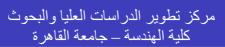


### مشروع الطرق المؤدية إلى التعليم العالى





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## مشروع الطرق المؤدية إلى التعليم العالى

#### الشر كاء

- كلية الهندسة، جامعة القاهرة. مؤسسة فورد.
- جامعات: القاهرة، وعين شمس، وأسيوط، وحلوان، والمنيا، وجنوب الوادى، والفيوم، وبنى سويف، وسوهاج.
  - جمعية جيل المستقبل. المجلس القومي للمرأة.

#### الكتب الانجليزية

- **1-** Planning and Controlling.
- **2-** Systems and Creative Thinking.
- **3-** Research Methods and Writing Research Proposals.
- 4- Statistical Data Analysis.
- 5- Teams and Work Groups.
- **6-** Risk Assessment and Risk Management.
- 7- Communication Skills.
- 8- Negotiation Skills.
- 9- Analytical Thinking.
- **10-** Problem Solving and Decision Making.
- 11- Stress Management.
- **12-** Accounting for Management and Decision Making.
- 13- Basics of Managerial Economics.
- **14-** Economic Feasibility Studies.
- **15-** Health, Safety and Environment.
- **16-** Wellness Guidelines: Healthful Life.
- 17- General Lectures Directory.

موقع المشروع على شبكة الإنترنت www.Pathways.cu.edu.eg

#### رسالة المشروع

رفع مهارات الطلاب والخريجين من الجامعات المختلفة لمساعدتهم على الاندماج السريع في المجتمع وصقل مهاراتهم بما يتناسب مع حاجة البحث العلمي وسوق العمل.

#### مطبوعات البرامج التدريبية الكتب العربية

- ١- المحاجة: طرق قياسها وأساليب تنميتها.
- ٢- القواعد اللغوية الأساسية للكتابة العلمية.
- ٣- دليل مشروعات التخرج من برنامج "تنمية مهارات البحث العلمى".
  - ٤- التخطيط والرقابة.
  - ٥- التفكير النمطي والإبداعي.
  - ٦- مناهج البحث وكتابة المشروع المقترح للبحث.
    - ٧- التحليل الإحصائي للبيانات.
    - ٨- تكوين الفرق والعمل الجماعي.
      - ٩- تقييم وإدارة المخاطر.
        - ١٠ ـ مهارات الاتصال.
        - ١١- مهارات التفاوض.
  - ١٢- التفكير التحليلى: القدرة والمهارة والاسلوب.
    - ١٣- حل المشاكل وصنع القرار.
      - ٤١- إدارة الضغوط.
    - ١٥- المحاسبة للإدارة وصنع القرار.
      - ١٦- أساسيات الاقتصاد الإداري.
      - ١٧ ـ دراسات الجدوى الاقتصادية.
- ١٨- البيئة والتنمية المستدامة: الإطار المعرفى والتقييم المحاسبي.
- ١٩- إرشادات الصحة العامة: من أجل حياة صحية.
  - ٢- إنشاء المشروعات الصغيرة وتنميتها.
  - ٢١ ـ أضواء حول الموضوعات المعاصرة.

الناشر: مركز تطوير الدراسات العليا والبحوث – كلية الهندسة – جامعة القاهرة. ت: ٥٦٧٨٢١٦ (٢٠٢+)، ٥٦٧٨٢١٦ (٢٠٠٠) فاكس: ٥٧١٦٦٢٠ (٢٠٠٠) دعوة على شبكة الإنترنت: www.capscu.com بريد إلكتروني: capscu@capscu.com

# إعداد أ.د. أماني موسى محمد

القاهرة ۲۰۰۷ الترقيم الدولى: 7-137-403 ISBN الترقيم الدولى: 7-137

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## النتائج التعليمية المستهدفة

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Statistica Status Statistics

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.Descriptive Statistics .Statistical Inference

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                                                 Quantitative
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D	В	Е	C	D	В	D	C	Е	A
В	Е	C	D	В	D	D	A	Е	C
С	D	A	C	Е	D	C	C	D	В
D	Е	D	D	A	D	D	C	D	C
D	A	В	D	В	D	C	D	C	Е
D	В	C	C	Е	D	C	C	D	A

 $\dots$ (B) (A)

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51	95	70	74	73	90	71	74	90	67
91	72	83	89	50	80	72	84	85	69
62	82	87	76	91	76	87	75	78	79
71	96	81	88	64	82	73	57	86	70
80	81	75	85	74	90	83	66	77	91

70 90 80 .(Quantitative Data) (Qualitative Data) :(Qualitative Data) . () :(Quantitative Data) ( .(Frequency Distribution) f (HHT)

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A		6
В	<i> </i>	8
С	## ## ## I	16
D		22
Е	JHT	8
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A	6
В	8
С	16
D	22
Е	8
	60

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A	В	С	D	Е	
6	8	16	22	8	60

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(Range)

R = 97 - 50 = 47 : R

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 $L = 47 / 5 = 9.4 \sim 10$ 

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. 50+10 = 60 :

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		( )
50-59	III	3
60-69	JHT 111	5
70-79	####### III	18
80-89	HT HTHT1	16
90-99	HT III	8
		50

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3
5
18
16
8
50

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50-59	60-69	70-79	80-89	90-99	
3	5	18	16	8	50

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.Relative Frequency Table

.Percentage Frequency Table •

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	50-59	0.06
	60-69	0.10
	70-79	0.36
	80-89	0.32
	90-99	0.16
		1.00

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50-59	6
60-69	10
70-79	36
80-89	32
90-99	16
	100

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49.5-59.5	3
59.5-69.5	5
69.5-79.5	18
79.5-89.5	16
89.5-99.5	8
	50

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	( )		:(	( - )	
50.50	40.5.50.5	545	2	0.06	(
50-59	49.5-59.5	54.5	3	0.06	6
60-69	59.5-69.5	64.5	5	0.10	10
70-79	69.5-79.5	74.5	18	0.36	36
80-89	79.5-89.5	84.5	16	0.32	32
90-99	89.5-99.5	94.5	8	0.16	16
			50	1.00	100

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#### **Cumulative Frequency "Less Than"**

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< 49.5	0
<59.5	3
<69.5	8
<79.5	26
<89.5	42
<99.5	50

#### **Cumulative Frequency "or More"**

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> 49.5	50
>59.5	47
>69.5	42
>79.5	24
>89.5	8
>99.5	0

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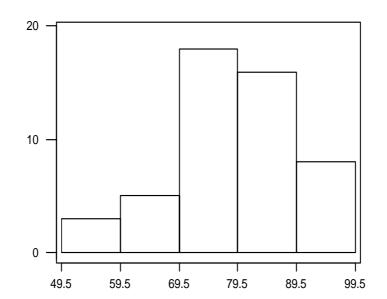
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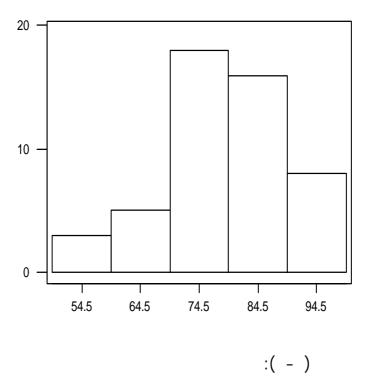
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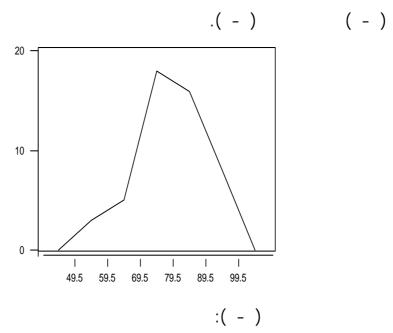
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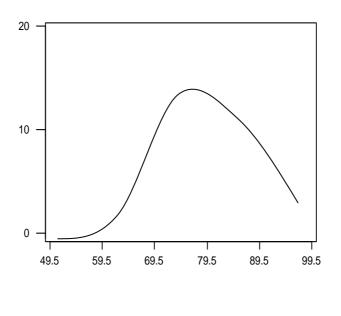
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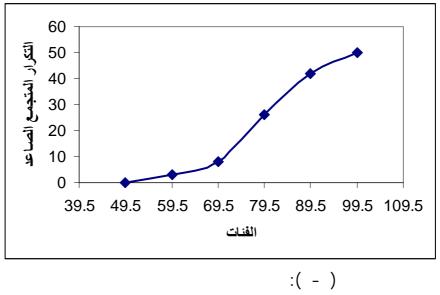
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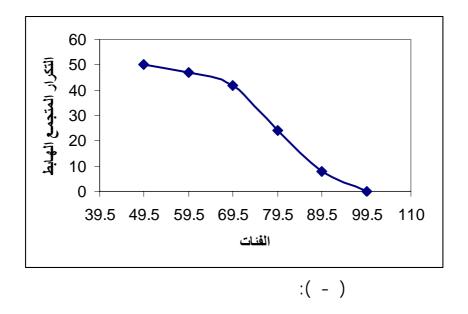


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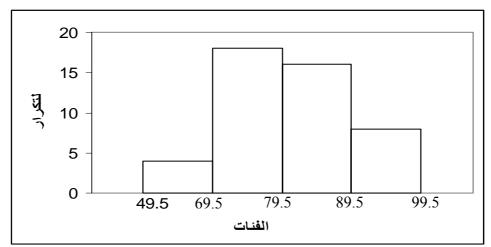
			- (	,
50-69	70-79	80-89	90-99	
8	18	16	8	50

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49.5-69.5	69.5-79.5	79.5-89.5	89.5-99.5
8	18	16	8
4	18	16	8

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132	125	117	124	103	117	110	127	96	129
130	122	118	114	103	119	106	125	114	100
125	128	106	111	115	123	119	114	117	143
136	92	115	118	121	137	139	120	104	125
119	115	101	129	87	108	110	133	135	126
127	103	110	126	118	82	104	137	120	95
146	126	119	105	132	126	118	100	113	119
106	125	117	102	146	129	124	113	95	148

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80-89, 90-99, 100-109, ..., 140-149

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44	98	40	60	66	71	82	64	72	68
55	69	77	78	88	60	65	68	79	69
62	64	71	66	61	75	83	70	55	62
57	72	61	62	74	62	67	66	60	50

40-49, 50-59,..., 90-99

_		
	0-59	E
-		
	60-69	D
	70-79	C
	80-89	В
	90-99	A

50-59	60-69	70-79	80-89	90-99	100-119	120-129
8	10	16	15	10	8	3

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155-	158-	161-	164-	167-	170-	173-	176-
4	10	77	235	368	220	80	6

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 $\sum (x_1, x_2, ..., x_n)$ 

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 $\sum_{i=1}^{n} x_i = x_1 + x_2 + \dots + x_n$ 

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 $\sum x$  y. x

 $c (y_1, y_2, ..., y_n)$ 

(i)  $\sum_{i=1}^{n} (x_i \pm y_i) = \sum_{i=1}^{n} x_i \pm \sum_{i=1}^{n} y_i$ 

(ii)  $\sum_{i=1}^{n} c = nc$ 

(iii)  $\sum_{i=1}^{n} cx_i = c \sum_{i=1}^{n} x_i$ 

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 $(x_1, x_2, ..., x_n) x$ 

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 $\overline{x} = \frac{x_1 + x_2 + \dots + x_n}{n}$   $= \frac{1}{n} \sum_{i=1}^{n} x_i$ 

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60, 72, 40, 80, 63

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 $\sum_{i=1}^{5} x_i = 60 + 72 + 40 + 80 + 63$ = 315

· ( ) : /

$$\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i = \frac{1}{5} (315) = 63$$

.

$$\sum_{i=1}^{5} x_i = 63 + 63 + 63 + 63 + 63 = 315$$

$$f_1, f_2, ..., f_k$$
  $(x_1, x_2, ..., x_k)$   $k$ 

:

$$\overline{x} = \frac{f_1 x_1 + f_2 x_2 + \dots + f_k x_k}{f_1 + f_2 + \dots + f_k}$$

$$= \frac{\sum_{i=1}^k f_i x_i}{\sum_{i=1}^k f_i}$$

$$= \frac{1}{n} \sum_{i=1}^k f_i x_i$$

 $n = \sum_{i=1}^{k} f_i$ 

 $: \qquad \qquad \overline{x} \qquad \qquad : \textbf{()}$ 

5-6	7-8	9-10	11-12	13-14
2	5	8	4	1

•

	(x)	(f)	x f
5-6	5.5	2	11
7-8	7.5	5	37.5
9-10	9.5	8	76
11-12	11.5	4	46
13-14	13.5	1	13.5
		20	184

$$\bar{x} = \frac{1}{n} \sum_{i=1}^{k} f_i x_i = \frac{1}{20} (184) = 9.2$$

$$(d_1, d_2, ..., d_n)$$
  $(x_1, x_2, ..., x_n)$ 

$$d_i = x_i - \overline{x}, \qquad i = 1, 2, \dots, n$$

$$\sum_{i=1}^{n} (x_i - \bar{x}) = \sum_{i=1}^{n} d_i = 0$$

$$\overline{x} = \frac{1}{n} \sum_{i=1}^{n} x_i \Rightarrow n \ \overline{x} = \sum_{i=1}^{n} x_i \qquad \dots (1)$$

$$\therefore \sum_{i=1}^{n} (x_i - \bar{x}) = \sum_{i=1}^{n} x_i - \sum_{i=1}^{n} \bar{x} = \sum_{i=1}^{n} x_i - n \; \bar{x} = 0 \qquad \dots (2)$$

$$(x_1, x_2, \dots, x_n)$$
  $x$  :

$$(d_1, d_2, ..., d_n)$$

$$d_i = x_i \pm b$$
,  $i = 1, 2, ..., n$ 

$$\bar{x} = \bar{d} \mp b$$

 $\therefore d_i = x_i \pm b, \qquad i = 1, 2, ..., n$ 

$$\Rightarrow \sum_{i=1}^{n} d_i = \sum_{i=1}^{n} (x_i \pm b) = \sum_{i=1}^{n} x_i \pm n b$$

$$\Rightarrow \frac{1}{n} \sum_{i=1}^{n} d_i = \frac{1}{n} \sum_{i=1}^{n} x_i \pm b$$

$$\Rightarrow \overline{d} = \overline{x} \pm b$$
$$\Rightarrow \overline{x} = \overline{d} \mp b$$

$$\Rightarrow \bar{x} = \bar{d} \mp b$$

: 
$$\sum_{i=1}^{5} d_i$$
  $b = 50$  ()

$$\sum_{i=1}^{5} d_i = (60 - 50) + (72 - 50) + (40 - 50) + (80 - 50) + (63 - 50)$$
$$= 10 + 22 - 10 + 30 + 13 = 65$$

 $\bar{d} = \frac{1}{5} (65) = 13$  $\bar{x} = \frac{5}{d} + b = 13 + 50 = 63$ 

 $(x_1, x_2, ..., x_n)$ 

 $\overline{(ax)} = a \overline{x}$ 

.( )

 $\overline{(ax \pm b)} = a \ \overline{x} \pm b$ 

 $(x_1, x_2, ..., x_n)$ 

 $\sum_{i=1}^{n} (x_i - c)^2 \ge \sum_{i=1}^{n} (x_i - \bar{x})^2 , \bar{x} \neq c$ 

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60, 72, 40, 80, 63

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40, 60, 63, 72, 80 ) 63 () .( :( ) 72, 60, 72, 40, 80, 63 40, 60, 63, 72, 72, 80 Med = (63+72) / 2 = 67.5 $f_1$  $f_2$  $\boldsymbol{A}$ L $f_2$  $f_1$ 

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< 4.5	0
< 6.5	2
< 8.5	7
< 10.5	15
< 12.5	19
< 14.5	20

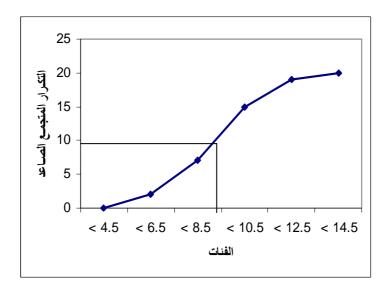
15, 7 10 
$$\left(\frac{20}{2} = 10\right)$$
 : 10  $A = 8.5$ ,  $f_1 = 7$ ,  $f_2 = 15$ ,  $L = 10.5 - 8.5 = 2$ 

Med =  $8.5 + \frac{10 - 7}{15 - 7}$ . 2 = 9.25,

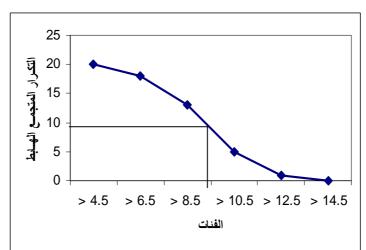
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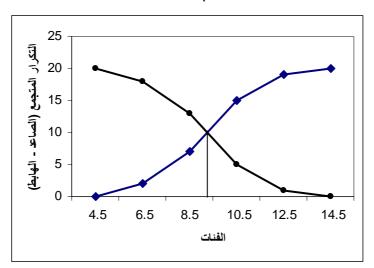
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 $\sum_{i=1}^{n} \left| x_i - Med \right| \leq \sum_{i=1}^{n} \left| x_i - a \right|$ 

 $a \neq Med$ :

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2, 6, 9, 4, 6, 10, 6

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4, 3, 7, 9, 4, 4, 7, 4

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5, 7, 5, 7, 8, 9, 7, 5, 10

7 5 : .5,7

: :( ) 4, 9, 8, 12, 11, 7, 15

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 $f_1$ 

 $\cdot f$  A

L -

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$$Mod = A + \frac{f - f_1}{2f - f_1 - f_2}.$$
 L

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5 – 6	7 – 8	9 – 10	11 – 12	13 – 14
2	5	8	4	1

f = 8,  $f_1 = 5$ ,  $f_2 = 4$ , A = 8.5L = 10.5 - 8.5 = 2

 $Mod = 8.5 + \frac{8-5}{16-5-4}.2$ 

Mod = 9.36

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 $x_1, x_2, ..., x_n$  G.M.  $\sqrt[n]{x_1 x_2 ... x_n} \text{ G.M.} = :$ 

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 $Log G.M. = \frac{1}{n} \left( \sum_{i=1}^{n} Log(x_i) \right)$ 

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3, 5, 6, 6, 7, 10, 12

G.M.=  $\sqrt[7]{3.5.6.6.7.10.12}$ 

:

Log G.M.= 
$$\frac{1}{7}$$
 (Log 3 + Log 5 + Log 6 + Log 6 + Log 7 + Log 10 + Log 12)  
=  $\frac{1}{7}$  (0.4771 + 0.699 + 0.7782 + 0.7782 + 0.8451 + 1 + 1.0729)  
= 0.8081  
G.M.= 6.43

$$\bar{x} = \frac{1}{7}(3+5+6+6+7+10+12) = 7$$

G.M.  $\bar{x}$ 

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 $X_2, \dots, X_k$ 

k

G.M.=  $\sqrt[n]{x_1^{f_1} x_2^{f_2} ... x_n^{f_n}}$ 

 $f_1, f_2, ..., f_k$ 

 $n = \sum_{i=1}^k f_i :$ 

 $X_1, X_2, ..., X_n$ 

Н

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$$H = \frac{1}{\frac{1}{n} \sum_{i=1}^{n} \frac{1}{x_i}} = \frac{n}{\sum_{i=1}^{n} \frac{1}{x_i}}$$

.

$$\frac{1}{H} = \frac{1}{n} \sum_{i=1}^{n} \frac{1}{x_i}$$

:( )

3,5,6,6,7,10,12

 $\frac{1}{H} = \frac{1}{7} \left( \frac{1}{3} + \frac{1}{5} + \frac{1}{6} + \frac{1}{6} + \frac{1}{10} + \frac{1}{12} \right)$  $\frac{1}{H} = \frac{1}{7} \left( \frac{140 + 84 + 70 + 70 + 60 + 42 + 35}{420} \right)$  $\frac{1}{H} = \frac{501}{2940} \Rightarrow H = 5.87$ 

 $f_1, f_2, ..., f_k$   $x_1, x_2, ..., x_k$ : k

 $\frac{1}{H} = \frac{1}{n} \sum_{i=1}^{n} \frac{f_i}{x_i} = \frac{1}{n} \left( \frac{f_1}{x_1} + \frac{f_2}{x_2} + \dots + \frac{f_k}{x_k} \right)$  $n = \sum_{i=1}^{k} f_i :$ 

 $Q_1$   $Q_3$   $Q_2$   $Q_1$ 

 $Q_3$  ( )  $Q_2$  $D_9 \quad \dots \quad D_2 \quad D_1$ 

 $D_1$  $D_2$ 

 $P_1$   $P_{99}$  ...  $P_2$   $P_1$ 

$$\frac{2n}{4}$$
 $\frac{n}{4} \quad \frac{n}{2}$ 
 $\frac{2n}{100}$ 
 $\frac{n}{100} \quad \frac{n}{2}$ 
 $\vdots$ 

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< 4.5	0
< 4.5 < 6.5	2
$D_2$	
< 8.5	7
< 10.5	15
P <sub>90</sub>	
< 12.5	19
< 14.5	20

 $D_2$ 

$$D_2 = A + \frac{(\frac{2n}{10} - f_1)}{f_2 - f_1} L$$

$$f_2 \qquad f_1 \qquad n \qquad A$$

 $: \hspace{1cm} L$ 

$$D_2 = 6.5 + \frac{4-2}{7-2}.2 = 7.3$$

 $: \qquad \qquad P_{90}$ 

$$P_{90} = A' + \frac{\left(\frac{90n}{100} - f_1'\right)}{f_2' - f_1'} L$$

$$P_{90} = 10.5 + \frac{18 - 15}{19 - 15}.2 = 12$$

			:	y x	
х	1	2	4	-2	5
y	-1	1	5	-7	7

i) 
$$\sum x$$
,  $\sum y$ ,  $\sum xy$ ,  $\sum x^2$ ,  $\sum y^2$ ,  $\sum x^3$ ,  $\sum y^3$ ,  $\sum xy^2$   
ii)  $(\sum x)^2$ ,  $((\sum x) + 2)^2$ ,  $\sum (x - 3y)^2$ ,  $\sum x(x + 4)$ 

(i) 
$$\sum (\frac{y}{x}) = \frac{\sum y}{\sum x}$$
, ii)  $\sum xy = \sum x \sum y$ 

(iii) 
$$\sum (x-c)(x+c) = \sum x^2 - nc^2$$
, (iv)  $(\sum x)^2 = \sum x^2$ 

6,6,9,8,6,10,9,9,8,7,8,6,7,8,8,11,10,11,8,8

2	8
3	10
5	20
7	20
8	6
9	6

40-49	50-59	60-69	70-79	80-89	90-99
6	10	17	17	6	4

20-29	30-39	40-49	50-59	60-69	70-79
9	12	15	8	4	2

0, 2, 4, 6 : ()

( )

( )

: Z Y X

X	59,61,62,58,60
Y	50,60,66,54,70
Z	39,65,46,78,72

.Measures of Dispersion

- = R

:

. = -

. = -

:

: R :()

82, 40, 62, 70, 30, 80

= = :

R = 82 - 30 = 52

: R :()

40-49	50-59	60-69	70-79	80-89	90-99
2	9	15	11	2	1

: :

, = :

R = 94.5 - 44.5 = 50

, = :

, =

R = 99.5 - 39.5 = 60

:

. -

: .

Qn  $Q_2$   $Q_n$ 

 $\frac{n}{4}$   $Q_1$   $\frac{3n}{4}$   $Q_3$   $Q_3$   $Q_1$ 

 ${\mathcal Q}$ 

 $Q = \frac{Q_3 - Q_1}{2}, \qquad (1)$   $Q_2 \qquad \frac{n}{2} \qquad Q_2$ 

.

. Q

:

.  $Q_1$  -

.  $Q_3$  -

( )

:( )

67,65,69,58,55,71,72,70

55,58,65,67,69,70,71,72

$$Q_1 = \frac{58+65}{2} = 61.5,$$
  $Q_3 = \frac{70+71}{2} = 70.5$ 

 $Q = \frac{Q_3 - Q_1}{2} = 4.5$ 

:()

59,67,65,69,58,55,70,72,74

55,58,59,65,67,69,70,72,74

$$Q_1 = 59$$
,

$$Q_1 = 59,$$

$$Q_3 = 70$$

$$Q = \frac{Q_3 - Q_1}{2} = 5.5$$

 $Q_1$ 

 $Q_3$ 

( )  $Q_3$   $Q_1$ 

$$Q_{1} = A_{1} + \frac{\left(\frac{n}{4} - f_{1}\right)}{f_{2} - f_{1}} L, \qquad (2)$$

$$Q_3 = A_2 + \frac{(\frac{3n}{4} - f_1')}{f_2' - f_1'} L, \qquad (3)$$

.() :( )

< 20.5	0
< 39.5 < 49.5	2
<u>\ 49.3</u>	2
< 59.5	11
< 59.5 < 69.5	26
< 79.5	37
< 89.5	39
< 99.5	40

$$n = 40,$$
  $\frac{n}{4} = 10,$   $\frac{3n}{4} = 30,$   $L = 10$ 

$$Q_1 = 49.5 + (\frac{10-2}{11-2}) 10$$

$$Q_1 = 49.5 + 8.89 = 58.39$$

$$Q_3 = 69.5 + (\frac{30 - 26}{37 - 26}) 10$$

$$Q_3 = 69.5 + 3.64 = 73.14$$

$$Q = \frac{Q_3 - Q_1}{2} = 7.38$$

•

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•

.

 $\overline{x}$  : M.D.

M.D.= 
$$\frac{1}{n} \sum_{i=1}^{n} |x_i - \overline{x}|,$$
 (4)

:

$$M.D. = \frac{\sum_{i=1}^{n} f_i |x_i - \overline{x}|}{n}, \qquad (5)$$

n

.

:( )

6,5,7,7,8,9,9,5

:

x	$x-\overline{x}$	$ x-\overline{x} $
6	-1	1
5	-2	2
7	0	0
7	0	0
8	1	1
9	2	2
9	2	2
5	-2	2
56	0	10

$$\bar{x} = \frac{\sum x}{n}$$
 $\bar{x} = \frac{56}{8} = 7$ 
M.D.= $\frac{10}{8} = 1.25$ ,

( )

.( ):

:

Classes	х	f	f x	$x-\overline{x}$	$ x-\overline{x} $	$ x-\overline{x}  f$
40-49	44.5	2	89	-21.25	21.25	42.5
50-59	54.5	9	490.5	-11.25	11.25	101.25
60-69	64.5	15	967.5	-1.25	1.25	18.75
70-79	74.5	11	819.5	8.75	8.75	96.75
80-89	84.5	2	169	18.75	18.75	37.5
90-99	94.5	1	94.5	28.75	28.75	28.75
		40	2630			325

$$\bar{x} = \frac{\sum fx}{n}$$

$$\bar{x} = \frac{2630}{40} = 65.75$$

$$M.D. = \frac{325}{40} = 8.125,$$

:

( )

 $\sigma^{^2}$ 

:

N

 $\overline{X}$   $X_1, X_2, ..., X_N$  :

 $(X_1 - \overline{X})^2, (X_2 - \overline{X})^2, \dots, (X_N - \overline{X})^2$ 

$$\sigma^2$$

$$\sigma^2 = \frac{1}{N} \sum_{i=1}^{N} (X_i - \overline{X})^2 , \qquad (6)$$

.

$$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (X_i - \overline{X})^2} , \qquad (7)$$

 $\mathbf{J}^2$ 

 $: \qquad (n-1)$ 

.()

$$S^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \overline{x})^{2}, \qquad (8)$$

$$S = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (x_i - \overline{x})^2} , \qquad (9)$$

 $\sigma^2$   $S^2$  ( )

.

8,9,7,6,5

$$\bar{x} = \frac{\sum x}{n}$$

$$\bar{x} = \frac{35}{5} = 7$$

$$S^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2},$$

$$S^{2} = \frac{1}{5-1}(10) = 2.5$$
$$S = \sqrt{2.5} = 1.581,$$

: ()

$$S^{2} = \frac{1}{n-1} \left( \sum_{i=1}^{n} x_{i}^{2} - \frac{\left(\sum_{i=1}^{n} x_{i}\right)^{2}}{n} \right), \tag{10}$$

•

$$S^2 = \frac{1}{n-1} \sum_{i=1}^{n} (x_i - \overline{x})^2$$

$$S^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i}^{2} - 2x_{i}\overline{x} + \overline{x}^{2})$$

$$S^{2} = \frac{1}{n-1} \left( \sum_{i=1}^{n} x_{i}^{2} - 2 \bar{x} \sum_{i=1}^{n} x_{i} + n \bar{x}^{2} \right)$$

$$S^2 = \frac{1}{n-1} \left( \sum_{i=1}^{n} x_i^2 - n \overline{x}^2 \right)$$

$$S^{2} = \frac{1}{n-1} \left( \sum_{i=1}^{n} x_{i}^{2} - \frac{\left(\sum_{i=1}^{n} x_{i}\right)^{2}}{n} \right)$$

 $. \qquad \sum x^2 \quad \sum x \qquad \qquad ( \quad )$ 

.( ) :( )

х	$x^2$
8	64 81
9	81
7	49
6	36
5	49 36 25
35	255

$$S^{2} = \frac{1}{n-1} \left( \sum_{i=1}^{n} x_{i}^{2} - \frac{\left( \sum_{i=1}^{n} x_{i} \right)^{2}}{n} \right)$$

$$S^2 = \frac{1}{4}(255 - \frac{(35)^2}{5}) = 2.5$$

$$S = \sqrt{2.5} = 1.581$$
,

( )

$$c$$
 :

.

$$S^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2}$$

$$S^{2} = \frac{1}{n-1} \left( \sum_{i=1}^{n} [(d_{i} \pm c) - (\bar{d} \pm c)]^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (d_{i} - \bar{d})^{2} ,$$
(11)

:

:

$$S^{2} = \frac{1}{n-1} \left( \sum_{i=1}^{n} d_{i}^{2} - \frac{\left(\sum_{i=1}^{n} d_{i}\right)^{2}}{n} \right)$$

$$S^{2} = \frac{1}{4} \left( 30 - \frac{(10)^{2}}{5} \right) = 2.5$$

$$S = \sqrt{2.5} = 1.581,$$

$$()$$

:

;

 $c x_1, x_2, ..., x_n$ 

:  $d_1, d_2, ..., d_n$ 

 $d_1 = cx_1, d_2 = cx_2, ..., d_n = cx_n$ 

$$S_{x}^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2}$$

$$S_{x}^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (\frac{d_{i}}{c} - \frac{\bar{d}}{c})^{2} = \frac{1}{n-1} \frac{1}{c^{2}} \sum_{i=1}^{n} (d_{i} - \bar{d})^{2}$$

$$S_{x}^{2} = \frac{1}{c^{2}} S_{d}^{2}, \Rightarrow S_{x} = \frac{1}{c} S_{d}, \qquad (12)$$

( )

 $S_x = c S_d, (13)$ 

.( )

 $\bar{x}$  :

 $.\overline{x} \neq a$  a

:

$$\sum (x-a)^2 = \sum (x+\overline{x}-\overline{x}-a)^2$$

$$= \sum [(x-\overline{x})+(\overline{x}-a)]^2$$

$$= \sum (x-\overline{x})^2 + n(\overline{x}-a)^2 + 2(\overline{x}-a)\sum (x-\overline{x})$$

$$= \sum (x-\overline{x})^2 + n(\overline{x}-a)^2$$

 $n(\overline{x}-a)^2$ 

 $\sum (x-a)^2 < \sum (x-\overline{x})^2$   $S_2^2 \qquad S_1^2 \qquad \qquad n_2 \qquad n_1$  :

 $S^{2} = \frac{(n_{1} - 1)S_{1}^{2} + (n_{2} - 1)S_{2}^{2}}{n_{1} + n_{2} - 1}$ 

 $x_1, x_2, ..., x_{n_1}, y_1, y_2, ..., y_{n_2}$ 

$$S_1^2 = \frac{1}{n_1 - 1} \sum_{i=1}^{n_1} (x_i - \overline{x})^2$$

$$S_2^2 = \frac{1}{n_2 - 1} \sum_{i=1}^{n_2} (y_i - \overline{x})^2$$

$$(n_{1}-1) S_{1}^{2} = \sum_{i=1}^{n_{1}} (x_{i} - \bar{x})^{2}$$

$$(n_{2}-1) S_{2}^{2} = \sum_{i=1}^{n_{2}} (y_{i} - \bar{y})^{2}$$

$$(n_{1}-1) S_{1}^{2} + (n_{2}-1) S_{2}^{2} = \sum_{i=1}^{n_{1}} (x_{i} - \bar{x})^{2} + \sum_{i=1}^{n_{2}} (y_{i} - \bar{y})^{2} = \sum_{i=1}^{n_{1}+n_{2}} (z_{i} - \bar{x})^{2}$$

$$\therefore S^{2} = \frac{(n_{1}-1)S_{1}^{2} + (n_{2}-1)S_{2}^{2}}{n_{1} + n_{2} - 1}$$

$$\vdots$$

$$f_{1}, f_{2}, ..., f_{k} \qquad x_{1}, x_{2}, ..., x_{k} \qquad k$$

$$\vdots \qquad ( ) ( ) ( )$$

$$S^{2} = \frac{1}{n-1} \sum_{i=1}^{n} f_{i} (x_{i} - \overline{x})^{2}, S = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} f_{i} (x_{i} - \overline{x})^{2}}, \qquad (14)$$

$$S^{2} = \frac{1}{n-1} \left( \sum_{i=1}^{n} f_{i} x_{i}^{2} - \frac{\left(\sum_{i=1}^{n} f_{i} x_{i}\right)^{2}}{n} \right), \tag{15}$$

$$S^{2} = \frac{1}{n-1} \left( \sum_{i=1}^{n} f_{i} d_{i}^{2} - \frac{\left(\sum_{i=1}^{n} f_{i} d_{i}\right)^{2}}{n} \right), \tag{16}$$

: ( ) - :

Classes	X	f	xf	$x-\overline{x}$	$(x-\overline{x})^2$	$(x-\overline{x})^2 f$
40-49	44.5	2	89	-21.25	451.56	903.13
50-59	55.5	9	490.5	-11.25	126.56	1139.06
60-69	65.5	15	967.5	-1.25	1.56	23.44
70-79	75.5	11	819.5	8.75	76.56	842.19
80-89	85.5	2	169	18.75	351.56	703.13
90-99	95.5	1	94.5	28.75	826.56	826.56
Total		40	2630			4437.5

$$\bar{x} = \frac{1}{n} \sum_{i=1}^{k} f_i x_i = \frac{1}{40} (2630) = 65.75$$

$$S^2 = \frac{1}{n-1} \sum_{i=1}^{n} f_i (x_i - \bar{x})^2 = \frac{1}{40-1} (4437.5) = 113.78$$

$$S = 10.67,$$

: ( )

Classes	х	f	xf	$x^2 f$
40-49	44.5	2	89	3960.5
50-59	55.5	9	490.5	26732.25
60-69	65.5	15	967.5	62403.75
70-79	75.5	11	819.5	61052.75
80-89	85.5	2	169	12280.5
90-99	95.5	1	94.5	8930.25
Total		40	2630	177360

$$S^{2} = \frac{1}{n-1} \left( \sum_{i=1}^{n} f_{i} x_{i}^{2} - \frac{\left(\sum_{i=1}^{n} f_{i} x_{i}\right)^{2}}{n} \right) = \frac{1}{40-1} (177360 - 172922.5) = 113.78$$

$$S = 10.67, \qquad ( )$$

$$c = 64.5$$
 ( )

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Classes	x	f	d = x - 64.5	df	$d^2 f$
40-49	44.5	2	-20	-40	800
50-59	55.5	9	-10	-90	900
60-69	65.5	15	0	0	0
70-79	75.5	11	10	110	1100
80-89	85.5	2	20	40	800
90-99	95.5	1	30	30	900
Total		40		50	4500

$$S^{2} = \frac{1}{n-1} \left( \sum_{i=1}^{n} f_{i} d_{i}^{2} - \frac{\left( \sum_{i=1}^{n} f_{i} d_{i} \right)^{2}}{n} \right) = \frac{1}{40-1} (4500 - 62.5) = 113.78$$

$$S = 10.67,$$

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Classes	X	f	d = x - 64.5	$\frac{d}{10} = d'$	d'f	$d'^2 f$
40-49	44.5	2	-20	-2	-4	8
50-59	55.5	9	-10	-1	-9	9
60-69	65.5	15	0	0	0	0
70-79	75.5	11	10	1	11	11
80-89	85.5	2	20	2	4	8
90-99	95.5	1	30	3	3	9
Total		40			5	45

$$S_{d'}^{2} = \frac{1}{n-1} \left( \sum_{i=1}^{n} f_{i} d_{i}^{\prime 2} - \frac{\left( \sum_{i=1}^{n} f_{i} d_{i}^{\prime} \right)^{2}}{n} \right) = \frac{1}{40-1} (45 - 0.625) = 1.1378$$

$$S_{d'} = 1.067, \qquad S_{x} = 10 S_{d'} = 10.67 \qquad ( )$$

•

$$\overline{x}$$
  $x_1, x_2, ..., x_n$   $X$  
$$\vdots \qquad Z \qquad s$$
 
$$Z_i = \frac{x_i - \overline{x}}{s}, \qquad i = 1, 2, ..., n$$

"  $Z_{i}$  .( ) "

:( )

.

 $\vdots \hspace{1cm} Z_1 \hspace{1cm} \vdots$ 

$$Z_1 = \frac{82 - 75}{10} = 0.7$$

$$Z_2 = \frac{89 - 81}{16} = 0.5$$

.

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$$1- r = \frac{3(\overline{x} - Med)}{s}, \tag{17}$$

$$2- r = \frac{\overline{x} - Mod}{s}, \tag{18}$$

:

$$3- r = \frac{m_3^2}{s^3}, (19)$$

$$m_3 = \frac{\sum (x - \overline{x})^3}{n},$$

$$m_3 = \frac{\sum f(x - \overline{x})^3}{n},$$

. ()

: :

$$\bar{x} = 65.75$$
,  $Med = 65.41$ ,  $Mod = 65.5$ ,  $s = 10.67$ 

: (

$$r = \frac{3(\bar{x} - Med)}{s} = \frac{3(65.75 - 65.41)}{10.67} = 0.069,$$
 (1)

: ( )

$$r = \frac{\bar{x} - Mod}{s} = \frac{65.75 - 65.5}{10.67} = 0.025,$$
 (2)

 $\vdots \hspace{1cm} k$ 

$$k = \frac{m_4}{s^4} - 3$$

$$m_4 = \frac{\sum (x - \overline{x})^4}{n} \,,$$

$$m_4 = \frac{\sum f(x - \overline{x})^4}{n},$$

:

:

58-60	61-63	64-66	67-69	70-72	73-75
2	7	14	15	8	4

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<u>.</u>

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< 10	10-14	15-19	20-24	25-29	30≤
5	20	35	19	13	8

: -

2, 5, 9, 4, 3, 6

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70, 70, 70, 70, 70, 70, 70

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( )

(x, y) $\boldsymbol{x}$ (Pearson) (x, y)(Spearman) y

 $(x_1, y_1), (x_2, y_2), ..., (x_n, y_n)$ 

X

: *r* 

$$r = \frac{\sum xy - \frac{(\sum x)(\sum y)}{n}}{\sqrt{(\sum x^2 - \frac{(\sum x)^2}{n})(\sum y^2 - \frac{(\sum y)^2}{n})}},$$
 (1)

 $: \qquad \qquad (r)$ 

<del>-</del>

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:( )

 x
 13
 9
 19
 15
 11
 8
 16
 11

 y
 15
 7
 17
 15
 10
 9
 14
 10

y x =

:

Х	У	-10x = x	-10 y = y	y x	$x^2$	y <sup>2</sup>
13	15	3	5	15	9	25
9	7	-1	-3	3	1	9
19	17	9	7	63	81	49
15	15	5	5	25	25	25
11	10	1	0	0	1	0
8	9	-2	-1	2	4	1
16	14	6	4	24	36	16
11	10	1	0	0	1	0
		22	17	132	158	125

$$r = \frac{\sum xy - \frac{(\sum x)(\sum y)}{n}}{\sqrt{(\sum x^2 - \frac{(\sum x)^2}{n})(\sum y^2 - \frac{(\sum y)^2}{n})}}$$

$$r = \frac{132 - \frac{(22 \times 17)}{8}}{\sqrt{(158 - \frac{(22)^2}{8})(125 - \frac{(17)^2}{8})}}$$

$$r = 0.93$$

-

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(x,y) (x,y)

•

:

$$r_{s} = 1 - \frac{6\sum d^{2}}{n(n^{2} - 1)},$$
 (2)  
 $d(x, y)$   $n$   $r_{s}$   
 $\vdots$   $(x, y)$ 

:( )

x	A	С	С	С	В	D
у	В	В	D	С	A	Е

:

х	у	a = x	b = y	d = a - b	$d^2$
A	В	6	4.5	1.5	2.25
C	В	3	4.5	-1.5	2.25
C	D	3	2	1	1
C	С	3	3	0	0
В	A	5	6	-1	1
D	Е	1	1	0	0
					6.5

$$r_{s} = 1 - \frac{6\sum d^{2}}{n(n^{2} - 1)}$$

$$r_{s} = 1 - \frac{6 \times 6.5}{6(36 - 1)}$$

$$r_{s} = 1 - 0.186$$

$$r_{s} = 0.814$$

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. ...

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:

C.C

A	В
С	D

: C.C

$$C.C = \frac{AD - BC}{AD + BC},$$
 (3)

( )

:

:( )

5	5
3	4

:

C.C = 
$$\frac{AD - BC}{AD + BC}$$
  
C.C =  $\frac{(5 \times 4) - (3 \times 5)}{(5 \times 4) + (3 \times 5)}$ 

C.C = 0.14

X .C s Y r

Y	$Y_1$	$Y_2$		$Y_s$	
$X_1$	$f_{11}$	$f_{12}$	•••	$f_{1s}$	$f_{1.}$
$X_2$	$f_{21}$	$f_{22}$	•••	$f_{2s}$	$f_{2.}$
:	:	:	:	:	:
$X_r$	$f_{r1}$	$f_{r2}$	•••	$f_{rs}$	$f_{r.}$
	$f_{.1}$	$f_{.2}$	•••	$f_{.s}$	$f_{\cdot \cdot}$

: C B

$$C = \sqrt{\frac{B-1}{B}}, \tag{4}$$

$$B = \frac{(f_{11})^2}{f_{.1}f_{1.}} + \frac{(f_{12})^2}{f_{.2}f_{1.}} + \ldots + \frac{(f_{rs})^2}{f_{.s}f_{r.}}$$

:( )

 X

 6
 4
 10

 7
 2
 9

 6
 5
 11

 19
 11
 30

. C

: B :

$$B = \frac{6^{2}}{19 \times 10} + \frac{7^{2}}{19 \times 9} + \frac{6^{2}}{19 \times 11} + \frac{4^{2}}{11 \times 10} + \frac{2^{2}}{11 \times 9} + \frac{5^{2}}{11 \times 11}$$

$$B = 1.05$$

: C

$$C = \sqrt{\frac{B-1}{B}}$$

$$C = \sqrt{\frac{1.05-1}{1.05}}$$

$$C = 0.22$$

(x,y) ( - )

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*x* . *y x* 

x y

:

y = a + bx, (5)

: (y ) a

 $a = \bar{y} - b\bar{x}, \qquad (6)$ 

 $\vdots \hspace{1cm} x \hspace{1cm} y \hspace{1cm} b$ 

$$b = \frac{\sum xy - \frac{(\sum x)(\sum y)}{n}}{\sum x^2 - \frac{(\sum x)^2}{n}},$$

$$(7)$$

$$(6) \quad x \quad y \quad (7)$$

:

Х	У	xy	$x^2$	y <sup>2</sup>
15	13	195	225	169
7	9	63	49	81
17	19	323	289	361
15	15	225	225	225
10	11	110	100	121
9	8	72	81	64
14	16	224	196	256
10	11	110	100	121
97	102	1322	1265	1398

$$b = \frac{\sum xy - \frac{(\sum x)(\sum y)}{n}}{\sum x^2 - \frac{(\sum x)^2}{n}}$$

$$b = \frac{1322 - \frac{97 \times 102}{8}}{1265 - \frac{(97)^2}{8}} = 0.96$$

$$a = \overline{y} - b\overline{x}$$

$$a = \frac{102}{8} - 0.96(\frac{97}{8})$$

$$a = 1.11$$

x = 1.11 + 0.06x

y = 1.11 + 0.96x

( ; /

		•			_
		•			

x	3	2	1	1	5	6	1	4
у	31	44	60	70	18	17	71	29
(		)	(	)				

.

. *x y* 

. y x

х	56	66	42	44	38	27	39	40
y	31	38	27	22	19	25	20	28

 $\cdot x$  y

A	В	D	Е	С	D	Е	В
A	C	E	D	С	D	E	В

.

```
X
             X
        X
              X
    p
```

n

X

n

$$P(X = x) = \binom{n}{x} p^{x} q^{n-x},$$
  $x = 0,1,2,...,n$ 

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$$n = 15,$$
  $p = 0.8,$   $q = 0.2$   
 $P(X = x) = {15 \choose x} (0.8)^x (0.2)^{15-x},$   $x = 0,1,2,...,15$ 

$$P(X=15) = \begin{pmatrix} 15\\15 \end{pmatrix} (0.8)^{15} (0.2)^{15-15}$$

 $P(X = 15) = 1 \times 0.035 \times 1$ P(X = 15) = 0.035

$$P(X=8) = {15 \choose 8} (0.8)^8 (0.2)^{15-8}$$

 $P(X = 8) = 6435 \times 0.1677722 \times 0.0000128$ 

P(X = 8) = 0.013819

$$P(X = 6) = {15 \choose 6} (0.8)^6 (0.2)^{15-6}$$

 $P(X = 6) = 5005 \times 0.262144 \times 0.000000512$ 

P(X = 6) = 0.000672

 $P(X=0) = {15 \choose 0} (0.8)^0 (0.2)^{15-0}$  $P(X = 0) = 1 \times 1 \times 0$ P(X = 0) = 0

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n = 20, p = 0.6, q = 0.4  $P(X = x) = {20 \choose x} (0.6)^x (0.4)^{20-x},$  x = 0,1,2,...,20

 $P(X = 7) = {20 \choose 7} (0.6)^7 (0.4)^{20-7}$ 

 $P(X = 7) = 77520 \times 0.0279936 \times 0.00000671$ 

P(X = 7) = 0.014563

 $P(X=0) = {20 \choose 0} (0.6)^0 (0.4)^{20-0}$  $P(X = 0) = 1 \times 1 \times 0.000$ 

P(X = 0) = 0

 $P(X = 20) = {20 \choose 20} (0.6)^{20} (0.4)^{20-20}$ 

 $P(X = 20) = 1 \times 0.00004 \times 1$ P(X = 20) = 0.00004

 $P(X=10) = \begin{pmatrix} 20\\10 \end{pmatrix} (0.6)^{10} (0.4)^{20-10}$ 

 $P(X = 10) = 184756 \times 0.006046618 \times 0.0001$ 

P(X = 10) = 0.111715

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n = 3, p = 0.8, q = 0.2 $P(X = x) = {3 \choose x} (0.8)^x (0.2)^{3-x},$  x = 0,1,2,3

 $P(X-3) = \binom{3}{3} (0.8)^3 (0.2)^{3-3}$ 

 $P(X=3) = \begin{pmatrix} 3\\3 \end{pmatrix} (0.8)^3 (0.2)^{3-3}$   $P(X=3) = 4 \times 0.542 \times 1$ 

 $P(X = 3) = 1 \times 0.512 \times 1$ P(X = 3) = 0.512

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1-  $P(X = 2) = 1 - {3 \choose 2} (0.8)^2 (0.2)^{3-2}$ = 1- (3 × 0.64 × 0.2) = 1- 0.384

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 $P(X=0) = \begin{pmatrix} 3 \\ 0 \end{pmatrix} (0.8)^0 (0.2)^{3-0}$ 

 $P(X=0) = 1 \times 1 \times 0.008$ 

1- P(X = 2) = 0.616

P(X = 0) = 0.008

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 $P(X \ge 1) = P(X = 1) + P(X = 2) + P(X = 3)$ 

 $P(X \ge 1) = \begin{pmatrix} 3 \\ 1 \end{pmatrix} (0.8)^{1} (0.2)^{3-1} + \begin{pmatrix} 3 \\ 2 \end{pmatrix} (0.8)^{2} (0.2)^{3-2} + \begin{pmatrix} 3 \\ 3 \end{pmatrix} (0.8)^{3} (0.2)^{3-3}$ 

 $P(X \ge 1) = 0.096 + 0.384 + 0.512$ 

 $P(X \ge 1) = 0.992$ 

 $P(X \le 1) = P(X = 1) + P(X = 0)$  $P(X \le 1) = 0.096 + 0.008$  $P(X \le 1) = 0.104$  $\mathbf{X}$ x = 0,1,2,... (... λ  $\mathbf{X}$  $P(X = x) = \frac{e^{-\lambda} \lambda^x}{x!}, \qquad x = 0,1,2,....$ :( )

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$$\lambda = 5,$$

$$P(X = x) = \frac{e^{-5}5^{x}}{x!},$$

$$1 - P(X = 10) = \frac{e^{-5}5^{10}}{10!}$$

$$P(X = 10) = 0.018132789$$

$$2 - P(X < 3) = P(X = 0) + P(X = 1) + P(X = 2)$$

$$P(X < 3) = \frac{e^{-5}5^{0}}{0!} + \frac{e^{-5}5^{1}}{1!} + \frac{e^{-5}5^{2}}{2!}$$

$$P(X < 3) = \frac{3}{0!} + \frac{3}{1!} + \frac{3}{2!}$$

$$P(X < 3) = 0.006737947 + 0.033689735 + 0.084224337$$

$$P(X < 3) = 0.124652$$

3- 
$$P(X > 1) = 1$$
-  $P(X \le 1)$   
 $P(X > 1) = 1$ -  $(P(X = 0) + P(X = 1))$   
 $P(X > 1) = 1$ -  $(0.006737947 + 0.033689735)$   
 $P(X > 1) = 1$ -  $0.040428$   
 $P(X > 1) = 0.959572318$   
4-  $P(4 \le X \le 8) = P(X = 4) + P(X = 5) + P(X = 6) + P(X = 7) + P(X = 8)$   
 $P(4 \le X \le 8) = \frac{e^{-5}5^4}{4!} + \frac{e^{-5}5^5}{5!} + \frac{e^{-5}5^6}{6!} + \frac{e^{-5}5^7}{7!} + \frac{e^{-5}5^8}{8!}$   
 $P(4 \le X \le 8) = 0.17546737 + 0.17546737 + 0.146222808 + 0.104444863 + 0.065278039$ 

$$P(4 \le X \le 8) = 0.66688045$$

$$\lambda = 5 \times \frac{1}{2} = 2.5$$

$$P(X = x) = \frac{e^{-2.5} \cdot 2.5^{x}}{x!}, \qquad x = 0,1,2,....$$

$$1 - P(X = 10) = \frac{e^{-2.5} \cdot 2.5^{10}}{10!}$$

$$P(X = 10) = 0.000215725$$

$$2 - P(X < 3) = P(X = 0) + P(X = 1) + P(X = 2)$$

$$P(X < 3) = \frac{e^{-2.5} \cdot 2.5^{0}}{0!} + \frac{e^{-2.5} \cdot 2.5^{1}}{1!} + \frac{e^{-2.5} \cdot 2.5^{2}}{2!}$$

$$P(X < 3) = 0.082084999 + 0.205212497 + 0.256515621$$

P(X < 3) = 0.543813

$$3- P(X > 1) = 1- P(X \le 1)$$

$$P(X > 1) = 1 - (P(X = 0) + P(X = 1))$$

$$P(X > 1) = 1 - (0.082084999 + 0.205212497)$$

$$P(X > 1) = 1 - 0.287297$$

$$P(X > 1) = 0.712703$$

$$4 - P(4 \le X \le 8) = P(X = 4) + P(X = 5) + P(X = 6) + P(X = 7) + P(X = 8)$$

$$P(4 \le X \le 8) = \frac{e^{-2.5} \cdot 2.5^4}{4!} + \frac{e^{-2.5} \cdot 2.5^5}{5!} + \frac{e^{-2.5} \cdot 2.5^6}{6!} + \frac{e^{-2.5} \cdot 2.5^7}{7!} + \frac{e^{-2.5} \cdot 2.5^8}{8!}$$

$$P(4 \le X \le 8) = 0.133601886 + 0.066800943 + 0.027833726 + 0.009940617 + 0.003106443$$

 $P(4 \le X \le 8) = 0.241284$ 

 $\lambda = 5 \times 2 = 10$   $e^{-10}10^{x}$ 

$$P(X = x) = \frac{e^{-10}10^{x}}{x!},$$

$$1- P(X = 10) = \frac{e^{-10}10^{10}}{10!}$$

$$P(X = 10) = 0.125110036$$

2- 
$$P(X < 3) = P(X = 0) + P(X = 1) + P(X = 2)$$

$$P(X < 3) = \frac{e^{-10}10^{0}}{0!} + \frac{e^{-10}10^{1}}{1!} + \frac{e^{-10}10^{2}}{2!}$$

$$P(X < 3) = 0.0000454 + 0.000454 + 0.00227$$

$$P(X < 3) = 0.002769$$

3- 
$$P(X > 1) = 1$$
-  $P(X \le 1)$ 

$$P(X > 1) = 1 - (P(X = 0) + P(X = 1))$$

$$P(X > 1) = 1 - (0.0000454 + 0.000454)$$

$$P(X > 1) = 1 - 0.000499$$

$$P(X > 1) = 0.999501$$

$$4- P(4 \le X \le 8) = P(X = 4) + P(X = 5) + P(X = 6) + P(X = 7) + P(X = 8)$$

$$P(4 \le X \le 8) = \frac{e^{-10}10^4}{4!} + \frac{e^{-10}10^5}{5!} + \frac{e^{-10}10^6}{6!} + \frac{e^{-10}10^7}{7!} + \frac{e^{-10}10^8}{8!}$$

$$P(4 \le X \le 8) = 0.01891664 + 0.03783327 + 0.06305546 + 0.09007923 +$$

$$+0.11259903$$

$$P(4 \le X \le 8) = 0.322484$$

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 $\lambda = 2$ 

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$$P(X = x) = \frac{e^{-2} 2^{x}}{x!},$$

$$x = 0,1,2,....$$

$$P(X = 3) = \frac{e^{-2} 2^{3}}{3!}$$

$$P(X = 3) = 0.18044704$$

. ...

X :

$$P(X = x) = \frac{\binom{a}{x} \binom{b}{n-x}}{\binom{N}{n}}, \qquad x = 0,1,2,...,n$$

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. n - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N - a + b = N

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X a

b

$$P(X = x) = \frac{\binom{8}{x} \binom{40}{5 - x}}{\binom{48}{5}}, \qquad x = 0,1,2,3,4,5$$

$$P(X = 0) = \frac{\binom{8}{0} \binom{40}{5 - 0}}{\binom{48}{5}}$$

$$P(X = 0) = \frac{1 \times 658008}{1712304}$$

$$P(X = 0) = \frac{1 \times 658008}{1712304}$$

$$P(X = 0) = 0.38$$

$$P(X = 1) = \frac{\binom{8}{1}\binom{40}{5-1}}{\binom{48}{5}}$$

$$P(X = 1) = \frac{8 \times 91390}{1712304}$$

$$P(X = 1) = \frac{8 \times 91390}{1712304}$$

$$P(X = 1) = 0.43$$

$$P(X \ge 2) = 1 - (P(X = 0) + P(X = 1))$$
  
 $P(X \ge 2) = 1 - (0.38 + 0.43)$   
 $P(X \ge 2) = 0.19$ 

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X a

b

:

$$P(X = x) = \frac{\binom{4}{x} \binom{76}{3 - x}}{\binom{80}{3}}, \qquad x = 0,1,2,3$$

:

$$P(X = 1) = \frac{\binom{4}{1}\binom{76}{3-1}}{\binom{80}{3}}$$

$$P(X=1) = \frac{4 \times 2860}{82160}$$

$$P(X = 1) = 0.14$$

μ

X .

$$f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}(\frac{x-\mu}{\sigma})^2}$$

$$(X \approx N(\mu, \sigma^2))$$

$$-\infty < X < \infty$$
,  $-\infty < \mu < \infty$ ,  $\sigma > 0$ 

 $Z \approx N(0,1)$  Z

:

$$f(z) = \frac{1}{\sqrt{2\pi}} e^{-\frac{z^2}{2}}, \qquad -\infty < z < \infty$$

( )  $Z = \frac{x - \mu}{\sigma}$ 

 $X \approx N(16,16)$ 

 $Z = \frac{x - 16}{4}$  $\mathbf{Z}$ 

:()

2-  $P(z \le 1.07)$ 1-  $P(z \le 1.72)$ ,  $3 - P(z \ge 0.29)$  $4 - P(-1.91 \le z \le 0.45)$ 

1-  $P(z \le 1.72) = 0.9573$ 

 $2 - P(z \le 1.07) = 0.8577$ 

 $3-P(z \ge 0.29) = 1-P(z < 0.29)$  $P(z \ge 0.29) = 1 - 0.6141$ 

 $P(z \ge 0.29) = 0.3859$ 

4-  $P(-1.91 \le z \le 0.45) = P(z \le 0.45)$  -  $P(z \le -1.91)$ 

 $P(-1.91 \le z \le 0.45) = 0.6736 - 0.0281$  $P(-1.91 \le z \le 0.45) = 0.6455$ 

:()  $X \approx N(16,16)$ 

1-  $P(X \le 14)$ 

2-  $P(X \ge 22)$ X

1-  $x = 14 \implies Z = \frac{x - \mu}{\sigma}$  $\Rightarrow z = \frac{14 - 16}{4} = -0.5$ 

 $\Rightarrow P(X \le 14) = P(Z \le -0.5) = 0.3085$ 

2-  $x = 22 \implies Z = \frac{x - \mu}{\sigma}$ 

$$\Rightarrow z = \frac{22 - 16}{4} = 1.5$$

$$\Rightarrow P(X \ge 22) = P(Z \ge 1.5) = 1 - P(Z < 1.5)$$

$$\Rightarrow P(Z \ge 1.5) = 1 - 0.9332 = 0.0668$$

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 $X \approx N(105,100)$ 

$$P(100 \le X \le 114) = P(\frac{100 - 105}{10} \le \frac{X - \mu}{\sigma} \le \frac{114 - 105}{10})$$

$$P(100 \le X \le 114) = P(-0.5 \le Z \le 0.9)$$

$$P(100 \le X \le 114) = P(z \le 0.9) - P(z \le -0.5)$$

$$P(100 \le X \le 114) = 0.8159 - 0.3085$$

$$P(100 \le X \le 114) = 0.5074$$

t(0.95, 5)

$$f(t) = c(1 + \frac{t^2}{v})^{-v + \frac{1}{2}},$$
  $-\infty < t < \infty$ 

:( )

t(0.90, 7)

t(0.975, 20) = 2.086

```
t(0.995, 12) = 3.055
t(0.95, 5) = 2.015
t(0.90, 7) = 1.415
                                                                                  :( )
                                     t(0.995, v) = 2.921
t(0.975, \nu) = 2.228
t(0.95, v) = 1.721
                                     t(0.90, v) = 1.337
t(0.975, v) = 2.228 \implies v = 10
t(0.995, v) = 2.921 \implies v = 16
t(0.95, v) = 1.721 \implies v = 21
t(0.90, v) = 1.337 \implies v = 16
                     .F
                                                              F > 0
                         F(v_1, v_2)
                                                           F
               \nu_2
                     \nu_{\scriptscriptstyle 1}
                                                                                  c
                                            \alpha) F(\alpha, \nu_1, \nu_2)
         F
                                                                            : :( )
F (0.01, 11, 15)
                   F (0.05, 10, 7)
F(0.01, 11, 15) = 0.235
F(0.05, 10, 7) = 0.318
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%

Z - P(Z < 1.8)- P(Z > -0.5)- P(-0.2 < Z < 0.5)X

% X .X

. /

 $\vdots \qquad \qquad t \qquad \qquad -$ 

t(0.95, 20)

t(0.90, 28)

*t* (0.99,12)

t(0.975, 7)

*t* (0.995, 13)

: b - (b, 5) = 2.015 t

t (b, 20) = 1.325

t (b, 23) = 2.069

t (b, 12) = 2.681

t (b, 15) = 2.131

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F (0.01, 7, 12)

F (0.05, 12, 5)

F (0.01, 5, 8)

F (0.05, 5, 5)

: b -

F(b, 8, 9) = 3.23

F(b, 9, 11) = 4.63

F(b, 3, 24) = 3.72

F(b, 2, 24) = 3.4

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.Statistical Hypothesis Parametric Statistical Test of Hypothesis Null Hypothesis  $.\,H_{\scriptscriptstyle o}$ Alternative Hypothesis  $.\,H_1$ 

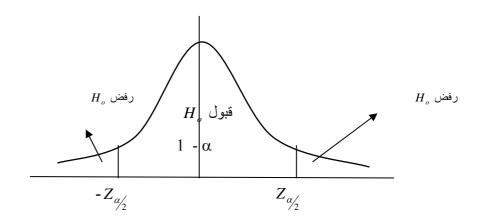
.Significant " :  $H_o$ ) α , ) α .(... ,  $H_{o}$ .β  $H_o$  $H_o$  $H_o$  $\alpha$ β  $H_{o}$ ( )  $H_o$ :( (1-α)

 $\alpha$ 

: ( )  $\mu$ 

: -

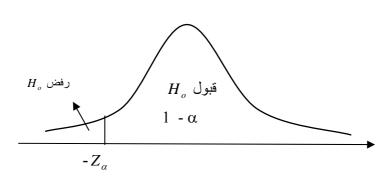
 $H_o$ :  $\mu = \mu_o$  $H_1$ :  $\mu \neq \mu_o$ 



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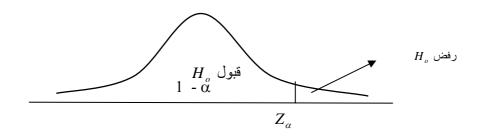
 $H_o$ :  $\mu = \mu_o$  $H_1$ :  $\mu < \mu_o$ 



-

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 $H_o$ :  $\mu = \mu_o$  $H_1$ :  $\mu > \mu_o$ 



μ

 $Z = \frac{\overline{x} - \mu_o}{\sigma / \sqrt{n}}$  $\sigma$ 

 $Z \sim N(0,1)$ Z  $\overline{x}$ 

> $\mu_o$ ) α

 $Z_{\alpha}$   $-Z_{\alpha/2}$   $Z_{\alpha/2}$ 

:( )

 $H_o$ :  $\mu = 160$  $H_1: \mu \neq 160$ 

 $Z = \frac{\overline{x} - \mu_o}{\sigma / \sqrt{n}}$ 

 $\sigma$  = 5, n = 64 $\bar{x} = 155, \qquad \mu_o = 160,$ 

 $\alpha = 0.05$  $\Rightarrow Z = \frac{155 - 160}{\frac{5}{\sqrt{64}}},$ 

Z = -8(1) Z : *I* 

 $Z \qquad (\alpha = 0.05) \qquad -$ 

 $Z_{\frac{\alpha}{2}} = Z_{0.05/2} = Z_{0.025}$ 

 $Z_{0.025} = 1.96$ 

 $: \qquad -Z_{\frac{\alpha}{2}} = -1.96$ 

Z Z Z

.  $\mu = 160$   $Z \qquad (\alpha = 0.01)$ 

 $Z \qquad (\alpha = 0.01) \qquad -$ 

 $Z_{\alpha/2} = Z_{0.01/2} = Z_{0.005}$  $Z_{0.005} = 2.58$ 

 $\vdots \qquad -Z_{\frac{\alpha}{2}}$ 

 $-Z_{\alpha/2} = -2.58$  Z Z Z

 $\mu = 160$ 

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 $H_o: \mu = 240$  $H_1: \mu < 240$ 

 $Z = \frac{\overline{x} - \mu_o}{\sigma / \sqrt{n}}$ 

: *I* 

 $\bar{x} = 235, \qquad \mu_o = 240, \qquad \sigma = 18, \qquad n = 9$ 

 $\alpha = 0.01$   $\Rightarrow Z = \frac{235 - 240}{\frac{18}{\sqrt{9}}},$ 

 $Z = -0.83 \tag{1}$ 

 $ar{Z}$  -

 $Z (\alpha = 0.1)$ 

:

 $-Z_{\alpha} = -Z_{0.1}$   $-Z_{0.1} = -1.28$ (2) Z Z Z Z Z(1) (1) U = 240

n

. · ·

v = n - k

 $\cdot$  . k

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: z ( > )

 $t = \frac{\overline{x} - \mu_o}{S / \sqrt{n}}$ 

t t S

 $\frac{\alpha}{2}$   $\alpha$  (v=n-1)

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: - :

 $H_o: \mu = 15$  $H_1: \mu > 15$ 

 $t = \frac{\overline{x} - \mu_o}{S / \sqrt{n}}$ 

 $\overline{x}=17, \qquad \mu_o=15, \qquad S=2, \qquad n=7$   $\alpha=0.05$   $A=\frac{17-15}{1}$ 

 $\Rightarrow t = \frac{17 - 15}{\frac{2}{\sqrt{7}}},$   $t = 2.65 \tag{1}$ 

. t -

 $t \qquad (\alpha = 0.05)$ 

 $t_{(n-1,\alpha)} = t_{(7-1,0.05)}$   $t_{(6,0.05)} = 1.943$  (2) t t t ( ) ( )

. ...

$$H_o: \mu_1 - \mu_2 = 0, \qquad \Leftrightarrow \qquad H_o: \mu_1 = \mu_2$$
  
 $H_1: \mu_1 \neq \mu_2,$ 

or  $H_1: \mu_1 < \mu_2$ ,

or  $H_1: \mu_1 > \mu_2$ Z

$$Z = \frac{(\overline{x}_1 - \overline{x}_2) - (\mu_1 - \mu_2)_o}{\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}}$$

$$(\sigma_2^2 \ \sigma_1^2)$$

$$(< n_2) \ (< n_1)$$

:( )

$$.(\alpha = 0.05)$$

 $H_o: \mu_1 = \mu_2$  $H_1: \mu_1 < \mu_2$ 

Z

$$Z = \frac{(\overline{x}_1 - \overline{x}_2) - (\mu_1 - \mu_2)_o}{\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}}$$

$$Z = \frac{(69 - 74) - 0}{\sqrt{\frac{230}{60} + \frac{215}{85}}}$$

$$Z = \frac{-5}{\sqrt{6.36}}$$

$$Z = -1.98,$$
(1)

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$$-Z_{\alpha} = -Z_{0.05} - Z_{0.05} = -1.65$$

$$Z Z Z Z () ()$$

$$\overline{x}_2$$
  $\overline{x}_1$  :  $n_2$   $n_1$ 

 $t = \frac{(\overline{x}_1 - \overline{x}_2) - (\mu_1 - \mu_2)_o}{\sqrt{S_p^2 (\frac{1}{n_1} + \frac{1}{n_2})}}$ 

$$S_p^2 = \frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2}$$

 $(v = n_1 + n_2 - 2) t$ 

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 $H_o: \mu_1 = \mu_2$  $H_1: \mu_1 \neq \mu_2$  $: S_p^2$ 1-  $S_p^2 = \frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2}$  $S_p^2 = \frac{(11-1)(7)^2 + (6-1)(5)^2}{11+6-2}$  $S_p^2 = \frac{10 \times 49 + 5 \times 25}{15}$  $S_p^2 = 41 \tag{1}$ 2-  $t = \frac{(\overline{x}_1 - \overline{x}_2) - (\mu_1 - \mu_2)_o}{\sqrt{S_p^2(\frac{1}{n_1} + \frac{1}{n_2})}}$  $t = \frac{(80 - 75) - 0}{\sqrt{41(\frac{1}{11} + \frac{1}{6})}}$  $t = \frac{5}{\sqrt{10.56}}$ t = 1.54(2)  $(\alpha = 0.05)$  $t_{(n_1+n_2-2,\alpha/2)} = t_{(11+6-2,0.025)}$  $t_{(15,0.025)} = \pm 2.131$ (3) ()()

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 $t \qquad \qquad t = \frac{\overline{d} - \overline{D}_o}{s_d / \sqrt{n}}$ (v = n - 1) $\boldsymbol{S}_d$ 

n  $\overline{D}_{\!\scriptscriptstyle o}$ 

 $\bar{d}$ 

 $H_o: \overline{D}_o = 0, \qquad \Leftrightarrow \qquad H_o: \overline{D}_o = \mu_1 - \mu_2$ 

 $H_1: \overline{D}_o \neq 0$ ,

or  $H_1: \overline{D}_o < 0$ , or  $H_1: \overline{D}_o > 0$ 

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 $H_o: \overline{D}_o = 0$  $H_1: \overline{D}_o \neq 0$ 

. t -

$$t = \frac{\overline{d} - \overline{D}_o}{s_d / \sqrt{n}}$$
1-  $\overline{D}_o = 0$ 
2-  $n = 7$ 

:

$(d^2)$	( d)	
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	-	
	-	
	-	

$$\overline{d} = \frac{\sum_{i=1}^{n} d_i}{n}$$

$$\overline{d} = \frac{-4343}{7}$$

$$\overline{d} = -620.43$$
(1)
$$s_d = \frac{1}{n-1} \sqrt{\sum_{i=1}^{n} d_i^2 - \frac{(\sum_{i=1}^{n} d_i)^2}{n}}$$

$$s_d = \frac{1}{7-1} \sqrt{3595551 - \frac{(-4343)^2}{7}}$$

$$s_d = \frac{1}{6} \sqrt{901029.71}$$

$$s_d = \frac{1}{6} (949.23)$$

$$s_d = 158.2$$
(2)
$$t = \frac{-620.43}{158.2 / \sqrt{7}}$$

$$t = -10.38$$
(3)

. t -

 $(\alpha = 0.05)$ t  $t_{(n-1,\frac{\alpha}{2})} = t_{(6,0.025)}$  $t_{(6,0.025)} = \pm 2.448$ (4) t () () ) .%  $\pi$ p  $\pi$  $H_o$ :  $\pi = \pi_o$ ,  $H_1: \pi \neq \pi_o$ , or  $H_1: \pi \leq \pi_o$ ,  $H_1: \pi > \pi_o$ n  $\boldsymbol{Z}$  $Z = \frac{p - \pi_o}{\sqrt{\frac{\pi_o (1 - \pi_o)}{n}}}$ Z Z

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 $H_o: \pi = 0.06$  $H_1: \pi > 0.06$ 

: Z -

 $Z = \frac{p - \pi_o}{\sqrt{\frac{\pi_o (1 - \pi_o)}{n}}}$ 

:

 $p = \frac{20}{180}$  p = 0.11

 $Z = \frac{0.11 - 0.06}{\sqrt{\frac{0.06(1 - 0.06)}{180}}}$   $Z = \frac{0.05}{\sqrt{\frac{0.06 \times 0.94}{180}}}$ 

 $\sqrt{\frac{0.00 \times 0.51}{180}}$   $Z = \frac{0.05}{0.02}$ 

Z = 2.5 (1) :% Z

 $Z_{\alpha} = Z_{0.01}$   $Z_{0.01} = 2.33 \tag{2}$ 

% z z () ()

 $(\pi_1 - \pi_2)$ 

 $\vdots \qquad \qquad Z \qquad \qquad p_1 - p_2$ 

$$Z = \frac{(p_1 - p_2) - (\pi_1 - \pi_2)_0}{\sqrt{\overline{p}(1 - \overline{p})(\frac{1}{n_1} + \frac{1}{n_2})}}$$
(1)

 $\overline{P} = \frac{n_1 p_1 + n_2 p_2}{n_1 + n_2}$ 

:  $H_o: (\pi_1 - \pi_2) = 0$ ( )

 $H_1: (\pi_1 - \pi_2) \neq 0,$ or,  $H_1: (\pi_1 - \pi_2) > 0$ or,  $H_1$ :  $(\pi_1 - \pi_2) < 0$ 

 $H_o: (\pi_1 - \pi_2) = \pi$ ,  $\pi \neq 0$ 

 $Z = \frac{(p_1 - p_2) - (\pi_1 - \pi_2)_0}{\sqrt{\frac{p_1(1 - p_1)}{n_1} + \frac{p_2(1 - p_2)}{n_2}}},$ (2)

 $H_1: (\pi_1-\pi_2)\neq \pi$ , or,  $H_1: (\pi_1 - \pi_2) > \pi$ or,  $H_1: (\pi_1 - \pi_2) \le \pi$ 

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$$H_o: (\pi_1 - \pi_2) = 0,$$
  
 $H_1: (\pi_1 - \pi_2) > 0$ 

: Z -

$$Z = \frac{(p_1 - p_2) - (\pi_1 - \pi_2)_0}{\sqrt{\overline{p}(1 - \overline{p})(\frac{1}{n_1} + \frac{1}{n_2})}}$$

$$p_1 = \frac{80}{100} = 0.8$$

$$p_2 = \frac{62}{100} = 0.62$$

$$\overline{P} = \frac{n_1 p_1 + n_2 p_2}{n_1 + n_2}$$

$$\overline{P} = \frac{100 \times 0.8 + 100 \times 0.62}{100 + 100}$$

$$\overline{P} = \frac{142}{200}$$

$$\overline{P} = 0.71$$

$$Z = \frac{0.8 - 0.62 - 0}{\sqrt{0.71 \times 0.29(\frac{1}{100} + \frac{1}{100})}}$$

$$Z = \frac{0.18}{\sqrt{0.21 \times 0.02}}$$

$$Z = 2.78 \tag{1}$$

. Z

$$Z_{\alpha} = Z_{0.05}$$

$$Z_{0.05} = 1.65 \tag{2}$$

% z z () ()

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 $H_o: (\pi_1 - \pi_2) = 0.04,$ 

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 $H_1: (\pi_1 - \pi_2) < 0.04$ 

$$Z = \frac{(p_1 - p_2) - (\pi_1 - \pi_2)_0}{\sqrt{\frac{p_1(1 - p_1)}{n_1} + \frac{p_2(1 - p_2)}{n_2}}}$$

$$p_1 = \frac{12}{100} = 0.12$$

$$p_2 = \frac{15}{150} = 0.1$$

$$Z = \frac{(0.12 - 0.1) - 0.04}{\sqrt{\frac{0.12 \times 0.88}{100} + \frac{0.1 \times .09}{150}}}$$

$$Z = \frac{-0.02}{\sqrt{0.0011 + 0.0006}}$$

$$Z = -0.49 \qquad (1)$$

. Z

$$Z_{\alpha} = -Z_{0.05}$$
 $Z_{0.05} = -1.65$  (2)
%  $Z$   $Z$  ( ) ( )

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## :**Z**

	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.0000	0.0040	0.0080	0.0120	0.0160	0.0199	0.0239	0.0279	0.0319	0.0359
0.1	0.0398	0.0438	0.0478	0.0517	0.0557	0.0596	0.0636	0.0675	0.0714	0.0753
0.2	0.0793	0.0832	0.0871	0.0910	0.0948	0.0987	0.1026	0.1064	0.1103	0.1141
0.3	0.1179	0.1217	0.1255	0.1293	0.1331	0.1368	0.1406	0.1443	0.1480	0.1517
0.4	0.1554	0.1591	0.1628	0.1664	0.1700	0.1736	0.1772	0.1808	0.1844	0.1879
0.5	0.1915	0.1950	0.1985	0.2019	0.2054	0.2088	0.2123	0.2157	0.2190	0.2224
0.6	0.2257	0.2291	0.2324	0.2357	0.2389	0.2422	0.2454	0.2486	0.2517	0.2549
0.7	0.2580	0.2611	0.2642	0.2673	0.2704	0.2734	0.2764	0.2794	0.2823	0.2852
0.8	0.2881	0.2910	0.2939	0.2967	0.2995	0.3023	0.3051	0.3078	0.3106	0.3133
0.9	0.3159	0.3186	0.3212	0.3238	0.3264	0.3289	0.3315	0.3340	0.3365	0.3389
1.0	0.3413	0.3438	0.3461	0.3485	0.3508	0.3531	0.3554	0.3577	0.3599	0.3621
1.1	0.3643	0.3665	0.3686	0.3708	0.3729	0.3749	0.3770	0.3790	0.3810	0.3830
1.2	0.3849	0.3869	0.3888	0.3907	0.3925	0.3944	0.3962	0.3980	0.3997	0.4015
1.3	0.4032	0.4049	0.4066	0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4177
1.4	0.4192	0.4207	0.4222	0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4319
1.5	0.4332	0.4345	0.4357	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4441
1.6	0.4452	0.4463	0.4474	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4545
1.7	0.4554	0.4564	0.4573	0.4582	0.4591	0.4599	0.4608	0.4616	0.4625	0.4633
1.8	0.4641	0.4649	0.4656	0.4664	0.4671	0.4678	0.4686	0.4693	0.4699	0.4706
1.9	0.4713	0.4719	0.4726	0.4732	0.4738	0.4744	0.4750	0.4756	0.4761	0.4767
2.0	0.4772	0.4778	0.4783	0.4788	0.4793	0.4798	0.4803	0.4808	0.4812	0.4817
2.1	0.4821	0.4826	0.4830	0.4834	0.4838	0.4842	0.4846	0.4850	0.4854	0.4857
2.2	0.4861	0.4864	0.4868	0.4871	0.4875	0.4878	0.4881	0.4884	0.4887	0.4890
2.3	0.4893	0.4896	0.4898	0.4901	0.4904	0.4906	0.4909	0.4911	0.4913	0.4916
2.4	0.4918	0.4920	0.4922	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4936
2.5	0.4938	0.4940	0.4941	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4952
2.6	0.4953	0.4955	0.4956	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4964
2.7	0.4965	0.4966	0.4967	0.4968	0.4969	0.4970	0.4971	0.4972	0.4973	0.4974
2.8	0.4974	0.4975	0.4976	0.4977	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981
2.9	0.4981	0.4982	0.4982	0.4983	0.4984	0.4984	0.4985	0.4985	0.4986	0.4986
3.0	0.4987	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990

df\p	0.40	0.25	0.10	0.05	0.025	0.01	0.005	0.0005
1	0.324920	1.000000	3.077684	6.313752	12.70620	31.82052	63.65674	636.6192
2	0.288675	0.816497	1.885618	2.919986	4.30265	6.96456	9.92484	31.5991
3	0.276671	0.764892	1.637744	2.353363	3.18245	4.54070	5.84091	12.9240
4	0.270722	0.740697	1.533206	2.131847	2.77645	3.74695	4.60409	8.6103
5	0.267181	0.726687	1.475884	2.015048	2.57058	3.36493	4.03214	6.8688
6	0.264835	0.717558	1.439756	1.943180	2.44691	3.14267	3.70743	5.9588
7	0.263167	0.711142	1.414924	1.894579	2.36462	2.99795	3.49948	5.4079
8	0.261921	0.706387	1.396815	1.859548	2.30600	2.89646	3.35539	5.0413
9	0.260955	0.702722	1.383029	1.833113	2.26216	2.82144	3.24984	4.7809
10	0.260185	0.699812	1.372184	1.812461	2.22814	2.76377	3.16927	4.5869
11	0.259556	0.697445	1.363430	1.795885	2.20099	2.71808	3.10581	4.4370
12	0.259033	0.695483	1.356217	1.782288	2.17881	2.68100	3.05454	4.3178
13	0.258591	0.693829	1.350171	1.770933	2.16037	2.65031	3.01228	4.2208
14	0.258213	0.692417	1.345030	1.761310	2.14479	2.62449	2.97684	4.1405
15	0.257885	0.691197	1.340606	1.753050	2.13145	2.60248	2.94671	4.0728
16	0.257599	0.690132	1.336757	1.745884	2.11991	2.58349	2.92078	4.0150
17	0.257347	0.689195	1.333379	1.739607	2.10982	2.56693	2.89823	3.9651
18	0.257123	0.688364	1.330391	1.734064	2.10092	2.55238	2.87844	3.9216
19	0.256923	0.687621	1.327728	1.729133	2.09302	2.53948	2.86093	3.8834
20	0.256743	0.686954	1.325341	1.724718	2.08596	2.52798	2.84534	3.8495
21	0.256580	0.686352	1.323188	1.720743	2.07961	2.51765	2.83136	3.8193
22	0.256432	0.685805	1.321237	1.717144	2.07387	2.50832	2.81876	3.7921
23	0.256297	0.685306	1.319460	1.713872	2.06866	2.49987	2.80734	3.7676
24	0.256173	0.684850	1.317836	1.710882	2.06390	2.49216	2.79694	3.7454
25	0.256060	0.684430	1.316345	1.708141	2.05954	2.48511	2.78744	3.7251
	T	T		T		T	T	
26	0.255955	0.684043	1.314972	1.705618	2.05553	2.47863	2.77871	3.7066
27	0.255858	0.683685	1.313703	1.703288	2.05183	2.47266	2.77068	3.6896
28	0.255768	0.683353	1.312527	1.701131	2.04841	2.46714	2.76326	3.6739
29	0.255684	0.683044	1.311434	1.699127	2.04523	2.46202	2.75639	3.6594
30	0.255605	0.682756	1.310415	1.697261	2.04227	2.45726	2.75000	3.6460
	Т	T		Т		Т	Т	Г
inf	0.253347	0.674490	1.281552	1.644854	1.95996	2.32635	2.57583	3.2905

# **Chi-Square Table**

df/ area	.995	.990	.975	.950	.900	.750	.500
1	0.00004	0.00016	0.00098	0.00393	0.01579	0.10153	0.45494
2	0.01003	0.02010	0.05064	0.10259	0.21072	0.57536	1.38629
3	0.07172	0.11483	0.21580	0.35185	0.58437	1.21253	2.36597
4	0.20699	0.29711	0.48442	0.71072	1.06362	1.92256	3.35669
5	0.41174	0.55430	0.83121	1.14548	1.61031	2.67460	4.35146
6	0.67573	0.87209	1.23734	1.63538	2.20413	3.45460	5.34812
7	0.98926	1.23904	1.68987	2.16735	2.83311	4.25485	6.34581
8	1.34441	1.64650	2.17973	2.73264	3.48954	5.07064	7.34412
9	1.73493	2.08790	2.70039	3.32511	4.16816	5.89883	8.34283
10	2.15586	2.55821	3.24697	3.94030	4.86518	6.73720	9.34182
11	2.60322	3.05348	3.81575	4.57481	5.57778	7.58414	10.34100
12	3.07382	3.57057	4.40379	5.22603	6.30380	8.43842	11.34032
13	3.56503	4.10692	5.00875	5.89186	7.04150	9.29907	12.33976
14	4.07467	4.66043	5.62873	6.57063	7.78953	10.16531	13.33927
15	4.60092	5.22935	6.26214	7.26094	8.54676	11.03654	14.33886
16	5.14221	5.81221	6.90766	7.96165	9.31224	11.91222	15.33850
17	5.69722	6.40776	7.56419	8.67176	10.08519	12.79193	16.33818
18	6.26480	7.01491	8.23075	9.39046	10.86494	13.67529	17.33790
19	6.84397	7.63273	8.90652	10.11701	11.65091	14.56200	18.33765
20	7.43384	8.26040	9.59078	10.85081	12.44261	15.45177	19.33743
21	8.03365	8.89720	10.28290	11.59131	13.23960	16.34438	20.33723
22	8.64272	9.54249	10.98232	12.33801	14.04149	17.23962	21.33704
23	9.26042	10.19572	11.68855	13.09051	14.84796	18.13730	22.33688
24	9.88623	10.85636	12.40115	13.84843	15.65868	19.03725	23.33673
25	10.51965	11.52398	13.11972	14.61141	16.47341	19.93934	24.33659
26	11.16024	12.19815	13.84390	15.37916	17.29188	20.84343	25.33646
27	11.80759	12.87850	14.57338	16.15140	18.11390	21.74940	26.33634
28	12.46134	13.56471	15.30786	16.92788	18.93924	22.65716	27.33623
29	13.12115	14.25645	16.04707	17.70837	19.76774	23.56659	28.33613
30	13.78672	14.95346	16.79077	18.49266	20.59923	24.47761	29.33603

# **Chi-Square Table (Cont.)**

df/ area	.250	.100	.050	.025	.010	.005
1	1.32330	2.70554	3.84146	5.02389	6.63490	7.87944
2	2.77259	4.60517	5.99146	7.37776	9.21034	10.59663
3	4.10834	6.25139	7.81473	9.34840	11.34487	12.83816
4	5.38527	7.77944	9.48773	11.14329	13.27670	14.86026
5	6.62568	9.23636	11.07050	12.83250	15.08627	16.74960
6	7.84080	10.64464	12.59159	14.44938	16.81189	18.54758
7	9.03715	12.01704	14.06714	16.01276	18.47531	20.27774
8	10.21885	13.36157	15.50731	17.53455	20.09024	21.95495
9	11.38875	14.68366	16.91898	19.02277	21.66599	23.58935
10	12.54886	15.98718	18.30704	20.48318	23.20925	25.18818
11	13.70069	17.27501	19.67514	21.92005	24.72497	26.75685
12	14.84540	18.54935	21.02607	23.33666	26.21697	28.29952
13	15.98391	19.81193	22.36203	24.73560	27.68825	29.81947
14	17.11693	21.06414	23.68479	26.11895	29.14124	31.31935
15	18.24509	22.30713	24.99579	27.48839	30.57791	32.80132
16	19.36886	23.54183	26.29623	28.84535	31.99993	34.26719
17	20.48868	24.76904	27.58711	30.19101	33.40866	35.71847
18	21.60489	25.98942	28.86930	31.52638	34.80531	37.15645
19	22.71781	27.20357	30.14353	32.85233	36.19087	38.58226
20	23.82769	28.41198	31.41043	34.16961	37.56623	39.99685
			ı			
21	24.93478	29.61509	32.67057	35.47888	38.93217	41.40106
22	26.03927	30.81328	33.92444	36.78071	40.28936	42.79565
23	27.14134	32.00690	35.17246	38.07563	41.63840	44.18128
24	28.24115	33.19624	36.41503	39.36408	42.97982	45.55851
25	29.33885	34.38159	37.65248	40.64647	44.31410	46.92789
			T			
26	30.43457	35.56317	38.88514	41.92317	45.64168	48.28988
27	31.52841	36.74122	40.11327	43.19451	46.96294	49.64492
28	32.62049	37.91592	41.33714	44.46079	48.27824	50.99338
29	33.71091	39.08747	42.55697	45.72229	49.58788	52.33562
30	34.79974	40.25602	43.77297	46.97924	50.89218	53.67196

df2/ df1	1	2	3	4	5	6	7	8	9	10
1	39.86346	49.50000	53.59324	55.83296	57.24008	58.20442	58.90595	59.43898	59.85759	60.19498
2	8.52632	9.00000	9.16179	9.24342	9.29263	9.32553	9.34908	9.36677	9.38054	9.39157
3	5.53832	5.46238	5.39077	5.34264	5.30916	5.28473	5.26619	5.25167	5.24000	5.23041
4	4.54477	4.32456	4.19086	4.10725	4.05058	4.00975	3.97897	3.95494	3.93567	3.91988
5	4.06042	3.77972	3.61948	3.52020	3.45298	3.40451	3.36790	3.33928	3.31628	3.29740
6	3.77595	3.46330	3.28876	3.18076	3.10751	3.05455	3.01446	2.98304		2.93693
7	3.58943	3.25744	3.07407	2.96053	2.88334	2.82739	2.78493	2.75158	2.72468	2.70251
8	3.45792	3.11312	2.92380	2.80643	2.72645	2.66833	2.62413	2.58935	2.56124	2.53804
9	3.36030	3.00645	2.81286	2.69268	2.61061	2.55086	2.50531	2.46941	2.44034	2.41632
10	3.28502	2.92447	2.72767	2.60534	2.52164	2.46058	2.41397	2.37715	2.34731	2.32260
									1	
11	3.22520	2.85951	2.66023	2.53619	2.45118		2.34157			
12	3.17655	2.80680	2.60552	2.48010	2.39402	2.33102	2.28278		2.21352	2.18776
13	3.13621	2.76317	2.56027	2.43371	2.34672	2.28298	2.23410			2.13763
14	3.10221	2.72647	2.52222	2.39469	2.30694	2.24256	2.19313	2.15390		2.09540
15	3.07319	2.69517	2.48979	2.36143	2.27302	2.20808	2.15818	2.11853	2.08621	2.05932
		n e							1	
16	3.04811	2.66817	2.46181	2.33274	2.24376		2.12800			
17	3.02623	2.64464	2.43743	2.30775	2.21825	2.15239	2.10169			2.00094
18	3.00698	2.62395	2.41601	2.28577	2.19583	2.12958	2.07854	2.03789	2.00467	1.97698
19	2.98990	2.60561	2.39702	2.26630	2.17596	2.10936	2.05802	2.01710	1.98364	1.95573
20	2.97465	2.58925	2.38009	2.24893	2.15823	2.09132	2.03970	1.99853	1.96485	1.93674
									T	
21	2.96096		2.36489			2.07512	2.02325			
22	2.94858	2.56131	2.35117	2.21927	2.12794	2.06050				1.90425
23	2.93736	2.54929	2.33873	2.20651	2.11491	2.04723	1.99492	1.95312	1.91888	1.89025
24	2.92712	2.53833	2.32739	2.19488	2.10303	2.03513	1.98263	1.94066	1.90625	1.87748
25	2.91774	2.52831	2.31702	2.18424	2.09216	2.02406	1.97138	1.92925	1.89469	1.86578
0.0	2 00012	2 71010	2 2 2 7 4 2		2.00210	2 01200	1.06104	1.010=6	1.00405	1.05503
26	2.90913	2.51910			2.08218					1.85503
27	2.90119		2.29871	2.16546		2.00452	1.95151			
28	2.89385	2.50276	2.29060	2.15714	2.06447	1.99585	1.94270			1.83593
29	2.88703	2.49548	2.28307	2.14941	2.05658	1.98781	1.93452	1.89184		1.82741
30	2.88069	2.48872	2.27607	2.14223	2.04925	1.98033	1.92692	1.88412	1.84896	1.81949
40	2.02.52.5	2.4402=	2.22600	2.00007	1.00602	1.02600	1.05050	1.02007	1.70200	1.7/2/0
40	2.83535	2.44037	2.22609			1.92688		1.82886		
60	2.79107	2.39325	2.17741	2.04099	1.94571	1.87472	1.81939	1.77483	1.73802	1.70701
120	2.74781	2.34734	2.12999	1.99230		1.82381	1.76748	1.72196		1.65238
inf	2.70554	2.30259	2.08380	1.94486	1.84727	1.77411	1.71672	1.67020	1.63152	1.59872

df2/	12	15	20	24	30	40	60	120	INF
df1	60.70521	(1.22024	61.74020	(2.00205	62.26407	(2.52005	(2.70429	62.06064	(2.22012
2	60.70521	61.22034	61.74029	62.00205 9.44962	62.26497	62.52905	62.79428	63.06064	63.32812
3	9.40813	9.42471	9.44131		9.45793 5.16811	9.46624	9.47456	9.48289	9.49122
	5.21562	5.20031	5.18448	5.17636		5.15972	5.15119	5.14251	5.13370
4	3.89553	3.87036	3.84434	3.83099	3.81742	3.80361	3.78957	3.77527	3.76073
5	3.26824	3.23801	3.20665	3.19052	3.17408	3.15732	3.14023	3.12279	3.10500
	2.00472	2.07122	2.02(24	2.01024	2.70006	2 70117	2.7(105	2.74220	2.7221.6
6	2.90472	2.87122	2.83634	2.81834	2.79996	2.78117	2.76195	2.74229	2.72216
7	2.66811	2.63223	2.59473	2.57533	2.55546	2.53510	2.51422	2.49279	2.47079
8	2.50196	2.46422	2.42464	2.40410	2.38302	2.36136	2.33910	2.31618	2.29257
9	2.37888	2.33962	2.29832	2.27683	2.25472	2.23196	2.20849	2.18427	2.15923
10	2.28405	2.24351	2.20074	2.17843	2.15543	2.13169	2.10716	2.08176	2.05542
		0.4.5=0=	0.4000=	<b>0</b> 4000:	00-10-1		20251	1.000.5=	4.0=54:
11	2.20873	2.16709	2.12305	2.10001	2.07621	2.05161	2.02612	1.99965	1.97211
12	2.14744	2.10485	2.05968	2.03599	2.01149	1.98610	1.95973	1.93228	1.90361
13	2.09659	2.05316	2.00698	1.98272	1.95757	1.93147	1.90429	1.87591	1.84620
14	2.05371	2.00953	1.96245	1.93766	1.91193	1.88516	1.85723	1.82800	1.79728
15	2.01707	1.97222	1.92431	1.89904	1.87277	1.84539	1.81676	1.78672	1.75505
16	1.98539	1.93992	1.89127	1.86556	1.83879	1.81084	1.78156	1.75075	1.71817
17	1.95772	1.91169	1.86236	1.83624	1.80901	1.78053	1.75063	1.71909	1.68564
18	1.93334	1.88681	1.83685	1.81035	1.78269	1.75371	1.72322	1.69099	1.65671
19	1.91170	1.86471	1.81416	1.78731	1.75924	1.72979	1.69876	1.66587	1.63077
20	1.89236	1.84494	1.79384	1.76667	1.73822	1.70833	1.67678	1.64326	1.60738
21	1.87497	1.82715	1.77555	1.74807	1.71927	1.68896	1.65691	1.62278	1.58615
22	1.85925	1.81106	1.75899	1.73122	1.70208	1.67138	1.63885	1.60415	1.56678
23	1.84497	1.79643	1.74392	1.71588	1.68643	1.65535	1.62237	1.58711	1.54903
24	1.83194	1.78308	1.73015	1.70185	1.67210	1.64067	1.60726	1.57146	1.53270
25	1.82000	1.77083	1.71752	1.68898	1.65895	1.62718	1.59335	1.55703	1.51760
26	1.80902	1.75957	1.70589	1.67712	1.64682	1.61472	1.58050	1.54368	1.50360
27	1.79889	1.74917	1.69514	1.66616	1.63560	1.60320	1.56859	1.53129	1.49057
28	1.78951	1.73954	1.68519	1.65600	1.62519	1.59250	1.55753	1.51976	1.47841
29	1.78081	1.73060	1.67593	1.64655	1.61551	1.58253	1.54721	1.50899	1.46704
30	1.77270	1.72227	1.66731	1.63774	1.60648	1.57323	1.53757	1.49891	1.45636
40	1.71456	1.66241	1.60515	1.57411	1.54108	1.50562	1.46716	1.42476	1.37691
60	1.65743	1.60337	1.54349	1.51072	1.47554	1.43734	1.39520	1.34757	1.29146
120	1.60120	1.54500	1.48207	1.44723	1.40938	1.36760	1.32034	1.26457	1.19256
inf	1.54578	1.48714	1.42060	1.38318	1.34187	1.29513	1.23995	1.16860	1.00000
			<b>_</b> 000	02 10		/010			

# F Table for alpha=.05

df2/ df1	1	2	3	4	5	6	7	8	9	10
1	161.4476	199.5000	215.7073	224.5832	230.1619	233.9860	236.7684	238.8827	240.5433	241.8817
2	18.5128	19.0000	19.1643	19.2468	19.2964	19.3295	19.3532	19.3710	19.3848	19.3959
3	10.1280	9.5521	9.2766	9.1172	9.0135	8.9406	8.8867	8.8452	8.8123	8.7855
4	7.7086	6.9443	6.5914	6.3882	6.2561	6.1631	6.0942	6.0410	5.9988	5.9644
5	6.6079	5.7861	5.4095	5.1922	5.0503	4.9503	4.8759	4.8183	4.7725	4.7351
6	5.9874	5.1433	4.7571	4.5337	4.3874	4.2839	4.2067	4.1468	4.0990	4.0600
7	5.5914	4.7374	4.3468	4.1203	3.9715	3.8660	3.7870	3.7257	3.6767	3.6365
8	5.3177	4.4590	4.0662	3.8379	3.6875	3.5806	3.5005	3.4381	3.3881	3.3472
9	5.1174	4.2565	3.8625	3.6331	3.4817	3.3738	3.2927	3.2296	3.1789	3.1373
10	4.9646	4.1028	3.7083	3.4780	3.3258	3.2172	3.1355	3.0717	3.0204	2.9782
								,	_	,
11	4.8443	3.9823	3.5874	3.3567	3.2039		3.0123			
12	4.7472	3.8853	3.4903	3.2592	3.1059		2.9134	2.8486		
13	4.6672	3.8056		3.1791	3.0254		2.8321	2.7669		
14	4.6001	3.7389			2.9582		2.7642			
15	4.5431	3.6823	3.2874	3.0556	2.9013	2.7905	2.7066	2.6408	2.5876	2.5437
	1		Γ		Γ	1		1	,	
16	4.4940	3.6337					2.6572			
17	4.4513	3.5915		2.9647	2.8100		2.6143			
18	4.4139				2.7729		2.5767			
19	4.3807	3.5219		2.8951	2.7401		2.5435			
20	4.3512	3.4928	3.0984	2.8661	2.7109	2.5990	2.5140	2.4471	2.3928	2.3479
						T			T	
21	4.3248	3.4668		2.8401	2.6848		2.4876			
22	4.3009	3.4434		2.8167	2.6613		2.4638			
23	4.2793	3.4221	3.0280				2.4422			
24	4.2597	3.4028		2.7763			2.4226			
25	4.2417	3.3852	2.9912	2.7587	2.6030	2.4904	2.4047	2.3371	2.2821	2.2365
26	4 2252	2.2600	2.0752	2.7426	2.5060	2 4741	2 2002	2 2205	2.2655	2 2107
26	4.2252			2.7426			2.3883			
27	4.2100		2.9604				2.3732			
28	4.1960									
29	4.1830		2.9340							
30	4.1709	3.3158	2.9223	2.6896	2.5336	2.4205	2.3343	2.2662	2.2107	2.1646
40	4.0847	3.2317	2.8387	2.6060	2 4405	2.3359	2.2490	2.1802	2.1240	2.0772
60	4.0012	3.2317		2.5252	2.4495 2.3683		2.2490			
120	3.9201	3.0718	2.6802	2.3232	2.3889		2.1868			
inf		2.9957								
IIII	3.8415	2.995/	2.6049	2.3719	2.2141	2.0986	2.0096	1.9384	1.8799	1.8307

# F Table for alpha=.05 (Cont.)

df2/ df1	12	15	20	24	30	40	60	120	INF
1	243.9060	245.9499	248.0131	249.0518	250.0951	251.1432	252.1957	253.2529	254.3144
2	19.4125	19.4291	19.4458	19.4541	19.4624	19.4707	19.4791	19.4874	19.4957
3	8.7446	8.7029	8.6602	8.6385	8.6166	8.5944	8.5720	8.5494	8.5264
4	5.9117	5.8578	5.8025	5.7744	5.7459	5.7170	5.6877	5.6581	5.6281
5	4.6777	4.6188	4.5581	4.5272	4.4957	4.4638	4.4314	4.3985	4.3650
6	3.9999	3.9381	3.8742	3.8415	3.8082	3.7743	3.7398	3.7047	3.6689
7	3.5747	3.5107	3.4445	3.4105	3.3758	3.3404	3.3043	3.2674	3.2298
8	3.2839	3.2184	3.1503	3.1152	3.0794	3.0428	3.0053	2.9669	2.9276
9	3.0729	3.0061	2.9365	2.9005	2.8637	2.8259	2.7872	2.7475	2.7067
10	2.9130	2.8450	2.7740	2.7372	2.6996	2.6609	2.6211	2.5801	2.5379
	· · · · · · · · · · · · · · · · · · ·			,			,		
11	2.7876	2.7186	2.6464	2.6090	2.5705	2.5309	2.4901	2.4480	
12	2.6866	2.6169	2.5436	2.5055	2.4663	2.4259	2.3842	2.3410	2.2962
13	2.6037	2.5331	2.4589	2.4202	2.3803	2.3392	2.2966	2.2524	2.2064
14	2.5342	2.4630	2.3879	2.3487	2.3082	2.2664	2.2229	2.1778	
15	2.4753	2.4034	2.3275	2.2878	2.2468	2.2043	2.1601	2.1141	2.0658
16	2.4247	2.3522	2.2756	2.2354	2.1938	2.1507	2.1058	2.0589	
17	2.3807	2.3077	2.2304	2.1898	2.1477	2.1040	2.0584	2.0107	1.9604
18	2.3421	2.2686	2.1906	2.1497	2.1071	2.0629	2.0166	1.9681	1.9168
19	2.3080	2.2341	2.1555	2.1141	2.0712	2.0264	1.9795	1.9302	1.8780
20	2.2776	2.2033	2.1242	2.0825	2.0391	1.9938	1.9464	1.8963	1.8432
21	2 2504	2 1757	2.00(0	2.05.40	2.0102	1.0645	1.0165	1.0657	1.0117
21	2.2504	2.1757	2.0960	2.0540	2.0102	1.9645	1.9165	1.8657	1.8117
22	2.2258 2.2036	2.1508 2.1282	2.0707 2.0476	2.0283 2.0050	1.9842	1.9380 1.9139	1.8894 1.8648	1.8380 1.8128	1.7831 1.7570
24	2.2036	2.1282	2.0476	1.9838	1.9605 1.9390	1.8920	1.8424	1.7896	
25	2.1634	2.1077	2.0207	1.9643	1.9390	1.8718	1.8217	1.7684	1.7110
23	2.1049	2.0009	2.0073	1.7043	1.9192	1.0710	1.021/	1.7004	1./110
26	2.1479	2.0716	1.9898	1.9464	1.9010	1.8533	1.8027	1.7488	1.6906
27	2.1323	2.0558	1.9736	1.9299	1.8842	1.8361	1.7851	1.7306	
28	2.1179	2.0411	1.9586	1.9147	1.8687	1.8203	1.7689	1.7138	
29	2.1045	2.0275	1.9446	1.9005	1.8543	1.8055	1.7537	1.6981	1.6376
30	2.0921	2.0148	1.9317	1.8874	1.8409	1.7918	1.7396	1.6835	
	1	01.0	,,	2.0071	0.07	,, 20	,0,0	0020	
40	2.0035	1.9245	1.8389	1.7929	1.7444	1.6928	1.6373	1.5766	1.5089
60	1.9174	1.8364	1.7480	1.7001	1.6491	1.5943	1.5343	1.4673	
120	1.8337	1.7505	1.6587	1.6084	1.5543	1.4952	1.4290	1.3519	
inf	1.7522	1.6664	1.5705	1.5173	1.4591	1.3940	1.3180	1.2214	

# F Table for alpha=.025

df2/ df1	1	2	3	4	5	6	7	8	9	10
1	647.7890	799.5000	864.1630	899.5833	921.8479	937.1111	948.2169	956.6562	963.2846	968.6274
2	38.5063	39.0000	39.1655	39.2484	39.2982	39.3315	39.3552	39.3730	39.3869	39.3980
3	17.4434	16.0441	15.4392	15.1010	14.8848	14.7347	14.6244	14.5399	14.4731	14.4189
4	12.2179	10.6491	9.9792	9.6045	9.3645	9.1973	9.0741	8.9796	8.9047	8.8439
5	10.0070	8.4336	7.7636	7.3879	7.1464	6.9777	6.8531	6.7572	6.6811	6.6192
6	8.8131	7.2599	6.5988	6.2272	5.9876	5.8198	5.6955	5.5996	5.5234	5.4613
7	8.0727	6.5415	5.8898	5.5226	5.2852	5.1186	4.9949	4.8993	4.8232	4.7611
8	7.5709	6.0595	5.4160	5.0526	4.8173	4.6517	4.5286	4.4333	4.3572	4.2951
9	7.2093	5.7147	5.0781	4.7181	4.4844	4.3197	4.1970	4.1020	4.0260	3.9639
10	6.9367	5.4564	4.8256	4.4683	4.2361	4.0721	3.9498	3.8549	3.7790	3.7168
						,				
11	6.7241	5.2559	4.6300	4.2751	4.0440	3.8807	3.7586			
12	6.5538	5.0959	4.4742	4.1212	3.8911	3.7283	3.6065		3.4358	
13	6.4143	4.9653	4.3472	3.9959	3.7667	3.6043	3.4827		3.3120	
14	6.2979	4.8567	4.2417	3.8919	3.6634	3.5014			3.2093	
15	6.1995	4.7650	4.1528	3.8043	3.5764	3.4147	3.2934	3.1987	3.1227	3.0602
						,	,			
16	6.1151	4.6867	4.0768	3.7294	3.5021	3.3406			3.0488	2.9862
17	6.0420	4.6189	4.0112	3.6648	3.4379	3.2767	3.1556	3.0610	2.9849	2.9222
18	5.9781	4.5597	3.9539	3.6083	3.3820	3.2209	3.0999	3.0053	2.9291	2.8664
19	5.9216	4.5075	3.9034	3.5587	3.3327	3.1718	3.0509		2.8801	2.8172
20	5.8715	4.4613	3.8587	3.5147	3.2891	3.1283	3.0074	2.9128	2.8365	2.7737
	1		T		Γ	1	1	1	1	1
21	5.8266	4.4199	3.8188	3.4754		3.0895			2.7977	
22	5.7863	4.3828	3.7829	3.4401	3.2151	3.0546	2.9338		2.7628	
23	5.7498	4.3492	3.7505	3.4083	3.1835	3.0232	2.9023		2.7313	
24	5.7166	4.3187	3.7211	3.3794	3.1548	2.9946	2.8738	2.7791	2.7027	2.6396
25	5.6864	4.2909	3.6943	3.3530	3.1287	2.9685	2.8478	2.7531	2.6766	2.6135
						I · · -				
26	5.6586	4.2655	3.6697	3.3289	3.1048					
27	5.6331	4.2421	3.6472	3.3067	3.0828					
28	5.6096	4.2205	3.6264	3.2863	3.0626		2.7820		2.6106	
29	5.5878	4.2006	3.6072	3.2674	3.0438		2.7633			
30	5.5675	4.1821	3.5894	3.2499	3.0265	2.8667	2.7460	2.6513	2.5746	2.5112
40		4.0.5.0	2.4622	2.1251	2 005 =		0.6000	0.7000	0.4510	2 2002
40	5.4239	4.0510	3.4633	3.1261	2.9037				2.4519	
60	5.2856	3.9253	3.3425	3.0077	2.7863	2.6274			2.3344	
120	5.1523	3.8046	3.2269	2.8943	2.6740	2.5154	2.3948		2.2217	2.1570
inf	5.0239	3.6889	3.1161	2.7858	2.5665	2.4082	2.2875	2.1918	2.1136	2.0483

# F Table for alpha=.025 (Cont.)

df2/ df1	12	15	20	24	30	40	60	120	INF
1	976.7079	984.8668	993.1028	997.2492	1001.414	1005.598	1009.800	1014.020	1018.258
2	39.4146	39.4313	39.4479	39.4562	39.465	39.473	39.481	39.490	39.498
3	14.3366	14.2527	14.1674	14.1241	14.081	14.037	13.992	13.947	13.902
4	8.7512	8.6565	8.5599	8.5109	8.461	8.411	8.360	8.309	8.257
5	6.5245	6.4277	6.3286	6.2780	6.227	6.175	6.123	6.069	6.015
	2 1 11 21 21 21 21 21 21 21 21 21 21 21								
6	5.3662	5.2687	5.1684	5.1172	5.065	5.012	4.959	4.904	4.849
7	4.6658	4.5678	4.4667	4.4150	4.362	4.309	4.254	4.199	4.142
8	4.1997	4.1012	3.9995	3.9472	3.894	3.840	3.784	3.728	3.670
9	3.8682	3.7694	3.6669	3.6142	3.560	3.505	3.449	3.392	3.333
10	3.6209	3.5217	3.4185	3.3654	3.311	3.255	3.198	3.140	3.080
		т	т		-	-		-	
11	3.4296	3.3299	3.2261	3.1725		3.061	3.004	2.944	
12	3.2773	3.1772	3.0728	3.0187	2.963	2.906	2.848	2.787	2.725
13	3.1532	3.0527	2.9477	2.8932	2.837	2.780	2.720	2.659	2.595
14	3.0502	2.9493	2.8437	2.7888	2.732	2.674	2.614	2.552	2.487
15	2.9633	2.8621	2.7559	2.7006	2.644	2.585	2.524	2.461	2.395
					1	1		1	
16	2.8890	2.7875	2.6808	2.6252		2.509	2.447	2.383	2.316
17	2.8249	2.7230	2.6158	2.5598		2.442	2.380	2.315	2.247
18	2.7689	2.6667	2.5590	2.5027	2.445	2.384	2.321	2.256	2.187
19	2.7196	2.6171	2.5089	2.4523	2.394	2.333	2.270	2.203	2.133
20	2.6758	2.5731	2.4645	2.4076	2.349	2.287	2.223	2.156	2.085
					1				
21	2.6368	2.5338	2.4247	2.3675		2.246	2.182	2.114	
22	2.6017	2.4984	2.3890	2.3315	2.272	2.210	2.145	2.076	2.003
23	2.5699	2.4665	2.3567	2.2989	2.239	2.176	2.111	2.041	1.968
24	2.5411	2.4374	2.3273	2.2693	2.209	2.146	2.080	2.010	
25	2.5149	2.4110	2.3005	2.2422	2.182	2.118	2.052	1.981	1.906
26	2 4000	2 20/7	2 2750	2 2174	2 1 5 7	2.002	2.026	1 05 4	1 070
26 27	2.4908	2.3867	2.2759 2.2533	2.2174		2.093	2.026	1.954	
	2.4688	2.3644		2.1946		2.069 2.048	2.002	1.930	
28 29	2.4484 2.4295	2.3438 2.3248	2.2324 2.2131	2.1735 2.1540	2.112 2.092	2.048	1.980 1.959	1.907 1.886	1.829
30						2.028			
30	2.4120	2.3072	2.1952	2.1359	2.074	2.009	1.940	1.866	1.787
40	2.2882	2.1819	2.0677	2.0069	1.943	1.875	1.803	1.724	1.637
60	2.2662	2.1619	1.9445	1.8817	1.815	1.744	1.667	1.724	1.482
120	2.1092	1.9450	1.8249	1.7597	1.690	1.614	1.530	1.433	1.462
inf	1.9447	1.8326	1.7085	1.6402		1.484	1.388	1.433	
ШІ	1.944/	1.8320	1./085	1.0402	1.300	1.484	1.388	1.208	1.000

# F Table for alpha=.01

df2/ df1	1	2	3	4	5	6	7	8	9	10
1	4052.181	4999.500	5403.352	5624.583	5763.650	5858.986	5928.356	5981.070	6022.473	6055.847
2	98.503	99.000	99.166	99.249	99.299	99.333	99.356	99.374		
3	34.116	30.817	29.457	28.710	28.237	27.911	27.672	27.489		27.229
4	21.198	18.000	16.694	15.977	15.522	15.207	14.976	14.799	14.659	14.546
5	16.258	13.274	12.060	11.392	10.967	10.672	10.456	10.289	10.158	10.051
									,	,
6	13.745	10.925								
7	12.246	9.547		7.847	7.460		6.993	6.840		
8	11.259			7.006			6.178			
9	10.561	8.022	6.992	6.422	6.057		5.613			
10	10.044	7.559	6.552	5.994	5.636	5.386	5.200	5.057	4.942	4.849
				ادر با با		ا د د د		. =		
11	9.646									
12	9.330	6.927	5.953	5.412	5.064		4.640			
13	9.074		5.739			4.620	4.441	4.302		
14	8.862	6.515								
15	8.683	6.359	5.417	4.893	4.556	4.318	4.142	4.004	3.895	3.805
										I
16	8.531	6.226		4.773			4.026			
17	8.400	6.112	5.185				3.927	3.791		
18	8.285	6.013		4.579				3.705		
19	8.185	5.926				3.939		3.631		
20	8.096	5.849	4.938	4.431	4.103	3.871	3.699	3.564	3.457	3.368
	0.01=							• • •		
21	8.017	5.780								
22	7.945						3.587	3.453		
23	7.881	5.664								
24	7.823	5.614					3.496			
25	7.770	5.568	4.675	4.177	3.855	3.627	3.457	3.324	3.217	3.129
26	7.701	5.500	4.627	4 1 40	2.010	2.501	2 421	2.200	2.102	2.004
26	7.721	5.526					3.421	3.288		
27	7.677									
28	7.636									
29	7.598									
30	7.562	5.390	4.510	4.018	3.699	3.473	3.304	3.173	3.067	2.979
40	7 21 4	5.179	1212	2 020	2 514	2 201	2 124	2.993	2 000	2 001
40	7.314 7.077	4.977					3.124			
120								2.823		
120	6.851	4.787						2.663		
inf	6.635	4.605	3.782	3.319	3.017	2.802	2.639	2.511	2.407	2.321

# F Table for alpha=.01 (Cont.)

df2/ df1	12	15	20	24	30	40	60	120	INF
1	6106.321	6157.285	6208.730	6234.631	6260.649	6286.782	6313.030	6339.391	6365.864
2	99.416	99.433	99.449	99.458	99.466	99.474	99.482	99.491	99.499
3	27.052	26.872	26.690	26.598	26.505	26.411	26.316	26.221	26.125
4	14.374	14.198	14.020	13.929	13.838	13.745	13.652	13.558	13.463
5	9.888	9.722	9.553	9.466	9.379	9.291	9.202	9.112	9.020
	<u> </u>								
6	7.718	7.559	7.396	7.313	7.229	7.143	7.057	6.969	6.880
7	6.469	6.314	6.155	6.074	5.992	5.908	5.824	5.737	5.650
8	5.667	5.515	5.359	5.279	5.198	5.116	5.032	4.946	4.859
9	5.111	4.962	4.808	4.729	4.649	4.567	4.483	4.398	4.311
10	4.706	4.558	4.405	4.327	4.247	4.165	4.082	3.996	3.909
11	4.397	4.251	4.099	4.021	3.941	3.860	3.776	3.690	3.602
12	4.155	4.010	3.858	3.780	3.701	3.619	3.535	3.449	3.361
13	3.960	3.815	3.665	3.587	3.507	3.425	3.341	3.255	3.165
14	3.800	3.656	3.505	3.427	3.348	3.266	3.181	3.094	3.004
15	3.666	3.522	3.372	3.294	3.214	3.132	3.047	2.959	2.868
			,					1	
16	3.553	3.409	3.259	3.181	3.101	3.018	2.933	2.845	2.753
17	3.455	3.312	3.162	3.084	3.003	2.920	2.835	2.746	2.653
18	3.371	3.227	3.077	2.999	2.919	2.835	2.749	2.660	2.566
19	3.297	3.153	3.003	2.925	2.844	2.761	2.674	2.584	2.489
20	3.231	3.088	2.938	2.859	2.778	2.695	2.608	2.517	2.421
21	3.173	3.030	2.880	2.801	2.720	2.636	2.548	2.457	2.360
22	3.121	2.978	2.827	2.749	2.667	2.583	2.495	2.403	2.305
23	3.074	2.931	2.781	2.702	2.620	2.535	2.447	2.354	2.256
24	3.032	2.889	2.738	2.659	2.577	2.492	2.403	2.310	2.211
25	2.993	2.850	2.699	2.620	2.538	2.453	2.364	2.270	2.169
26	2.050	2.01.5	2 ((1	2.505	2.502	2.417	2 227	2 222	2 121
26 27	2.958	2.815	2.664	2.585	2.503	2.417	2.327	2.233	2.131
	2.926	2.783	2.632	2.552	2.470	2.384	2.294	2.198	2.097
28	2.896	2.753	2.602	2.522	2.440	2.354	2.263	2.167	2.064
29	2.868	2.726	2.574	2.495	2.412	2.325	2.234	2.138	2.034
30	2.843	2.700	2.549	2.469	2.386	2.299	2.208	2.111	2.006
40	2.665	2.522	2.369	2.288	2.203	2.114	2.019	1.917	1.805
60	2.665	2.322	2.369	2.288	2.203	1.936	1.836	1.726	1.601
120	2.496	2.332	2.198	1.950	1.860	1.763	1.656	1.726	1.381
inf	2.330	2.192	1.878						
IIII	2.185	2.039	1.8/8	1.791	1.696	1.592	1.473	1.325	1.000

Helping Formula	as - 2005:
$\frac{\overline{x} - \mu_o}{s / \sqrt{n}}, \frac{\overline{d} - \overline{D}_o}{s_d / \sqrt{n}}$	$\overline{P} = \frac{n_1 p_1 + n_2 p_2}{n_1 + n_2}$
$\overline{x} \pm t_{(\alpha/2, n-1)} \frac{s}{\sqrt{n}}$	$(p_1 - p_2) \pm Z_{\alpha/2} \sqrt{\frac{p_1(1 - p_1)}{n_1} + \frac{p_2(1 - p_2)}{n_2}}$
$\frac{p-\pi_o}{\sqrt{\frac{\pi_o(1-\pi_o)}{n}}}$	$S_{Y X} = \sqrt{\frac{\sum Y^2 - \hat{a} \sum Y - \hat{b} \sum XY}{n-2}}$
$p \pm z_{\alpha/2}.\sqrt{\frac{p(1-p)}{n}}$	$R^{2} = \frac{\hat{a}\sum Y + \hat{b}\sum XY - n\overline{Y}^{2}}{\sum Y^{2} - n\overline{Y}^{2}}$
$\frac{(\overline{x}_{1} - \overline{x}_{2}) - (\mu_{1} - \mu_{2})_{o}}{\sqrt{S_{p}^{2}(\frac{1}{n_{1}} + \frac{1}{n_{2}})}}$	LSD = $\sqrt{\text{MSE}} \cdot \sqrt{\frac{2}{n}} \cdot t_{(2(n-1),\alpha/2)}$
$S_p^2 = \frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2}$	$\hat{Y} = \hat{a} + \hat{b}X$
$\frac{(\overline{x}_{1} - \overline{x}_{2}) - (\mu_{1} - \mu_{2})_{o}}{\sqrt{\frac{S_{1}^{2}}{n_{1}} + \frac{S_{2}^{2}}{n_{2}}}}$	$\hat{b}_{Y X} = \frac{\sum XY - n\overline{XY}}{\sum X^2 - n\overline{X}^2}$
$(\overline{x}_1 - \overline{x}_2) \pm Z_{\alpha/2} \sqrt{S_p^2 (\frac{1}{n_1} + \frac{1}{n_2})}$	$\hat{a} = \overline{Y} - \hat{b}\overline{X}, \overline{X} = \frac{\sum X}{n}, \overline{Y} = \frac{\sum Y}{n}$
$(\overline{x}_1 - \overline{x}_2) \pm t_{(\alpha/2)}, n_1 + n_2 - 2) \sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}$	Expected Frequency = $\frac{\text{row sum} \times \text{col sum}}{\text{Total Sum}}$ ,
·	$\chi^{2} = \sum_{\forall cells} \frac{(O_{i} - E_{i})^{2}}{E_{i}}   cc = \sqrt{\frac{\chi^{2}}{\chi^{2} + n}}$
$\overline{d} = \frac{\sum d}{n}, \ S_d = \sqrt{\frac{\sum d_i^2 - n\overline{d}^2}{n-1}}$	Normal Value for Sign Test= $\frac{2R-n}{\sqrt{n}}$ , $R = \#(+)$
$\overline{d} \pm t_{(\alpha/2}, n-1) \frac{S_d}{\sqrt{n}}$	$Z = \frac{V - \frac{n(n+1)}{4}}{\sqrt{n(n+1)(2n+1)/24}},$ $V = \text{Sum of (+) ranks}$
$\frac{(p_1 - p_2) - (\pi_1 - \pi_2)_0}{\sqrt{\frac{p_1(1 - p_1)}{n_1} + \frac{p_2(1 - p_2)}{n_2}}}$ $\frac{(p_1 - p_2) - (\pi_1 - \pi_2)_0}{\sqrt{\frac{p_1(1 - p_2) - (\pi_1 - \pi_2)_0}{n_2}}}$	$V = \text{Sum of (+) ranks}$ $r_S = 1 - \frac{6\sum d_i^2}{n(n^2 - 1)}$
$\frac{(p_1 - p_2) - (\pi_1 - \pi_2)_0}{\sqrt{\overline{p}(1 - \overline{p})(\frac{1}{n_1} + \frac{1}{n_2})}}$	$r_{P} = \frac{\sum XY - n\overline{X}\overline{Y}}{\sqrt{(\sum X^{2} - n\overline{X}^{2})(\sum Y^{2} - n\overline{Y}^{2})}}$

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