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```
In [1]: 1 import yfinance as yf
2 import matplotlib.pyplot as plt
3 import pandas as pd
4 import numpy as np
5 import datetime
6 import io
7 import datetime
8 import matplotlib.lines as mlines
9 from fredapi import Fred
10 import statsmodels.formula.api as smf
11 import datetime
12
```

```
In [2]: 1 df = pd.read_csv("desktop/hw2.csv", parse_dates = True, index_col = 0)
2 df
```

```
Out[2]:
```

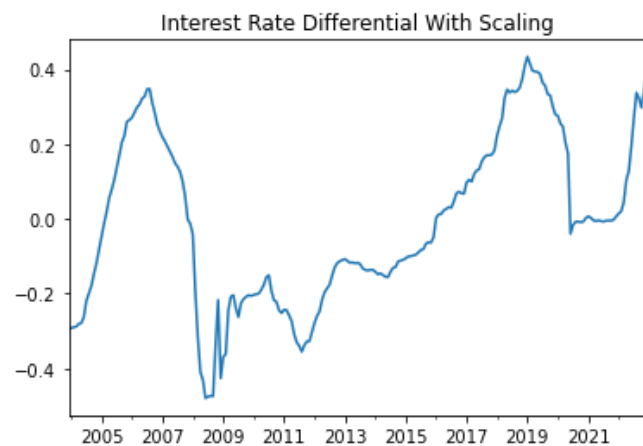
	I_US	I_EU	Inf_US	Inf_EU	Euro
2003-12-01	1.11	2.1590	0.019284	0.021933	1.196501
2004-01-01	1.10	2.1463	0.020352	0.020207	1.258194
2004-02-01	1.06	2.0895	0.020263	0.018343	1.246805
2004-03-01	1.05	2.0706	0.016885	0.016654	1.244803
2004-04-01	1.05	2.0288	0.017401	0.017175	1.236507
...
2022-08-01	2.50	0.0366	0.084821	0.088662	1.020825
2022-09-01	2.76	0.3947	0.082492	0.091406	1.003905
2022-10-01	3.21	1.0109	0.082224	0.099272	0.982956
2022-11-01	3.85	1.4277	0.077631	0.106206	0.988631
2022-12-01	4.46	1.8252	0.071179	0.100546	1.042535

229 rows × 5 columns

```
In [3]: 1 def scale(x):  
2     return (x-x.min())/(x.max()-x.min())  
3  
4 # Apply Scaling  
5 df["ir_diff"] = scale(df["I_US"]) - scale(df["I_EU"])  
6 df.dropna(inplace= True)
```

```
In [4]: 1 plt.title("Interest Rate Differential With Scaling")  
2 df["ir_diff"].plot()
```

Out[4]: <AxesSubplot:title={'center':'Interest Rate Differential With Scaling'}>



```
In [5]: 1 k = 0.05  
2 w = 5  
3 z = 0  
4  
5 df["Filter"] = df.ir_diff.ewm(alpha = k, adjust = False).mean()
```

```
In [6]: 1 df["Filter Error"] = df.ir_diff - df["Filter"]
2
3 # compute the rolling standard deviation
4 df["std"] = df["Filter Error"].rolling(w).std()
5
6 # create our confidence intervals or "boundaries of inaction"
7 # these are scaled by teh number of standard deviations "z"
8 df["Upper"] = df["Filter"] + z*df["std"]
9 df["Lower"] = df["Filter"] - z*df["std"]
10
11 # Create signal that evaluates whether we are outside the threshold
12 # then multiply by the direction of the mistake
13 # (we use economic theory to decide which direction is long or short)
14 df["test"] = np.where(df["Filter Error"].abs()>z*df["std"], -1, 0)*np.sign(df["Filter Error"])
```

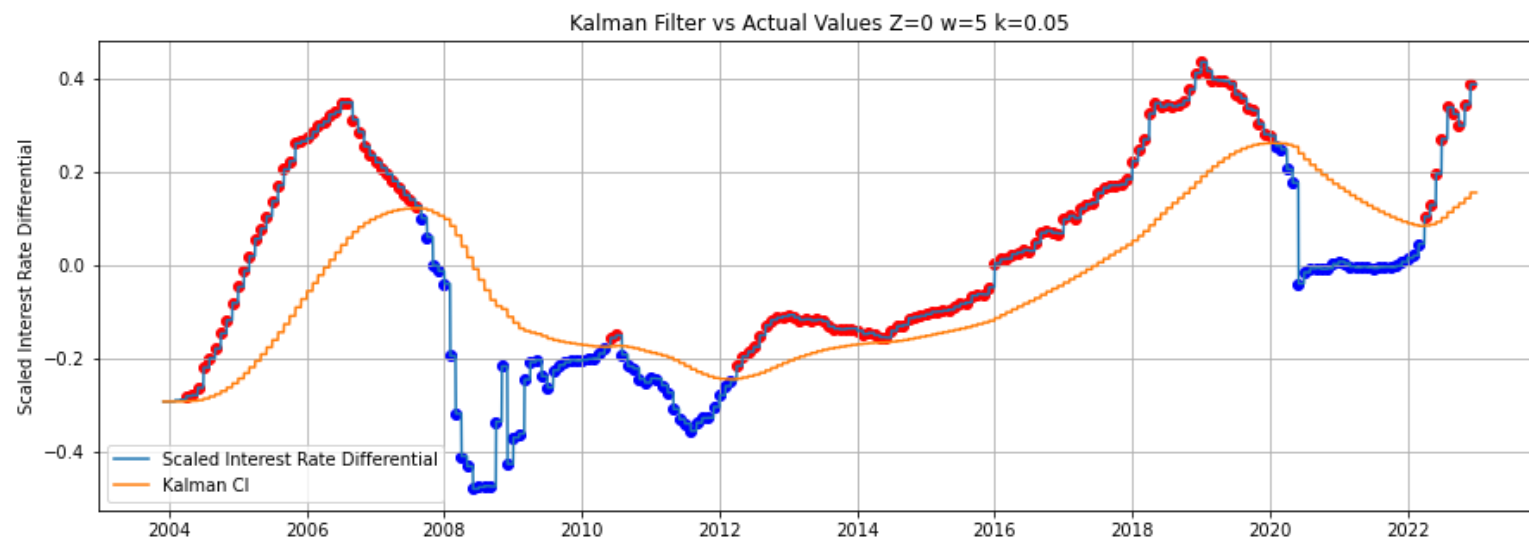
```
In [ ]: 1
```

```
In [8]: 1 i = 41
2
3 # create a new column that we will populate with our daily position
4 daily.loc[:, str(i)+"_signal"] = 0
5
6 # loop through each day in the dataset
7 for j in daily.index:
8     # If our monthly signal is not 0
9     if daily.loc[j, "test"] != 0:
10         # Make the next i days equal to the monthly signal
11         daily.loc[j:j+datetime.timedelta(i), str(i)+"_signal"] = daily.loc[j, "test"]
12
13 # Below is the holding period I use for the CI strategy
14 i = 171
15 daily.loc[:, str(i)+"_signal"] = 0
16 for j in daily.index:
17     if daily.loc[j, "test"] != 0:
18         daily.loc[j:j+datetime.timedelta(i), str(i)+"_signal"] = daily.loc[j, "test"]
19
```

```

In [9]: 1 data2 = daily.dropna()
2 fig, ax = plt.subplots(figsize = (15, 5))
3 ax.set_title("Kalman Filter vs Actual Values " + "Z="+str(z) + " w=" + str(w)+ " k=" + str(k))
4
5 ax.set_ylabel("Scaled Interest Rate Differential")
6
7 # Plot the actual series and the filter
8 ax.plot(data2["ir_diff"])
9 ax.plot(data2["Filter"])
10
11 # This code block is used to add confidence intervals when z > 0
12 #ax.fill_between(data2.index, data2.Lower, data2.Upper, color='b', alpha=.2)
13
14 # add scatterplots using boolean indexing
15 # We change the colors and shapes based on the conditions
16 ax.scatter(data2[data2.test == 1].index, data2[data2.test == 1]["ir_diff"], color = "blue")
17 ax.scatter(data2[data2.test == -1].index, data2[data2.test == -1]["ir_diff"], color = "red")
18 ax.legend(["Scaled Interest Rate Differential", "Kalman CI"])
19
20 # this code can let us zoom in on certain time periods
21 #plt.xlim([datetime.date(2022, 1, 1), datetime.date(2023, 1, 1)])
22 ax.grid()

```



I would short if the price today is low but expected to increase in the future. I would long if price is low today but expected to rise in the future.

```
In [11]: 1 daily["Euro"]=df['Euro']
```

```
In [13]: 1 daily["Euro"] = daily["Euro"].ffill()
```

```
In [14]: 1 start = daily[["Euro", "41_signal"]].index[0]
```

```
In [15]: 1 df1 = daily[daily.test != 0][["41_signal", "Euro"]].copy()
2 df1['D'] = df1["41_signal"]
```

```
In [16]: 1 df1 = df1[:-1].copy()
```

```
In [17]: 1 df1['s_current'] = daily[daily.index.isin(df1.index)][ "Euro"].values
2 df1['s_future'] = daily[daily.index.isin(df1.index+datetime.timedelta(41))][ "Euro"].values
3
4 # Get the realized exchange rate
5 df1['R'] = np.where(df1['s_future'] >= df1['s_current'], 1, -1)
```

```
In [19]: 1 df1['W'] = (df1['D']-np.mean(df1['D']))*(df1['R']-np.mean(df1['R']))
2 T_B = np.mean(df1['W'])
3 T_B
```

```
Out[19]: -0.001594387755102041
```

Yes, it did pass the binomial test.

```
In [20]: 1 dy = df1['W'] - np.mean(df1['W'])
2 gamma_0 = sum((dy)**2)/len(df1)
3 gamma_1 = np.mean((dy*dy.shift(-1))[:len(df1)-1])
4 LRV = gamma_0 + 2*(1-1/2)*gamma_1
```

```
In [21]: 1 from scipy.stats import norm
2
3 statistic = T_B/np.sqrt(LRV/df1.shape[0])
4 print('Test statistic : ', statistic, ', 5 % critical value : ', round(norm.ppf(0.95),2))
```

```
Test statistic : -0.02468504071733396 , 5 % critical value : 1.64
```

Based on the t-stat, the Newey-West LRV estimator Null cannot be rejected.

```
In [22]: 1 df1['W_2'] = df1['D']*(df1['s_future']-df1['s_current'])  
2 T_WB = np.mean(df1['W_2'])
```

```
In [23]: 1 T_WB
```

```
Out[23]: -0.000108124954359872
```

It passed the weighted directional test which allows to reject the null hypothesis that the expected value of our weighted forecasts is 0 .

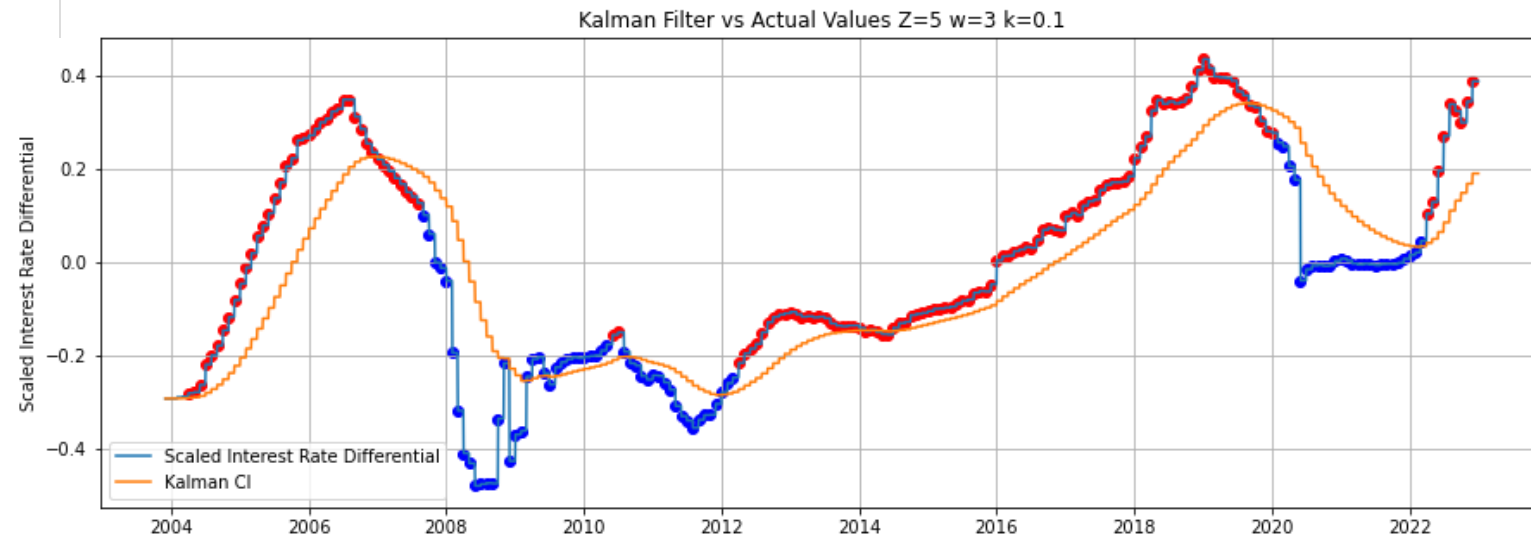

```
In [37]: 1 k = 0.1
2 w = 3
3 z = 5
4
5 df["Filter"] = df.ir_diff.ewm(alpha = k, adjust = False).mean()
6 # Create a dataframe at a daily frequency wiyh start and end
7 # dates that cover the observation period
8 drange = pd.date_range(start =df.index[0], end = "01/01/2023")
9 daily = pd.DataFrame(index = drange)
10
11 # Integrate the monthly dta into the daily data
12 daily["test"] = df["test"]
13
14 daily["Upper"] = df["Upper"]
15 daily["Lower"] = df["Lower"]
16 daily["Filter"] = df["Filter"]
17 daily["ir_diff"] = df["ir_diff"]
18
19 # Fill NA values with the last available value
20 daily["Upper"] = daily["Upper"].ffill()
21 daily["Lower"] = daily["Lower"].ffill()
22 daily["Filter"] = daily["Filter"].ffill()
23 daily["ir_diff"] = daily["ir_diff"].ffill()
24
25 # fill the remaining NA values with 0's
26 # also populates the test column
27 daily = daily.fillna(0)
28
29 # We let the holding period (i) be 41 days
30 i = 41
31
32 # create a new column that we will populate with our daily position
33 daily.loc[:, str(i)+"_signal"] = 0
34
35 # loop through each day in the dataset
36 for j in daily.index:
37     # If our monthly signal is not 0
38     if daily.loc[j, "test"] != 0:
39         # Make the next i days equal to the monthly signal
40         daily.loc[j:j+datetime.timedelta(i), str(i)+"_signal"] = daily.loc[j, "test"]
41
42 # Below is the holding period I use for the CI strategy
43 i = 171
44 daily.loc[:, str(i)+"_signal"] = 0
45 for j in daily.index:
46     if daily.loc[j, "test"] != 0:
47         daily.loc[j:j+datetime.timedelta(i), str(i)+"_signal"] = daily.loc[j, "test"]
48
49 data2 = daily.dropna()
50 fig, ax = plt.subplots(figsize = (15, 5))
```



```

51 ax.set_title("Kalman Filter vs Actual Values " + "Z="+str(z) + " w=" + str(w)+ " k=" + str(k))
52
53 ax.set_ylabel("Scaled Interest Rate Differential")
54
55 # Plot the actual series and the filter
56 ax.plot(data2["ir_diff"])
57 ax.plot(data2["Filter"])
58
59 # This code block is used to add confidence intervals when z > 0
60 #ax.fill_between(data2.index, data2.Lower, data2.Upper, color='b', alpha=.2)
61
62 # add scatterplots using boolean indexing
63 # We change the colors and shapes based on the conditions
64 ax.scatter(data2[data2.test == 1].index, data2[data2.test == 1]["ir_diff"], color = "blue")
65 ax.scatter(data2[data2.test == -1].index, data2[data2.test == -1]["ir_diff"], color = "red")
66 ax.legend(["Scaled Interest Rate Differential", "Kalman CI"])
67
68 # this code can let us zoom in on certain time periods
69 #plt.xlim([datetime.date(2022, 1, 1), datetime.date(2023, 1, 1)])
70 ax.grid()

```



```

In [29]: 1 daily["Eruo"]=df['Euro']
2         daily["Eruo"] = daily["Eruo"].ffill()
3         start = daily[["Eruo", "41_signal"]].index[0]
4         df1 = daily[daily.test != 0][["41_signal", "Eruo"]].copy()
5         df1['D'] = df1["41_signal"]
6         df1 = df1[:-1].copy()
7         df1['s_current'] = daily[daily.index.isin(df1.index)][ "Eruo"].values
8         df1['s_future'] = daily[daily.index.isin(df1.index+datetime.timedelta(41))][ "Eruo"].values
9
10        # Get the realized exchange rate
11        df1['R'] = np.where(df1['s_future'] >= df1['s_current'], 1, -1)
12        ## Sample Covariance
13        df1['W'] = (df1['D']-np.mean(df1['D']))*(df1['R']-np.mean(df1['R']))
14        T_B = np.mean(df1['W'])
15        ## Newey-West LRV estimator
16        dy = df1['W'] - np.mean(df1['W'])
17        gamma_0 = sum((dy)**2)/len(df1)
18        gamma_1 = np.mean((dy*dy.shift(-1))[:len(df1)-1])
19        LRV = gamma_0 + 2*(1-1/2)*gamma_1
20        ## Test-statistic
21        from scipy.stats import norm
22
23        statistic = T_B/np.sqrt(LRV/df1.shape[0])
24        print('Test statistic : ', statistic, ', 5 % critical value : ', round(norm.ppf(0.95),2))

```

Test statistic : -0.02468504071733396 , 5 % critical value : 1.64

```

In [30]: 1 # Weighted Mean
2         df1['W_2'] = df1['D']*(df1['s_future']-df1['s_current'])
3         T_WB = np.mean(df1['W_2'])
4         ## Newey-West LRV estimator
5         dy_2 = df1['W_2'] - np.mean(df1['W_2'])
6         gamma_0 = sum((dy_2)**2)/len(df1)
7         gamma_1 = np.mean((dy_2*dy_2.shift(-1))[:len(df1)-1])
8         LRV_2 = gamma_0 + 2*(1-1/2)*gamma_1
9         ## Test-statistic
10        statistic_2 = T_WB/np.sqrt(LRV_2/len(df1))
11        print('Test statistic : ', statistic_2, ', 5 % critical value : ', round(norm.ppf(0.95),2))

```

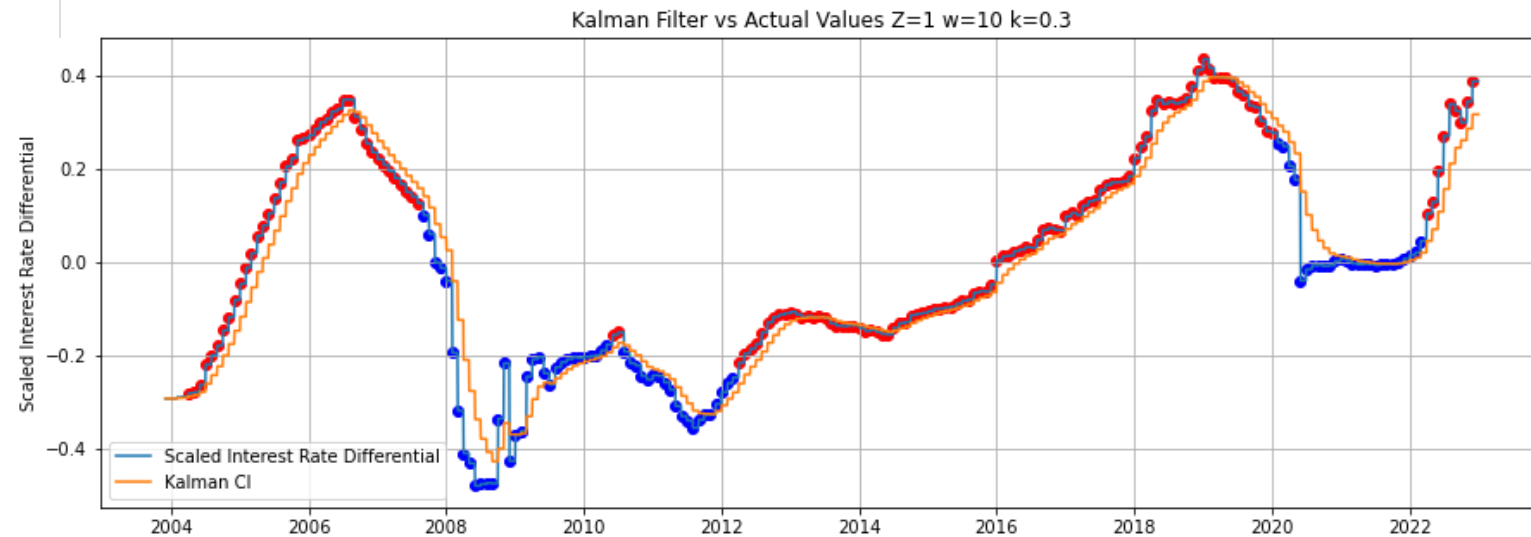
Test statistic : -0.04557798345955551 , 5 % critical value : 1.64


```
In [31]: 1 k = 0.3
2 w = 10
3 z = 1
4
5 df["Filter"] = df.ir_diff.ewm(alpha = k, adjust = False).mean()
6 # Create a dataframe at a daily frequency wiyh start and end
7 # dates that cover the observation period
8 drange = pd.date_range(start =df.index[0], end = "01/01/2023")
9 daily = pd.DataFrame(index = drange)
10
11 # Integrate the monthly dta into the daily data
12 daily["test"] = df["test"]
13
14 daily["Upper"] = df["Upper"]
15 daily["Lower"] = df["Lower"]
16 daily["Filter"] = df["Filter"]
17 daily["ir_diff"] = df["ir_diff"]
18
19 # Fill NA values with the last available value
20 daily["Upper"] = daily["Upper"].ffill()
21 daily["Lower"] = daily["Lower"].ffill()
22 daily["Filter"] = daily["Filter"].ffill()
23 daily["ir_diff"] = daily["ir_diff"].ffill()
24
25 # fill the remaining NA values with 0's
26 # also populates the test column
27 daily = daily.fillna(0)
28
29 # We let the holding period (i) be 41 days
30 i = 41
31
32 # create a new column that we will populate with our daily position
33 daily.loc[:, str(i)+"_signal"] = 0
34
35 # loop through each day in the dataset
36 for j in daily.index:
37     # If our monthly signal is not 0
38     if daily.loc[j, "test"] != 0:
39         # Make the next i days equal to the monthly signal
40         daily.loc[j:j+datetime.timedelta(i), str(i)+"_signal"] = daily.loc[j, "test"]
41
42 # Below is the holding period I use for the CI strategy
43 i = 171
44 daily.loc[:, str(i)+"_signal"] = 0
45 for j in daily.index:
46     if daily.loc[j, "test"] != 0:
47         daily.loc[j:j+datetime.timedelta(i), str(i)+"_signal"] = daily.loc[j, "test"]
48
49 data2 = daily.dropna()
50 fig, ax = plt.subplots(figsize = (15, 5))
```

```

51 ax.set_title("Kalman Filter vs Actual Values " + "Z="+str(z) + " w=" + str(w)+ " k=" + str(k))
52
53 ax.set_ylabel("Scaled Interest Rate Differential")
54
55 # Plot the actual series and the filter
56 ax.plot(data2["ir_diff"])
57 ax.plot(data2["Filter"])
58
59 # This code block is used to add confidence intervals when z > 0
60 #ax.fill_between(data2.index, data2.Lower, data2.Upper, color='b', alpha=.2)
61
62 # add scatterplots using boolean indexing
63 # We change the colors and shapes based on the conditions
64 ax.scatter(data2[data2.test == 1].index, data2[data2.test == 1]["ir_diff"], color = "blue")
65 ax.scatter(data2[data2.test == -1].index, data2[data2.test == -1]["ir_diff"], color = "red")
66 ax.legend(["Scaled Interest Rate Differential", "Kalman CI"])
67
68 # this code can let us zoom in on certain time periods
69 #plt.xlim([datetime.date(2022, 1, 1), datetime.date(2023, 1, 1)])
70 ax.grid()

```



```

In [32]: 1 daily["Euro"]=df['Euro']
2 daily["Euro"] = daily["Euro"].ffill()
3 start = daily[["Euro", "41_signal"]].index[0]
4 df1 = daily[daily.test != 0][["41_signal", "Euro"]].copy()
5 df1['D'] = df1["41_signal"]
6 df1 = df1[:-1].copy()
7 df1['s_current'] = daily[daily.index.isin(df1.index)][ "Euro"].values
8 df1['s_future'] = daily[daily.index.isin(df1.index+datetime.timedelta(41))][ "Euro"].values
9
10 # Get the realized exchange rate
11 df1['R'] = np.where(df1['s_future'] >= df1['s_current'], 1, -1)
12 ## Sample Covariance
13 df1['W'] = (df1['D']-np.mean(df1['D']))*(df1['R']-np.mean(df1['R']))
14 T_B = np.mean(df1['W'])
15 ## Newey-West LRV estimator
16 dy = df1['W'] - np.mean(df1['W'])
17 gamma_0 = sum((dy)**2)/len(df1)
18 gamma_1 = np.mean((dy*dy.shift(-1))[:len(df1)-1])
19 LRV = gamma_0 + 2*(1-1/2)*gamma_1
20 ## Test-statistic
21 from scipy.stats import norm
22
23 statistic = T_B/np.sqrt(LRV/df1.shape[0])
24 print('Test statistic : ', statistic, ', 5 % critical value : ', round(norm.ppf(0.95),2))

```

Test statistic : -0.02468504071733396 , 5 % critical value : 1.64

```

In [33]: 1 # Weighted Mean
2 df1['W_2'] = df1['D']*(df1['s_future']-df1['s_current'])
3 T_WB = np.mean(df1['W_2'])
4 ## Newey-West LRV estimator
5 dy_2 = df1['W_2'] - np.mean(df1['W_2'])
6 gamma_0 = sum((dy_2)**2)/len(df1)
7 gamma_1 = np.mean((dy_2*dy_2.shift(-1))[:len(df1)-1])
8 LRV_2 = gamma_0 + 2*(1-1/2)*gamma_1
9 ## Test-statistic
10 statistic_2 = T_WB/np.sqrt(LRV_2/len(df1))
11 print('Test statistic : ', statistic_2, ', 5 % critical value : ', round(norm.ppf(0.95),2))

```

Test statistic : -0.04557798345955551 , 5 % critical value : 1.64

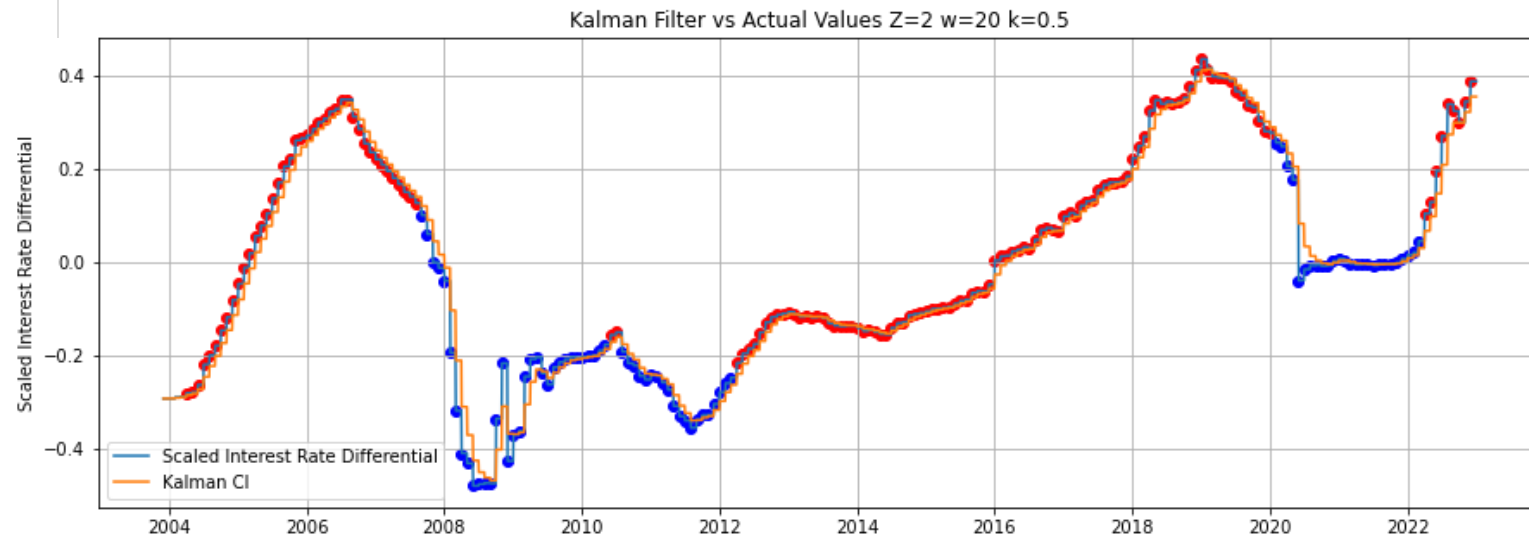

```
In [34]: 1 k = 0.5
2 w = 20
3 z = 2
4
5 df["Filter"] = df.ir_diff.ewm(alpha = k, adjust = False).mean()
6 # Create a dataframe at a daily frequency wiyh start and end
7 # dates that cover the observation period
8 drange = pd.date_range(start =df.index[0], end = "01/01/2023")
9 daily = pd.DataFrame(index = drange)
10
11 # Integrate the monthly dta into the daily data
12 daily["test"] = df["test"]
13
14 daily["Upper"] = df["Upper"]
15 daily["Lower"] = df["Lower"]
16 daily["Filter"] = df["Filter"]
17 daily["ir_diff"] = df["ir_diff"]
18
19 # Fill NA values with the last available value
20 daily["Upper"] = daily["Upper"].ffill()
21 daily["Lower"] = daily["Lower"].ffill()
22 daily["Filter"] = daily["Filter"].ffill()
23 daily["ir_diff"] = daily["ir_diff"].ffill()
24
25 # fill the remaining NA values with 0's
26 # also populates the test column
27 daily = daily.fillna(0)
28
29 # We let the holding period (i) be 41 days
30 i = 100
31
32 # create a new column that we will populate with our daily position
33 daily.loc[:, str(i)+"_signal"] = 0
34
35 # loop through each day in the dataset
36 for j in daily.index:
37     # If our monthly signal is not 0
38     if daily.loc[j, "test"] != 0:
39         # Make the next i days equal to the monthly signal
40         daily.loc[j:j+datetime.timedelta(i), str(i)+"_signal"] = daily.loc[j, "test"]
41
42 # Below is the holding period I use for the CI strategy
43 i = 100
44 daily.loc[:, str(i)+"_signal"] = 0
45 for j in daily.index:
46     if daily.loc[j, "test"] != 0:
47         daily.loc[j:j+datetime.timedelta(i), str(i)+"_signal"] = daily.loc[j, "test"]
48
49 data2 = daily.dropna()
50 fig, ax = plt.subplots(figsize = (15, 5))
```



```

51 ax.set_title("Kalman Filter vs Actual Values " + "Z="+str(z) + " w=" + str(w)+ " k=" + str(k))
52
53 ax.set_ylabel("Scaled Interest Rate Differential")
54
55 # Plot the actual series and the filter
56 ax.plot(data2["ir_diff"])
57 ax.plot(data2["Filter"])
58
59 # This code block is used to add confidence intervals when z > 0
60 #ax.fill_between(data2.index, data2.Lower, data2.Upper, color='b', alpha=.2)
61
62 # add scatterplots using boolean indexing
63 # We change the colors and shapes based on the conditions
64 ax.scatter(data2[data2.test == 1].index, data2[data2.test == 1]["ir_diff"], color = "blue")
65 ax.scatter(data2[data2.test == -1].index, data2[data2.test == -1]["ir_diff"], color = "red")
66 ax.legend(["Scaled Interest Rate Differential", "Kalman CI"])
67
68 # this code can let us zoom in on certain time periods
69 #plt.xlim([datetime.date(2022, 1, 1), datetime.date(2023, 1, 1)])
70 ax.grid()

```



```

In [35]: 1 daily["Euro"]=df['Euro']
2 daily["Euro"] = daily["Euro"].ffill()
3 start = daily[["Euro", "100_signal"]].index[0]
4 df1 = daily[daily.test != 0][["100_signal", "Euro"]].copy()
5 df1['D'] = df1["100_signal"]
6 df1 = df1[:-1].copy()
7 df1['s_current'] = daily[daily.index.isin(df1.index)][ "Euro"].values
8 df1['s_future'] = daily[daily.index.isin(df1.index+datetime.timedelta(41))][ "Euro"].values
9
10 # Get the realized exchange rate
11 df1['R'] = np.where(df1['s_future'] >= df1['s_current'], 1, -1)
12 ## Sample Covariance
13 df1['W'] = (df1['D']-np.mean(df1['D']))*(df1['R']-np.mean(df1['R']))
14 T_B = np.mean(df1['W'])
15 ## Newey-West LRV estimator
16 dy = df1['W'] - np.mean(df1['W'])
17 gamma_0 = sum((dy)**2)/len(df1)
18 gamma_1 = np.mean((dy*dy.shift(-1))[:len(df1)-1])
19 LRV = gamma_0 + 2*(1-1/2)*gamma_1
20 ## Test-statistic
21 from scipy.stats import norm
22
23 statistic = T_B/np.sqrt(LRV/df1.shape[0])
24 print('Test statistic : ', statistic, ', 5 % critical value : ', round(norm.ppf(0.95),2))

```

Test statistic : -0.02468504071733396 , 5 % critical value : 1.64

```

In [36]: 1 # Weighted Mean
2 df1['W_2'] = df1['D']*(df1['s_future']-df1['s_current'])
3 T_WB = np.mean(df1['W_2'])
4 ## Newey-West LRV estimator
5 dy_2 = df1['W_2'] - np.mean(df1['W_2'])
6 gamma_0 = sum((dy_2)**2)/len(df1)
7 gamma_1 = np.mean((dy_2*dy_2.shift(-1))[:len(df1)-1])
8 LRV_2 = gamma_0 + 2*(1-1/2)*gamma_1
9 ## Test-statistic
10 statistic_2 = T_WB/np.sqrt(LRV_2/len(df1))
11 print('Test statistic : ', statistic_2, ', 5 % critical value : ', round(norm.ppf(0.95),2))

```

Test statistic : -0.04557798345955551 , 5 % critical value : 1.64

The behavior of the strategy did not really change. After trying different parameters, I got very similar results and all strategies with different parameters passed all tests. I noticed that as I increase the values of k, z, w; the Kalman confidence interval and the Scaled Interest Rate Differential fit the data slightly better.

3

In [83]: 1 **import** math

```
In [93]: 1 face_value = 1000
2 coupon = 50
3 market_price = 984.96
4 t = 10
5
6 YTM = ((50 + (face_value-market_price)/2))/face_value+market_price/2
7
8
9 print("YTM = {:.5f}".format(ytm))
```

YTM = 0.05000

```
In [94]: 1 probability = 0.2
2 expected_cash_flow = (1 - probability) * face_value
3 present_value = expected_cash_flow / (1 + ytm)
4 present_value
```

Out[94]: 761.9047619047619

4

A

```
In [103]: 1 def yield_to_maturity(face_value, coupon_rate, market_price, iterations=100):
2         ytm = coupon_rate
3         for i in range(iterations):
4             modified_duration = face_value / (coupon_rate + ytm)
5             ytm = coupon_rate + (market_price - face_value) / modified_duration
6         return ytm
7
8 face_value = 1000
9 coupon_rate = 50 / face_value
10 market_price = 1000
11
12 ytm = yield_to_maturity(face_value, coupon_rate, market_price)
13 print("Yield to maturity:", ytm)
```

Yield to maturity: 0.05

```
In [104]: 1 probability = 0.2
2 expected_cash_flow = (1 - probability) * face_value
3 present_value = expected_cash_flow / (1 + ytm)
4 present_value
```

Out[104]: 761.9047619047619

B

```
In [96]: 1 def cashFlw(F, c, n):
2     csh = F*c
3     cf = list()
4     for i in range(n-1):
5         cf.append(csh)
6     cf.append(F + csh)
7     return cf
8
9 def discount(r, n):
10    d = list()
11    for i in range(1, n+1):
12        d.append(1/((1+r)**i))
13    return d
14
15 def numerator(F, c, r, n):
16    cf = cashFlw(F, c, n)
17    d = discount(r, n)
18    total = 0
19    for i in range(1, n+1):
20        total += (i*cf[i-1]*d[i-1])
21    return total
22
23 def denominator(F, c, r, n):
24    csh = F*c
25    den = 0
26    for i in range(1, n):
27        den = den + (csh/((1+r)**i))
28    den += ((csh+F)/((1+r)**n))
29    return den
30
31 def duration(F, c, r, n):
32    num = numerator(F, c, r, n)
33    den = denominator(F, c, r, n)
34    return num/den
```

```
In [100]: 1 # 10-Year Coupon Bond
          2
          3 F = 1000
          4 n = 10
          5 i = 0.1
          6 c = 0.15
          7
          8 duration1 = duration(F, c, i, n)
          9 duration1
```

Out[100]: 6.281090250274969

```
In [102]: 1 # 7-Year Coupon Bond
          2
          3
          4 F2 = 1000
          5 n2 = 7
          6 i2 = 0.03
          7 c2 = 0.03
          8
          9 duration2 = duration(F2, c2, i2, n2)
         10 duration2
```

Out[102]: 6.417191443878188

Despite the magnitude of change in interest rate, the 7-year coupon bond would experience a greater change since it has a slightly higher duration, implying that is is more sensitive to changes in interest rates.

C

Portfolio duration = $(0.3 \times 6.417) + (0.7 \times 6.237) = 6.291$

5

A

The ECP announced that they would raise the interest rate by 0.5% in Feb 2023 preceding an increase of 0.5% in Dec 2022. In Dec 2022, the ECP was reassessing the rate of holdings of securities but in Feb 2023 they decided to reduce their holdings of securities. In both statements, The FOMC decided to raise the interest rate by 0.25% in Feb 2023 and Dec 2022. Both FOMC statements were not different to me. They increased interest rates to reduce unemployment & inflation and

they decided to reduce their treasury holdings.

B

Despite the ECP's clear intentions of increasing interest rates consistently, I was surprised that the Euro depreciated because I expected foreign investments to sufficiently increase money to flow through EU countries and reduce inflation. Nothing surprised me in the the FOMC February statement. What is most surprising is that they both decided to raise interest rates within a few months.

C

There might have not been enough foreign investments in Europe. The ECP has the capability of reducing their treasury holdings even more to attempt to reduce inflation.

6

The Federal reserve can sell more government bonds to decrease money supply, which could slow down economic growth and therefore lower inflation.