$$

$$F_{q, [n - m(k + 1)]} = \frac{[SSR_r - (SSR_1 + SSR_2 \dots + SSR_m)]/q}{(SSR_1 + SSR_2 \dots + SSR_m)/[n - m(k + 1)]}$$