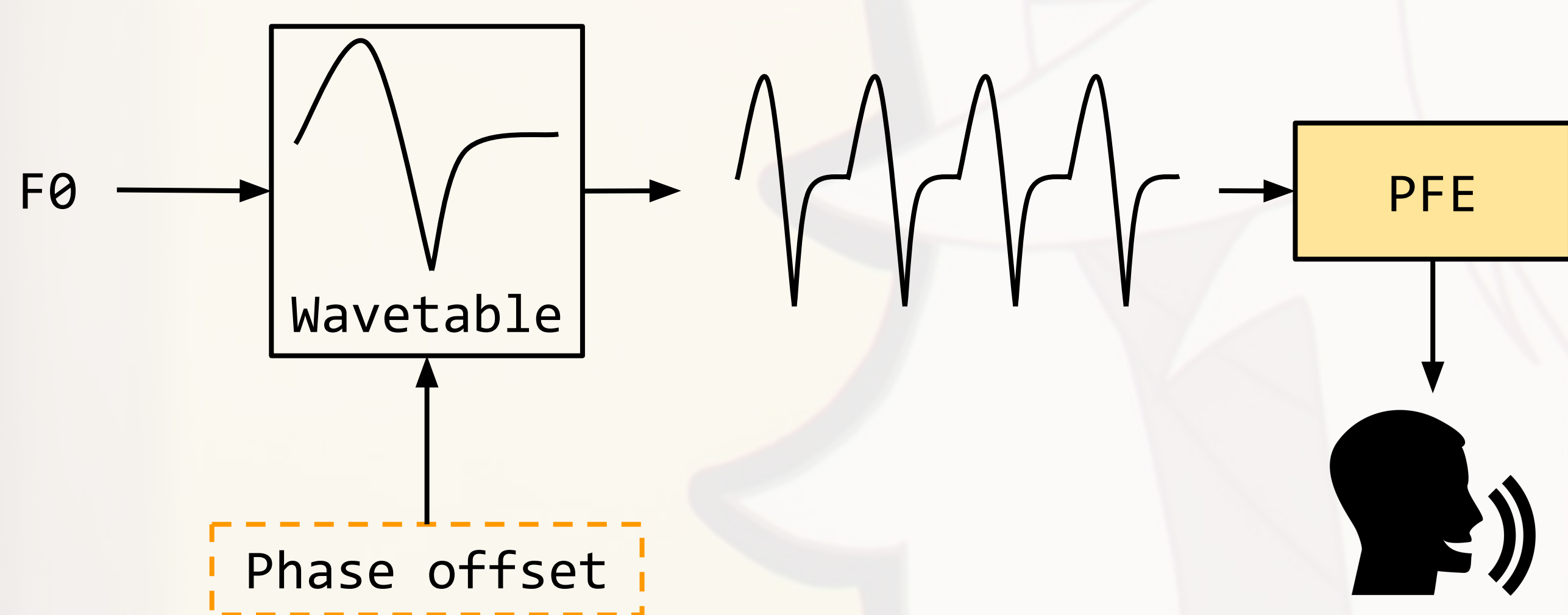


Phase-Accurate End-to-End Analysis-by-Synthesis for Singing Voice

Motivations

Neural vocoders are commonly trained using spectral and adversarial losses, which does not consider the **phase information** in voice. Phase is critical for editing and manipulating voices. In addition, **end-to-end learning** enables joint modelling for all the system components at once, ensuring the system behave the same regardless during training or evaluation. Learning phase-accurate synthesis in an end-to-end way enables more robust system.

The Synthesiser (Modified from GOLF [1])



Additive Wavetable

Linear interpolation on fixed-size wavetables introduces aliasing. Solution: **Band-limited additive synthesis**.

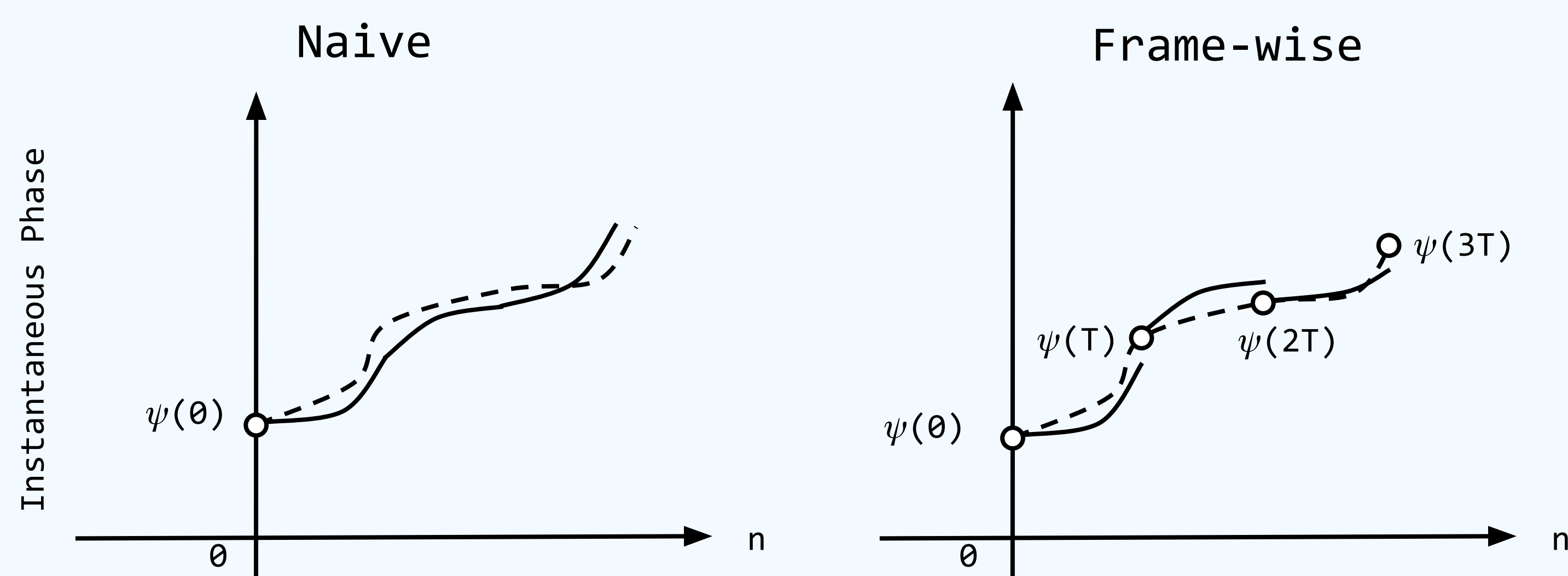
$$x(n) = a_1 \cos(\psi(n)) + \sum_{k=2}^{\lfloor \frac{\pi}{f_0(n)} \rfloor} a_k \cos(k\psi(n) + \phi_k)$$

- Control parameters
 - $\psi(n)$: Instantaneous phase
- Wavetable parameters
 - $\{a_1, a_2, \dots, a_k\}$: Amplitudes
 - $\{\phi_2, \phi_3, \dots, \phi_k\}$: Relative phase differences

Instantaneous Phase Calculation

$$\psi(n) = \psi(0) + \sum_{m=1}^n f_0(m)$$

- $\psi(0)$: Initial phase, $f_0(n)$: Instantaneous frequency
- Issue: F_0 estimation errors accumulate
- Solution: Inspired by quasi-harmonic model [2], predict sub-sampled $\psi(mT)$ where $m \in \{0, 1, 2, \dots\}$.
 - Errors are limited within T samples



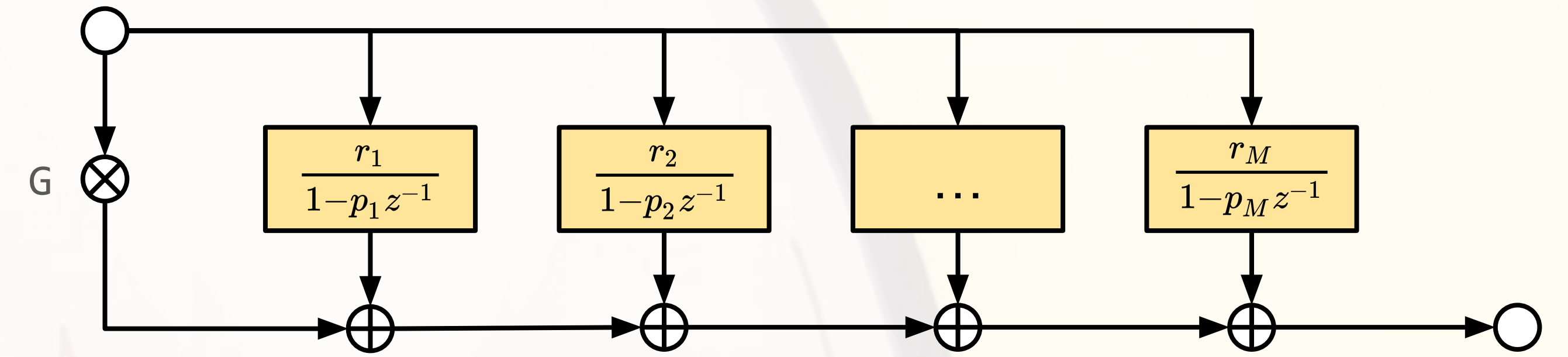
- Solid lines: Predicted $\psi(n)$
- Dashed lines: Ground truth $\psi(n)$

The first author is a research student at the UKRI CDT in AI and Music, supported jointly by UK Research and Innovation [grant number EP/S022694/1] and Queen Mary University of London.

Partial Fraction Expansion (PFE) Filter

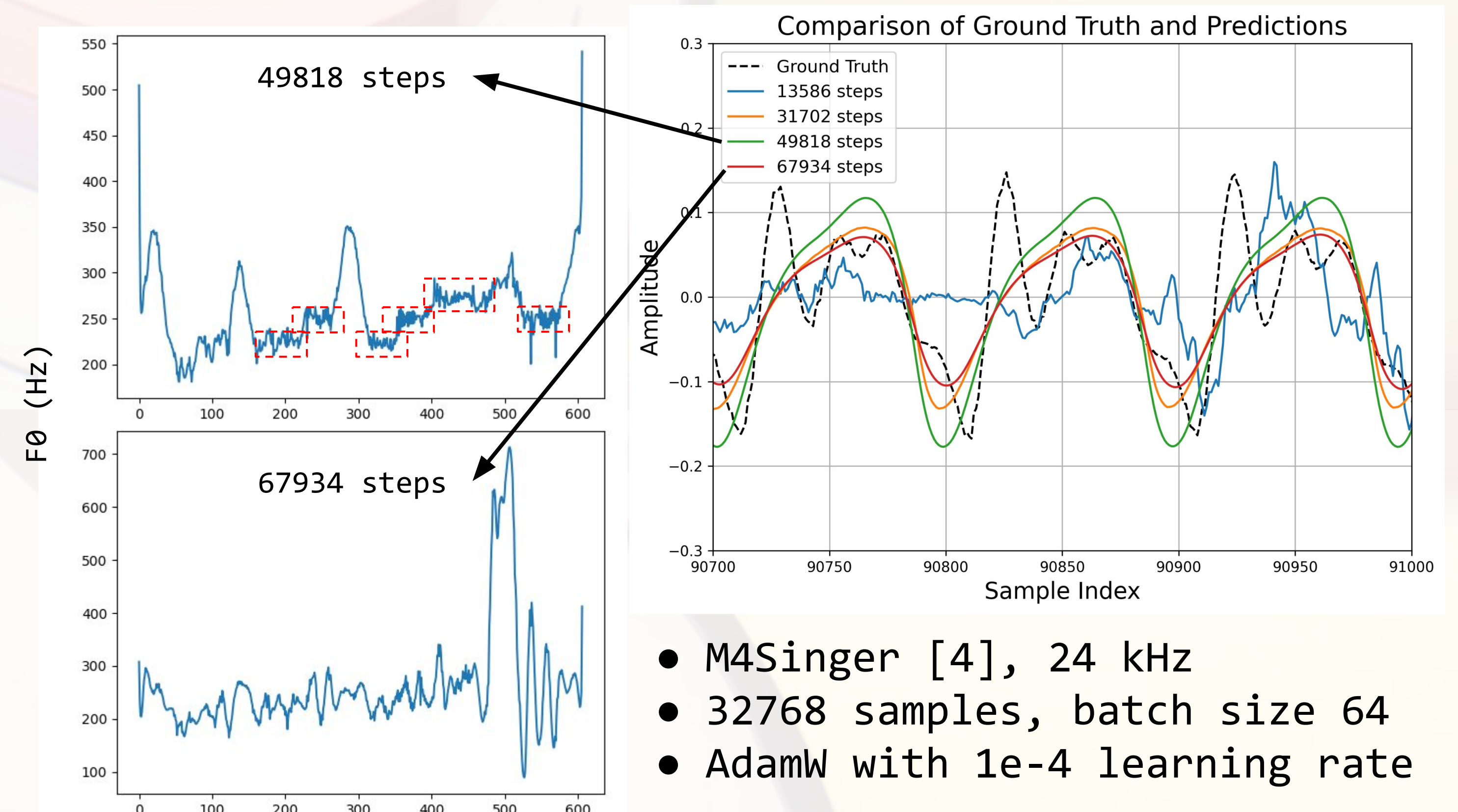
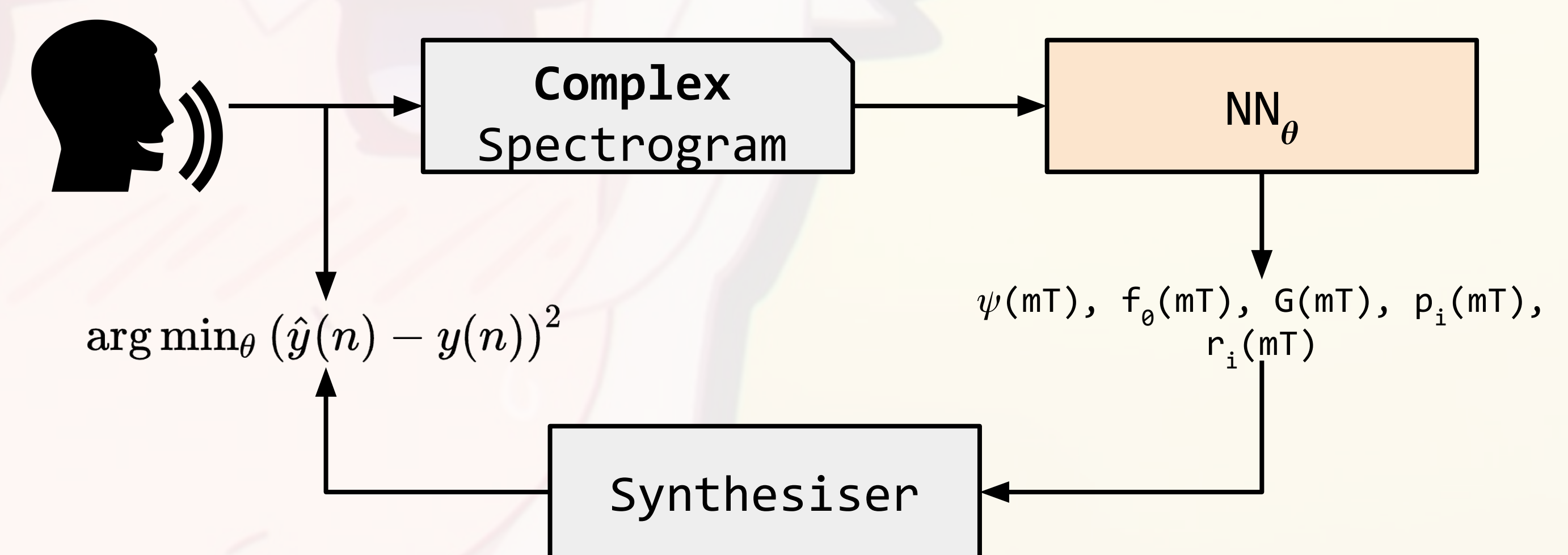
Advantages over linear prediction (all-pole) filter:

- Can be **accelerated on the GPU** using parallel scan [3].
- Guarantee **time-varying stability** when poles are inside the unit circle.



G: filter gain, p_i : pole, r_i : residue, M: filter order

End-to-End Copy Synthesis Experiment



- M4Singer [4], 24 kHz
- 32768 samples, batch size 64
- AdamW with 1e-4 learning rate

Results

- < 50k steps: Successfully captures the instantaneous phase and the glottal pulses are aligned.
- > 50k steps: Complex amplitude and frequency modulations emerge and the learnt $f_0(n) \neq$ instantaneous frequency. The encoder tries to fit the **non-deterministic components**.

Conclusions and Future Works

- End-to-end phase modelling is feasible with frame-wise phase accumulation and time-domain loss function.
- Insert more zeros to the filter (longer FIRs) to increase capacity.
- Modelling the stochastic components by neural nets with regularisation to avoid simply copying the input.

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