

SOEN 321

Exercise 1

(Although these questions will be solved with you during the tutorial, you should try solving them by yourself before the tutorial)

Prob. 1 Consider the affine cipher in which the ciphertext c is given by $C = aP + b \pmod{26}$. The cryptanalyst observed the following plaintext/ciphertext pairs (p,c) : $(1,10)$ and $(2,17)$.

1. Recover the key (a,b) used in the encryption system above.
2. What is the ciphertext corresponding to the plaintext $p=3$?

Prob. 2 Consider the Hill cipher in which the ciphertext is related to the plaintext using the form

$$\begin{pmatrix} c_1 & c_2 \end{pmatrix} = \begin{pmatrix} p_1 & p_2 \end{pmatrix} \begin{pmatrix} k_1 & k_2 \\ k_3 & k_4 \end{pmatrix} \pmod{26}$$

The cryptanalyst observed the following plaintext/ciphertext pairs $(p_1 \ p_2)/(c_1 \ c_2)$: $(1 \ 2)/(16 \ 23)$ and $(3 \ 3)/(1 \ 16)$.

Determine the key corresponding to this system.