CONCORDIA UNIVERSITY

Department of Mathematics & Statistics

Course	Number	Section(s)	
Mathematics	208/2		All
Examination	Date	Time	Pages
Midterm	November 2015	1 Hour 30 minutes	2
Instructors		Course Ex	aminer
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FORMULAE:

$$A = P(1+i)^n$$
, $A = Pe^{rt}$, $FV = PMT \frac{(1+i)^n - 1}{i}$, $PV = PMT \frac{1 - (1+i)^{-n}}{i}$

Special Instructions:

- > Answer all questions.
- ▷ Only approved calculators are allowed.

MARKS

- [5+5] 1. A manufacturer has been selling 1200 television sets a week at \$480 each. A market survey indicates that for each \$30 rebate offered to a buyer, the number of sets sold will increase by 300 per week.
 - (A) Find the demand function p(x), where x is the number of the television sets sold per week and p(x) is the price of one set.
 - (B) How large rebate should the company offer to a buyer, in order to maximize its revenue?
- $[2\frac{1}{2} \times 4]$ 2. Solve for x in the following equations:

(A)
$$7^{x^2+x-9} = 343^{-3x+5}$$

(B)
$$\log_2(x-3) + \log_2(2x-4) = 2$$

(C)
$$e^{x^2-2x+5} = \left(\frac{1}{\sqrt[4]{e}}\right)^{-8x^2+12x+28}$$

(D)
$$\log_4(x^2 + x + 4) = 2$$

[(3+4)+3] 3.

- (A) If the 8th and 19th terms of an arithmetic sequence are 9 and -24 respectively, find the 50th term and the sum of the first 61 terms of the sequence.
- (B) Find the sum of the entire infinite geometric sequence $2, -\frac{1}{2}, \frac{1}{8}, \dots$, if it exists.
- [5+5] 4. A radio commercial for a loan company states: "You only pay \$0.29 a day for each \$500 borrowed." If you borrow \$1,500 for 120 days, what amount will you repay, and what annual interest rate is the company actually charging?
- [5+5] 5. A bond issue is approved for building a marina in a city. The city is required to make regular payments every 3 months into a sinking fund paying 5.4% compounded quarterly. At the end of 10 years, the bond obligation will be retired with a cost of \$5,000,000.
 - (A) What should each payment be?
 - (B) How much interest is earned during the 10th year?
- [5+5] 6. Consider a \$21,281.27 loan for 7 years at 8% interest compounded quarterly and a payment of \$1000 per quarter-year.
 - (A) Compute the unpaid balance after 5 years.
 - (B) How much interest is paid during the fifth year?