

Midterm Review

Finding Candidate keys

- $R = \{A, B, C, D, E, F, G, H\}$

- $F = \{ CH \rightarrow G, \rightarrow$
 - $A \rightarrow BC,$
 - $B \rightarrow CFH,$
 - $E \rightarrow A,$
 - $F \rightarrow EG\}$

1. Start with **all** the attributes not present on the RHS = $\{D\}$

2. Calculate closure of $\{D\}$ and all $\{DX\}$

- $\{D\} = D$
- $\{DA\} = ADBC FHEG = \text{candidate key}$
- $\{DB\} = DBC FHEGA = \text{candidate key}$
- $\{DC\} = DC$
- $\{DE\} = DEA$ stop, DA already a candidate key thus we know DE = candidate key
- $\{DF\} = DFE$ stop, DE already a candidate key thus we know DF = candidate key

3. **Candidate Keys** = $\{DA, DB, DE, DF\} = 4$ possibilities

Finding Canonical(Minimal) Cover

1. Decompose all FDs in **standard form**

- i.e. only one attribute on the RHS

2. Check LHS for **Redundant Attributes**:

- Check FD's with attributes on the LHS for redundant

- for each FD $AB \twoheadrightarrow C$ in G , check if A or B on the LHS is redundant

- Can A be removed from $AB \twoheadrightarrow C$?

- Check $A \twoheadrightarrow C$
- if $C \twoheadrightarrow A$ then A is **Redundant**
- then A can be removed from $AB \twoheadrightarrow C$

- Can B be removed from $AB \twoheadrightarrow C$?

- Check $B \twoheadrightarrow C$
- if $C \twoheadrightarrow B$ then B is **Redundant**
- then B can be removed from $AB \twoheadrightarrow C$

3. Remove **Redundant FD's**:

- Remove each FD one at a time, and check for the closure of F with it removed. If the result can be achieved without the FD it is redundant.

- $(G - \{X \twoheadrightarrow A\}) \twoheadrightarrow F$?

- For every FD $X \twoheadrightarrow A$ in G

- Remove $\{X \twoheadrightarrow A\}$ from G ; call the result G'
- Compute X^+ under G'
- If $A \in X^+$ under G' , then $X \twoheadrightarrow A$ is redundant and hence remove $X \twoheadrightarrow A$ from G .

1NF

- No attribute is allowed to be composite or multi valued

Example:

The following relation is **not** in 1NF: Student (SID, SName, {(CourseId, CourseName, Grade)})

2NF

- It is in 1NF

2. Every non-prime attribute of relation is fully functionally dependent on the primary key

For each non-key attribute, ask:

If I knew the value for part of the Primary-Key, could I tell what the value for a non-key attribute would be?

Example:

Inventory (Item, Supplier, Cost, SupplierAddress)

If I know just Item, can I find out SupplierAddress? NO




If I know just Supplier, can I find out SupplierAddress? YES

SupplierAddress is NOT fully functionally dependent upon the ENTIRE Primary-Key  NOT 2NF

3NF




One of the 3 must be met for every FD $X \twoheadrightarrow A$ 

Need to compute candidate keys in order to check!

1. $X \twoheadrightarrow A$ is a **trivial** FD ($A \twoheadrightarrow X$ ex: $AB \twoheadrightarrow A$)  
2. **LHS** is a superkey (i.e. a key is contained in **LHS**)
3. **RHS** is part of any key of **R** 

BCNF


One of the 3 must be met for every FD $X \twoheadrightarrow A$ 

1. $X \twoheadrightarrow A$ is a **trivial** FD ($A \twoheadrightarrow X$ ex: $AB \twoheadrightarrow A$)  
2. **X** is a superkey 
3. **RHS** is part of any key of **R**

BCNF can always obtain **lossless-join** decomposition

BCNF is not always **dependency-preserving**

Synthetic 3NF Decomposition

1. Compute the canonical cover F^+ 
2. Create relations
3. Check if at least one of the keys exists in the above relations
4. Add an extra relation containing those attributes that form any key of **R**

Example:

$R = \{A, B, C, D, E, F, G, H\}$

$F = \{CD \rightarrow A, EC \rightarrow H, GH \rightarrow B, AB, C \rightarrow D, EG \rightarrow A, H \rightarrow B, BE \rightarrow CD, EC \rightarrow B\}$

Candidate Keys = $\{BEFG, CEFG, EFGH\}$

1. $F_r = \{C \rightarrow AD, EC \rightarrow H, GH \rightarrow A, EG \rightarrow A, H \rightarrow B, BE \rightarrow C\}$

2. Create the relations:

R	F
$R_r = \{A, C, D\}$	$F_r = \{C \rightarrow AD\}$
$R_r = \{E, C, H\}$	$F_r = \{EC \rightarrow H\}$
$R_r = \{A, G, H\}$	$F_r = \{GH \rightarrow A\}$
$R_r = \{A, E, G\}$	$F_r = \{EG \rightarrow A\}$
$R_r = \{B, H\}$	$F_r = \{H \rightarrow B\}$
$R_r = \{B, C, E\}$	$F_r = \{BE \rightarrow C\}$

3. Check if at least one of the keys $\{BEFG, CEFG, EFGH\}$ exists in the above relations.
Since none of these keys is in the relations, this decomposition is **not lossless**.

4. add an extra relation containing those attributes that form any key of R:

R	F
$R_r = \{B, E, F, G\}$	$F_r = \{\}$

The relation schema is now **lossless** as well as **dependency preserving**.

Is R in 3NF ?

R = { A, B, C, D, E, F, G, H }

F = { CD → A, EC → H, GH → B, AB → C, D → EG, A → H, B → BE, CD → EC, EC → B }

Candidate Keys = { BEFG, CEFG, EFGH }

R is **NOT** in **3NF**, because CD → A violates the 3NF requirements

- 1. CD → A is not trivial FD
- 2. CD is not a superkey & CD is not a key
- 3. A is not part of any key of R either

Is Dependency is Preserved ?

Given a decomposed set of relations and FD's $R_1, R_2 \dots R_n$ and $F_1, F_2 \dots F_n$.

Compute $\{X\}^+$ for the original **R** under the original FD's and check if $\{X\}^+ \subseteq \{X\}^+$

Example:

R = (A, B, C, D)

F = { A → B, B → C, C → D }

Decomposed into:

R	F
$R_1 = \{A, B\}$	$F_1 = A \rightarrow B$
$R_2 = \{A, C, D\}$	$F_2 = C \rightarrow D, A \rightarrow D, A \rightarrow C$

Is the decomposition **R** = {R1, R2} dependency-preserving?

- Check if $A \rightarrow B$ is preserved

Compute A^+ under $\{A \rightarrow B\} \cup \{C \rightarrow D, A \rightarrow D, A \rightarrow C\}$
 $A^+ = \{ A, B, C, D \}$

 B A ? Yes

 A B is **preserved**

- Check if B  C is preserved

Compute B^+ under $\{ B \text{  C \} \cup \{ C \text{  D, A \text{  D, A \text{  B \}$

$B^+ = \{ B \}$

C  B ? NO

 B C is **not preserved**

Lossy Decomposition ?

The decompositio of relation R into R1 and R2 is **lossy** when the join of R1 and R2 does not yield the same relation as in R.