ORANGE JUICE ANALYSIS

OCTOBER 20, 2021

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Introduction

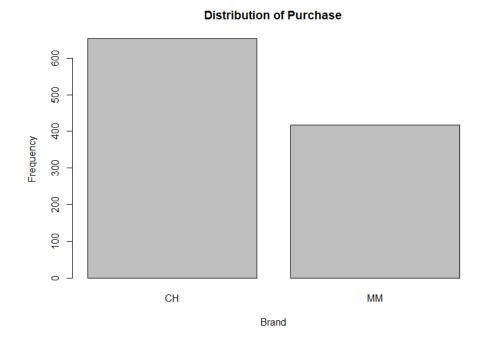
The aim of the analysis is to use decision tree to classify whether customer purchase Citrus Hill or Minute Maid Orange Juice. The model will be optimised with tree pruning methods and their respective performance will be compared.

Background of the dataset

The Old dataset is part of the ISLR package in R. It consists of 1070 rows of purchase record. There are 17 attributes including the predicting variable (ie. Purchase).

Exploratory data analysis

As tree-based model, unlike other statistical model, that has assumptions for the independent variables. Therefore, I will **skip the variables correlation part** and just discuss the distribution of the dependent variable (ie. Purchase) in this section.



There are more purchases for Citrus Hill (ie CH) than Minute Maid (ie. MM).

Methodology

Split the data into training and testing sets

Train test split is performed with 800 rows of data are randomly picked as the training set and the remaining 270 rows are used in the testing set.

Result

(a) Original classification tree

'Gini' criterion is used for training the model. Below is part of the summary output.

```
summary(rpart.gini)
Call:
rpart(formula = Purchase ~ ., data = oj_train, method = "class",
   parms = list(split = "gini"))
  n= 800
          CP nsplit rel error
                                  xerror
1 0.49201278
                  0 1.0000000 1.0000000 0.04410089
                  1 0.5079872 0.5335463 0.03672576
                  2 0.4728435 0.5175719 0.03631437
 0.01277955
                  4 0.4217252 0.4664537 0.03490406
 0.01000000
                  7 0.3833866 0.4472843 0.03433576
Variable importance
       LoyalCH
                      StoreID
                                    PriceDiff
                                                 SalePriceMM
            45
                             q
                                                            6
                      PriceMM
WeekofPurchase
                                       DiscMM
                                                   PctDiscMM
                ListPriceDiff
                                  SalePriceCH
       PriceCH
                                                       STORE
                                                            1
     SpecialCH
```

In the variable importance section, we can see that 'LoyalCH' is the most important variable, whereas 'STORE' and 'SpecialCH' are the least important. 'StoreID' and 'PriceDiff' are the second most important.

The training error is calculated to be 1.

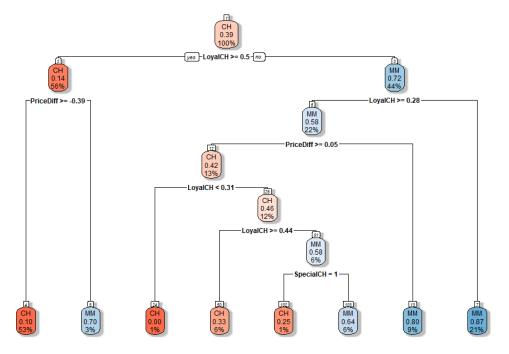
Number of terminal nodes

```
> print(rpart.gini)
n= 800
node), split, n, loss, yval, (yprob)
* denotes terminal node
  1) root 800 313 CH (0.60875000 0.39125000)
    2) LoyalCH>=0.5036 450 61 CH (0.86444444 0.13555556)
      4) PriceDiff>=-0.39 423 42 CH (0.90070922 0.09929078) *
      5) PriceDiff< -0.39 27
                                 8 MM (0.29629630 0.70370370) *
    3) LoyalCH< 0.5036 350 98 MM (0.28000000 0.72000000)
      6) LoyalCH>=0.2761415 180 76 MM (0.42222222 0.57777778) 12) PriceDiff>=0.05 106 45 CH (0.57547170 0.42452830)
         24) LoyalCH< 0.3084325 8
                                       0 CH (1.00000000 0.00000000)
          25) LoyalCH>=0.3084325 98 45 CH (0.54081633 0.45918367)
            102) SpecialCH>=0.5 8 2 CH (0.75000000 0.25000000) 103) SpecialCH< 0.5 44 16 MM (0.36363636 0.63636364)
       13) PriceDiff< 0.05 74 15 MM (0.20270270 0.79729730)
      7) LoyalCH< 0.2761415 170 22 MM (0.12941176 0.87058824) *
```

The asterisk specifies the terminal nodes, which have 8 in total.

Plot of the tree

The graph below displayed the details of the tree model.



There are 8 terminal nodes in total. Over half (ie. 53%) of the data falls on the node which is on the leftmost. As described by the graph, they are the points with 'LoyalCH' >=0.5 and 'PriceDiff'>=-0.39.

Predict the response on test data

(i) Testing error

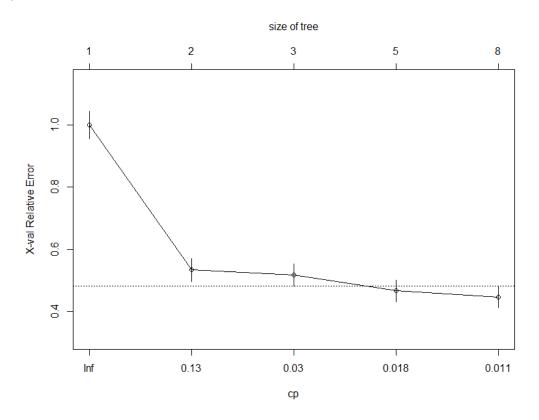
The testing error is calculated to be **0.1814815.**

(ii) Confusion matrix

pred	СН	MM	
CH	141	24	
MM	25	80	

Accuracy is calculated to be 81.9%.

Optimal tree size



From the graph above, it is shown that the error drops significantly when the tree size increases from 1 to 2 and then the error keeps dropping steadily onwards. The optimal tree size that corresponds to the lowest cross-validation classification error rate is 5.

(b) Tree pruning

I want to prune the tree to see if there is further improvement found. I therefore find the **cp value corresponds to the optimal tree size** that I found (ie. 5). The value is calculated as **0.01**, which is **the default cp** in the original tree-based model. **Therefore, if we prune the tree with cp=0.01, it should give us the same result.**

To verify if 0.01 is truly the optimal cp or not, it is suggested to grow out the tree again with negative cp value and check for the optimal cp.

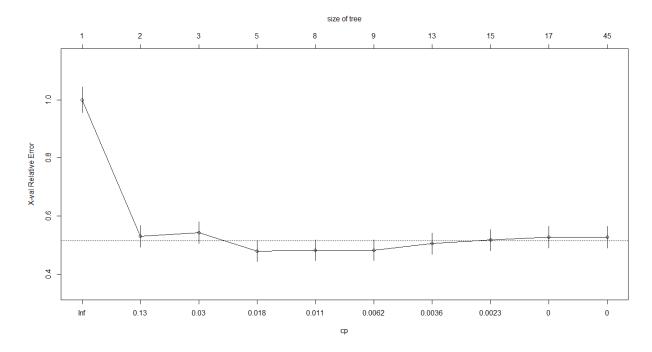
Tree growing with negative cp

I arbitrarily chose **cp=-0.1** to grow the tree. Below shows its summary.

```
rpart(formula = Purchase ~ ., data = oj_train, method = "class",
parms = list(split = "gini"), cp = -0.1)
    parms =
= 800
                    CP nsplit rel error
                                 0 1.0000000 1.0000000 0.04410089
1 0.5079872 0.5271565 0.03656280
2 0.4728435 0.5143770 0.03623048
      0.492012780
      0.035143770
      0.025559105
                                    0.4217252 0.4664537 0.03490406
                                    0.3833866 0.4824281 0.03536075 0.3738019 0.4888179 0.03553927
      0.009584665
      0.003993610
                                12 0.3578275 0.5175719 0.03631437
14 0.3514377 0.5111821 0.03614603
16 0.3482428 0.5015974 0.03588938
                                                    0.5111821 0.03614603
0.5015974 0.03588938
     \begin{array}{c} 0.001597444 \\ 0.0000000000 \end{array}
    -0.100000000
                                44 0.3482428 0.5015974 0.03588938
Variable importance
                                                        PriceDiff
                                                                             SalePriceMM WeekofPurchase
                   38
            DiscMM
                                PctDisdMM
                                                 ListPriceDiff
                                                                             SalePriceCH
                                                                                                               STORE
                                                                                                                                                               Store7
            DiscCH
                                PctDiscCH
```

As a side note, **again 'LoyalCH' is the most important** variable.

Find optimal tree size and the corresponding cp

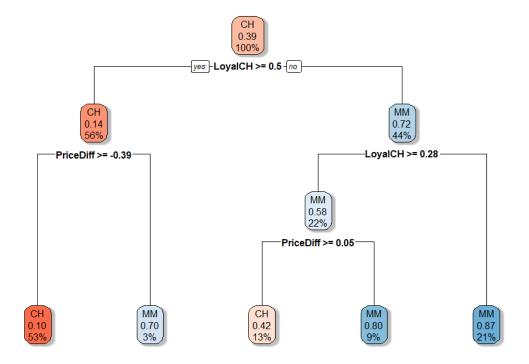


The optimal tree size is found to be 4 and the corresponding cp is

0.01277955, which is close to what we found in the original tree model. To improve
the original tree model, I am going to prune the tree with the newly found cp value.

Tree pruning with the cp=0.01277955

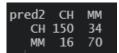
The below graph visualises the pruned tree.



There are 5 terminal nodes in total.

Its training error is calculated to be ${\bf 1}$ and the testing error is calculated to be

0.1851852. Below displays its confusion matrix:



Its corresponding accuracy is calculated to be 81.48%.

Findings

Comparison between the pruned and unpruned trees

The below table summarise the findings in both tree models.

	Original (unpruned)	Pruned
Training error	1	1
Testing error	0.1814815	0.1851852
Accuracy	81.9%.	81.48%.

The finding is **out of my expectation.** As we can see that the **testing error of the pruned tree is higher, and its accuracy is lower**. Therefore, **the original (unpruned) tree model is better.**