

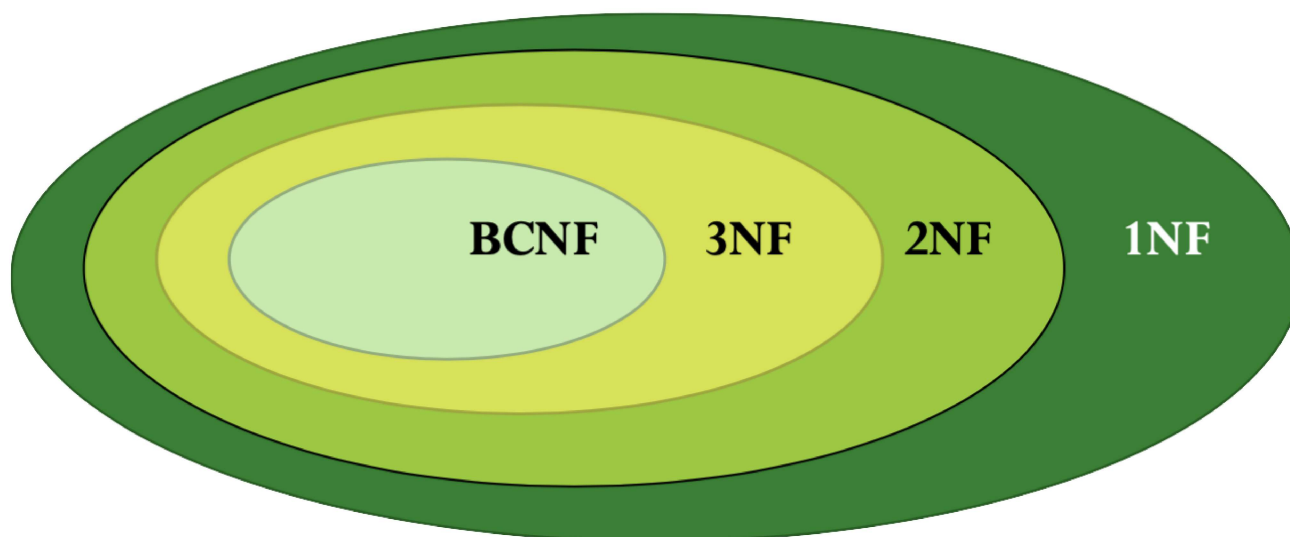
LECTURE 6 - NORMALIZATION

Normal Forms

We normalize to get rid of “extra” functional dependencies that causes redundancy and anomalies.

Normal Forms:

- **First normal form (1NF)**: components of tuples must be atomic
- **Second normal form (2NF)**: transitive FD's still allowed, no FD whose LHS is a proper subset of a key
- **Third normal form (3NF)**: LHS is superkey or RHS key subset
- **Boyce-Codd normal form (BCNF)**: LHS is superkey



Each normal form gets a little stricter and gets rid of more anomalies.

1NF

1. No attribute is allowed to be composite or multi valued

Example:

The following relation is **not** in 1NF: Student (SID, SName, {(CourseId, CouseName, Grade)})

2NF

1. It is in 1NF
2. Every non-prime attribute of relation is fully functionally dependent on the primary key

For each non-key attribute, ask:

If I knew the value for part of the Primary-Key, could I tell what the value for a non-key attribute would be?

Example:

Inventory (Item, Supplier, Cost, SupplierAddress)

If I know just Item, can I find out SupplierAddress? NO




If I know just Supplier, can I find out SupplierAddress? YES

SupplierAddress is NOT fully functionally dependent upon the ENTIRE Primary-Key  **NOT 2NF**

3NF




One of the 3 must be met for every FD $X \twoheadrightarrow A$  **A:**

Need to compute candidate keys in order to check!

1. $X \twoheadrightarrow A$ is a **trivial** FD ($A \twoheadrightarrow X$ ex: $AB \twoheadrightarrow A$)   
2. **LHS** is a superkey (i.e. a key is contained in **LHS**)
3. **RHS** is part of any key of **R**

BCNF


One of the 3 must be met for every FD $X \twoheadrightarrow A$  **A:**

1. $X \twoheadrightarrow A$ is a **trivial** FD ($A \twoheadrightarrow X$ ex: $AB \twoheadrightarrow A$)   
2. **X** is a superkey
3. **RHS** is part of any key of **R**

BCNF can always obtain **lossless-join** decomposition

BCNF is not always **dependency-preserving**

Synthetic 3NF Decomposition

1. Compute the canonical cover F^+ 
2. Create relations
3. Check if at least one of the keys exists in the above relations
4. Add an extra relation containing those attributes that form any key of **R**

Example:

$R = \{A, B, C, D, E, F, G, H\}$

$F = \{CD \rightarrow A, EC \rightarrow H, GH \rightarrow B, AB, C \rightarrow D, EG \rightarrow A, H \rightarrow B, BE \rightarrow CD, EC \rightarrow B\}$

Candidate Keys = $\{BEFG, CEFG, EFGH\}$

1. $F_1 = \{C \rightarrow AD, EC \rightarrow H, GH \rightarrow A, EG \rightarrow A, H \rightarrow B, BE \rightarrow C\}$

2. Create the relations:

R	F
$R_1 = \{A, C, D\}$	$F_1 = \{C \rightarrow AD\}$
$R_2 = \{E, C, H\}$	$F_2 = \{EC \rightarrow H\}$
$R_3 = \{A, G, H\}$	$F_3 = \{GH \rightarrow A\}$
$R_4 = \{A, E, G\}$	$F_4 = \{EG \rightarrow A\}$
$R_5 = \{B, H\}$	$F_5 = \{H \rightarrow B\}$
$R_6 = \{B, C, E\}$	$F_6 = \{BE \rightarrow C\}$

3. Check if at least one of the keys $\{BEFG, CEFG, EFGH\}$ exists in the above relations.
Since none of these keys is in the relations, this decomposition is **not lossless**.

4. add an extra relation containing those attributes that form any key of R:

R	F
$R_7 = \{B, E, F, G\}$	$F_7 = \{\}$

The relation schema is now **lossless** as well as **dependency preserving**.

Is R in 3NF or BCNF ?

$R = \{A, B, C, D, E, F, G, H\}$

$F = \{CD \twoheadrightarrow A, EC \twoheadrightarrow H, GH \twoheadrightarrow B, AB, C \twoheadrightarrow D, EG \twoheadrightarrow A, H \twoheadrightarrow B, BE \twoheadrightarrow CD, EC \twoheadrightarrow B\}$

Is Dependency is Preserved ?

Given a decomposed set of relations and FD's $R^1, R^2 \dots R^n$ and $F^1, F^2 \dots F^n$.

Compute $\{X\}^+$ for the original X under original FD's and check if $A \twoheadrightarrow \{X\}$

Example:

$R = (A, B, C, D)$

$F = \{A \twoheadrightarrow B, B \twoheadrightarrow C, C \twoheadrightarrow D\}$

Decomposed into:

R	F
$R^1 = \{A, B\}$	$F^1 = A \twoheadrightarrow B$
$R^2 = \{A, C, D\}$	$F^2 = C \twoheadrightarrow D, A \twoheadrightarrow D, A \twoheadrightarrow C$

Is the decomposition $R = \{R1, R2\}$ dependency-preserving?

- Check if $A \twoheadrightarrow B$ is preserved

Compute A^+ under $\{A \twoheadrightarrow B\} \cup \{C \twoheadrightarrow D, A \twoheadrightarrow D, A \twoheadrightarrow C\}$

$A^+ = \{A, B, C, D\}$

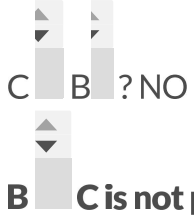
$B \twoheadrightarrow A^+$? Yes

$A \twoheadrightarrow B$ is **preserved**

- Check if $B \twoheadrightarrow C$ is preserved

Compute B^+ under $\{B \twoheadrightarrow C\} \cup \{C \twoheadrightarrow D, A \twoheadrightarrow D, A \twoheadrightarrow B\}$

$B^+ = \{B\}$



Lossy Decomposition ?

The decompositio of relation R into R1 and R2 is lossy when the join of R1 and R2 does not yield the same relation as in R.