

To get access to this week's code use the following link: [https://classroom.github.com/a/x9\\_wEY4G](https://classroom.github.com/a/x9_wEY4G)

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**General constraints for submissions:** Please adhere to these rules to make our and your life easier! We will deduct points if you fail to do so.

- Your code should work with *Python 3.8*.
- You should only fill out the *TODO-gaps* and not change anything else in the code.
- Add comments to your code, to help us understand your solution.
- Your code should adhere to the [PEP8](#) style guide. We allow line lengths of up to 120.
- While working on the exercise, push all commits to the `dev` branch (details in assignment 1). Only push your final results to the `master` branch, where they will be automatically tested in the cloud. If you push to `master` more than 3 times per exercise, we will deduct points.
- All provided unit tests have to pass: In your *GitHub* repository navigate to *Actions* → your last commit → Autograding → education/autograding to see which tests have passed. The points in autograding only show the number of tests passed and have nothing to do with the points you get for the exercise.
- `for` loops can be slow in Python, use vectorized `numpy` operations wherever possible (see assignment 1 for an example).
- Submit a *single PDF* named `submission.pdf` with the answers and solution paths to all pen and paper questions in the exercise. You can use [Latex](#) with the student template (provided in exercise 1 / ILIAS) or do it by hand.
- Please help us to improve the exercises by filling out and submitting the `feedback.md` file.
- We do not tolerate plagiarism. If you copy from other teams or the internet, you will get 0 points. Further action will be taken against repeat offenders!
- Passing the exercises ( $\geq 50\%$ ) is a requirement for passing the course.

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### How to run the exercise and tests

- See the `setup.pdf` in exercise 1 / ILIAS for installation details.
- We always assume you run commands in the *root folder* of the exercise repository.
- If you're using miniconda, don't forget to activate your environment with `conda activate mydlenv`
- Install the required packages with `pip install -r requirements.txt`
- Python files in the *root folder* of the repository contain the scripts to run the code.
- Python files in the `tests/` folder of the repository contain the tests that will be used to check your solution.
- Test everything at once with `python -m pytest`
- Run a single test with `python -m tests.test_something` (replace `something` with the test's name).
- To check your solution for the correct code style, run `pycodestyle --max-line-length 120`.
- The scripts `runtests.sh` (Linux/Mac) or `runtests.bat` (Windows) can be used to run all the tests described above.

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In this course, you will learn about the *foundations* of deep learning. Instead of going in-depth into any particular topic, the lectures will cover a wide variety of deep learning methods and their underlying principles. Similarly, these exercises will *not* train you to be a specialist deep learning practitioner, but rather aim to give you a deeper understanding of the canonical methods, by implementing them yourself and by applying them to some classical benchmark problems.

In this first exercise you will set up teams and learn about git and the workflow for future assignments. You will also do some small exercises to brush up your *linear algebra* and to get familiar with *python* and *numpy*.

At this point you should have worked through the `setup.pdf` and have a working python 3.8 and git installation ready. You should know how to navigate and run commands in the command prompt.

#### 1. [2 points] **Form teams of 3 students**

Exercises have to be completed in teams of up to 3 students. You can use the “Let's Team Up” thread on the ILIAS forum to find team members.

When you have found your partner(s), open the following link [https://classroom.github.com/a/x9\\_wEY4G](https://classroom.github.com/a/x9_wEY4G), create a group (your team name must start with `d12021-`, e.g. `d12021-my-team`) and have both your colleagues join that

group.

This will allow you to clone the template repository in which you can add your solutions to this exercise sheet.

**Note:** Make sure you and your team-mates are happy with each other. We will only allow changing your groups mid semester if you have a very good reason to do so.

## 2. [1 point] Upload your names on GitHub

Add a file called `members.txt` to your repository.

The file should contain the names of all members in the following way:

```
name 1; mail address 1; ILIAS username 1
name 2; mail address 2; ILIAS username 2
name 3; mail address 3; ILIAS username 3
```

If you have fewer members, add fewer lines.

We make use of GitHub Classroom's testing functionality. Essentially, for most exercise sheets we will require you to pass unit tests which are automatically evaluated whenever you push to GitHub. For example, for this exercise we run a test that expects the `members.txt` file to be present and checks if it is filled out correctly (valid emails and ILIAS usernames).

Testing costs build time on our server. It is only enabled when pushing to the `master` branch of your repository. You are only allowed to push to `master` up to 3 times – we will deduct points if you push more than that. Instead, run the tests locally (see “How to run the exercise and tests” above), push on the `dev` branch and only push your final solution to the `master` branch.

Here is how to create the `dev` branch:

- `git pull` to make sure you are up to date.
- `git checkout -b dev` to create the `dev` branch and switch to it.
- `git push --set-upstream origin dev` to connect your local `dev` branch with the repository.

Here is how to switch to the `dev` branch if it has already been created:

- `git pull` to make sure you are up to date.
- `git branch -a` to list all branches, you should see the `dev` branch.
- `git fetch -p` is only needed if you do **not** see the `dev` branch.
- `git checkout dev` to work on the `dev` branch.

Now that you are working on the `dev` branch, upload the file to your repository on *github*. To do this, run the following commands:

- `git pull` to make sure you are up to date.
- `git status` to see what has changed locally.
- `git add .` to add all changes (be careful to not upload the wrong files. If you want to upload only some files, either change the parameters of the `git add` command or change the `.gitignore` file.)
- `git status` again to see what has been added with the last command.
- `git commit -m "update members.txt"` to commit.
- `git push` to upload your changes.

Now, merge the `dev` branch to the `master` branch and push to see the auto-testing in action. This push to `master` does not count towards the maximum 3 pushes you are allowed to do per exercise.

- `git pull` to make sure you are up to date.
- `git checkout master` to switch from the `dev` to the `master` branch.
- `git merge dev` to merge `dev` into `master`. If you get merge conflicts, see e.g. [this link](#) on how to resolve them. Basically you will have to change the files by hand and then add and commit them.
- `git push` to upload the merge.

After uploading, in your repository on github under *Actions* → your last commit → Autograding → education/autograding, you can find out whether your `members.txt` file passed the `test_names` test.

**Note:** You can have as many branches as you want. It *can* make sense to create branches for each person working on the repository and merging them to `dev`, then merging to `master` at the end. However, you can also just all work on `dev` at the same time and merge as needed.

See [this link](#) for an overview of how git branches are used in a professional environment.

### 3. Pen and Paper tasks

Now you'll brush up your linear algebra a little by doing eigendecomposition by hand. Later we will see how we can do the same in python. You should explain how you arrived at your solution and show intermediate results.

If you'd like to review Linear Algebra, we recommend [Khan Academy](#). [The Matrix Cookbook](#) is another useful resource.

Provide your solution as a PDF file. You can use the template tex file we provided you for this.

- 1) [2 points] Calculate the eigendecomposition of the following matrix: (Explicitly write every part of the factorization)

$$A = \begin{bmatrix} 9 & 1 \\ 8 & 7 \end{bmatrix}$$

- 2) [1 1/2 points] Use the eigendecomposition of  $A$  above to show how you can efficiently compute  $A^{10}$  (you don't have to show the final value of the matrix).

- 3) [1 1/2 points] You are given the following matrix:

$$A = \begin{bmatrix} 4 & 8 & 2 \\ 8 & 41 & 24 \\ 2 & 24 & 21 \end{bmatrix}$$

$$\det(A) = 400$$

One of the eigenvalues is 1. Find the other two. **Hint:** You don't have to calculate the eigenvalues from scratch. Use the properties of eigenvalues.

- 4) [1 point] You are given the following matrix:

$$A = \begin{bmatrix} 100 & 100 & 100 \\ 99 & 99 & 102 \\ 98 & 98 & 104 \end{bmatrix}$$

$$\det(A) = 0$$

Find the eigenvalues of  $A$ .

### 4. [1 point] Code Warmup

To solve code exercises, you have to fill in code between the *START TODO* and *END TODO* markers in the code. Before you run any code, make sure you have the correct conda environment activated, and don't forget to install the required packages with `pip install -r requirements.txt`.

**Todo:** In the file `lib/example_file.py`, complete `example_function` by adding

```
return input_variable * 2
```

Execute the command `python example_script.py` to see the function in action.

Run `python -m tests.test_example` to test if the function is implemented correctly.

## 5. Getting to know numpy

### 1) Numpy tensors

You will now play around with some basics of tensor manipulation in *numpy*. The basic object in numpy is an homogeneous multidimensional array. Numpy's array class is called *ndarray*. Here is a quickstart tutorial: <https://numpy.org/devdocs/user/quickstart.html>

**Todo:** Run the script `run_numpy_arrays.py`. We will walk you through its code and output during this exercise.

Let's create two matrices and check their properties.

```
A = np.array(np.arange(4))
B = np.array([-1, 3])
print(f"A (shape: {A.shape}, type: {type(A)}) = {A}")
print(f"B (shape: {B.shape}, type: {type(B)}) = {B}")
```

#### Output:

```
A (shape: (4,), type: <class 'numpy.ndarray'>) = [0 1 2 3]
B (shape: (2,), type: <class 'numpy.ndarray'>) = [-1  3]
```

First, 2 arrays (also called tensors in the context of deep learning) are created. Each numpy tensor has an attribute `numpy.ndarray.shape` which describes the dimensions of the defined tensor. Type, shape and content of the tensors are the first output of the script. Please note how we are using **f-strings** to output variables.

In order to perform matrix multiplication and addition in numpy there are two methods: `numpy.matmul` and `numpy.add`. Please read their respective documentation in numpy before proceeding.

Next, we try to multiply the two tensors with `matmul`.

```
np.matmul(A, B)
```

#### Output:

```
ValueError: matmul: Input operand 1 has a mismatch in its core dimension 0,
with gufunc signature (n?,k),(k,m?)->(n?,m?) (size 2 is different from 4)
```

We get a *ValueError* due to the shape mismatch between the two numpy arrays we want to multiply. In order to deal with different array shapes during arithmetic operations, we can either **reshape** the arrays or **broadcast** the smaller array across the larger one such that they have compatible shapes.

```
C = A.reshape([2, 2])
print(f"C shape: {C.shape}, content:\n{C}")
```

#### Output:

```
C shape: (2, 2), content:
[[0 1]
 [2 3]]
```

Now the matrix multiplication  $CB$  works out.

```
matmul_result = np.matmul(C, B)
print(matmul_result)
```

#### Output:

```
[3 7]
```

When adding  $C$  with shape  $(2, 2)$  and  $B$  with shape  $(2, )$ ,  $B$  will be automatically broadcast to match the shape of  $C$ .

```
print(np.add(C, B))
```

**Output:**

```
[[ -1  4]
 [ 1  6]]
```

The star operator  $*$  will do an element-wise multiplication between the  $C$  and  $B$ . Again,  $B$  will be broadcast to fit.

```
print(C * B)
```

**Output:**

```
[[ 0  3]
 [-2  9]]
```

The function `np.diag` can transform the vector  $B$  shaped  $(2, )$  into a diagonal matrix of shape  $(2, 2)$ .

```
print(np.diag(B))
```

**Output:**

```
[[ -1  0]
 [ 0  3]]
```

For transposing a ndarray use `numpy.transpose` or the method `numpy.ndarray.T`.

```
print(np.transpose(C))
```

**Output:**

```
[[0 2]
 [1 3]]
```

Tensor operations are a central part of the exercises and deep learning in general, so play around with the script to get familiar with them. You could also just start an interactive python session with the command `python` and play around in there.

## 2) Remember that for loops can be slow

Use vectorized numpy expressions instead of manual loops wherever possible. We will **deduct points** if your code is too slow. The following is an example for computing the sum  $\sum_{i=0}^{N-1} i^2$  with  $N = 1000000$ :

This is **wrong** (Takes about *200ms*).

```
total = 0
for i in range(1000000):
    total += i ** 2
```

This is the **correct** way to circumvent the necessity of a loop (Takes about *8ms*):

```
import numpy as np
numbers = np.arange(1000000, dtype=np.int64)
total = (numbers ** 2).sum()
```

**Note:** The `np.int64` datatype means we use integers that are large enough to store the result. The square and sum operations are vectorized and run in fast C code internally.

3) [4 points] **Eigendecomposition**

Using `numpy.linalg` you can also perform many linear algebra functionalities. Given a square and symmetric matrix  $A$ , the eigendecomposition  $A = Q\Lambda Q^T$  with  $\Lambda = \text{diag}(\lambda_1, \dots, \lambda_n)$  can be done using `numpy.linalg.eig`.

**Todo:** Run the script `run_eigen.py` to see the eigendecomposition in action for  $A = \begin{bmatrix} 7 & -\sqrt{3} \\ -\sqrt{3} & 5 \end{bmatrix}$

Do not worry about the `NotImplementedError`, you will fix that now.

**Todo:** In file `lib/eigendecomp.py`, complete the function `get_matrix_from_eigdec` to return the square matrix  $A$ , given its eigenvalues  $\lambda_1, \dots, \lambda_n$  and eigenvectors  $Q$  as an input. **Note:** We are using `type hints` to make the code more readable and give you hints about the input and output.

**Todo:** Complete the `get_euclidean_norm` and `get_dot_product` functions. These take vectors as input and are used to show that the columns of  $Q$  are orthonormal, i.e. the columns are of unit length and are pairwise orthogonal (their dot product is 0).

**Todo:** Complete the `get_inverse` function by using the assumption that  $A$  is symmetric, therefore  $A^{-1} = Q\Lambda^{-1}Q^T$  with  $\Lambda^{-1} = \text{diag}(\lambda_1^{-1}, \dots, \lambda_n^{-1})$  is the inverse of  $A$ . Do **not** use `numpy.linalg.inv`. You can invert the diagonal matrix  $\Lambda$  without it.

4) [2 points] **Vector Norms** The length/norm of a vector can be defined in different ways. These vector norms share common properties but also have different characteristics. In numpy you can use the `numpy.linalg.norm` function to compute the  $L_p$  norm of a numpy array, where  $p \geq 1$ .

More formally, the  $L_p$  norm of a vector  $x$  is defined as:  $\|x\|_p = (\sum_{i=1}^n |x_i|^p)^{1/p}$

For  $p = 1$  we get the Manhattan norm, for  $p = 2$  we get the Euclidean norm and for  $p \rightarrow \infty$  we approximate the maximum norm:  $\|x\|_\infty = \max_i |x_i|$ .

Now to plot the norms, we create a 2-dimensional grid and color the norm values as a heat map. To create the grid, we use `meshgrid` which can transform two 1-dimensional vectors into a grid representation. For example:

```
N = 3
lin_x = np.linspace(-1, 1, N) # e.g. for N=3: [-1, 0, 1] with shape (3,)
lin_y = np.linspace(-1, 1, N) # same
X, Y = np.meshgrid(lin_x, lin_y)
print(f"X (shape {X.shape}): \n{X}\n")
print(f"Y (shape {Y.shape}): \n{Y}\n")
```

**Output:**

```
X (shape (3, 3)):
[[-1.  0.  1.]
 [-1.  0.  1.]
 [-1.  0.  1.]]

Y (shape (3, 3)):
[[-1. -1. -1.]
 [ 0.  0.  0.]
 [ 1.  1.  1.]]
```

This way, you can get the 2D-coordinates of the grid at  $i, j$  by accessing  $X_{i,j}$  and  $Y_{i,j}$

**Todo:** in file `lib/norms.py`, complete the function `get_norm` to compute the norm of each 2D vector composed by the  $i, j$ -th elements of the matrices  $X$  and  $Y$ . You will first need to stack the two matrices together to form a  $(N, N, 2)$  tensor (using `np.stack`) and then compute the  $L_p$ -norm (using `np.linalg.norm`). This way, you get the norm results for each point in the grid. Run the file `plot_norms.py` to see a plot of the 2-norm.

We have added an argument to the script with the `argparse` package. Run the command `python plot_norms.py -p 1` to see a plot of the 1-norm.

6. [1 bonus point] **Code Style**

On every exercise sheet we will also make use of `pycodestyle` to adhere to a common python standard. Your code will be automatically evaluated on submission (on push to master). Run `pycodestyle --max-line-length=120 .` to check your code locally.

7. [1 bonus point] **Feedback**

**Todo:** Please give us feedback by filling out the `feedback.md` file.

- Major Problems?
- Helpful?
- Duration (hours)? For this, please follow the instructions in the `feedback.md` file.
- Other feedback?

**This assignment is due on 28.10.2021 23:59 CEST.** Submit your solution for the tasks by uploading (`git push`) the PDF, txt file(s) and your code to your groups repository. The PDF has to include the name of the submitter(s). Teams of at most 3 students are allowed.