

SOEN331: Introduction to Formal Methods for Software Engineering

Assignment 4: Z Specifications

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$[Product, OrderId]$

$Order == \{order : \text{bag } Product \mid order \neq \emptyset\}$

$OrderState ::= pending \mid invoiced$

$Report ::= oder_not_pending \mid not_enough_stock \mid no_more_ids$

$Stock$ $stock : \text{bag } Product$
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$OrderInvoices$ $orders : OrderId \rightarrow OrderState$ $orderStatus : OrderId \rightarrow OrderState$
$\text{dom } orders = \text{dom } orderStatus$

$State$ $Stock$ $OrderInvoices$ $newids : \mathbb{P} OrderId$
$\text{dom } orders \cap newids = \emptyset$

$\Delta State$
$State$ $State'$
$newids' = newids \setminus \text{dom } orders'$

$InitState$
$State'$
$stock' = \emptyset$ $orders' = \emptyset$ $newids' = OrderId$

$NewOrder$
$\Delta State$ $order? : Order$ $id! : OrderId$
$id! \in newids$ $orders' = orders \cup \{id! \mapsto order?\}$ $orderStatus(id!) = pending$ $stock = stock'$

$InvoiceOrder$
$\Delta State$ $id? : OrderId$
$id? \in \text{dom } orders$ $orders(id?) \sqsubseteq stock$ $orderStatus(id?) = pending$ $stock' = stock \sqcup orders(id?)$ $orderStatus' = orderStatus \oplus \{id? \mapsto invoiced\}$ $orders = orders'$

<i>InvoiceError</i>
$\exists \text{State}$
$id? : \text{OrderId}$
$error! : \text{Report}$
$orderStatus(id?) \neq \text{pending}$
$error! = \text{order_not_pending}$

<i>StockError</i>
$\exists \text{State}$
$id? : \text{OrderId}$
$error! : \text{report}$
$\neg (\text{orders}(id?) \sqsubseteq \text{stock})$
$error! = \text{not_enough_stock}$

<i>InvoiceOrderOp</i>
$\text{InvoiceOrder} \vee \text{InvoiceError} \vee \text{StockError}$