

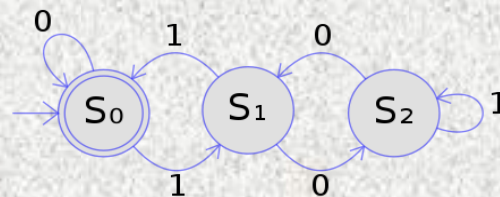
Sheet 2 (Scanner using Regular Expression (RE) and Finite Automaton (FA))

Q1) Given the following **RE**. Convert each one to its corresponding **FA**, then write a C++ code that accepts each one of them.

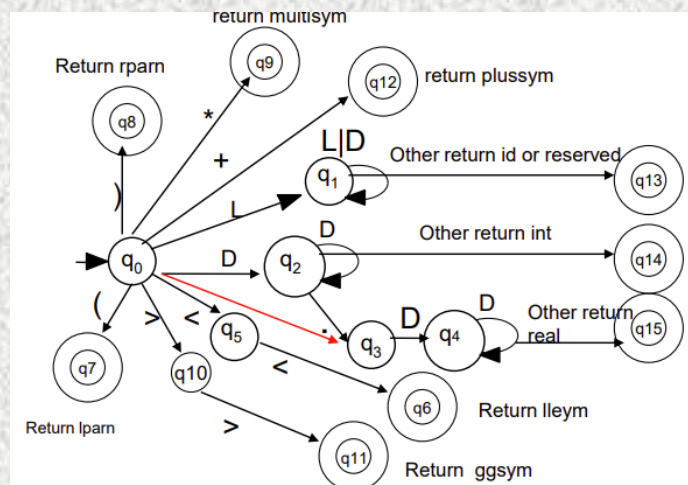
[Don't use file I/O, the input will be assigned in a string variable]

1. $a(b|a)^*$
2. $(letter | _) (letter | digit | _)^*$
3. $digit\ digit^* \cdot digit\ digit^*$
4. $"(L|D|\backslash)"^*$

Q2) Given the following **FA** that accepts any binary number divisible by 3, write a corresponding C++ code that accepts these binary numbers.



Q3) Given the following **FA**, write a corresponding C++ code that simulates this **FA**.





Q4) Consider the following BNF grammar for the **Wren** language. Convert it to its corresponding **FA**, then write a C++ code that simulates it for accepting any valid token.

$\langle \text{program} \rangle ::= \text{program} \langle \text{ident} \rangle \text{is} \langle \text{block} \rangle$
$\langle \text{block} \rangle ::= \langle \text{declaration} - \text{seq} \rangle \text{begin} \langle \text{command} - \text{seq} \rangle \text{end}$
$\langle \text{declaration} - \text{seq} \rangle ::= \varepsilon \mid \langle \text{declaration} - \text{seq} \rangle \langle \text{declaration} \rangle$
$\langle \text{declaration} \rangle ::= \text{var} \langle \text{var} - \text{list} \rangle : \langle \text{type} \rangle ;$
$\langle \text{type} \rangle ::= \text{integer} \mid \text{Boolean}$
$\langle \text{var} - \text{list} \rangle ::= \langle \text{var} \rangle \mid \langle \text{var} \rangle , \langle \text{var} - \text{list} \rangle$
$\langle \text{command} - \text{seq} \rangle ::= \langle \text{command} \rangle \mid \langle \text{command} - \text{seq} \rangle ; \langle \text{command} \rangle$
$\langle \text{command} \rangle ::= \langle \text{var} \rangle := \langle \text{expr} \rangle$ $\mid \text{read} \langle \text{var} \rangle$ $\mid \text{write} \langle \text{int} - \text{expr} \rangle$ $\mid \text{if} \langle \text{bool} - \text{expr} \rangle \text{then} \langle \text{command} - \text{seq} \rangle \text{end if}$ $\mid \text{if} \langle \text{bool} - \text{expr} \rangle \text{then} \langle \text{command} - \text{seq} \rangle$ $\quad \text{else} \langle \text{command} - \text{seq} \rangle \text{end if}$ $\mid \text{while} \langle \text{bool} - \text{expr} \rangle \text{do} \langle \text{command} - \text{seq} \rangle \text{end While}$
$\langle \text{expr} \rangle ::= \langle \text{int} - \text{expr} \rangle \mid \langle \text{bool} - \text{expr} \rangle$
$\langle \text{int} - \text{expr} \rangle ::= \langle \text{term} \rangle \mid \langle \text{int} - \text{expr} \rangle \langle \text{weak op} \rangle \langle \text{term} \rangle$
$\langle \text{term} \rangle ::= \langle \text{element} \rangle \mid \langle \text{term} \rangle \langle \text{strong op} \rangle \langle \text{element} \rangle$
$\langle \text{element} \rangle ::= \langle \text{numeral} \rangle \mid \langle \text{var} \rangle \mid (\langle \text{int} - \text{expr} \rangle) \mid - \langle \text{element} \rangle$
$\langle \text{bool} - \text{expr} \rangle ::= \langle \text{bool} - \text{term} \rangle \mid \langle \text{bool} - \text{expr} \rangle \text{or} \langle \text{bool} - \text{term} \rangle$
$\langle \text{bool} - \text{term} \rangle ::= \langle \text{bool} - \text{element} \rangle \mid \langle \text{boo} - \text{term} \rangle \text{and} \langle \text{bool} - \text{element} \rangle$



$\langle \text{element} \rangle ::= \langle \text{var} \rangle \mid \langle \text{comparison} \rangle \mid \text{not} (\langle \text{bool} - \text{expr} \rangle) \mid \text{true} \mid \text{false}$
$\langle \text{comparison} \rangle ::= \langle \text{int} - \text{expr} \rangle \langle \text{relation} \rangle \langle \text{int} - \text{expr} \rangle$
$\langle \text{var} \rangle ::= \langle \text{ident} \rangle$
$\langle \text{relation} \rangle ::= \langle \mid \mid \leq \mid \mid < \mid \mid = \mid \mid > \mid \mid \geq \mid \mid \rangle$
$\langle \text{weak op} \rangle ::= + \mid -$
$\langle \text{strong op} \rangle ::= * \mid /$
$\langle \text{ident} \rangle ::= \langle \text{letter} \rangle \mid \langle \text{ident} \rangle \langle \text{letter} \rangle \mid \langle \text{ident} \rangle \langle \text{digit} \rangle$ $\mid \langle \text{digit} \rangle$
$\langle \text{letter} \rangle ::= a \mid b \mid c \mid d \mid e \mid f \mid g \mid h \mid i \mid j \mid k \mid l \mid m \mid n \mid o$ $\mid p \mid q \mid r \mid s \mid t \mid u \mid v \mid w \mid x \mid y \mid z$
$\langle \text{numeral} \rangle ::= \langle \text{digit} \rangle \mid \langle \text{numeral} \rangle \langle \text{digit} \rangle$
$\langle \text{digit} \rangle ::= 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$

Q5) Consider we want to add the following rules to Wren language, modify the the **FA** of the **Wren** language, then write a C++ code the simulates the new one.

$\langle \text{Declaration} \rangle ::= \text{var} \langle \text{ident} \rangle [\langle \text{numeral} \rangle .. \langle \text{numeral} \rangle] : \langle \text{type} \rangle$
 $\langle \text{command} \rangle ::= \langle \text{ident} \rangle [\langle \text{ident} \rangle \mid \langle \text{numeral} \rangle] := \langle \text{expr} \rangle \mid$
 $\langle \text{ident} \rangle := \langle \text{ident} \rangle [\langle \text{ident} \rangle \mid \langle \text{numeral} \rangle] \mid$
 $\langle \text{ident} \rangle [\langle \text{ident} \rangle \mid \langle \text{numeral} \rangle] =$
 $\langle \text{ident} \rangle [\langle \text{ident} \rangle \mid \langle \text{numeral} \rangle]$