

# Overview of Reinforcement Learning-Part II

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# Major Components of an RL Agent

- An RL agent may include one or more of these components:
  - Policy: agent's behaviour function
  - Value function: how good is each state and/or action
  - Model: agent's representation of the environment

- A **policy** is the agent's behaviour
- It is a map from state to action, e.g.
- Deterministic policy:  $a = \pi(s)$
- Stochastic policy:  $\pi(a|s) = \mathbb{P}[A_t = a | S_t = s]$

# Value Function (1)

- Value function is a prediction of future reward
- Used to evaluate the goodness/badness of states
- And therefore to select between actions, e.g.

$$v_{\pi}(s) = \mathbb{E}_{\pi} [R_{t+1} + \gamma R_{t+2} + \gamma^2 R_{t+3} + \dots \mid S_t = s]$$

# Value Function (2)

- ▶ A **value function** is a prediction of future reward
  - ▶ “How much reward will I get from action  $a$  in state  $s$ ?”
- ▶  **$Q$ -value function** gives expected total reward
  - ▶ from state  $s$  and action  $a$
  - ▶ under policy  $\pi$
  - ▶ with discount factor  $\gamma$

$$Q^{\pi}(s, a) = \mathbb{E} [r_{t+1} + \gamma r_{t+2} + \gamma^2 r_{t+3} + \dots \mid s, a]$$

- ▶ Value functions decompose into a Bellman equation

$$Q^{\pi}(s, a) = \mathbb{E}_{s', a'} [r + \gamma Q^{\pi}(s', a') \mid s, a]$$

# Value Function (3)

- ▶ An optimal value function is the maximum achievable value

$$Q^*(s, a) = \max_{\pi} Q^{\pi}(s, a) = Q^{\pi^*}(s, a)$$

- ▶ Once we have  $Q^*$  we can act optimally,

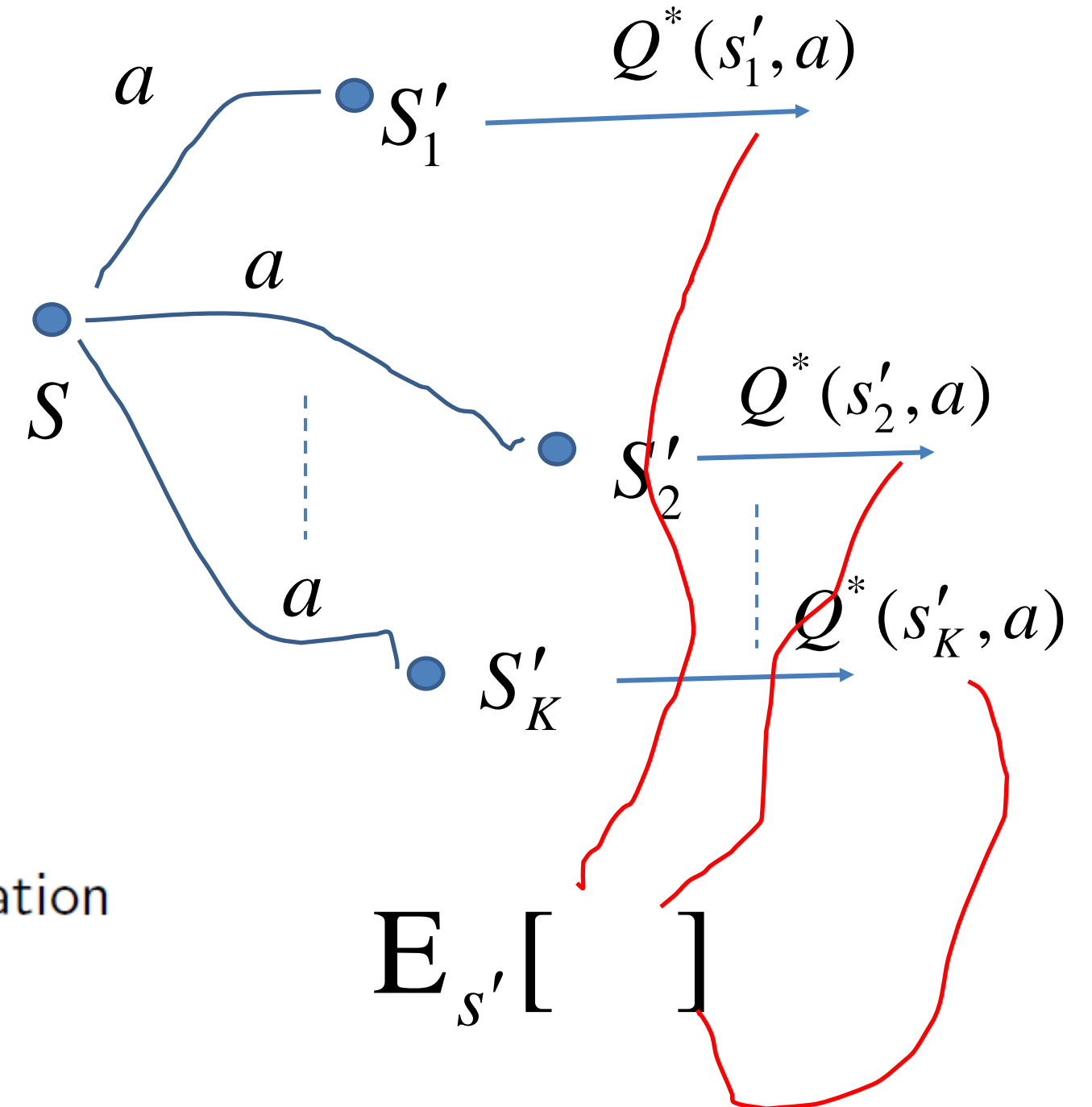
$$\pi^*(s) = \operatorname{argmax}_a Q^*(s, a)$$

- ▶ Optimal value maximises over all decisions. Informally:

$$\begin{aligned} Q^*(s, a) &= r_{t+1} + \gamma \max_{a_{t+1}} r_{t+2} + \gamma^2 \max_{a_{t+2}} r_{t+3} + \dots \\ &= r_{t+1} + \gamma \max_{a_{t+1}} Q^*(s_{t+1}, a_{t+1}) \end{aligned}$$

- ▶ Formally, optimal values decompose into a Bellman equation

$$Q^*(s, a) = \mathbb{E}_{s'} \left[ r + \gamma \max_{a'} Q^*(s', a') \mid s, a \right]$$



# Example of Value Function

- Each square represents a state
- **The return value is -1** everywhere on each transition
- **4 actions** for each state: north, south, east, west
- **Goal states** are the upper left corner and lower right corner

0	-14	-20	-22
-14	-18	-22	-20
-20	-22	-18	-14
-22	-20	-14	0

Value function for  
randomly policy

0	-1	-2	-3
-1	-2	-3	-2
-2	-3	-2	-1
-3	-2	-1	0

Optimal Value  
function

	←	←	↙
↑	↑	↖	↓
↑	↖	↘	↓
↙	→	→	

Optimal Policy



# Model

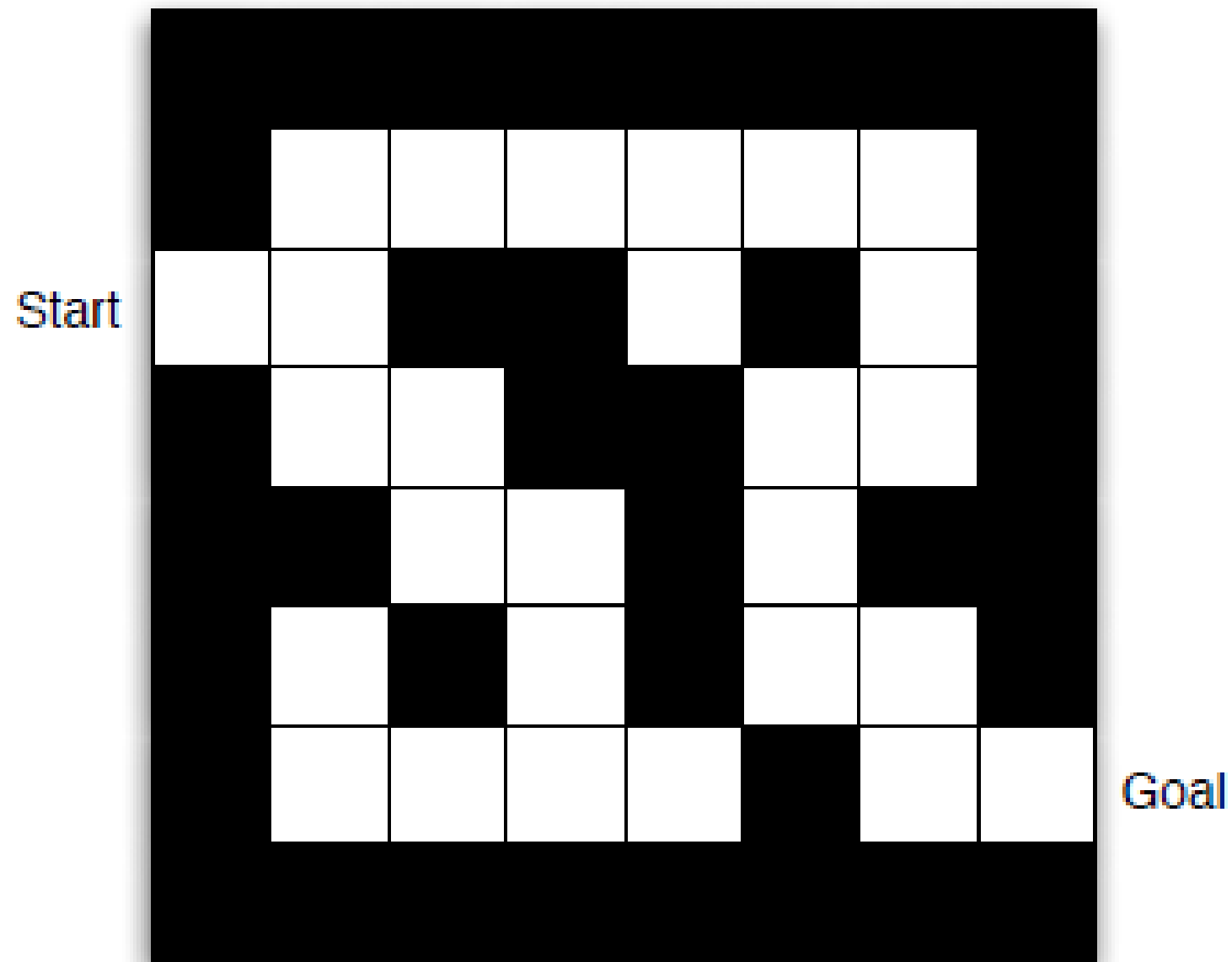
- A **model** predicts what the environment will do next
- $\mathcal{P}$  predicts the next state
- $\mathcal{R}$  predicts the next (immediate) reward, e.g.

$$\mathcal{P}_{ss'}^a = \mathbb{P}[S_{t+1} = s' \mid S_t = s, A_t = a]$$

$$\mathcal{R}_s^a = \mathbb{E}[R_{t+1} \mid S_t = s, A_t = a]$$

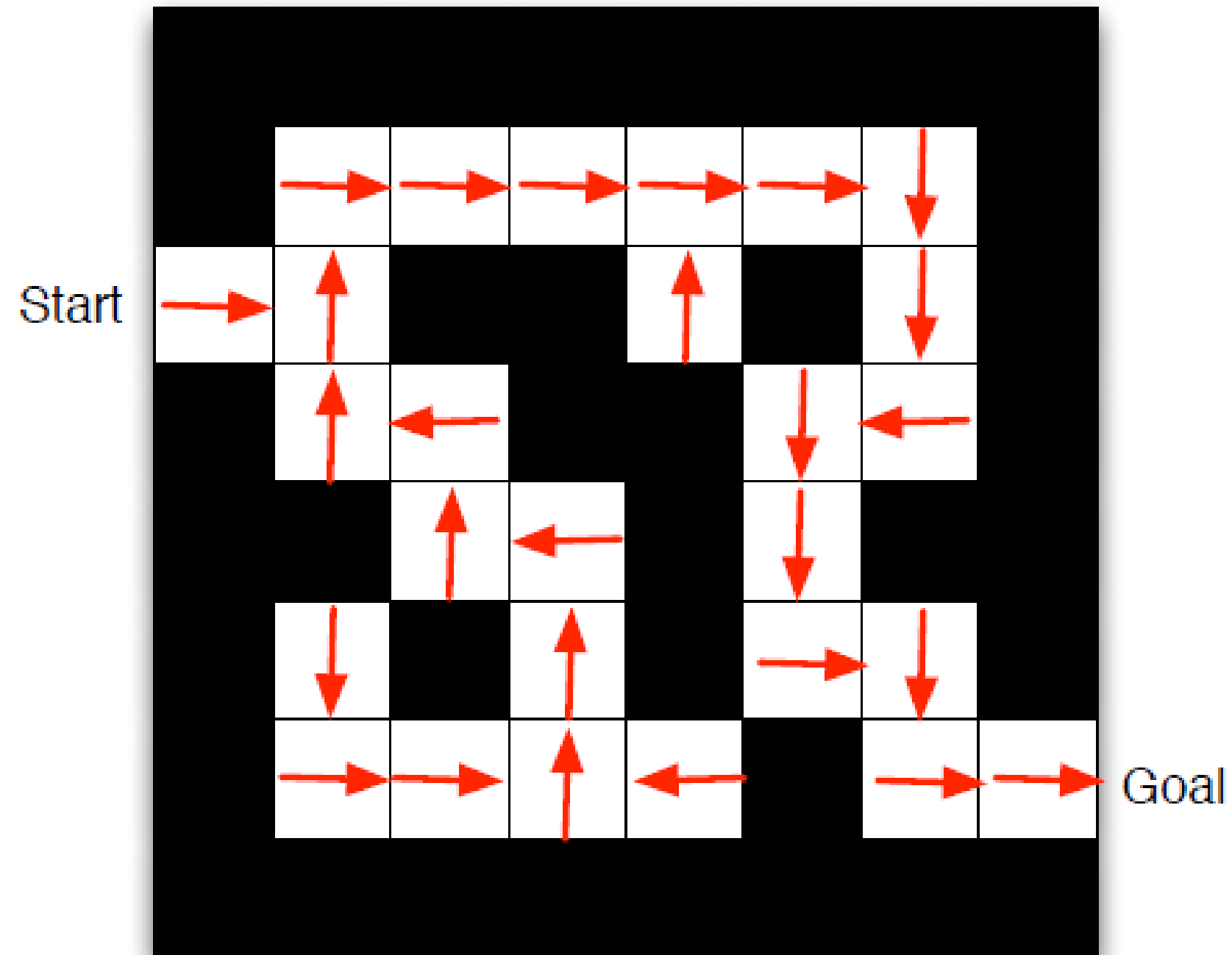


# Maze(미로) Example



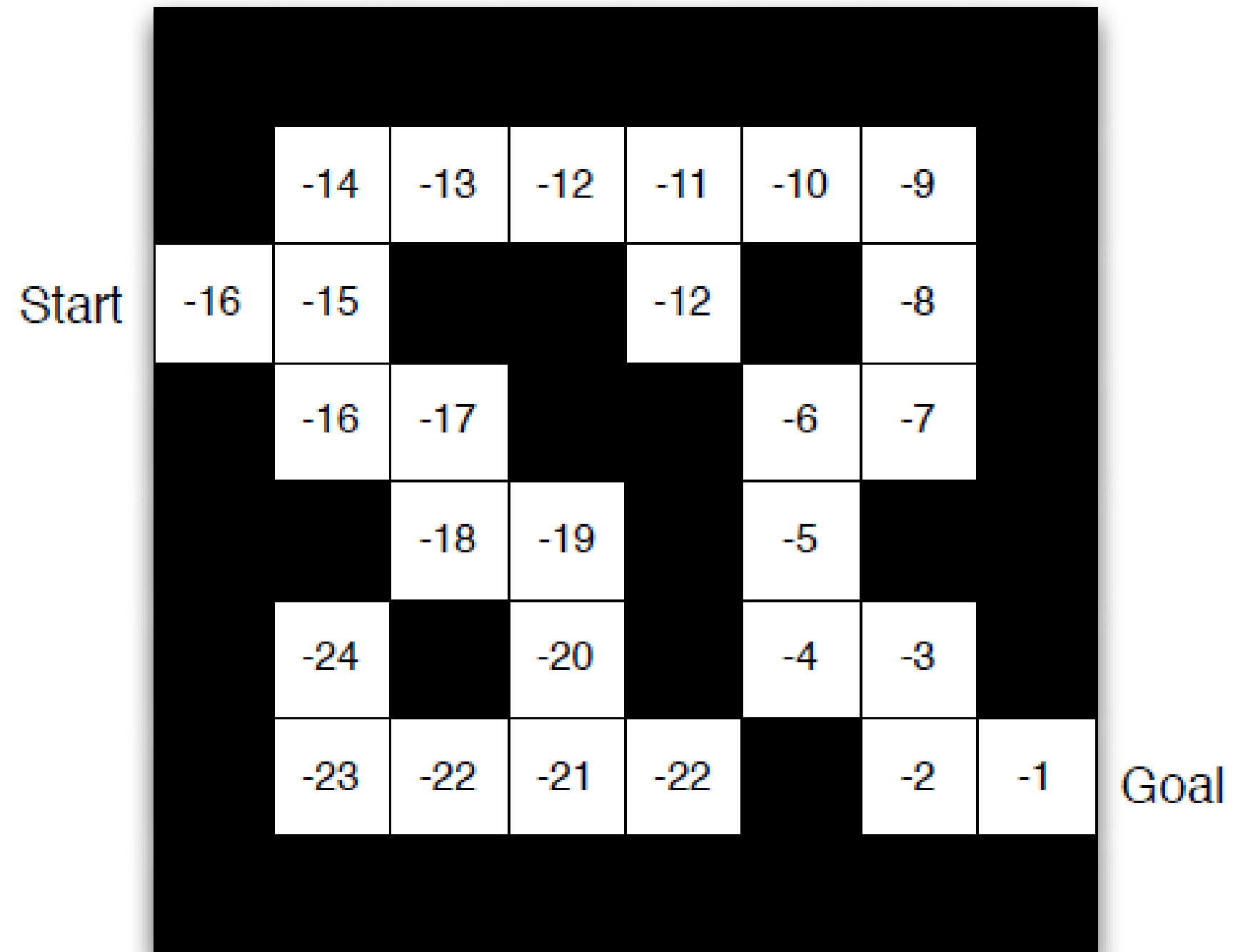
- Rewards: -1 per time-step
- Actions: N, E, S, W
- States: Agent's location

# Maze(미로) Example : Policy



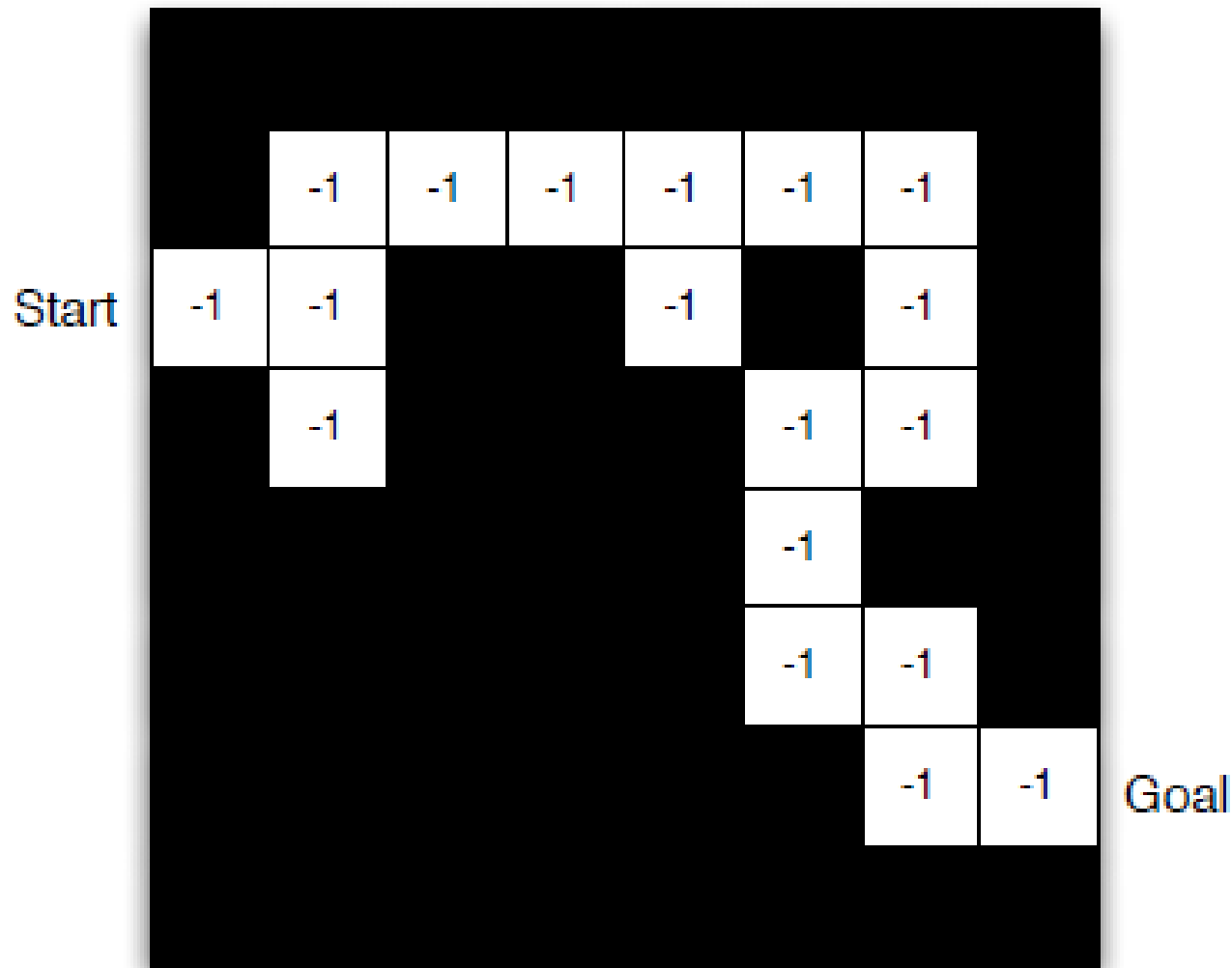
- Arrows represent policy  $\pi(s)$  for each state  $s$

# Maze(미로) Example : Value Function



- Numbers represent value  $v_{\pi}(s)$  of each state  $s$

# Maze(미로) Example : Model



- Agent may have an internal model of the environment
- Dynamics: how actions change the state
- Rewards: how much reward from each state
- The model may be imperfect

- Grid layout represents transition model  $\mathcal{P}_{ss'}^a = P(S' | S, a)$
- Numbers represent immediate reward  $\mathcal{R}_s^a$  from each state  $s$  (same for all  $a$ )

# Approaches to Reinforcement Learning

## Value-based RL

- ▶ Estimate the **optimal value function**  $Q^*(s, a)$
- ▶ This is the maximum value achievable under any policy

## Policy-based RL

- ▶ Search directly for the **optimal policy**  $\pi^*$
- ▶ This is the policy achieving maximum future reward

## Model-based RL

- ▶ Build a model of the environment
- ▶ Plan (e.g. by lookahead) using model

# Categorizing RL agents (1)

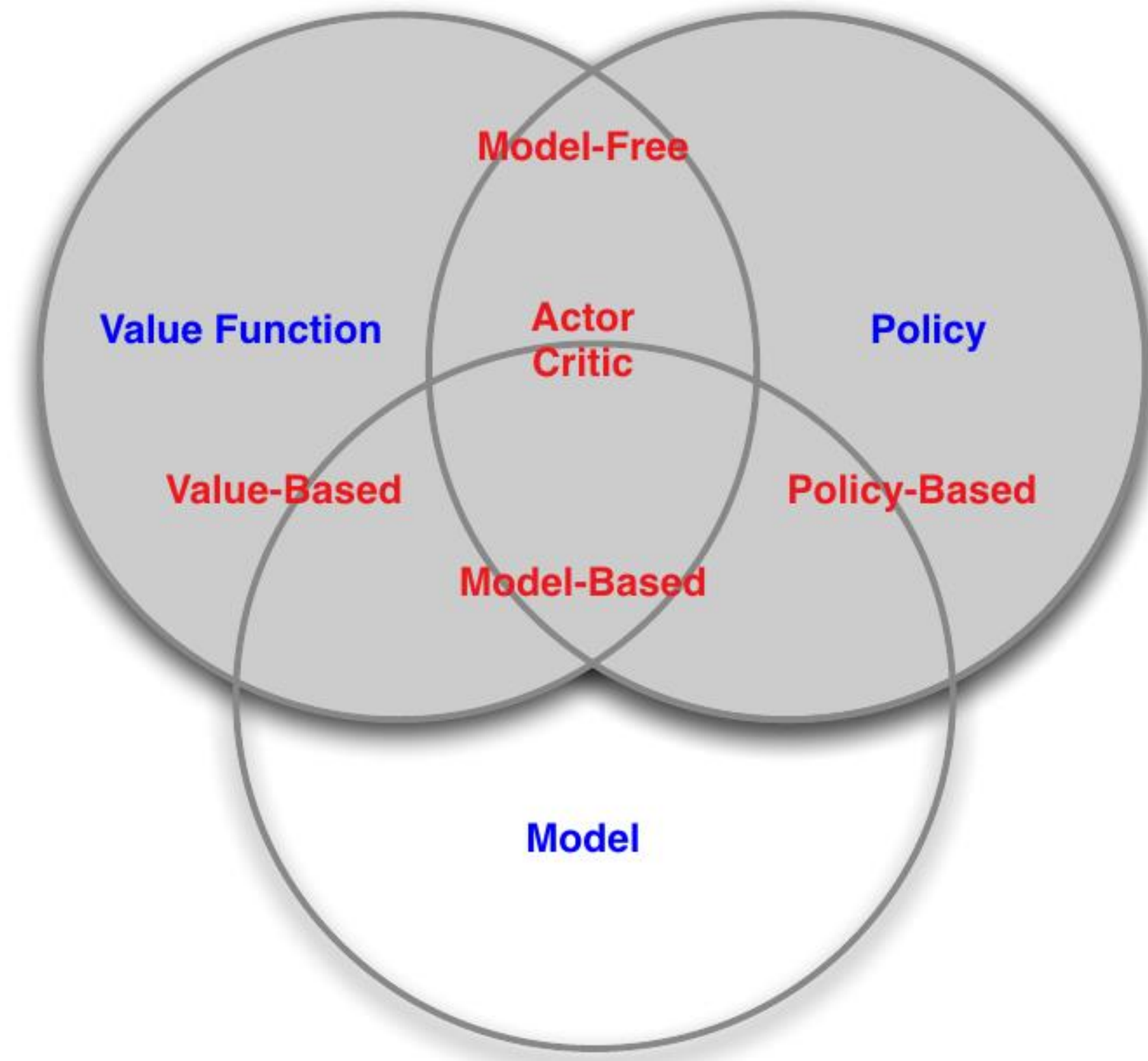
- Value Based
  - No Policy (Implicit)
  - Value Function
- Policy Based
  - Policy
  - No Value Function
- Actor Critic
  - Policy
  - Value Function

# Categorizing RL agents (2)

- Model Free
  - Policy and/or Value Function
  - No Model
- Model Based
  - Policy and/or Value Function
  - Model



# RL Agent Taxonomy

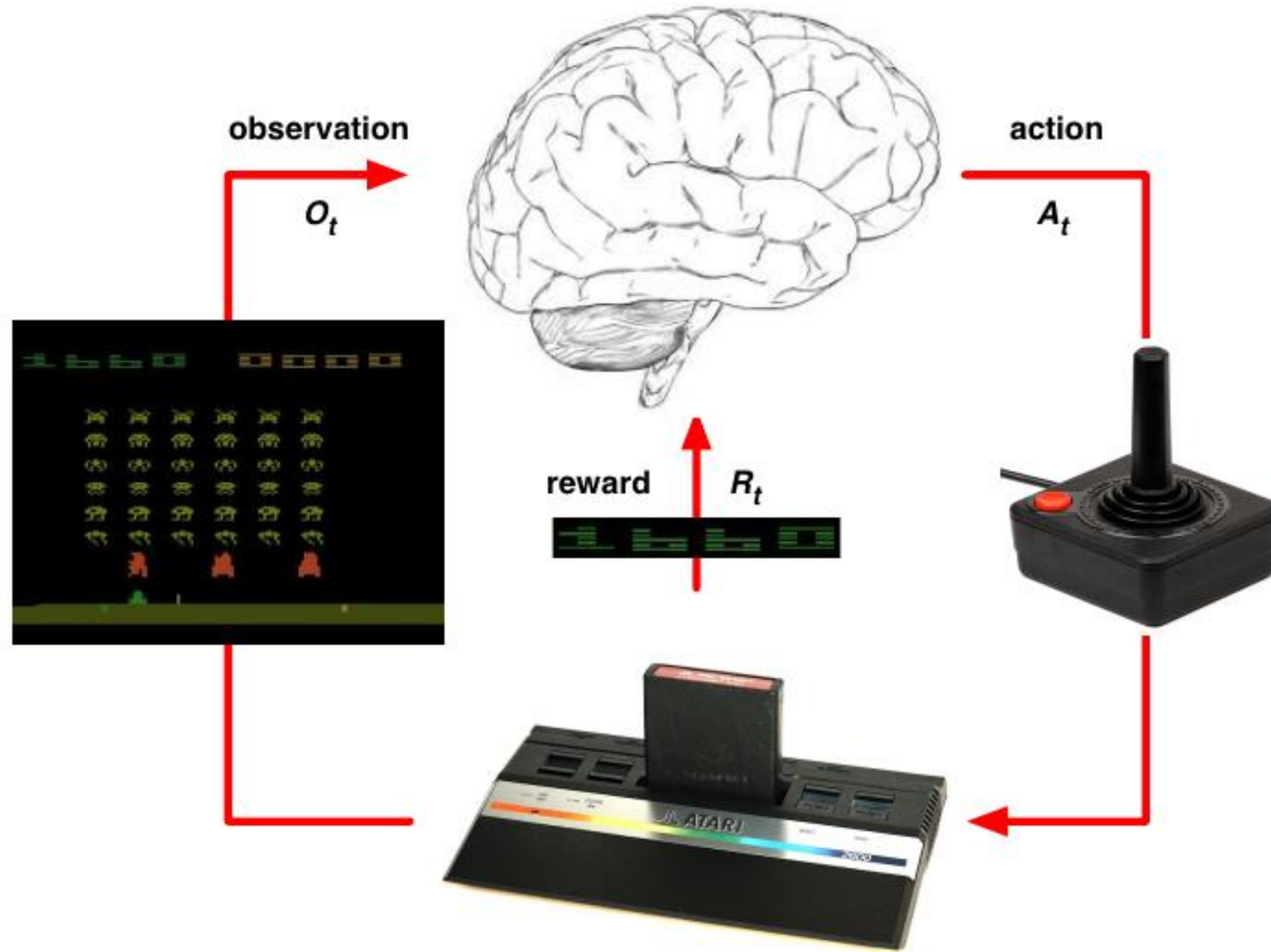


# Learning and Planning

Two fundamental problems in sequential decision making

- Reinforcement Learning:
  - The environment is initially unknown
  - The agent interacts with the environment
  - The agent improves its policy
- Planning:
  - A model of the environment is known
  - The agent performs computations with its model (without any external interaction)
  - The agent improves its policy
  - a.k.a. deliberation, reasoning, introspection, pondering, thought, search

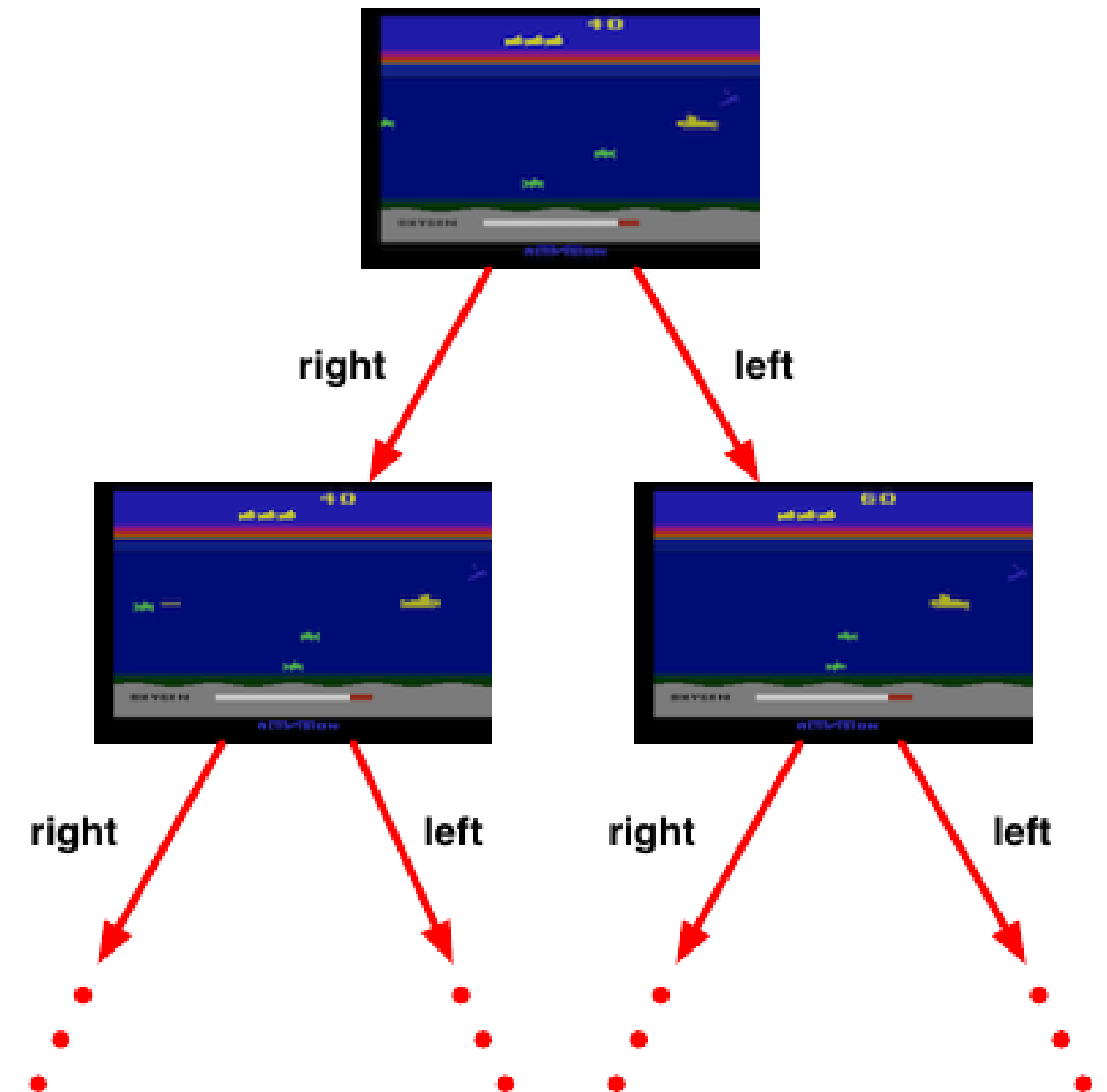
# Atari Example: Reinforcement Learning



- Rules of the game are unknown
- Learn directly from interactive game-play
- Pick actions on joystick, see pixels and scores

# Atari Example: Planning

- Rules of the game are known
- Can query emulator
  - perfect model inside agent's brain
- If I take action  $a$  from state  $s$ :
  - what would the next state be?
  - what would the score be?
- Plan ahead to find optimal policy
  - e.g. tree search



# Exploration and Exploitation (1)

- Reinforcement learning is like trial-and-error learning
- The agent should discover a good policy
- From its experiences of the environment
- Without losing too much reward along the way



# Exploration and Exploitation (2)

- *Exploration* finds more information about the environment
- *Exploitation* exploits known information to maximise reward
- It is usually important to explore as well as exploit

# Examples

- Restaurant Selection

  - Exploitation Go to your favourite restaurant

  - Exploration Try a new restaurant

- Online Banner Advertisements

  - Exploitation Show the most successful advert

  - Exploration Show a different advert

- Oil Drilling

  - Exploitation Drill at the best known location

  - Exploration Drill at a new location

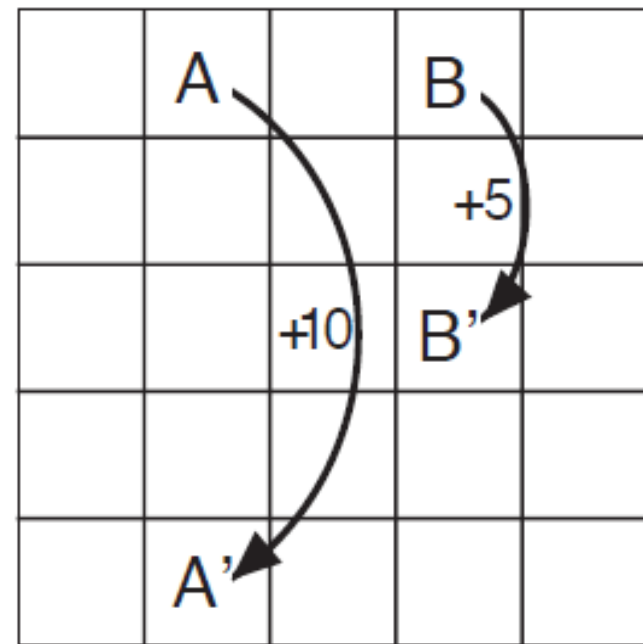
- Game Playing

  - Exploitation Play the move you believe is best

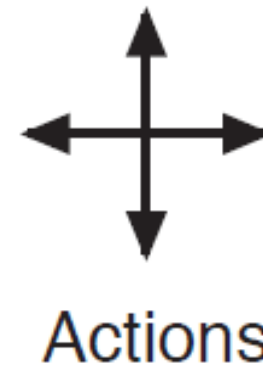
  - Exploration Play an experimental move



# Gridworld Example: Prediction



(a)



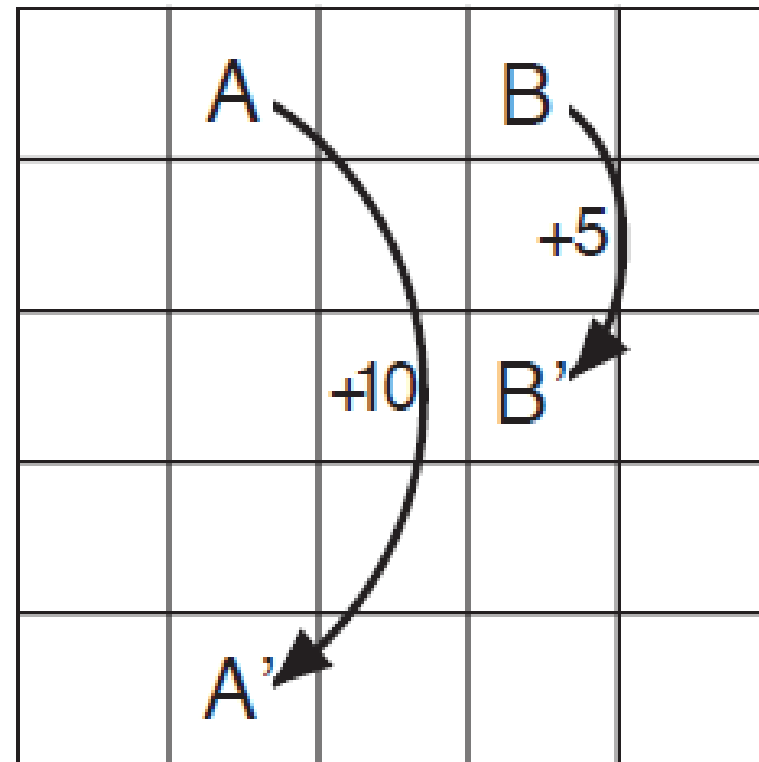
3.3	8.8	4.4	5.3	1.5
1.5	3.0	2.3	1.9	0.5
0.1	0.7	0.7	0.4	-0.4
-1.0	-0.4	-0.4	-0.6	-1.2
-1.9	-1.3	-1.2	-1.4	-2.0

(b)

What is the value function for the uniform random policy?

- At each grid cell, **four actions** are possible: north, south, east and west
- Actions taking agent off grid leaves its location unchanged but reward of '-1', other actions produces a reward of '0' except for state **A** and **B**
- From state A, all four actions yield a reward '+10' and take agent to A'
- From state B, all four actions yield a reward '+5' and take agent to B'
- Random policy: agent selects all four actions with equal probability in all states

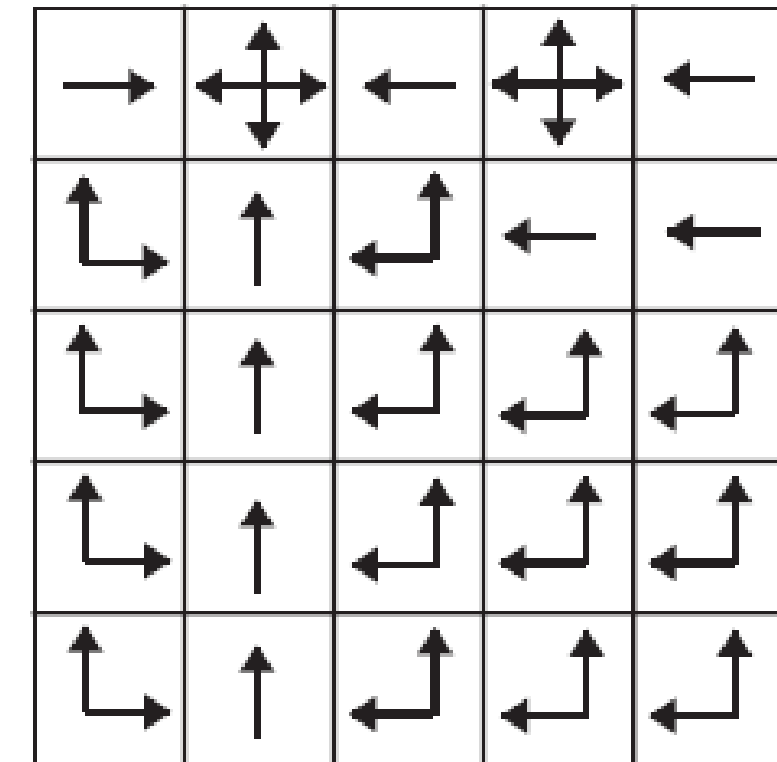
# Gridworld Example: Control



a) gridworld

22.0	24.4	22.0	19.4	17.5
19.8	22.0	19.8	17.8	16.0
17.8	19.8	17.8	16.0	14.4
16.0	17.8	16.0	14.4	13.0
14.4	16.0	14.4	13.0	11.7

b)  $v_*$



c)  $\pi_*$

What is the optimal value function over all possible policies?  
 What is the optimal policy?