

**Department of Computer Science and Software Engineering**  
**Comp 232 Mathematics for Computer Science    Fall 2020**  
**Assignment 3                      Due : November 14, 2020**

1. a) Use set identities to prove that  $A \cup (B - A) = A \cup B$   
  
b) Use set identities to prove that  $A \cap (B - A) = \phi$   
  
c) Use set identities to prove that  $\overline{A \cup (B \cap C)} = (\bar{C} \cup \bar{B}) \cap \bar{A}$
2. a) Prove or give a counterexample for the statement that if A and B are sets, then  $\mathcal{P}(A \cap B) = \mathcal{P}(A) \cap \mathcal{P}(B)$ .  
  
b) Let  $A = \{0, 1, \phi\}$ . List the elements of  $\mathcal{P}(A)$ .
3. Give an example of a function  $f: Z \rightarrow Z^+$  that is  
a) one to one, but not onto  
b) onto, but not one to one
4. Give a proof by cases that  $\lfloor 4x \rfloor = \lfloor x \rfloor + \lfloor x + 1/4 \rfloor + \lfloor x + 1/2 \rfloor + \lfloor x + 3/4 \rfloor$
5. Give an example of two uncountable sets A and B such that  $A - B$  is  
a) finite  
b) countably infinite  
c) uncountable

6. Use the Euclidean algorithm to find the following :

a)  $\gcd(985, 408)$

b)  $\gcd(7953, 5822)$

c)  $\gcd(38785, 16768)$

7. a) Find the value of  $10! \bmod 11$

b) Find the value of  $12! \bmod 13$

c) Make a conjecture about the value of  $(p-1)! \bmod p$ , where  $p$  is a prime.

8. Prove that for any positive integer  $n$ ,  $\gcd(7n+2, 4n+1) = 1$

9. Show that if  $a, b, c$ , and  $d$  are integers and  $a \neq 0$ , that if  $a \mid c$  and  $b \mid d$  then  $ab \mid cd$ .

10. Prove that if  $n$  is an odd positive integer then  $n^2 \equiv 1 \pmod{8}$ .