



# Benchmark Score 1/2

## Calculation

EEL  
3801

**Given:** Two computer systems: A and B. There is also a reference computer R.

**Sought:** Use the reference computer R to evaluate the two computer systems A and B under a benchmark suite that has the 3 workloads as listed below.

Workload Program of SPEC suite	Time (R) [seconds]	Time (A) [seconds]	Time (B) [seconds]
CPU	20	4	5
Memory	30	5	6
Graphics	12	3	4

### **Partial Credit 1:**

Which equation best applies for a given workload:

- a)  $\text{SpecRatio}(A) = \text{Time}(A) / \text{Time}(B)$
- b)  $\text{SpecRatio}(A) = \text{Time}(B) / \text{Time}(A)$
- c)  $\text{SpecRatio}(A) = \text{Time}(R) / \text{Time}(A)$
- d)  $\text{SpecRatio}(A) = \text{Time}(A) / \text{Time}(R)$
- e)  $\text{SpecRatio}(A) = \text{Time}(A) + \text{Time}(B) / \text{Time}(R)$
- f)  $\text{SpecRatio}(A) = \text{Time}(A) * \text{Time}(B) / \text{Time}(R)$
- g)  $\text{SpecRatio}(A) = \text{Time}(R) / [\text{Time}(A) + \text{Time}(B)]$
- h)  $\text{SpecRatio}(A) = \text{Time}(B) / [\text{Time}(A) + \text{Time}(R)]$

### **Partial Credit 2:**

What is the Graphics SpecRatio for System B?

### **Partial Credit 3:**

What is the ratio of SPECscores for System A relative to System B?

### **Partial Credit 4:**


Express Part 3 result as a declarative statement to explain the relative performance in a skype teleconference with your client.



# Benchmark Score 2/2

## Calculation

EEL  
3801

**Solution 1:**  $\text{SpecRatio}(A) = \text{Time}(R) / \text{Time}(A)$    $[\text{Time } R] / [\text{Time } A]$

**Solution 2:**  $\text{SpecRatio}(B\_Graphics) =$   
 $\text{Time}(R\_Graphics) / \text{Time}(B\_Graphics)$   
 $= 12/4 = 3$  as unitless ratio

**Solution 3:**

Workload Program of SPEC suite	Time (R) [seconds]	Time (A) [seconds]	SPECRatio(A) [unitless]	Time (B) [seconds]	SPECRatio(B) [unitless]
CPU	20	4	5	5	4
Memory	30	5	6	6	5
Graphics	12	3	4	4	3

**Solution 4:**

$$\text{SPECscore} = \sqrt[n]{\prod_{i=1}^n \text{SPECratio}(i)}$$

$$\text{SPECscoreA} = (5 \cdot 6 \cdot 4)^{1/3} = 4.93$$

$$\text{SPECscoreB} = (4 \cdot 5 \cdot 3)^{1/3} = 3.91$$

$$\text{ScoreA} / \text{ScoreB} = 4.93 / 3.91 = 1.26$$

*“System A is roughly 5 times faster than the reference system for these 3 benchmark programs.”*

*“System A is roughly 1.26-fold faster than System B for these 3 benchmark programs.”*

*“System A is roughly 26% faster than System B for these 3 benchmark programs.”*



# SPECRatios 1/2

## Calculation

EEL  
3801

**Given:** A recently-released Dell server became available. We seek to determine its performance rating using the SPEC procedure according to the four benchmarks listed below:

System	Integer	Encryption	Graphics	Database
Reference	1 sec	8 sec	0.8 sec	2 sec
Dell server	500 msec	2000 msec	100msec	500msec

**Partial Credit 1:** What is the SPECRatio of the Dell server for the Integer benchmark?

- a) 0.0005
- b) 0.5
- c) 0.707
- d) 2
- e) 4.707
- f) 8
- g) 16
- h) 70.700
- i) none of the choices listed

**Partial Credit 2:** What is the SPECscore of the Dell server? Round your answer to the nearest integer.

- a) 4
- b) 263
- c) 66
- d) 3
- e) 5
- f) 3
- g) 2
- h) 300
- i) none of the answers listed



# SPECRatios 2/2

## Calculation

EEL  
3801

**Solution:** SPECRatio(CPU) = 1sec/0.5sec = 2.0 — Thus, select choice d) for **Partial Credit 1.**

$$\text{SPECRatio(Memory)} = 8/2 = 4.0$$

$$\text{SPECRatio(Graphics)} = 800/100 = 8.0$$

$$\text{SPECRatio(Floating-Point)} = 2/0.5 = 4.0$$

$$\text{SPECsScore} = (2 \cdot 4 \cdot 8 \cdot 4)^{1/4} = (2^{1+2+3+2})^{1/4} = (2^8)^{1/4} = 2^{[8 \cdot 1/4]} = 2^2 = 4.0$$

Thus, select choice a) for **Partial Credit 2.**

*“Roughly 4-fold speedup over the reference machine for these various workloads.”*

*“Roughly 4 times faster than the reference machine for these various workloads.”*

*T<sub>ref</sub>/T<sub>new</sub>=4.0, e.g. T<sub>ref</sub>=4 sec then T<sub>new</sub>=1 sec so 3 seconds was reduced compared to reference. So 3/4 reduction = 75% reduction.*

*“Execution time reduced by 75% compared to reference machine for these various workloads.”*



# Amdahl's Law

## Evaluating Architecture Tradeoffs

EEL  
3801

**Given:** The running time of a program on a Dell Server System is comprised entirely of:

- CPU: 6 sec
- Main Memory access: 14 sec
- SSD access: 5 sec

**Partial Credit 1:** The CTO of the company committed to reduce running time by at least 25%, and she provided you with a budget for exactly one of the following which have the same cost and development effort:

- a) make the processor twice as fast, or else
- b) make memory access twice as fast.

As project lead, you need to determine if the CTO's performance goal is achievable, and also indicate which approach you choose for your team?

**Solution 1:** Two ways to answer this question: find time or find speedup:

$$\text{Exec Time}_{\text{fasterprocessor}} = 6/2 + 14 + 5 = 22 \text{ sec}$$

$$\text{Exec Time}_{\text{fastermemory}} = 6 + 14/2 + 5 = 18 \text{ sec}$$

$$\text{Speedup}_{\text{fasterprocessor}} = 1 / [19/25 + (6/25)/2] = 25/22 = 1.14\text{-fold}$$

$$\text{Speedup}_{\text{fastermemory}} = 1 / [11/25 + (14/25)/2] = 25/18 = 1.39\text{-fold}$$

*Better to make memory faster → select choice b)*

*→ using option b) reduces running time from 6+14+5=25 secs to 18 secs for 25-18=7 seconds reduced, thus 7 sec / 25 sec = 28% reduction. So the CTO's goal of 25% reduction is achievable.*

**Partial**

**Credit 2:** Which of the choices listed provides the mathematical expression for Speedup: a)  $\log_N(f)$

b)  $1/(1-f_{\text{unenhanced}})$

c)  $1/f_{\text{enhanced}}$

d)  $\text{ExecTime}_{\text{new}} / \text{ExecTime}_{\text{old}}$

e)  $\text{ExecTime}_{\text{old}} / \text{ExecTime}_{\text{new}}$

**Solution 2:** e) by definition below:

$$\text{Speedup}_{\text{overall}} = \frac{\text{Execution time}_{\text{old}}}{\text{Execution time}_{\text{new}}} = \frac{1}{(1 - \text{Fraction}_{\text{enhanced}}) + \frac{\text{Fraction}_{\text{enhanced}}}{\text{Speedup}_{\text{enhanced}}}}$$

A remembrance hint is to recall is that if it runs faster, then speedup should be greater than unity.

Thus, being faster means  $\text{ExecTime}_{\text{old}}$  must be in the numerator. The other choices don't relate to speedup.



# Amdahl's Law

## Evaluating Architecture Tradeoffs

EEL  
3801

**Given:** The running time of a program on a IBM Server System is comprised entirely of:

- *CPU time:* 4 sec
- *Main Memory access time:* 10 sec
- *Disk access time:* 6 sec

The company CTO has provided you with the following approaches:

- *Approach (A):* make the processor twice as fast at a cost of \$5
- *Approach (B):* make memory access twice as fast at a cost of \$10
- *Approach (C):* make disk access twice as fast at a cost of \$2

**Partial credit 1:** What is the running time of the program if only Approach (A) is applied?

**Partial credit 2:** What is the running time of the program if both Approach (A) and Approach (B) are applied simultaneously?

**Partial credit 3:** Which of the following choices provides the lowest cost option to achieve a speedup factor of at least 1.4-fold?

- a) Approach A alone
- b) Approach B alone
- c) Approach C alone
- d) Approach A and Approach B when applied together simultaneously
- e) Approach B and Approach C when applied together simultaneously
- f) Approach A and Approach C when applied together simultaneously
- g) Approach A and Approach B and Approach C when applied together simultaneously



# Amdahl's Law

## Evaluating Architecture Tradeoffs

EEL  
3801

**Part 1:** What is the running time of the program if only Approach (A) is applied?

**Sol 1:** Approach (A):  $4/2 + 10 + 6 \text{ sec} = 2+10+6 \text{ sec} = 18 \text{ sec}$

**Part 2:** What is the running time of the program if both Approach (A) and Approach (B) are applied simultaneously?

**Sol 2:** Approach (AB):  $4/2 + 10/2 + 6 \text{ sec} = 2+5+6 \text{ sec} = 13 \text{ sec}$

**Part 3:** Which of the following choices provides the lowest cost option to achieve a speedup factor of at least 1.4-fold?

**Sol 3:** CTO requirement is a speedup of 40%.

Thus,  $\text{Speedup} = \{ \text{Time}(\text{old}) \} / \{ \text{Time}(\text{new}) \} \geq 1.4$  so finding

$\text{Time}(\text{old})$  to be  $4+10+6=20 \text{ sec}$  in the given statement. Then,  $20/T_{\text{new}} \geq 1.4$  so:

$T_{\text{new}} = 20 \text{ sec} / 1.4 \leq 14.28 \text{ sec}.$

So let's see which approaches listed achieve 14.28 secs or less, at the lowest cost:

- Approach(C) requires  $4+10+6/2=17 \text{ sec}$  which does not meet the performance requirement.
- Approach(AB) meets CTO's performance requirement at a cost of \$15.
- Approach(BC) meets CTO's performance requirement at a cost of \$12.
- Approach(AC) costs just  $\$5+\$2=\$7$  but requires  $4/2+10+6/2=15 \text{ seconds}$  which does not meet the performance requirement.

→ **Tip:** skip checking execution time of Approach(ABC) as it costs more than Approach(BC) already found to be sufficient 😊



# Amdahl's Law

## Multicore Speedup / Benefit Analysis

EEL  
3801

**Given:** Consider a program that takes 10 seconds to run on dual-core Intel Xeon running at 2GHz under ideal conditions. This program has 30% sequential code and the remainder is infinitely parallelizable.

**Sought:** What is the minimum time possible to execute this program on an 8-core Intel Xeon CPU running at 2GHz, if all other parameters were to remain unchanged? Round your answer to the nearest second.

**Solution:** Amdahl's law can be used as the execution time, fraction of parallel code, and number of cores is known. Here, observe the parallel portion is  $f=0.7$ .

First compute idealized speedup for the dual-core case that is occurring when  $f=0.7$ . That is  $S=1/((1-f) + f/N) = 1/(0.3+0.7/2) = 1.54$  over the uniprocessor case, which is speedup for 2 cores denoted  $S_2$ . So running on dual core is 1.54-fold faster than a single core. Since we know the execution time in seconds on the dual core, we can find the uni-core execution time since  $S=T_{\text{unenhanced}}/T_{\text{enhanced}}$ . Thus,  $1.54=T_1/(10 \text{ seconds})$  so  $T_1 = 15.4$  seconds where  $T_1$  represents the unenhanced execution time on 1 processor core.

Thus, if the dual-core case took 10 seconds which represented 1.54 fold speedup over the uniprocessor, then by definition of speedup= $T_{\text{old}}/T_{\text{new}}=T_1/T_N$  we find the uni-core time to be 15.4 seconds.

Since maximum speedup on 8 cores =  $S=1/((1-f) + f/N)$  where  $f=0.7$ , but now  $N=8$ . So we find next  $S_8 = 1/(0.3+ 0.7/8)=2.58$  then  $2.58= T_1 / T_8$  implying  $T_8 = 5.97$  seconds which rounds to 6 seconds.

Intuitively, this is consistent that if the program was 70% parallelizable then running on 1 core it took 15 seconds, two cores took 10 seconds, and 8 cores requires 6 seconds.





# Amdahl's Law for Speedup

## AminoPak: composite use of CPI, clock rate, speedup 1/2

EEL  
3801

**Given:** Cellgene Biosciences Inc. is executing the AminoPak protein-folding application and has hired you to increase the performance. They're currently using one AMD single-core processor which has a 2.8 GHz clock rate with CPI=1.0 for all instructions.

The dynamic instruction mix of AminoPak is 80% floating-point instructions, 5% integer instructions, and 15% data transfer instructions. AminoPak is infinitely parallelizable except for the completely sequential `GetAmino()` routine (which is 2% of the total AminoPak application time) and also the completely sequential `RotateBond()` routine (which is 3% of the total AminoPak application time).

You're considering recommending a single alternative processor chip, as a replacement for the current AMD processor chip.

**Design A:** The datasheet for a 2.8 GHz Intel Broadwell single-core processor indicates that compared to a 2.8 GHz AMD single-core processor, it will:

- speedup floating-point instructions by 32-fold,
- provide CPI=3.2 for integer instructions while leaving the number of instructions unchanged, and
- double the time taken by each data transfer instruction.

What speedup factor would a 2.8 GHz Intel Broadwell single-core processor provide compared to the 2.8 GHz AMD single-core CPU?

- a) 0.05-fold
- b) 5%
- c) 5-fold
- d) 3.2-fold
- e) 32%
- f) 32-fold
- g) 0.846
- h) 84.6%
- i) 2.06
- j) 20%
- k) 20-fold
- z) none of the choices listed

**Solution A:**  $\text{Speedup} = 1 / (\text{fraction\_enhanced} / \text{enhancement\_factor} + \text{fraction\_slowed\_down} * \text{slow\_down\_factor})$ .  
 $\text{Speedup} = 1 / (0.8 / 32 + 0.05 * 3.2 + 0.15 * 2) = 2.06$ . Thus, select choice i).



# Amdahl's Law for Speedup

## AminoPak: composite use of CPI, clock rate, speedup 2/2

EEL  
3801

**Design B:** An AMD quad-core processor has an identical ISA to the AMD single-core processor, but a clock rate of 4.0 GHz and twice the Effective CPI. What best-case speedup factor would it provide for AminoPak compared to the baseline AMD single-core CPU as described above?

- a) 0.05-fold
- b) 2.48-fold
- c) 3.47-fold
- d) 34.7%
- e) 347%
- f) 3470%
- g) 5-fold
- h) 5.67-fold
- i) 0.714
- j) 7.14%
- k) 71.4-fold
- z) insufficient information to determine

**Solution B:** Without regards to clock rate, Amdahl's law indicates:

$\text{Speedup}_4 = 1 / [ (1-f) + (f/4) ]$  where  $f$ =parallel fraction.

Here in this question, it is given that  $f=1-(0.03+0.02)=0.95$ , so substituting for  $f$ :

$$\text{Speedup}_4 = 1 / [ (1-0.95) + (0.95/4) ] = 1 / [ 0.05 + 0.2375 ] = 1/0.2875 = 3.47$$

Meanwhile, the clock rate has also been increased to 4.0 GHz from the previous 2.8 GHz, thus execution is speeded up by  $[4.0 \text{ GHz}] / [2.8 \text{ GHz}] = 1.43$  due to the clock rate alone while each instruction requires twice as many clocks, resulting in a relative speed of  $1.43/2 = 0.714$ .

Resulting in a composite impact of:

$3.47 \times 0.714 = 2.48$ -fold speedup. Thus, select choice b).