## MATH 209/4 all sections except EC: - Fundamental Mathematics II

## Midterm - March 3, 2018 (1h30min) Only approved calculators are permitted.

## MARKS

[5] 1. Let  $g(x) = 2 - 13x^3$ . Work out the following in detail:  $\lim_{a \to 0} \frac{[g(x+a) - g(x)]}{a}$ 

- [10] 2. (a) If  $f(x) = -7x^{25} 8$ , find f'(x). Do not simplify.
  - (b) If  $f(x) = (5x^8 2)[ln(x^2) + 5]$ , find f'(x). Do not simplify.
  - (c) Find g'(x) if  $g(x) = \frac{2x^3 e^x}{|e^{3x} + \ln(x)|}$ . Do not simplify.
  - (d) Find the value of dy if  $y = x^4 + 3$ , x = 3 and the change in x is 0.2.
- [7] 3. A sum of seven thousand dollars is invested for eight years. Assume that interest is compounded continuously and determine the annual rate of return in the following three cases:
  - (a) the value after 8 years is nineteen thousand dollars.
  - (b) the value after 8 years is seven thousand dollars.
  - (c) the value after 8 years is six thousand dollars.
- [8] 4. The cost of printing x books is given by the function C(x) = 10,000 + 15x.
  - (a) Find the average cost per unit if 100 books are printed.
  - (b) Find the marginal average cost when 100 books are printed and interpret the results.
  - (c) Use (a) and (b) to estimate the average cost per book if 101 books are printed.
- [7] 5. Sales of x units of a product are found to be given by the function  $S(x) = 3x^4 + x^2 5$ . At what rate are sales changing when x = 4?
- [8] 6. A point is moving along the negative x axis at a constant rate of 5 units per second. Find the rate of change of its distance from (1,1) when x=-3.
- [15] 7. (a) Give an example of a function f whose derivative equals 1 when evaluated at x = 2 and equals 4 when evaluated at x = 3.
  - (b) Prove or disprove the following statement. There is a polynomial of degree 2 which has a derivative and is a derivative.
    - (c) Without using the quotient rule find the derivative of the function  $\ln(\frac{x+3}{x-7})$