Problem 1: Expected Value of Soccer Days

Applying the Formula:

- Let's list out the values and their probabilities:
 - x1=0 P(X=0)=0.2
 - x2=1, P(X=1)=0.5
 - x3=2, P(X=2)=0.3
- Now, compute each term:
 - $0 \times 0.2 = 0$
 - 1×0.5=0.5
 - 2×0.3=0.6
- Summing these up:
- E(X)=0+0.5+0.6=1.1

Problem 2: Mean and Standard Deviation of Even **Numbers on Die Rolls**

- 1. Identifying Possible Values of X:
 - X can be 0, 1, or 2.
 - X=0: Both rolls are odd.
 - X=1: One roll is even, and the other is odd.
 - X=2 Both rolls are even.

1. Calculating Probabilities for Each Value of XX:

- determine the probability of rolling an even number on a single die:
 - There are 3 even numbers (2, 4, 6) out of 6 possible outcomes
 - So, **P(Even)=3/6 =0.5**
 - Similarly, P(Odd)=0.5
- calculate the probabilities for each value of X:
 - P(X=0): Both rolls are odd.
 - P(X=0)=P(Odd)×P(Odd)=0.5×0.5=0.25
 - P(X=1): One even and one odd. There are two scenarios: • First roll even, second roll odd.
 - First roll odd, second roll even.
 - P(X=1)=2×(P(Even)×P(Odd))=2×(0.5×0.5)=0.5
 - P(X=2): Both rolls are even.

 - P(X=2)=P(Even)×P(Even)=0.5×0.5=0.25

Calculating the Mean $\mu\mu$: $E(X) = \Sigma (xi \boxtimes P(X=xi)) = 0 \times 0.25 + 1 \times 0.5 + 2 \times 0.25 = 0 + 0.5 + 0.5 = 1$

Calculating the Variance $\sigma 2\sigma 2$:

 $\sigma 2 = E(X2) - [E(X)]2$ $E(X2) = \Sigma (xi2 \square P(X=xi)) = 02 \times 0.25 + 12 \times 0.5 + 22 \times 0.25 = 0 + 0.5 + 1 = 1.5$ $\sigma 2=1.5-(1)2=1.5-1=0.5$ $\sigma = 0.5 \approx 0.7071$

Problem 3: Expected Values Involving Random Variable

- 1. Part (a): E[2X-4]
 - Calculation:
 - *E*[2*X*-4]=2*E*[*X*]-4=2(1)-4=2-4=-2
 - Conclusion: • E[2X-4]=-2
- 2. Part (b): E[X2]
 - We know E[X]=1 but we need E[X2] • Recall that var(X)=E[X2]-(E[X])2
 - Given var(X)=4 and E(X)=1
- 4=E[X2]-(1)2\(E[X2]=4+1=5 3. Part (c): E[(2X-4)2]E[(2X-4)2]
 - (2X-4)2=4X2-16X+16 • E[4X2-16X+16]
 - E[4X2-16X+16]=4(5)-16(1)+16=20-16+16=20

Problem 4: 1. Part 1

 $P(X=x)=y \Sigma P(X=x,Y=y)$

• For X=0 • P(X=0)=P(X=0,Y=0)+P(X=0,Y=1)=.

- For X=1 • P(X=1)=P(X=1,Y=0)+P(X=1,Y=1)=0.10+0.40=0.50

$P(Y=y)=x \sum P(X=x,Y=y)$ • For Y=0

- P(Y=0)=P(X=0,Y=0)+P(X=1,Y=0)=0.45+0.10=0.55
- For Y=1 • P(Y=1)=P(X=0,Y=1)+P(X=1,Y=1)=0.05+0.40=0.45
- 2. Part (ii): Are X and Y Independent?

 $P(X=x,Y=y)=P(X=x) \ P(Y=y)$ for all x,y

Two random variables X and Y are independent if:

P(X=0,Y=0)=0.45

 $P(X=0) \times P(Y=0) = 0.50 \times 0.55 = 0.275$

3. Part (iii): Find the Mean and Variance of X

Since $0.45 \neq 0.2750$ X and Y are not independent.

 $E[X]=x \sum x \mathbb{Z}P(X=x)$

 $E[X] = 0 \times 0.50 + 1 \times 0.50 = 0 + 0.50 = 0.50$

 $E[X2]=x \sum x2 P(X=x)$

Var(X)=E[X2]-(E[X])2

 $E[X2] = 02 \times 0.50 + 12 \times 0.50 = 0 + 0.50 = 0.50$

Var(X)=0.50-(0.50)2=0.50-0.25=0.25

- 4. Part (iv): Find the Mean and Variance of Y
 - E[Y]=0.45*E*[Y]=0.45, Var(Y)=0.2475Var(Y)=0.2475