

1. (1 point) Consider the function $f(x) = 3x^3 - 4x$ on the interval $[-5, 5]$. Find the average or mean slope of the function on this interval. _____

By the Mean Value Theorem, we know there exists at least one c in the open interval $(-5, 5)$ such that $f'(c)$ is equal to this mean slope.

For this problem, there are two values of c that work. The smaller one is _____ and the larger one is _____

Correct Answers:

- 71
- -2.88675134594813
- 2.88675134594813

2. (1 point) Consider the function $f(x) = \frac{1}{x}$ on the interval $[1, 10]$.

(A) Find the average or mean slope of the function on this interval.

Average Slope = _____

(B) By the Mean Value Theorem, we know there exists a c in the open interval $(1, 10)$ such that $f'(c)$ is equal to this mean slope. Find all values of c that work and list them (separated by commas) in the box below.

List of values: _____

Correct Answers:

- -0.1
- 3.16227766016838

3. (1 point) Consider the function $f(x) = 10\sqrt{x} + 6$ on the interval $[2, 10]$.

(A) Find the average or mean slope of the function on this interval.

Average Slope = _____

(B) By the Mean Value Theorem, we know there exists at least one c in the open interval $(2, 10)$ such that $f'(c)$ is equal to this mean slope. Find all values of c that work and list them (separated by commas) in the box below.

List of values: _____

Correct Answers:

- 2.18508012224411
- 5.23606797749979

4. (1 point) Consider the function $f(x) = 1 - 4x^2$ on the interval $[-4, 8]$.

(A) Find the average or mean slope of the function on this interval, i.e.

$$\frac{f(8) - f(-4)}{8 - (-4)} = \underline{\hspace{2cm}}$$

(B) By the Mean Value Theorem, we know there exists a c in the open interval $(-4, 8)$ such that $f'(c)$ is equal to this mean slope. For this problem, there is only one c that works. Find it.

$c = \underline{\hspace{2cm}}$

Correct Answers:

- -16
- 2

5. (1 point)

Find the limit. Use l'Hospital's Rule if appropriate. Use INF to represent positive infinity, NINF for negative infinity, and D for the limit does not exist.

$$\lim_{x \rightarrow (\pi/2)^+} \frac{5 \cos x}{1 - \sin x} = \underline{\hspace{2cm}}$$

Correct Answers:

- NINF

6. (1 point)

Find the limit. Use l'Hospital's Rule if appropriate. Use INF to represent positive infinity, NINF for negative infinity, and D for the limit does not exist.

$$\lim_{x \rightarrow 0} \frac{7x + 7 \sin x}{6x + 6 \cos x} = \underline{\hspace{2cm}}$$

Correct Answers:

- 0

7. (1 point)

Find the limit. Use l'Hospital's Rule if appropriate. Use INF to represent positive infinity, NINF for negative infinity, and D for the limit does not exist.

$$\lim_{x \rightarrow -\infty} 2x^2 e^x = \underline{\hspace{2cm}}$$

Correct Answers:

- 0

8. (1 point) Evaluate the following limit. Enter -I if your answer is $-\infty$, enter I if your answer is ∞ , and enter DNE if the limit does not exist.

$$\lim_{x \rightarrow 0} \left(\frac{1}{2x} - \frac{1}{e^{2x} - 1} \right) = \underline{\hspace{2cm}}$$

Correct Answers:

- 0.5

9. (1 point) Compute the following limits using l'Hôpital's rule if appropriate. Use INF to denote ∞ and MINF to denote $-\infty$.

$$\lim_{x \rightarrow 0} \frac{1 - \cos(8x)}{1 - \cos(5x)} = \underline{\hspace{2cm}}$$

$$\lim_{x \rightarrow 1} \frac{6^x - 5^x - 1}{x^2 - 1} = \underline{\hspace{2cm}}$$

Correct Answers:

- 2.56

- 1.35168362659891

10. (1 point) Find the following limits, using l'Hôpital's rule if appropriate

$$\lim_{x \rightarrow \infty} \frac{\arctan(x^5)}{x^4} = \underline{\hspace{2cm}}$$

$$\lim_{x \rightarrow 0^+} \sqrt[4]{x} \ln(x) = \underline{\hspace{2cm}}$$

Correct Answers:

- 0
- 0