



## ENGR 213

### Applied Ordinary Differential Equations

### Second Mid Term Exam

March 12<sup>th</sup> 2017

**Student Name:** \_\_\_\_\_

**Student ID Number:** \_\_\_\_\_

**ENGR 213 Section:** \_\_\_\_\_

**Course Given BY:** \_\_\_\_\_

- Exam is closed book close notes.
- No use of any electronic devices.
- Use only the approved calculator.
- Write your answers in the provided space.

Q1	
Q2	
Q3	
Q4	
Q5	
Total	

**Problem#1**

Write the number  $(3+6i) + (4-i)(3+5i) + \frac{1}{2-i}$  in the form  $a+bi$ .

**Solution:**

**Problem#2**

Verify that  $y_1 = e^{5x}$  and  $y_2 = e^{-7x}$  are form a fundamental set of solutions of the differential equation  $y'' + 2y' - 35y = 0$  on the interval  $(-\infty, \infty)$ . Write the form of the general solution.

**Solution:**

**Problem#3****Solution:**

(a) Write the characteristic equation and the general solution of the differential equation:

$$y^{(6)} - 13y^{(5)} + 70y^{(4)} - 198y^{(3)} + 308y'' - 248y' + 80y = 0.$$

$y^{(k)}$  is the  $k$ -th derivative of  $y$ . For Your convenience, the roots of the characteristic equation are: 1, 2, 2, 2,  $3 + i$ ,  $3 - i$ . You do not have to check this.

(b) Find the general solution of the differential equation:  $x^2 y'' - 7xy' + 16y = 0$ , given one solution  $y_1 = x^4$ .

**Solution:**

**Problem#4**

Using the method of undetermined coefficients, solve the initial value problem

$$y'' + y' - 2y = (6x + 2)e^{-x}; y(0) = 0; y'(0) = 0.$$

**Solution:**

**Problem#5**

Solve the following differential Equation  $y'' + (3/x) y' + (5/x^2) y = 0$

**Solution:**