

Oct 2014

You can only use the faculty approved calculator with sticker.
Pens, pencils, erasers, and straight edges only. No crib sheets. NO CELL PHONES.
If you have a difficulty you may try making REASONABLE assumptions. State the assumption and how that assumption limits your answer. Justify your responses.

- 1) Four married couples have bought 8 seats in the same row for a concert. In how many ways can they be seated:
 - a) With no restrictions?
 - b) If each couple is to sit together?
 - c) If all the men sit together to the right of all the women?
- 2) In an engineering conference, 20% of the attendees are electrical engineers. Of these electrical engineers, 75% gave talks. Of those who are not electrical engineers, 20% gave talks. What is the probability that a randomly selected lecturer is an electrical engineers?
- 3) The cdf of X is as follows:

$$F(x) = \begin{cases} 0.00 & x < 1 \\ 0.20 & 1 \leq x < 3 \\ 0.40 & 3 \leq x < 4 \\ 0.45 & 4 \leq x < 6 \\ 0.7 & 6 \leq x < 12 \\ 1.0 & x \geq 12 \end{cases}$$

- a) Find the probability mass function of X. $f(x)$
 - b) Graph the pmf of X
 - c) Using just the cdf, compute the probability that X is between 3 and 6, inclusive
 - d) Find the expectation and the variance of X.
 - e) If another random variable $Y=X+1$ is formed, find the $E[Y]$.
- 4) Identical computer components are shipped in boxes of 5. About 15% of components have defects. Defects on components are independent of one another and the boxes are tested in a random order.
 - a) What is the probability that a randomly selected box has only non-defective components?
 - b) What is the expected number of non-defective components?
 - c) What is the standard deviation of the number of non-defective components?
 - d) What is the probability that at least 8 of randomly selected 10 boxes have only non-defective components?
 - e) What is the distribution of the number of boxes tested until a box without defective components is found? What are its parameters?
 - 5) Vehicles pass through a junction on a busy road at an average rate of 300 per hour.
 - a) Find the probability that none passes in a given minute.
 - b) What is the expected number passing in two minutes?
 - c) Find the probability that this expected number actually pass through in a given two-minute period.