Concordia University

Department of Computer Science and Software Engineering COMP 335: Introduction to Theoretical Computer Science Fall 2017

A Solution to Assignment 1

Evaluation: 30 pts

(3% of your final grade)

Due date and time: Thursday September 28th 2017 at 23:59

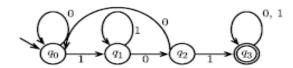
Answer#1

- (a) Accepts the language $(1+01)^*$, that is every string over $\{0,1\}$ in which every 0, if any, is followed by a 1.
- (b) Accepts strings in which no a appears or aa appears exactly once as a substring.
- (c) Accepts every string that starts and ends with the same symbol.
- (d) Accepts every string in which every run of a's, if any, is of length 2 or more.
- (e) Accepts $\lambda + (a+b)(ba+bb)*(\lambda +b) + a(ba+aa)*(\lambda+a+b)$

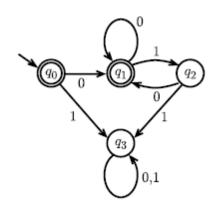
Answer#2

a)

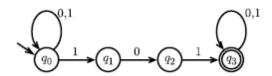
(1)



(2)

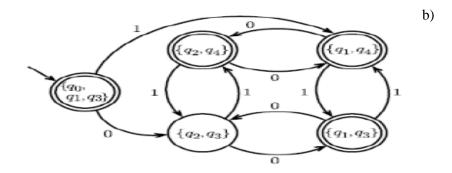


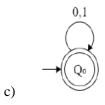
b)



Answer#3

a) Strings that have an even number of 0's or an odd number of 1's.





Answer#4

$$\begin{split} &M_1 = (\{q_1,\,q_2,\,q_3\},\,\{a,b\},\,\delta_1,\,q_1,\{q_2\}).\\ &M_2 = (\{q_1,\,q_2,\,q_3,\,q_4\},\,\{a,b\},\,\delta_2,\,q_1,\{q_1,\,q_4\}). \end{split}$$

The transition tables are:

δ_1	a	b
q_1	\mathbf{q}_2	q_1
q_2	q_3	q_3
\mathbf{q}_3	q_2	q_1

Initial state :q₁: Final state :q₂

δ_2	a	b
q_1	q_1	q_2
q_2	\mathbf{q}_3	q_4
q_3	q_2	q_1
q_4	\mathbf{q}_3	q_4

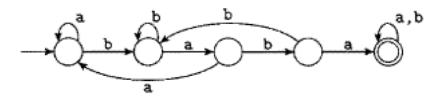
Initial state :q₁: Final state :q₄

Answer#5

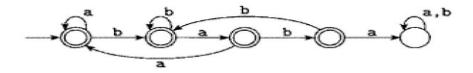
a) The left-hand DFA recognizes $\{w \mid w \text{ contains ab}\}$. The right-hand DFA recognizes its complements, $\{w \mid w \text{ doesn't contain ab}\}$.



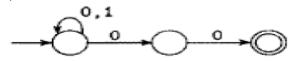
b) This DFA recognizes {w | w contains baba}.



This DFA recognizes {w | w does not contains baba}.



Answer#6



b)

