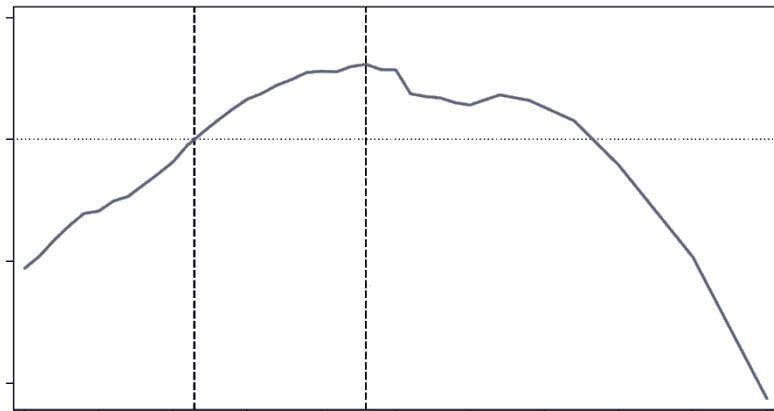


Optimal Progressivity of Personal Income Tax A General Equilibrium Evaluation for Spain

Darío Serrano-Puente (2020)

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Banco de España
DG of Economics, Statistics and Research

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- ❑ Is the Spanish economy positioned at its **optimal progressivity level in personal income tax?**

- ❑ What are the aggregate, distributional, and welfare consequences of moving towards such an optimal level?

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- ❑ Piketty (2015), Kopczuk (2019), Saez and Zucman (2019) → what are the **most effective policies to address economic inequality?**
- ❑ Now in Spain:
 - How to **finance the fiscal stimulus recovery plans** to alleviate the economic consequences of **COVID-19** crisis and the upcoming unavoidable **fiscal consolidation process**.
 - PGE 2021 → **a personal income tax (PIT) rate increase for the high-income earners**, i.e. an increase in the progressivity of the PIT.
- ❑ OECD (2020) → OECD average of $\frac{\text{PIT revenue}}{\text{Total tax revenue}}$ has been around **30-35%** in recent years.

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- ❑ A **heterogeneous households general equilibrium** model featuring:
 - **life-cycle profiles** → households face **uninsurable idiosyncratic labor productivity shocks** defining aging and retirement.
 - **dynamic elements** → households are born **inheriting some earnings abilities from their predecessors** (they are altruistic toward their descendants).
- ❑ Households decide **how much to work and how much to save**.
- ❑ Household income (labor, capital and other incomes) **taxed** with a **progressive** schedule.
- ❑ Social planner finds a **welfare-maximizing degree of progressivity** in the PIT.
- ❑ Model calibrated to replicate some **aggregate and distributional** characteristics of the **Spanish economy**.

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Main Findings

- ❑ Aggregate **social welfare maximized** when **progressivity level is increased** → average increase of 3.08% of consumption.
- ❑ The **poorest** working and non-working households **benefiting the most** and the **most efficient** working households and the **wealthiest** ones experiencing the **largest welfare losses**.
- ❑ **Reductions in wealth and income inequality** but negative effects on capital, labor, and output (**efficiency loss**).
- ❑ Households **between p20 and p80** → **decrease** in their effective average tax rates.
 - Ex.: Effective average tax rate within p40 and p60 would drop from 0.067 to 0.056.
- ❑ Households **above p80** → **drastic increment** in their effective average tax rate.
 - Ex.: Top 1% households from with an effective average tax rate change from 0.284 to 0.330.

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Broader Connections to Literature

- **Heterogeneous agents GE** models with incomplete markets → Huggett (1993), Aiyagari (1994), Krusell and Smith (1998), Quadrini (2000), De Nardi (2004).
- **Tax reform** evaluation with **GE** models for **Spain** → Pijoan-Mas and González Torrabadella (2006), Viegas and Ribeiro (2015).
- **Optimal taxation & progressivity** in a GE framework:
 - Conesa et al. (2009), Diamond and Saez (2011), Guner et al. (2017), Kindermann and Krueger (2018).
 - Conesa and Krueger (2006), Bakis et al. (2015), Heathcote et al. (2017), Díaz-Giménez and Pijoan-Mas (2019), Storesletten (2019).

Closest Match in Literature

- **Theoretical framework** → Castañeda et al. (2003).
- **Topic (Spain)** → Guner, N., J. López-Segovia, and R. Ramos (2020).

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- Setup → Castañeda et al. (2003 → modified version of the **stochastic neoclassical growth** model with **uninsured idiosyncratic risk** and no **aggregate uncertainty**).
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Main Features

- HHs that are **ex-ante identical**.
- Uninsured household-specific **shock** to HHs' endowments of efficiency labor units.
- HHs go through life cycle → **workers** or **retirees**.
- Once HHs retired → **probability of dying** → if HH dies, it is replaced by working-age descendant.
- HHs **altruistic** towards their descendants.

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I. Population & Endowment Dynamics

A measure one continuum of heterogeneous dynamic households endowed with ℓ **units of disposable time each period**.

Uncertainty in the model → Age and endowment of efficiency labor units

Controlled by one-dimensional shock, s , taking values:

- Worker → $s \in E = \{1, 2, \dots, J\}$
 - **Uninsured idiosyncratic stochastic process** determining their endowment of efficiency labor units → $e(s) > 0$
 - Exogenous positive **probability of retiring** → p_r → Jump from $s \in E$ to $s' \in R$.
- Retiree → $s \in R = \{J + 1, J + 2, \dots, 2J\}$
 - $e(s) = 0$
 - Exogenous positive **probability of dying** → $1 - p_s$.
 - If HH **dies** → Jump from $s \in R$ to $s' \in R$ → **replaced by a working-age descendant** that **inherits** the deceased household **estate**, a , and, possibly, some of its **earnings abilities**.

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$$\Gamma_{SS'} = \begin{bmatrix} \Gamma_{EE'} & \Gamma_{ER'} \\ \Gamma_{RE'} & \Gamma_{RR'} \end{bmatrix}$$

- $\Gamma_{EE'}$ → **working phase** of life cycle → stationary distr. of working HHs, γ_E^* .
- $\Gamma_{RR'}$ → **retirement phase** of life cycle → $\Gamma_{RR'} := \mathbf{I} p_s$.
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 - Intergenerational transmission of income → ϕ_1 transformation of γ_E^* .
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II. Preferences & Production Possibilities

- HHs value **consumption**, c , and **leisure**, $\ell - h \rightarrow$ they maximize:

$$E_0 \left[\sum_{t=0}^{\infty} \beta^t u(c, \ell - h) | s \right]$$

- Time discount factor $\rightarrow \beta$

Utility function

$$u(c, h) = \frac{c^{1-\sigma}}{1-\sigma} + \chi \frac{(\ell - h)^{1-\varphi}}{1-\varphi}$$

- Intertemporal elasticity of substitution of consumption $\rightarrow \frac{1}{\sigma}$
- Intertemporal elasticity of substitution of leisure $\rightarrow \frac{1}{\varphi}$
- Frisch elasticity of labor supply $\rightarrow \frac{(\ell-h)}{\varphi \cdot h}$

The Model Economy

II. Preferences & Production Possibilities

- Production technology transforms agg. capital, K , and agg. labor, L , into output, Y .

Production function

$$Y = A \cdot K^\alpha \cdot L^{1-\alpha}$$

- Total factor productivity $\rightarrow A = 1$
- Capital share $\rightarrow \alpha$
- Capital is assumed to depreciate geometrically at a constant rate $\rightarrow \delta$

- Wage, w , and interest rate, r \rightarrow from firms' profit maximization problem.

The Model Economy

III. Government Sector

- Total tax revenue, T , is used to finance government consumption, G , and transfers to retirees, Tr .

$$T = G + Tr$$

- Taxes levied on household income (from labor, capital and pensions), $y \rightarrow \tau(y)$.

Tax function → Augmented version of Heathcote et al. (2017)

$$\tau(y) = [y - \lambda^{1-\tau}] + \kappa \cdot y$$

- PIT schedule → $[y - \lambda^{1-\tau}]$, with average level of taxes, λ , and progressivity, τ .
- Other taxes (proportional to income) → $\kappa \cdot y$ → To match total tax revenues

- Transfers to retirees → $\omega(s)$

Recall

- If HH retired → $e(s) = 0$ and $\omega(s) > 0$ (constant for every retired HH, no dependent on past SS contributions)
- If HH worker → $e(s) > 0$ and $\omega(s) = 0$

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IV. Households' Decision Problem

- ❑ No insurance markets for the household-specific shock.
- ❑ Agents can save in the form of **riskless capital**, a , but they **cannot borrow**.

Bellman equation

Given individual state variables → s and a

$$v(a, s) = \max_{c, a', h} u(c, \ell - h) + \beta \sum_{s' \in S} \Gamma_{ss'} v(a', s')$$

$$s.t. \quad c + a' = y - \tau(y) + a$$

$$y = ar + e(s)hw + \omega(s)$$

$$\tau(y) = [y - \lambda y^{1-\tau}] + \kappa y$$

$$c \geq 0 \quad a' \in A \quad 0 \leq h \leq \ell$$

Solving household policy → $\{c(a, s), a'(a, s), h(a, s)\}$

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Calibration

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36 parameters

7 parameters

Normalization
conditions

29 parameters

Match characteristics of Spanish economy

Model Period → 1 Year
Base Calibration Year → 2015

7 parameters

Direct identification

22 parameters

Method of simulated
moments

Calibration

36 parameters

7 parameters
**Normalization
conditions**

29 parameters

Match characteristics of Spanish economy

Model Period → 1 Year
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Calibration

I. Normalization Conditions

- Endowment of **disposable time** → $\ell = 3.2$
- **Possible states** in which a HH can stay when worker or retiree → $J = 4$
- Endowment of efficiency **labor units of least productive HHs** → $e(1) = 1$
- **Diagonal elements** of submatrix $\Gamma_{EE'}$ → $\Gamma_{EE'_{1,1}}, \Gamma_{EE'_{2,2}}, \Gamma_{EE'_{3,3}}$ and $\Gamma_{EE'_{4,4}}$

Endowment process of working HHs

		$\Gamma_{EE'}$			
		$s' = 1$	$s' = 2$	$s' = 3$	$s' = 4$
$s = 1$	$e(1)$	$\Gamma_{EE'_{1,1}}$	$\Gamma_{EE'_{1,2}}$	$\Gamma_{EE'_{1,3}}$	$\Gamma_{EE'_{1,4}}$
$s = 2$	$e(2)$	$\Gamma_{EE'_{2,1}}$	$\Gamma_{EE'_{2,2}}$	$\Gamma_{EE'_{2,3}}$	$\Gamma_{EE'_{2,4}}$
$s = 3$	$e(3)$	$\Gamma_{EE'_{3,1}}$	$\Gamma_{EE'_{3,2}}$	$\Gamma_{EE'_{3,3}}$	$\Gamma_{EE'_{3,3}}$
$s = 4$	$e(4)$	$\Gamma_{EE'_{4,1}}$	$\Gamma_{EE'_{4,2}}$	$\Gamma_{EE'_{4,3}}$	$\Gamma_{EE'_{4,4}}$

Calibration

I. Normalization Conditions

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$s = 4$	$e(4)$	$\Gamma_{EE'_{4,1}}$	$\Gamma_{EE'_{4,2}}$	$\Gamma_{EE'_{4,3}}$	$\Gamma_{EE'_{4,4}}$

Calibration

II. Macro and Demographic Targets

- ❑ Time discount factor, $\beta = 0.96 \rightarrow {}^K/Y = 4.25$ capital-to-output \rightarrow BdE (2017,2019), Eurostat (2020), INE (2016) [Learn more...](#)
- ❑ Capital income share, $\alpha = 0.48 \rightarrow$ labor income share was 0.52 \rightarrow EU KLEMS (2020)
- ❑ Depreciation of capital, $\delta = 0.05 \rightarrow {}^I/Y = 0.22$ investment-to-output \rightarrow INE (2020)
- ❑ Curvature of consumption, $\sigma = 1.5 \rightarrow {}^1/\sigma = 0.66$ intertemporal elasticity of substitution of consumption \rightarrow Standard in literature
- ❑ Relative share of consumption and leisure in utility, $\chi = 0.5 \rightarrow {}^H/\ell = 0.31$ average hours worked \rightarrow INE (2011)
- ❑ Curvature of leisure, $\varphi = 2.65 \rightarrow {}^{(\ell-h)}/h \cdot \varphi$ Frisch elasticity of labor supply between 0.5 and 1.5 (Range in literature for Spain) and economy matching rest of targets

Calibration

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Calibration

II. Macro and Demographic Targets

- Probability of retiring, $p_r = 0.03 \rightarrow$ expected duration of working lives is 35 \rightarrow Eurostat (2020)
- Probability of surviving, $p_s = 0.96 \rightarrow$ expected duration of retirement is 22.8 \rightarrow OECD (2015,2017)
- Life-cycle profile controller, $\phi_1 = 0.99 \rightarrow$ ratio of the average annual wage of agents between ages 45 and 49 to that of agents between ages 25 and 29 is 1.56 \rightarrow INE (2017)
- Intergenerational income mobility controller, $\phi_2 = 0.9715 \rightarrow$ correlation between the average income of one generation and the average income of its immediate descendants is 0.5 \rightarrow Llaneras et al. (2020)

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Calibration

III. Government Policy

Recall → tax function specification:

$$\tau(y) = [y - \lambda^{1-\tau}] + \kappa \cdot y$$

Using **administrative microdata on tax returns** from AEAT(2019) at household level and an estimation methodology presented by García-Miralles, E., N. Guner, and R. Ramos (2019).

- ❑ Average level of taxes of PIT, $\lambda = 0.89$
- ❑ Progressivity of PIT, $\tau = 0.11$

See fitting of the estimation.

- ❑ Normalized transfers to retirees, $\omega = 3.22 \rightarrow {}^T r_Y = 0.11$ transfers-to-output (social security contributions) → OECD (2020)
- ❑ Linear term on remaining taxes, $\kappa = 0.05 \rightarrow {}^T r_Y = 0.33$ tax-revenue-to-output, ${}^G r_Y = 0.22$ tax-revenue-to-output → OECD (2020)

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Calibration

IV. Income and Wealth Distributions

Remaining parameters of the endowment process of working HHs calibrated to match → **Gini coefficients** and **shares** p0-p40, p40-p60, p60-p80, p80-p100, p90-p95, p95-p99, p99, p100 of:

- Income (before taxes after transfers) → AEAT (2019)
- Wealth (net) → BdE (2017, 2019)

Endowment process of working HHs

		$\Gamma_{EE'}$			
		$s' = 1$	$s' = 2$	$s' = 3$	$s' = 4$
$s = 1$	$e(1)$	$\Gamma_{EE'_{1,1}}$	$\Gamma_{EE'_{1,2}}$	$\Gamma_{EE'_{1,3}}$	$\Gamma_{EE'_{1,4}}$
$s = 2$	$e(2)$	$\Gamma_{EE'_{2,1}}$	$\Gamma_{EE'_{2,2}}$	$\Gamma_{EE'_{2,3}}$	$\Gamma_{EE'_{2,4}}$
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Calibration - Recap

36 parameters

7 parameters

Normalization
conditions

29 parameters

Match characteristics of Spanish economy

Model Period → 1 Year
Base Calibration Year → 2015

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Direct identification

22 parameters

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**$J, \ell, e(1)$, and
diagonal $\Gamma_{EE'}$**

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$\alpha, \delta, \sigma, \lambda, \tau, p_r$ and p_s

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Direct identification

$\alpha, \delta, \sigma, \lambda, \tau, p_r$ and p_s

Method of simulated moments

$\beta, \varphi, \chi, \omega, \kappa, \phi_1, \phi_2, e(2),$
 $e(3), e(4)$, off-diagonal $\Gamma_{EE'}$

Calibration - Recap

36 parameters

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 $e(3), e(4)$, off-diagonal $\Gamma_{EE'}$

Calibration algorithm

Calibration

V. Calibration Outcomes

- Stochastic process of **endowment of efficiency labor units**

$e(s)$	$\gamma_{\mathcal{E}}^*$	$\Gamma_{\mathcal{E}\mathcal{E}}$ from s to s'			
		$s' = 1$	$s' = 2$	$s' = 3$	$s' = 4$
$s = 1$	1.00	15.17	89.58	10.36	0.01
$s = 2$	2.71	65.15	2.42	96.54	1.03
$s = 3$	7.80	18.39	0.01	3.60	96.34
$s = 4$	90.00	1.28	0.01	1.73	0.01
					98.25

Note: $e(s)$ denotes the relative endowment of efficiency labor units; $\gamma_{\mathcal{E}}^*$ denotes the stationary distribution of working-age households; $\Gamma_{\mathcal{E}\mathcal{E}}$ denotes the transition probabilities of the process on the endowment of efficiency labor units for working-age households that are still workers one period later.

- Joint stochastic process of age and endowment of efficiency labor units.

Calibration

V. Calibration Outcomes

- Stochastic process of **endowment of efficiency labor units**

	$e(s)$	$\gamma_{\mathcal{E}}^*$	$\Gamma_{\mathcal{E}\mathcal{E}}$ from s to s'			
			$s' = 1$	$s' = 2$	$s' = 3$	$s' = 4$
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- Joint stochastic process of age and endowment of efficiency labor units.

Calibration

V. Calibration Outcomes

□ Fitness of the **baseline (BE)** model economy

Macroeconomic and fiscal ratios								
Economy	K/Y	I/Y	G/Y	T/Y	Tr/Y	H/ell	$\rho_{o,y}$	$\rho_{f,s}$
Spain	4.25	21.94	22.27	33.63	11.36	30.83	1.56	0.50
BE	4.26	22.00	22.27	33.51	11.24	30.78	1.53	0.50
Distributional statistics								
Economy	Gini	Percentiles (%)					Top groups (%)	
		< 40	40-60	60-80	80-100	90-95	95-99	99-100
<i>The distribution of income (before all taxes and after transfers)</i>								
Spain	0.48	12.72	13.84	21.19	52.25	11.01	13.40	12.07
BE	0.45	14.72	13.72	21.32	50.24	10.85	13.35	13.57
<i>The distribution of wealth</i>								
Spain	0.68	3.62	9.65	18.11	68.62	12.93	19.79	20.27
BE	0.68	3.80	9.32	17.45	69.43	13.54	19.68	19.63

Note: H/ell denotes the share of disposable time allocated to market activities; $\rho_{o,y}$ denotes the ratio of the average income of agents between ages 45 and 49 (old) to that of agents between ages 25 and 29 (young); $\rho_{f,s}$ denotes the correlation between the average income of one generation (fathers) and the average income of their immediate descendants (sons).

Calibration

V. Calibration Outcomes

□ Fitness of the **baseline (BE)** model economy

Macroeconomic and fiscal ratios								
Economy	K/Y	I/Y	G/Y	T/Y	Tr/Y	H/ell	$\rho_{o,y}$	$\rho_{f,s}$
Spain	4.25	21.94	22.27	33.63	11.36	30.83	1.56	0.50
BE	4.26	22.00	22.27	33.51	11.24	30.78	1.53	0.50
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Economy	Gini	Percentiles (%)				Top groups (%)		
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Spain	0.68	3.62	9.65	18.11	68.62	12.93	19.79	20.27
BE	0.68	3.80	9.32	17.45	69.43	13.54	19.68	19.63

Note: H/ell denotes the share of disposable time allocated to market activities; $\rho_{o,y}$ denotes the ratio of the average income of agents between ages 45 and 49 (old) to that of agents between ages 25 and 29 (young); $\rho_{f,s}$ denotes the correlation between the average income of one generation (fathers) and the average income of their immediate descendants (sons).

Optimal Progressivity

Optimal Progressivity

I. Selection of Optimal Progressivity Level

- Grid of progressivity levels in PIT $\rightarrow 0.00 \leq \tau \leq 0.50$
- For each τ , compute a **GE economy** with a combination of **progressivity**, τ , **average level of taxes**, λ , and **transfers** to retirees, ω , that delivers:



- A **Benthamite social planner** (identical weights to every household in the economy) maximizes social or aggregate welfare
- **Social welfare is maximized** where the **aggregate consumption equivalent variation (CEV)** reaches its maximum.

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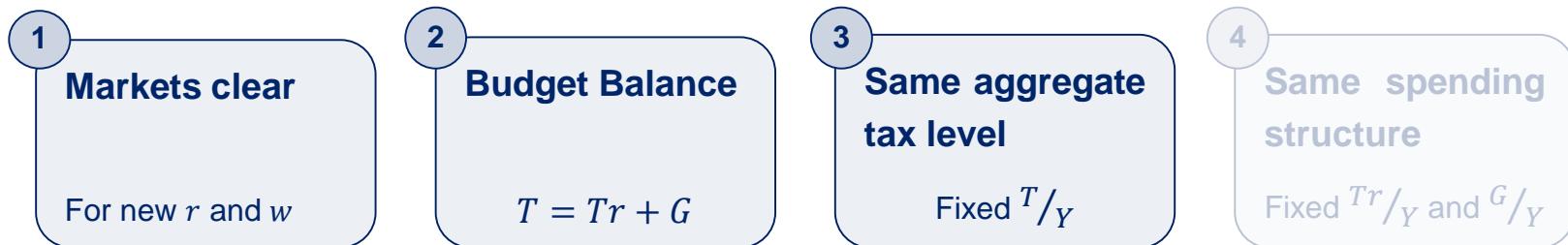


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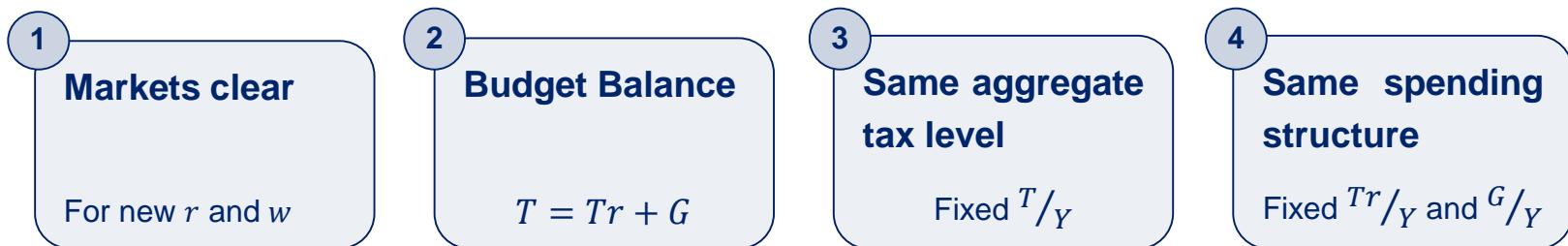


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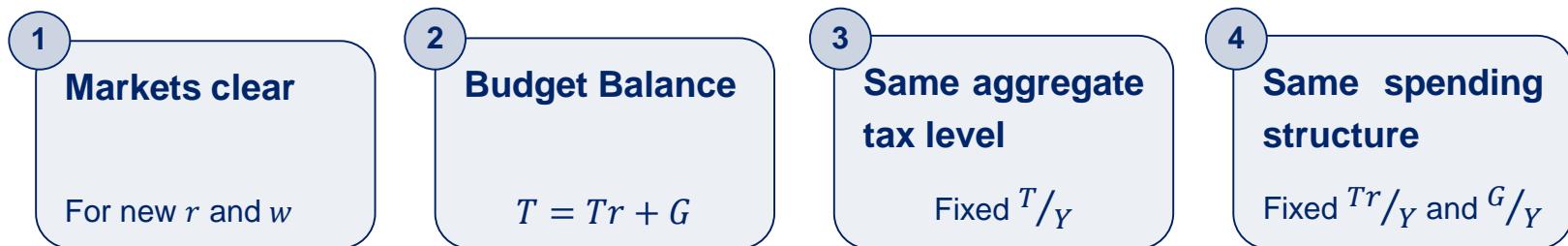


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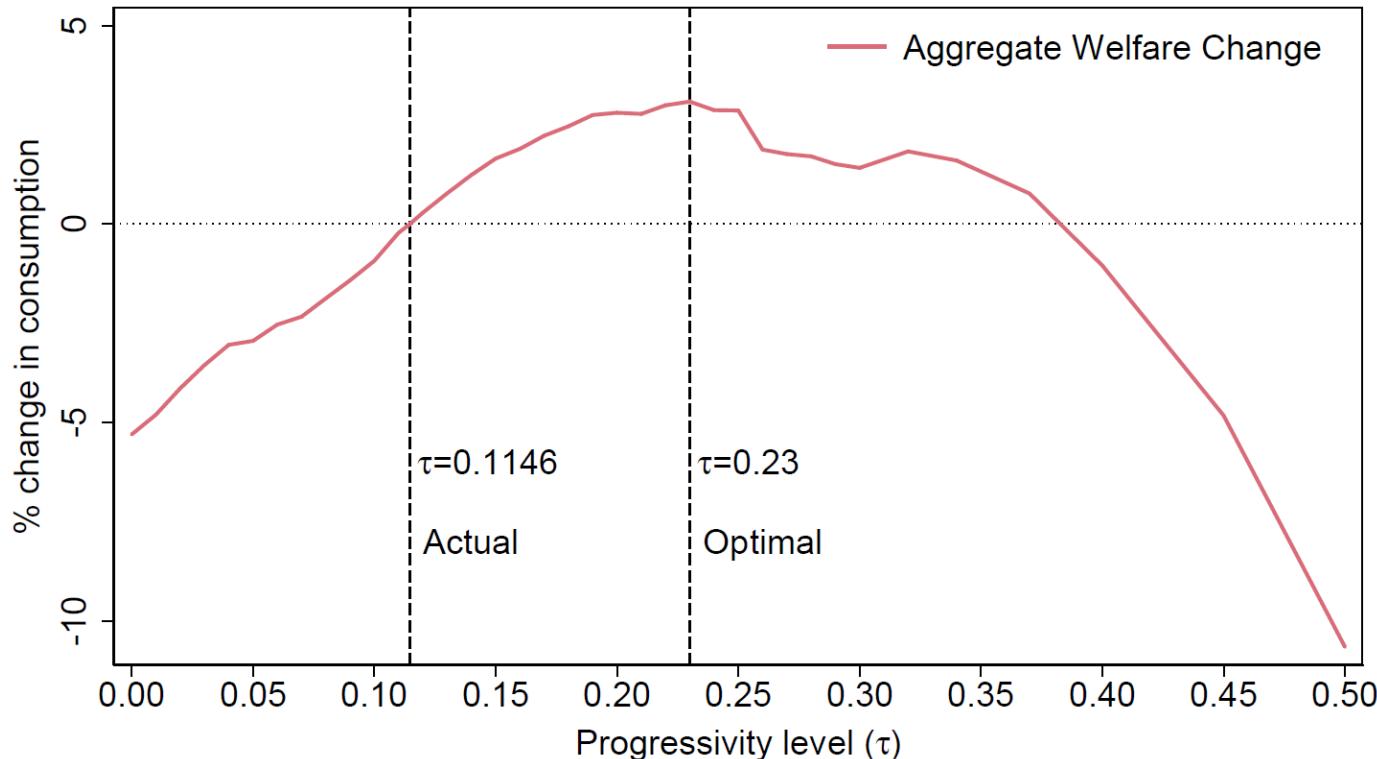


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- **Social welfare is maximized** where the **aggregate consumption equivalent variation (CEV)** reaches its maximum.

Optimal Progressivity

II. Aggregate Welfare Change

- Aggregate or **social welfare** is increased for a GE economy if **progressivity raises**.
- The **welfare-maximizing progressivity level** is $\tau = 0.23 \rightarrow \text{CEV} = 3,08\%$.



Optimal Progressivity

III. Decomposition of Aggregate Welfare Changes

Compute **optimal economy** (o):

- Ignoring** changes in **stationary distribution** of households (a)
- Ignoring** changes both in **stationary distribution** of households **and in equilibrium prices** (b)

Aggregate **CEV** can be decomposed as:

$$\text{CEV}_o = \underbrace{\text{CEV}_b}_{1} + \underbrace{(\text{CEV}_a - \text{CEV}_b)}_{2} + \underbrace{(\text{CEV}_o - \text{CEV}_a)}_{3}$$

Aggregate consumption equivalent variation	3.08%
Decomposition - Contributions (in %) to the aggregate welfare change by changes in:	
Tax system	121.38%
Equilibrium prices	-19.25%
Equilibrium distribution	-2.13%

Note: Each contribution to the aggregate welfare change is computed by dividing the consumption equivalent variation from changes in each factor by the aggregate consumption equivalent variation. Adding up three contributions makes one hundred percent.

Optimal Progressivity

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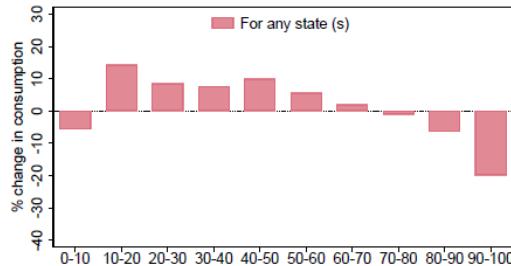
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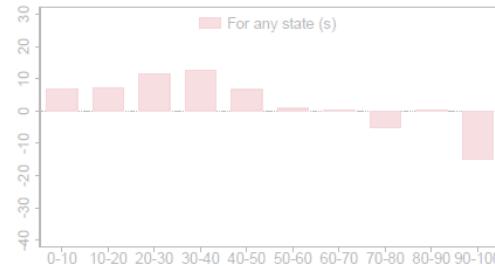
Optimal Progressivity

IV. Welfare Changes by Household Type

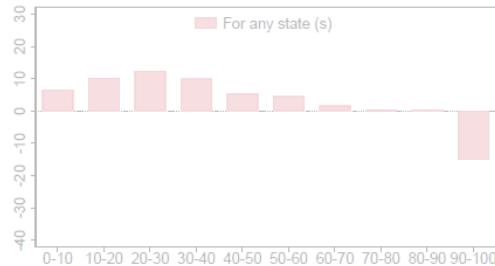
A: All Households Ranked by Wealth



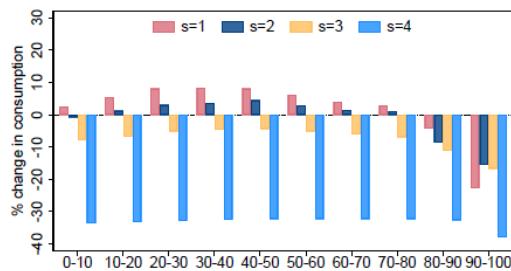
D: All Households Ranked by Income



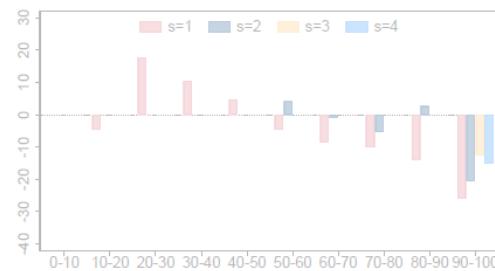
G: All Households Ranked by VF



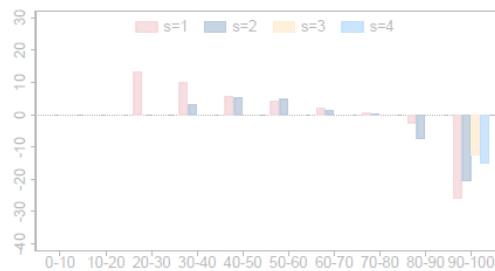
B: Workers Ranked by Wealth



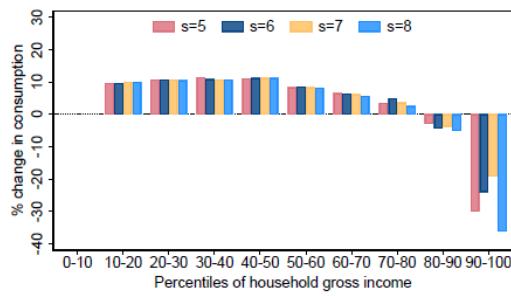
E: Workers Ranked by Income



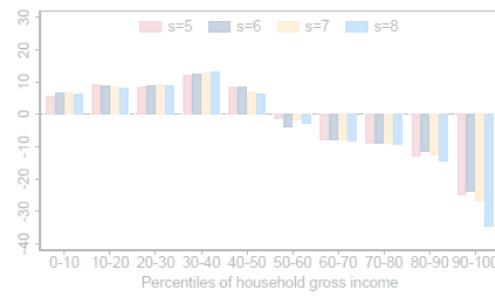
H: Workers Ranked by VF



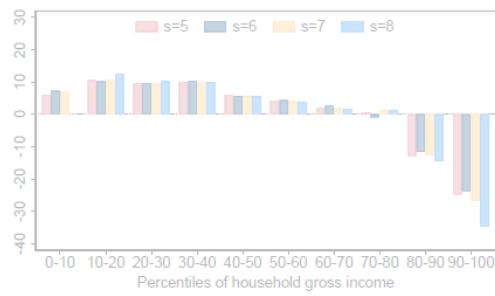
C: Non-Workers Ranked by Wealth



F: Non-Workers Ranked by Income



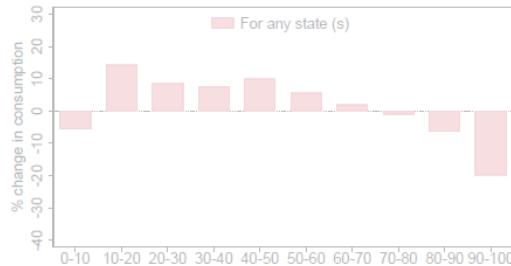
I: Non-Workers Ranked by VF



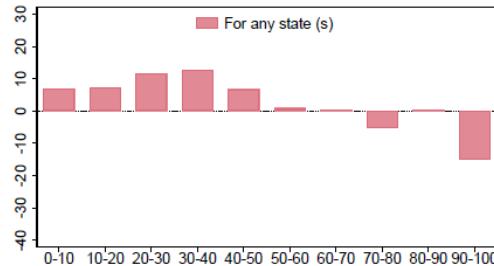
Optimal Progressivity

IV. Welfare Changes by Household Type

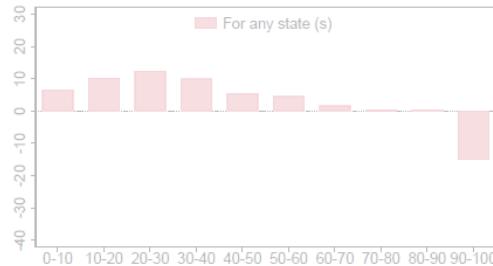
A: All Households Ranked by Wealth



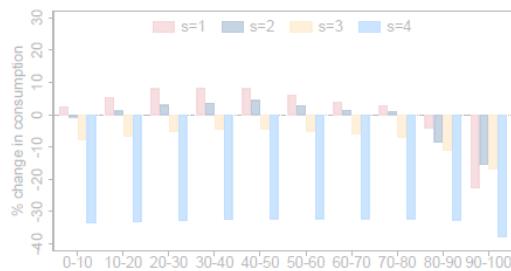
D: All Households Ranked by Income



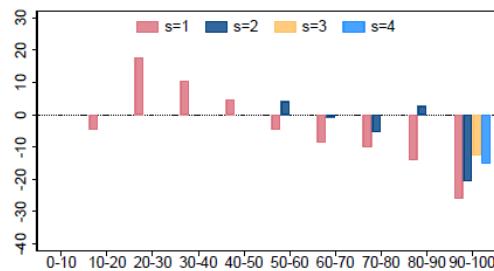
G: All Households Ranked by VF



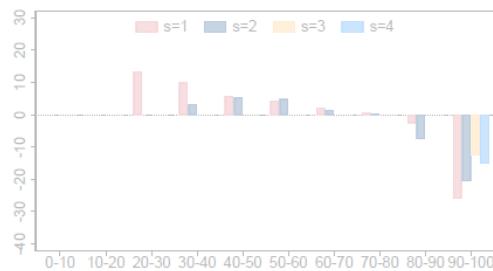
B: Workers Ranked by Wealth



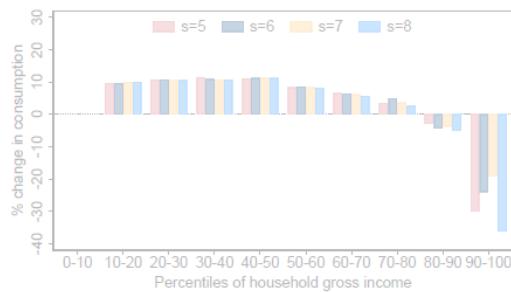
E: Workers Ranked by Income



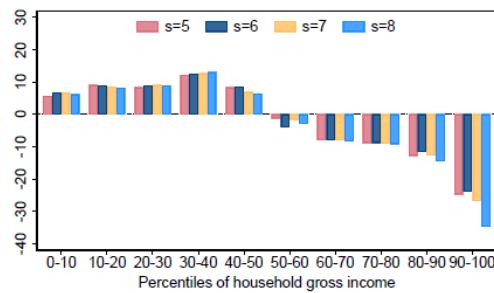
H: Workers Ranked by VF



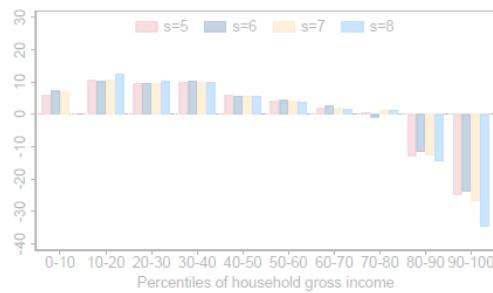
C: Non-Workers Ranked by Wealth



F: Non-Workers Ranked by Income



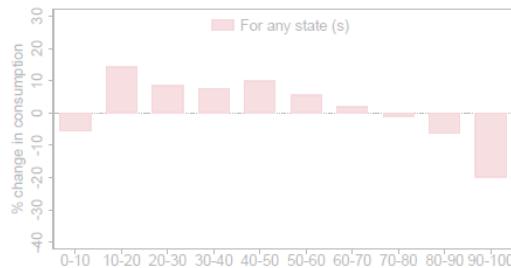
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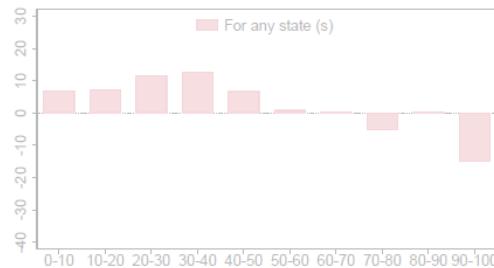
Optimal Progressivity

IV. Welfare Changes by Household Type

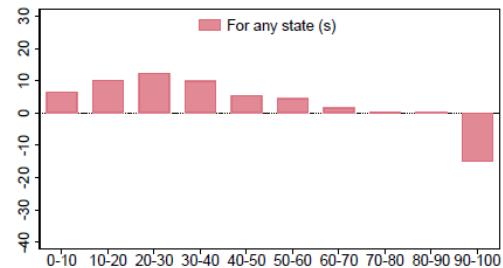
A: All Households Ranked by Wealth



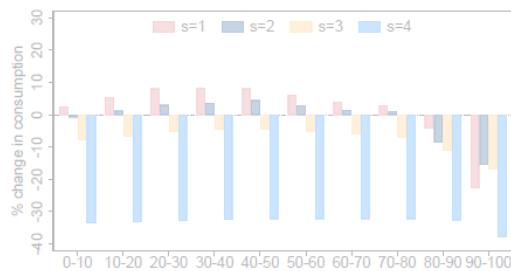
D: All Households Ranked by Income



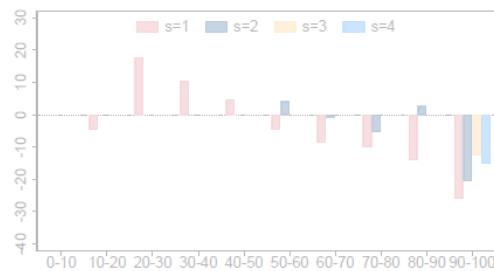
G: All Households Ranked by VF



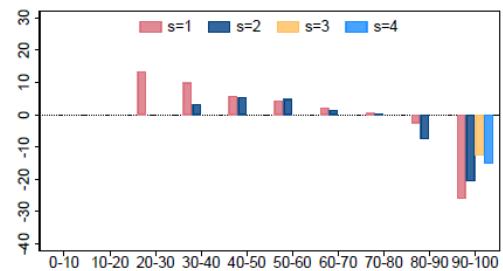
B: Workers Ranked by Wealth



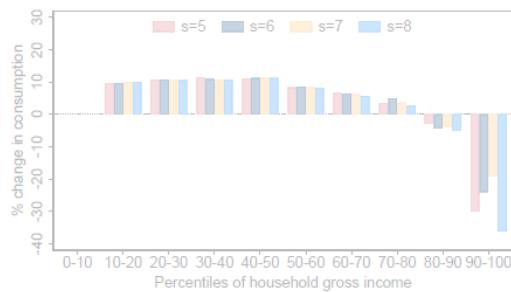
E: Workers Ranked by Income



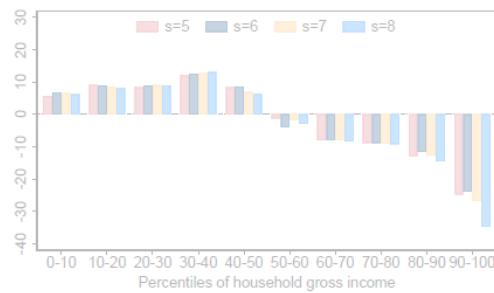
H: Workers Ranked by VF



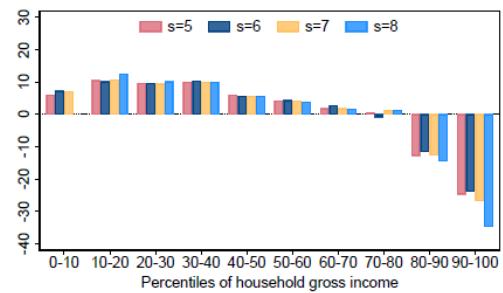
C: Non-Workers Ranked by Wealth



F: Non-Workers Ranked by Income



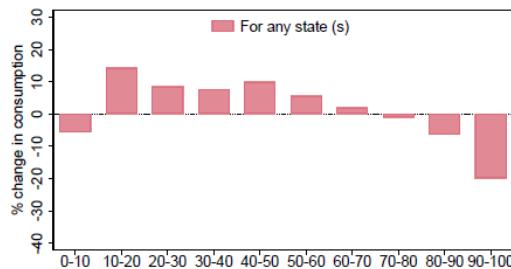
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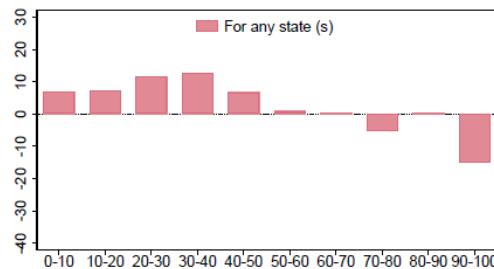
Optimal Progressivity

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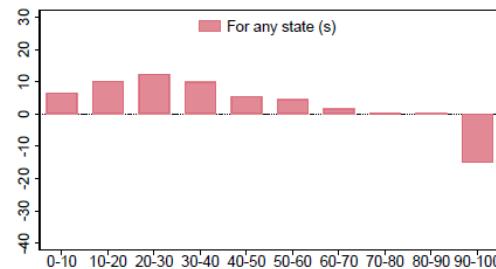
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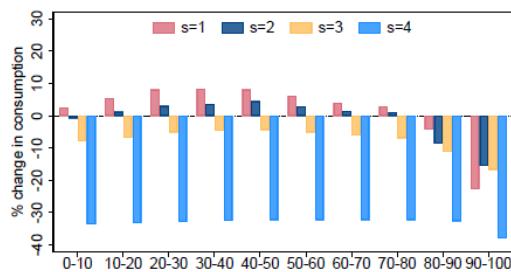
D: All Households Ranked by Income



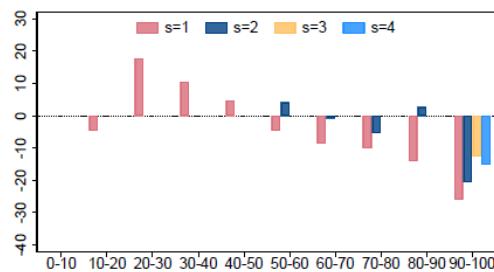
G: All Households Ranked by VF



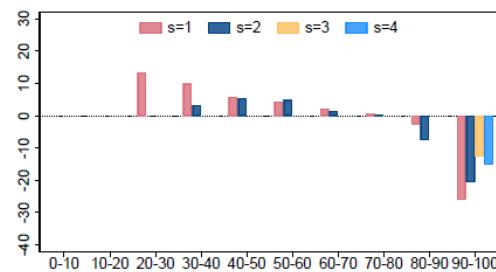
B: Workers Ranked by Wealth



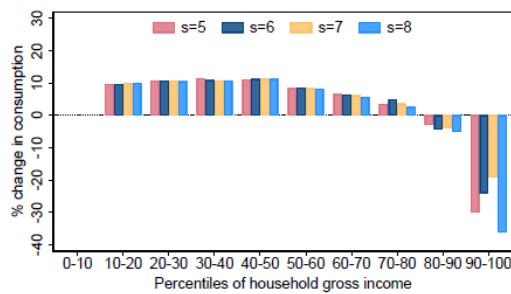
E: Workers Ranked by Income



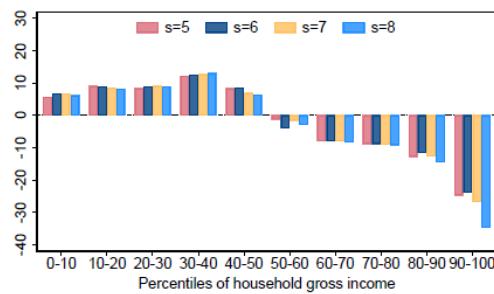
H: Workers Ranked by VF



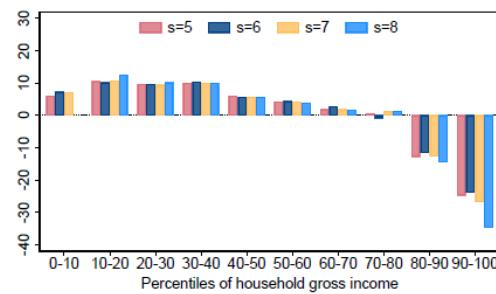
C: Non-Workers Ranked by Wealth



F: Non-Workers Ranked by Income

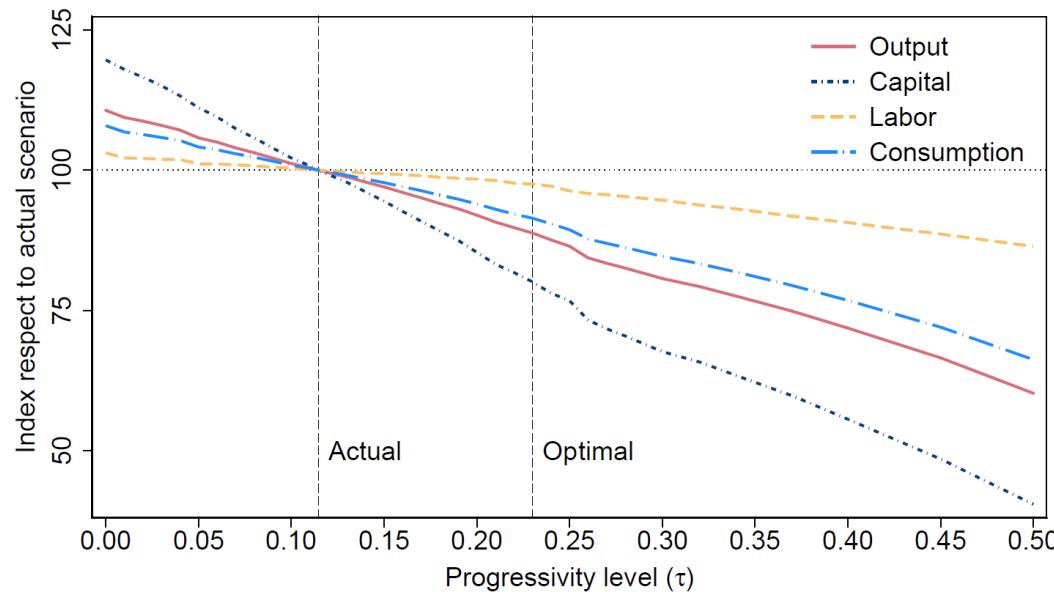


I: Non-Workers Ranked by VF



Optimal Progressivity

V. Effects on Macroeconomic and Fiscal Aggregates

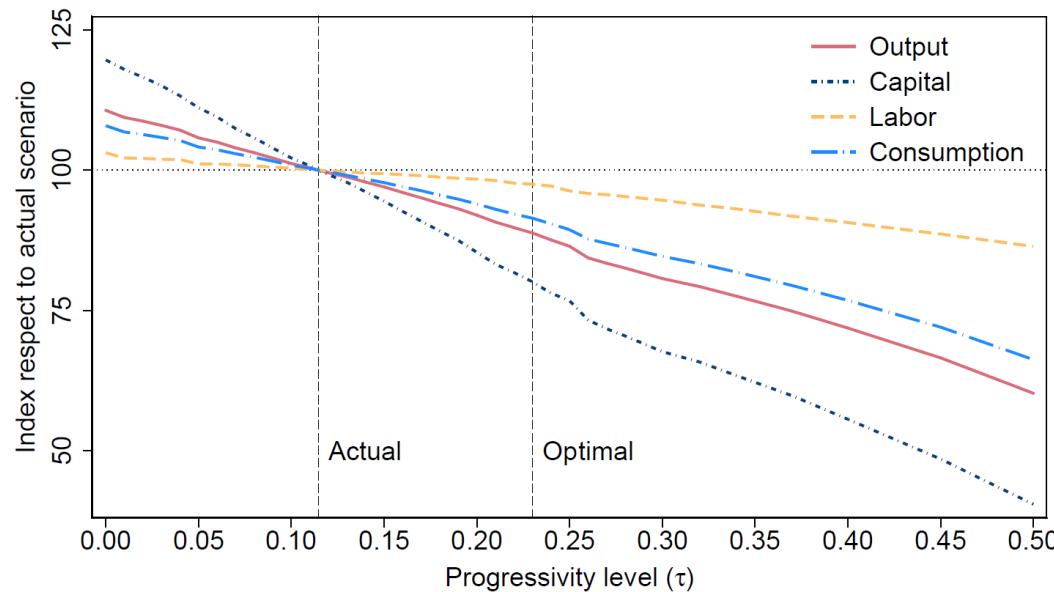


Economy	Y	K	L^*	H^{**}/ℓ	K/L	L/H	Y/H	K/Y	I/Y	G/Y	T/Y	Tr/Y
E_{BE}	11.29	48.12	3.03	30.78	15.88	3.08	11.46	4.26	22.00	22.27	33.51	11.24
$E_{0.23}$	10.02	38.55	2.96	29.66	13.05	3.11	10.56	3.85	19.85	22.27	33.51	11.24
% change	-11.25	-19.89	-2.31	-3.64	17.84	1.17	-7.86	-9.79	-9.80	0.00	0.00	0.00

Note: * L denotes aggregate labor input; ** H/ℓ denotes the share of disposable time allocated to market activities.

Optimal Progressivity

V. Effects on Macroeconomic and Fiscal Aggregates



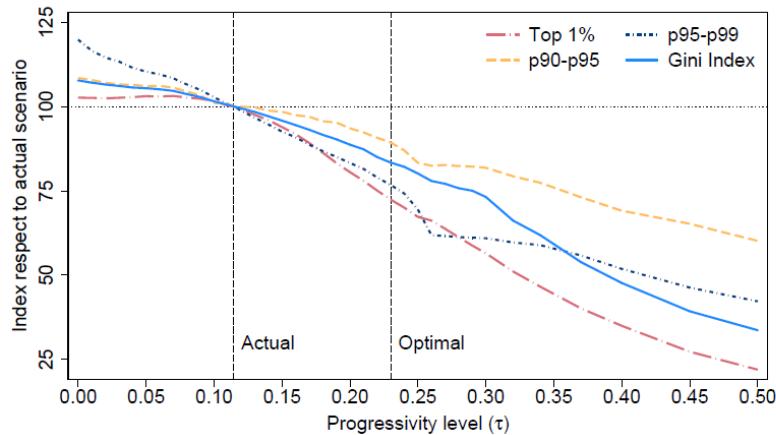
Economy	Y	K	L^*	H^{**}/ℓ	K/L	L/H	Y/H	K/Y	I/Y	G/Y	T/Y	Tr/Y
E_{BE}	11.29	48.12	3.03	30.78	15.88	3.08	11.46	4.26	22.00	22.27	33.51	11.24
$E_{0.23}$	10.02	38.55	2.96	29.66	13.05	3.11	10.56	3.85	19.85	22.27	33.51	11.24
% change	-11.25	-19.89	-2.31	-3.64	-17.84	1.17	-7.86	-9.79	-9.80	0.00	0.00	0.00

Note: * L denotes aggregate labor input; ** H/ℓ denotes the share of disposable time allocated to market activities.

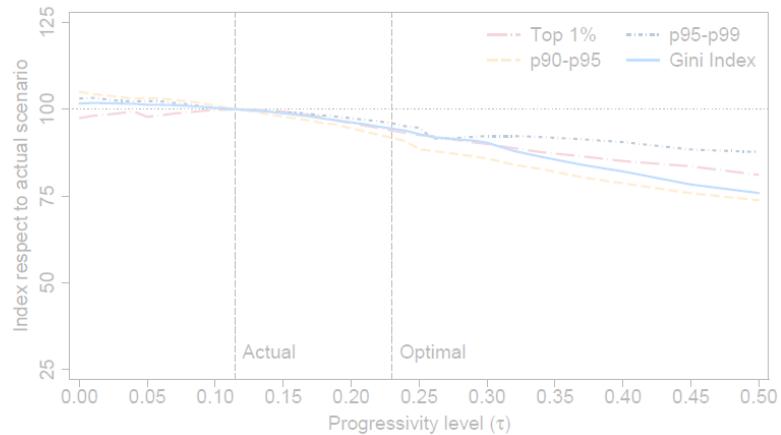
Optimal Progressivity

VI. Effects on Income and Wealth Inequality

Panel A: Wealth Inequality



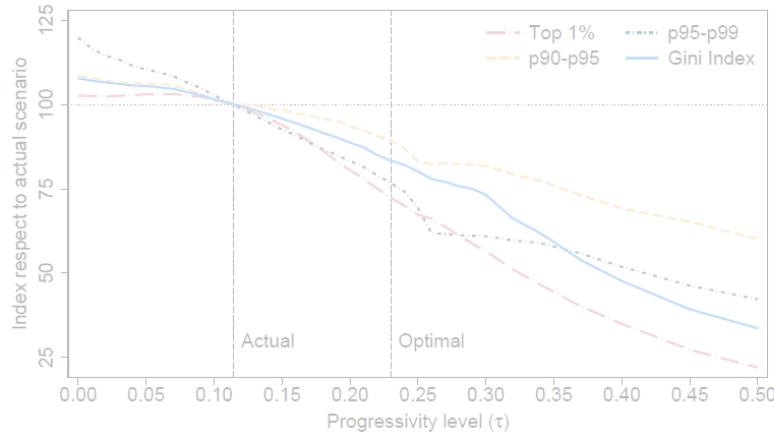
Panel B: Income Inequality



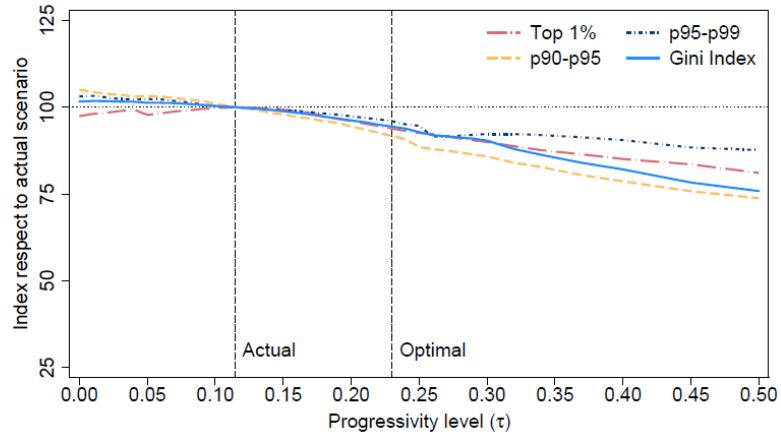
Optimal Progressivity

VI. Effects on Income and Wealth Inequality

Panel A: Wealth Inequality



Panel B: Income Inequality



Optimal Progressivity

VI. Effects on Income and Wealth Inequality

Economy	Gini	Percentiles (%)				Top groups (%)		
		< 40	40-60	60-80	80-100	90-95	95-99	99-100
<i>The distribution of income (before all taxes and after transfers)</i>								
E_{BE}	0.45	14.72	13.72	21.32	50.24	10.85	13.35	13.57
$E_{0.23}$	0.42	15.96	14.55	21.40	48.09	9.95	12.81	12.73
% change	-5.60	8.41	6.09	0.36	-4.28	-8.32	-4.04	-6.15
<i>The distribution of wealth</i>								
E_{BE}	0.68	3.80	9.32	17.45	69.43	13.54	19.68	19.63
$E_{0.23}$	0.56	7.57	13.41	21.47	57.55	12.10	15.10	14.21
% change	-16.62	99.05	43.98	23.02	-17.11	-10.66	-23.28	-27.62

Optimal Progressivity

VI. Effects on Income and Wealth Inequality

Economy	Gini	Percentiles (%)				Top groups (%)		
		< 40	40-60	60-80	80-100	90-95	95-99	99-100
<i>The distribution of income (before all taxes and after transfers)</i>								
E_{BE}	0.45	14.72	13.72	21.32	50.24	10.85	13.35	13.57
$E_{0.23}$	0.42	15.96	14.55	21.40	48.09	9.95	12.81	12.73
% change	-5.60	8.41	6.09	0.36	-4.28	-8.32	-4.04	-6.15
<i>The distribution of wealth</i>								
E_{BE}	0.68	3.80	9.32	17.45	69.43	13.54	19.68	19.63
$E_{0.23}$	0.56	7.57	13.41	21.47	57.55	12.10	15.10	14.21
% change	-16.62	99.05	43.98	23.02	-17.11	-10.66	-23.28	-27.62

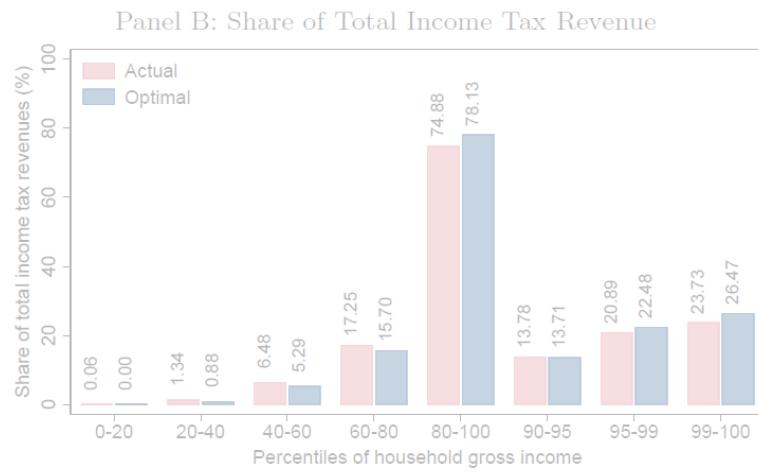
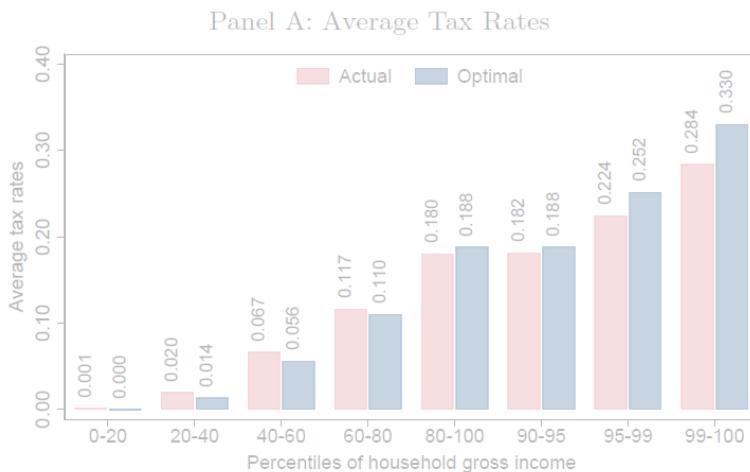
Optimal Progressivity

VII. Who Pays the Reform?

- Compute changes in **effective average PIT rate** over the **model income distribution**.

	Income percentiles (%)				Income top groups (%)			
	< 20	20-40	40-60	60-80	80-100	90-95	95-99	99-100
% change	-53.42	-34.64	-16.17	-5.33	4.04	3.68	12.13	16.21

- Evaluate changes in **effective average PIT rate** over the **actual income distribution** with administrative tax microdata at HH level → AEAT (2019).



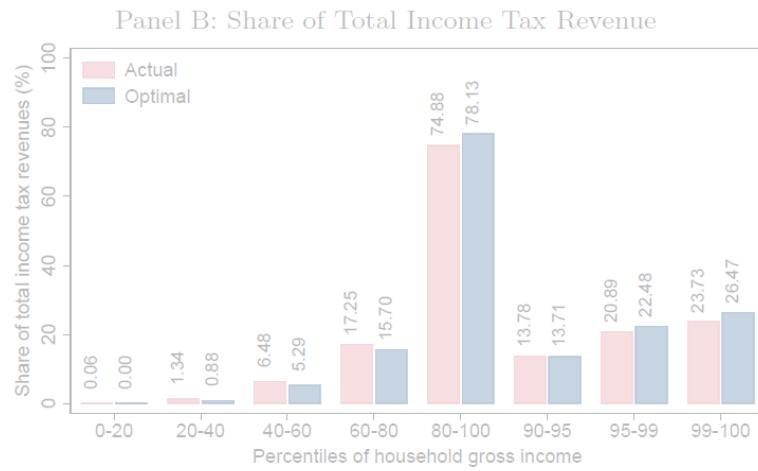
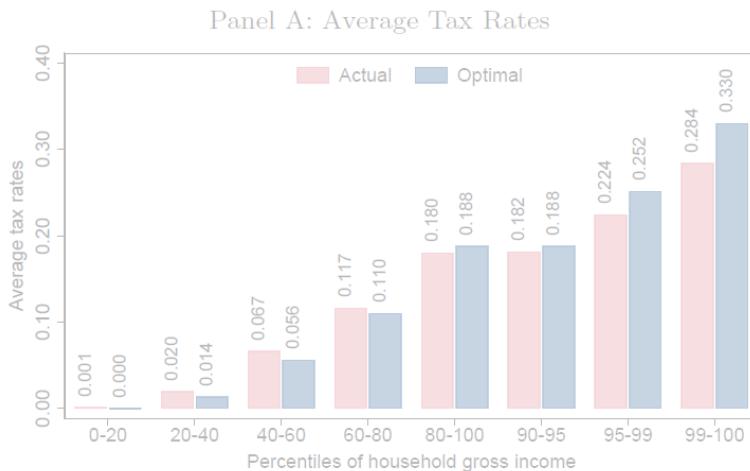
Optimal Progressivity

VII. Who Pays the Reform?

- Compute changes in **effective average PIT rate** over the **model income distribution**.

	Income percentiles (%)				Income top groups (%)			
	< 20	20-40	40-60	60-80	80-100	90-95	95-99	99-100
% change	-53.42	-34.64	-16.17	-5.33	4.04	3.68	12.13	16.21

- Evaluate **changes in effective average PIT rate** over the **actual income distribution** with administrative tax microdata at HH level → AEAT (2019).



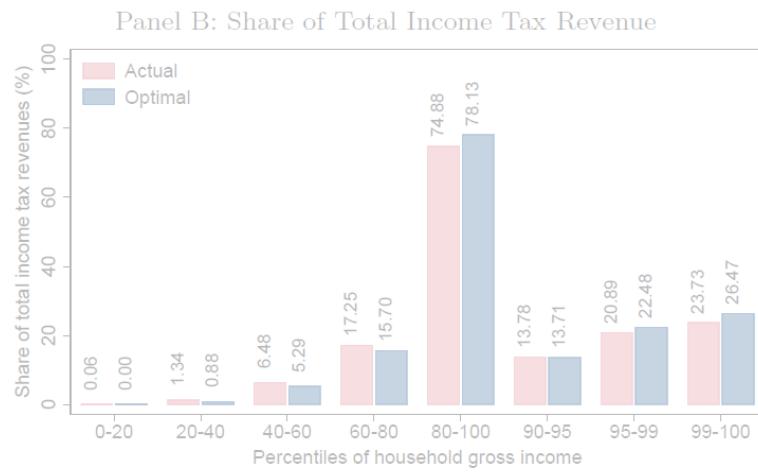
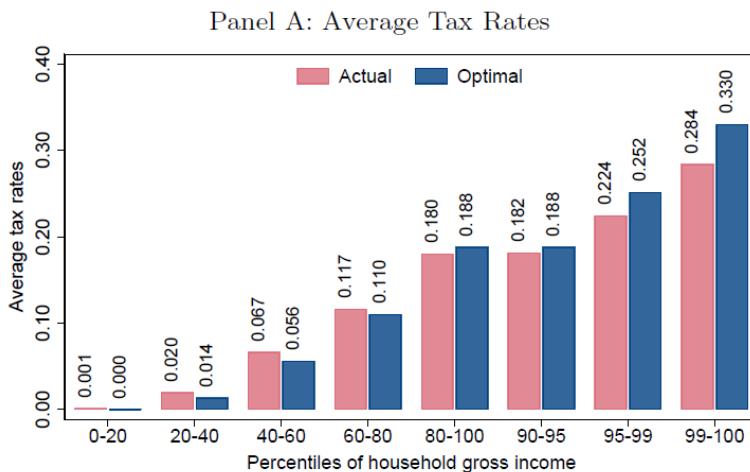
Optimal Progressivity

VII. Who Pays the Reform?

- Compute changes in effective average PIT rate over the model income distribution.

	Income percentiles (%)				Income top groups (%)			
	< 20	20-40	40-60	60-80	80-100	90-95	95-99	99-100
% change	-53.42	-34.64	-16.17	-5.33	4.04	3.68	12.13	16.21

- Evaluate changes in effective average PIT rate over the actual income distribution with administrative tax microdata at HH level → AEAT (2019).



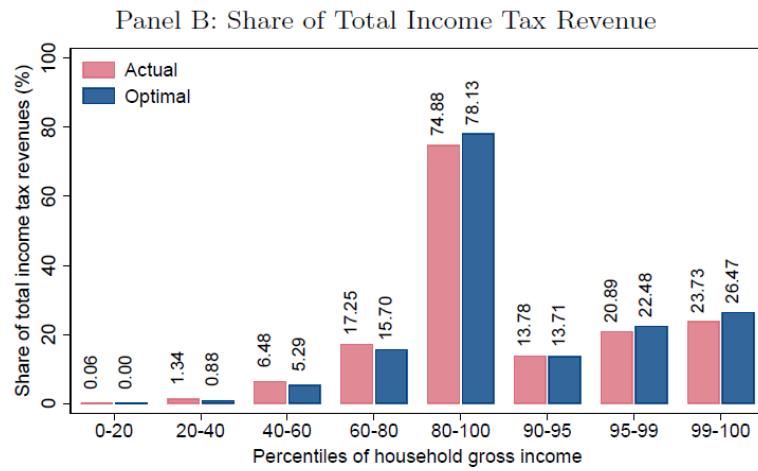
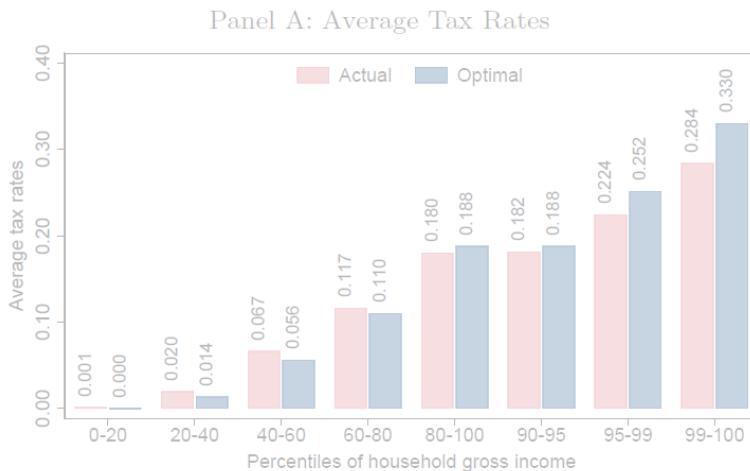
Optimal Progressivity

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Concluding Remarks

Conclusions – Q&A

- ❑ A **heterogeneous households general equilibrium** model featuring **life-cycle** and **dynastic** elements.
- ❑ Evaluate bunch of **progressivity reforms** in PIT.
- ❑ Elevating progressivity to a higher level than actual → **aggregate welfare gains**.
- ❑ Welfare-maximizing progressivity reform → τ from 0.11 to 0.23 → CEV = 3.08%.
- ❑ Most of gains → **poorest households** facing **lower effective** income tax rates and **richest households** affronting **higher effective** income tax rates.
- ❑ The **poorest working and non-working households** **benefiting the most** and the **most efficient working households** and the **wealthiest ones** experiencing the **largest trade-off and welfare losses**.
- ❑ Reductions in wealth and income inequality but negative effects on capital, labor, and output (**efficiency loss**).
- ❑ Households between p20 and p80 → decrease in their **effective average tax rates**.
 - Ex.: Effective average tax rate within p40 and p60 would drop from 0.067 to 0.056.
- ❑ Households above p80 → **drastic increment** in their **effective average tax rate**.
 - Ex.: Top 1% households from with an effective average tax rate change from 0.284 to 0.330.

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Other research questions:

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- ❑ Transitional dynamics → here only steady-state comparisons
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- ❑ Endogenous retirement decision vs. exogenous.
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- ❑ Firm heterogeneity (some degree of monopolistic power) → here only representative firm.
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Thank you!



A screenshot of a Twitter post from Darío Serrano-Puente (@darioserranopuente). The post features a profile picture of a man in a suit, a dark blue header with the text "Darío Serrano-Puente" and "@darioserranopuente", and a dark blue body with white text. The main message in the body reads: "This was a nice paper and presentation." Below this, a list item is shown with the icon for a note or list item (a circle with an 'i') followed by the text: "Official sources stated that is false and misleading". At the bottom of the post, the timestamp "10:38 AM · 11/17/20 · Twitter for iPhone" is visible.

Darío Serrano-Puente
@darioserranopuente

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Appendix

Appendix

I. Transition between Retirees and Descendants

[Return](#)

□ Mass-shifting procedure to depict submatrix $\Gamma_{RE'}$

■ Step 1

$$p_{51} = \gamma_1^* + \phi_1\gamma_2^* + \phi_1^2\gamma_3^* + \phi_1^3\gamma_4^*$$

$$p_{52} = (1 - \phi_1)[\gamma_2^* + \phi_1\gamma_3^* + \phi_1^2\gamma_4^*]$$

$$p_{53} = (1 - \phi_1)[\gamma_3^* + \phi_1\gamma_4^*]$$

$$p_{54} = (1 - \phi_1)\gamma_4^*$$

$$p_{61} = (1 - \phi_1)\gamma_1^*$$

$$p_{62} = \phi_1\gamma_1^* + \gamma_2^* + \phi_1\gamma_3^* + \phi_1^2\gamma_4^*$$

$$p_{63} = (1 - \phi_1)[\gamma_3^* + \phi_1\gamma_4^*]$$

$$p_{64} = (1 - \phi_1)\gamma_4^*$$

$$p_{71} = (1 - \phi_1)\gamma_1^*$$

$$p_{72} = (1 - \phi_1)[\phi_1\gamma_1^* + \gamma_2^*]$$

$$p_{73} = \phi_1^2\gamma_1^* + \phi_1\gamma_2^* + \gamma_3^* + \phi_1\gamma_4^*$$

$$p_{74} = (1 - \phi_1)\gamma_4^*$$

$$p_{81} = (1 - \phi_1)\gamma_1^*$$

$$p_{82} = (1 - \phi_1)[\phi_1\gamma_1^* + \gamma_2^*]$$

$$p_{83} = (1 - \phi_1)[\phi_1^2\gamma_1^* + \phi_1\gamma_2^* + \gamma_3^*]$$

$$p_{84} = \phi_1^3\gamma_1^* + \phi_1^2\gamma_2^* + \phi_1\gamma_3^* + \gamma_4^*$$

■ Step 2

$$p_{i1} = p_{i1} + \phi_2 p_{i2} + \phi_2^2 p_{i3} + \phi_2^3 p_{i4}$$

$$p_{i2} = (1 - \phi_2)[p_{i2} + \phi_2 p_{i3} + \phi_2^2 p_{i4}]$$

$$p_{i3} = (1 - \phi_2)[p_{i3} + \phi_2 p_{i4}]$$

$$p_{i4} = (1 - \phi_2)p_{i4}$$

Appendix

II. Help for Target Calculation

[Return](#)

- $\frac{K}{Y}$ is calculated:

$$\frac{\text{HH net wealth}}{\text{GDP}} = \frac{247,523\text{€}}{\frac{1,007,590,000\text{€}}{\left(\frac{\text{Population}}{\text{People per household}}\right)}} = 4,25$$

- I is the sum of:

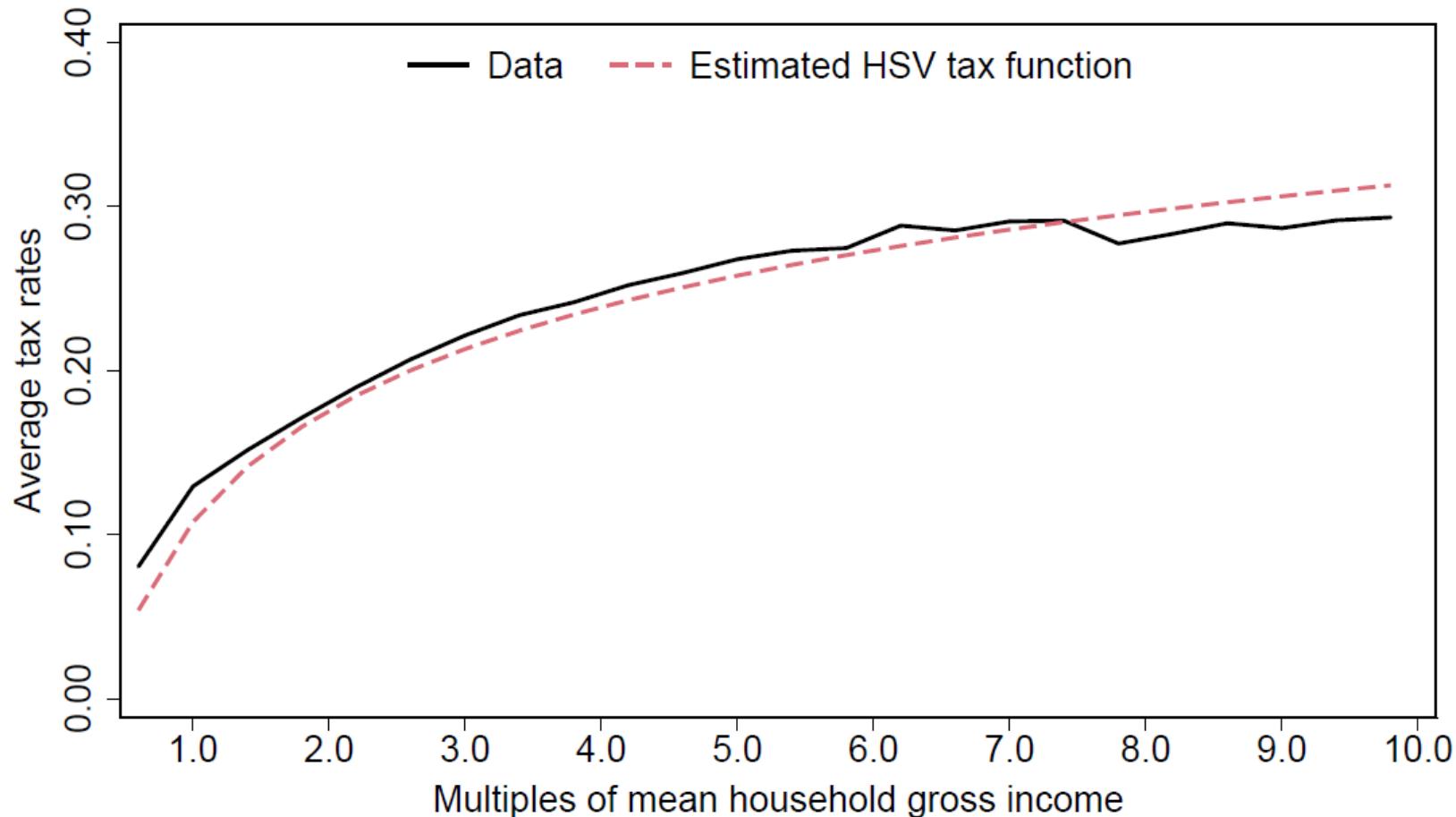
- gross private fixed domestic investment
- change in business inventories
- 75% of the private consumption expenditures in consumer durables (durables share in the total reported private consumption expenditures is 5%)

□ $\delta = \frac{K}{Y} = \frac{\frac{I}{Y}}{\frac{K}{Y}} = 0.0516$

Appendix

III. Fitting of The HSV Specification to Data (HHs, 2015)

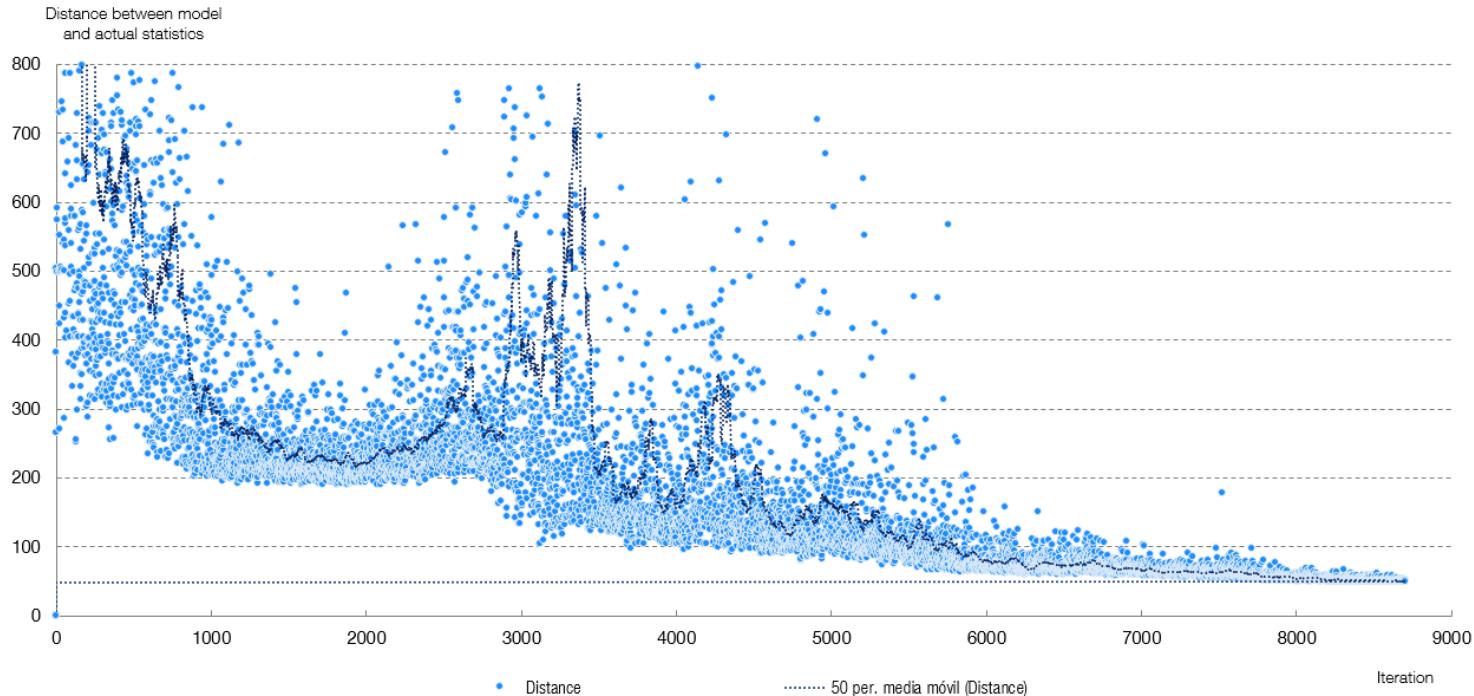
[Return](#)



Appendix

IV. Calibration Algorithm (Last 9,000 iterations)

[Return](#)



- ❑ Find in whole parameter space → Covariance-Matrix Adaptation - Evolutionary Strategy
- ❑ Minimize distance between model statistics and observed statistics
- ❑ 25,000 iterations of the model
- ❑ 1 minute per iteration in workstation → 38,192,544 search points per iteration

Appendix

V. Joint Age and Endowment Stochastic Process

[Return](#)

□ Joint stochastic process of age and endowment of efficiency labor units

$e(s)$	γ^*	Γ_{SS} from s to s'							
		$s' = 1$	$s' = 2$	$s' = 3$	$s' = 4$	$s' = 5$	$s' = 6$	$s' = 7$	$s' = 8$
$s = 1$	1.00	19.43	87.02	10.06	0.01	0.05	2.86	0.00	0.00
$s = 2$	2.71	35.18	2.35	93.78	1.00	0.01	0.00	2.86	0.00
$s = 3$	7.80	5.59	0.01	3.50	93.59	0.04	0.00	0.00	2.86
$s = 4$	90.00	0.35	0.01	1.68	0.01	95.44	0.00	0.00	2.86
$s = 5$	0.00	12.66	4.39	0.01	0.02	0.01	95.61	0.00	0.00
$s = 6$	0.00	22.92	4.26	0.13	0.02	0.02	0.00	95.61	0.00
$s = 7$	0.00	3.64	4.14	0.12	0.13	0.01	0.00	0.00	95.61
$s = 8$	0.00	0.23	4.03	0.12	0.23	0.13	0.00	0.00	95.61

Note: $e(s)$ denotes the relative endowments of efficiency labor units; γ^* denotes the stationary distribution households; Γ_{SS} denotes the transition probabilities of the process on the endowment of efficiency labor units and age.

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Appendix

VI. PGE 2021 – PIT proposed reform

[Return](#)

- Increase of the marginal labor income tax by 2 p.p. for people who earn above 130,000€ and 4 percentage points for people with earnings above 300,000€.
- Increase of the marginal capital income tax by 4 percentage points for all capital incomes above €140,000.
- Elimination or decrease of tax deductions due to contributions to private pension plans.
- Change in estimated progressivity → from $\tau = 0.1146$ to $\tau = 0.1203$ → **no welfare effect**



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