

Group Details:

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ASSIGNMENT 1

In this project, we are implementing the functions in c++ language.

Data structure for storing Graph:

Graph.h file

Used adjacency list for implementation because it takes less space and comparatively with adjacency matrix there will be few less comparisons.

```
class Graph
{
    int V; //-> no of nodes(customers)
    vector <int>* adj; //used array of vectors
};
```

Graph.cpp

It contains the basic functions of graph like adding edges in graph, printing the graph.

Graph_Operations.cpp

It contains the graph operations.

`void connectedComponents(ofstream& outfile);` - Used DFS traversal and it passes through all the elements that are connected.

`void one_cycle(ofstream& outfile);` - While doing dfs if the node is visited previously (or for the second time) we say it as found cycle and store this node as cyclestart and we will go back till to printcycle.

`vector<int> DijkstraSP(int& start, ofstream& outfile);` - used dijkshtra algorithm with priority queues and calculated shortest path.

Graph simulator.h && Graph simulator.cpp

```
void generateConnectedGraph(int n, ofstream& outfile);
void generateEmptyGraph(int n, ofstream& outfile);
void generateHeap(int n, ofstream& outfile);
void generateTruncatedHeap(int n, int m, ofstream& outfile);
void generateEquivalenceModKGraph(int n, int k, ofstream& outfile);
void generateNcycleGraph(int n, ofstream& outfile);
```

This file contains the 6 functions to generate the simulator graphs required to test the graph operations test cases.

Used mathematical conditions to generate the graph.

Simulated test.cpp

It has the main method to call the simulated graph functions:

For each type of graph, we called all the 3 operations, and the output is stored in **SimulatesTestResults.txt** included in zip file

CPU and peak memory usage report is saved as **SimulatedTestReports.DIAGSSESSION** in zip.

Also pasting output here:

//Tested creating a graph with pre-compiled values. For n=14

Adjacency list of vertex 0

head

Adjacency list of vertex 1

head -> 2

Adjacency list of vertex 2

head -> 1-> 3

Adjacency list of vertex 3

head -> 2-> 4-> 5

Adjacency list of vertex 4

head -> 3-> 6-> 7

Adjacency list of vertex 5

head -> 6-> 3-> 9

Adjacency list of vertex 6

head -> 4-> 5-> 10

Adjacency list of vertex 7

head -> 4-> 8

Adjacency list of vertex 8

head -> 7

Adjacency list of vertex 9

head -> 5

Adjacency list of vertex 10

head -> 6-> 11

Adjacency list of vertex 11

head -> 10-> 12-> 13

Adjacency list of vertex 12

head -> 11-> 13

Adjacency list of vertex 13

head -> 11-> 12

Following are connected components

0

1 2 3 4 6 5 9 10 11 12 13 7 8

finding cycle

Cycle found: 3 5 6 4 3

-----shortest path-----

Getting the shortest path from 1 to all other nodes.

Printing the shortest paths for node 1.

There is no path from 1 to node 0

The distance from node 1 to node 1 is: 0 and the path is 1

The distance from node 1 to node 2 is: 1 and the path is 1 - 2

The distance from node 1 to node 3 is: 2 and the path is 1 - 2 - 3

The distance from node 1 to node 4 is: 3 and the path is 1 - 2 - 3 - 4

The distance from node 1 to node 5 is: 3 and the path is 1 - 2 - 3 - 5

The distance from node 1 to node 6 is: 4 and the path is 1 - 2 - 3 - 4 - 6

The distance from node 1 to node 7 is: 4 and the path is 1 - 2 - 3 - 4 - 7

The distance from node 1 to node 8 is: 5 and the path is 1 - 2 - 3 - 4 - 7 - 8

The distance from node 1 to node 9 is: 4 and the path is 1 - 2 - 3 - 5 - 9

The distance from node 1 to node 10 is: 5 and the path is 1 - 2 - 3 - 4 - 6 - 10

The distance from node 1 to node 11 is: 6 and the path is 1 - 2 - 3 - 4 - 6 - 10 - 11

The distance from node 1 to node 12 is: 7 and the path is 1 - 2 - 3 - 4 - 6 - 10 - 11 - 12

The distance from node 1 to node 13 is: 7 and the path is 1 - 2 - 3 - 4 - 6 - 10 - 11 - 13

-----testing simulator functions-----

//An n-cycle: There is one connected component, every shortest path has length at most $n/2$, and there is a unique cycle of length n .

-----testing with n cycle-----

Adjacency list of vertex 0

head -> 1-> 10

Adjacency list of vertex 1

head -> 0-> 2

Adjacency list of vertex 2

head -> 1-> 3

Adjacency list of vertex 3

head -> 2-> 4

Adjacency list of vertex 4

head -> 3-> 5

Adjacency list of vertex 5

head -> 4-> 6

Adjacency list of vertex 6

head -> 5-> 7

Adjacency list of vertex 7

head -> 6-> 8

Adjacency list of vertex 8

head -> 7-> 9

Adjacency list of vertex 9

head -> 8-> 10

Adjacency list of vertex 10

head -> 0-> 9

Following are connected components

0 1 2 3 4 5 6 7 8 9 10

finding cycle

Cycle found: 0 10 9 8 7 6 5 4 3 2 1 0

-----shortest path-----

Getting the shortest path from 1 to all other nodes.

Printing the shortest paths for node 1.

The distance from node 1 to node 0 is: 1 and the path is 1 - 0

The distance from node 1 to node 1 is: 0 and the path is 1

The distance from node 1 to node 2 is: 1 and the path is 1 - 2

The distance from node 1 to node 3 is: 2 and the path is 1 - 2 - 3

The distance from node 1 to node 4 is: 3 and the path is 1 - 2 - 3 - 4

The distance from node 1 to node 5 is: 4 and the path is 1 - 2 - 3 - 4 - 5

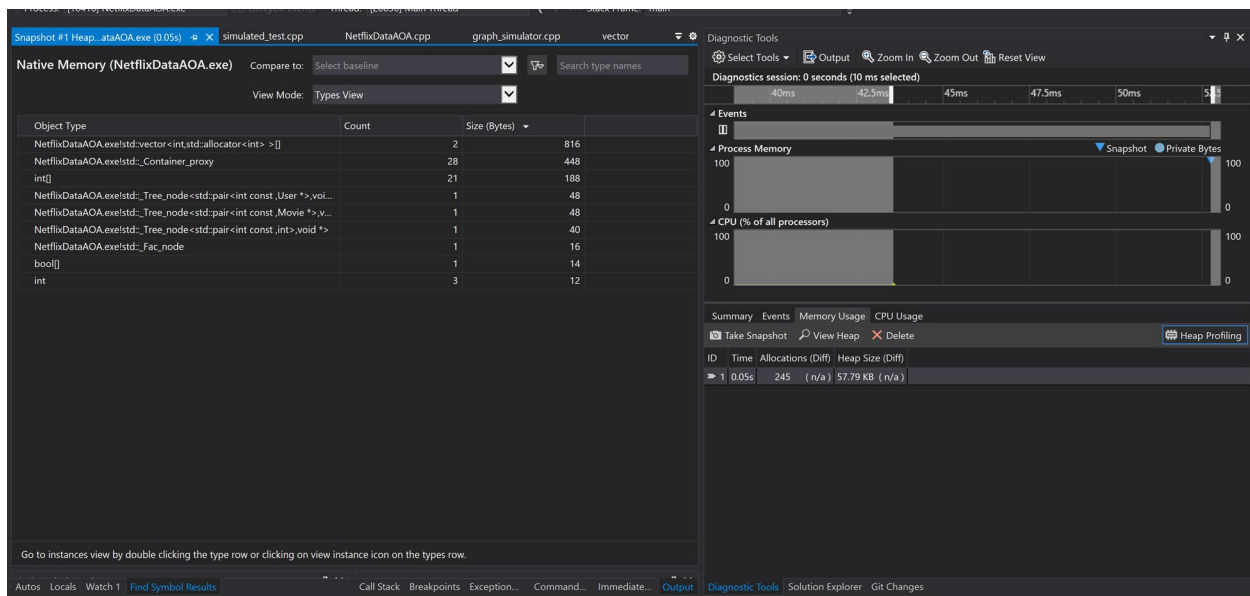
The distance from node 1 to node 6 is: 5 and the path is 1 - 2 - 3 - 4 - 5 - 6

The distance from node 1 to node 7 is: 5 and the path is 1 - 0 - 10 - 9 - 8 - 7

The distance from node 1 to node 8 is: 4 and the path is 1 - 0 - 10 - 9 - 8

The distance from node 1 to node 9 is: 3 and the path is 1 - 0 - 10 - 9

The distance from node 1 to node 10 is: 2 and the path is 1 - 0 - 10



-----testing with connected graph-----

// A complete graph on n vertices: There is one connected component, every shortest path has unit length, and there are many cycles.

Adjacency list of vertex 0

head -> 1-> 2-> 3-> 4-> 5-> 6-> 7-> 8-> 9

Adjacency list of vertex 1

head -> 0-> 2-> 3-> 4-> 5-> 6-> 7-> 8-> 9

Adjacency list of vertex 2

head -> 0-> 1-> 3-> 4-> 5-> 6-> 7-> 8-> 9

Adjacency list of vertex 3

head -> 0-> 1-> 2-> 4-> 5-> 6-> 7-> 8-> 9

Adjacency list of vertex 4

head -> 0-> 1-> 2-> 3-> 5-> 6-> 7-> 8-> 9

Adjacency list of vertex 5

head -> 0-> 1-> 2-> 3-> 4-> 6-> 7-> 8-> 9

Adjacency list of vertex 6

head -> 0-> 1-> 2-> 3-> 4-> 5-> 7-> 8-> 9

Adjacency list of vertex 7

head -> 0-> 1-> 2-> 3-> 4-> 5-> 6-> 8-> 9

Adjacency list of vertex 8

```
head -> 0-> 1-> 2-> 3-> 4-> 5-> 6-> 7-> 9
```

Adjacency list of vertex 9

```
head -> 0-> 1-> 2-> 3-> 4-> 5-> 6-> 7-> 8
```

Following are connected components

```
0 1 2 3 4 5 6 7 8 9
```

finding cycle

Cycle found: 0 2 1 0

-----shortest path-----

Getting the shortest path from 1 to all other nodes.

Printing the shortest paths for node 1.

The distance from node 1 to node 0 is: 1 and the path is 1 - 0

The distance from node 1 to node 1 is: 0 and the path is 1

The distance from node 1 to node 2 is: 1 and the path is 1 - 2

The distance from node 1 to node 3 is: 1 and the path is 1 - 3

The distance from node 1 to node 4 is: 1 and the path is 1 - 4

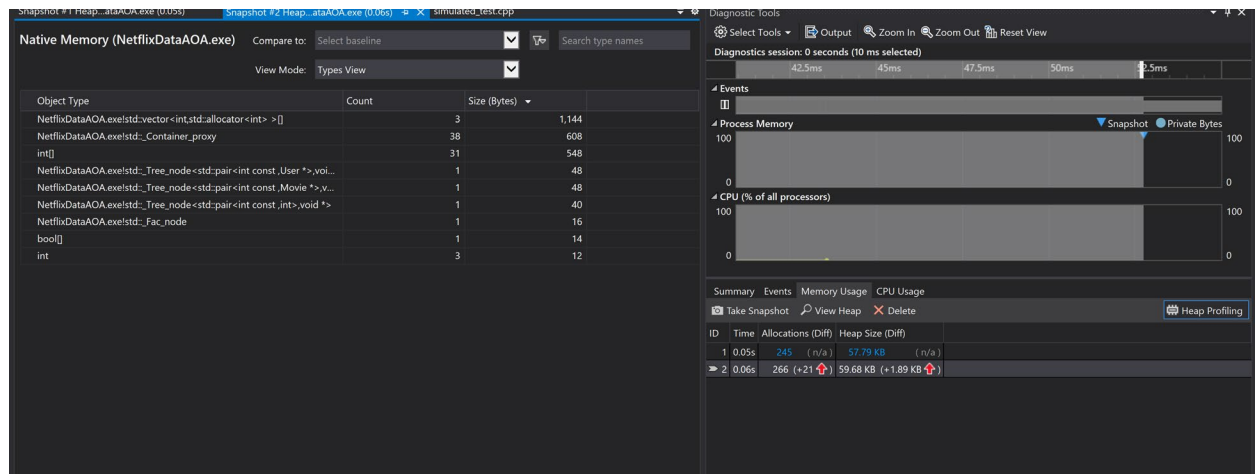
The distance from node 1 to node 5 is: 1 and the path is 1 - 5

The distance from node 1 to node 6 is: 1 and the path is 1 - 6

The distance from node 1 to node 7 is: 1 and the path is 1 - 7

The distance from node 1 to node 8 is: 1 and the path is 1 - 8

The distance from node 1 to node 9 is: 1 and the path is 1 - 9



// . An empty graph on n vertices: The vertices are integers from 0 through n – 1. There are no edges. There are n connected components, no paths, and no cycles

-----testing with empty graph-----

Adjacency list of vertex 0

head

Adjacency list of vertex 1

head

Adjacency list of vertex 2

head

Adjacency list of vertex 3

head

Adjacency list of vertex 4

head

Adjacency list of vertex 5

head

Adjacency list of vertex 6

head

Adjacency list of vertex 7

head

Adjacency list of vertex 8

head

Adjacency list of vertex 9

head

Adjacency list of vertex 10

head

Following are connected components

0

1

2

3

4

5

6

7

8

9

10

finding cycle

Acyclic

-----shortest path-----

Getting the shortest path from 1 to all other nodes.

Printing the shortest paths for node 1.

There is no path from 1 to node 0

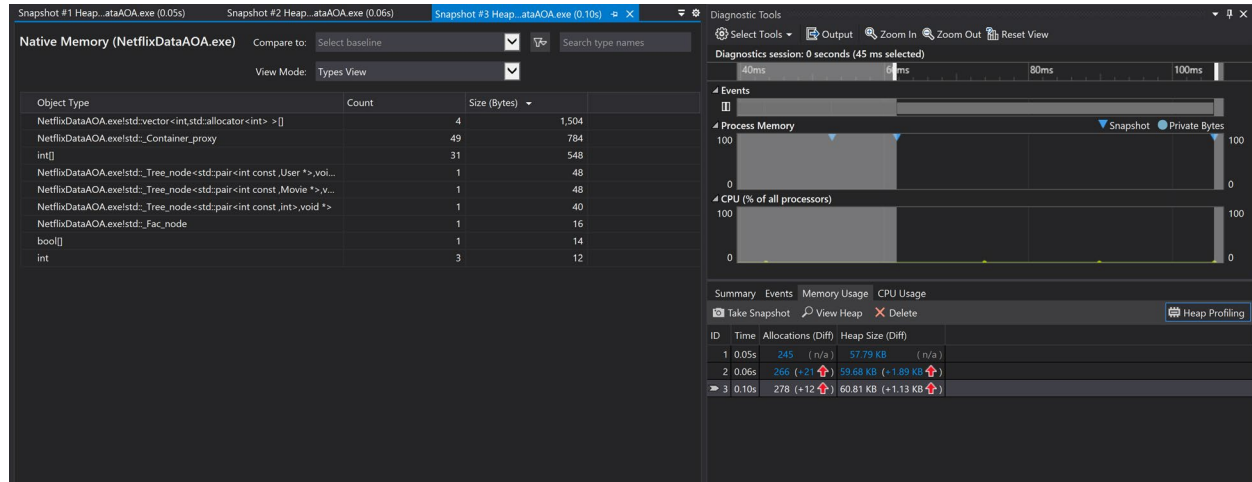
The distance from node 1 to node 1 is: 0 and the path is 1

There is no path from 1 to node 2

There is no path from 1 to node 3

There is no path from 1 to node 4

There is no path from 1 to node 5
 There is no path from 1 to node 6
 There is no path from 1 to node 7
 There is no path from 1 to node 8
 There is no path from 1 to node 9
 There is no path from 1 to node 10



// A heap: The vertices are integers from 0 through $n - 1$. The neighbors of a vertex v are $(v - 1)/2$, $2v + 1$, and $2v + 2$, provided those numbers are in the range for vertices. There is one connected component, the paths are short, and there are no cycles.

-----testing with heap -----

Adjacency list of vertex 0

head -> 0-> 10-> 1-> 2

Adjacency list of vertex 1

head -> 0-> 10-> 3-> 4

Adjacency list of vertex 2

head -> 0-> 10-> 5-> 6

Adjacency list of vertex 3

head -> 1-> 10-> 7-> 8

Adjacency list of vertex 4

head -> 1-> 10-> 9-> 10

Adjacency list of vertex 5

head -> 2-> 10

Adjacency list of vertex 6

head -> 2-> 10

Adjacency list of vertex 7

head -> 3-> 10

Adjacency list of vertex 8

head -> 3-> 10

Adjacency list of vertex 9

head -> 4-> 10

Adjacency list of vertex 10

head -> 0-> 1-> 2-> 3-> 4-> 5-> 6-> 7-> 8-> 9-> 4-> 10-> 10

Following are connected components

0 10 1 3 7 8 4 9 2 5 6

finding cycle

Acyclic

-----shortest path-----

Getting the shortest path from 1 to all other nodes.

Printing the shortest paths for node 1.

The distance from node 1 to node 0 is: 1 and the path is 1 - 0

The distance from node 1 to node 1 is: 0 and the path is 1

The distance from node 1 to node 2 is: 2 and the path is 1 - 0 - 2

The distance from node 1 to node 3 is: 1 and the path is 1 - 3

The distance from node 1 to node 4 is: 1 and the path is 1 - 4

The distance from node 1 to node 5 is: 2 and the path is 1 - 10 - 5

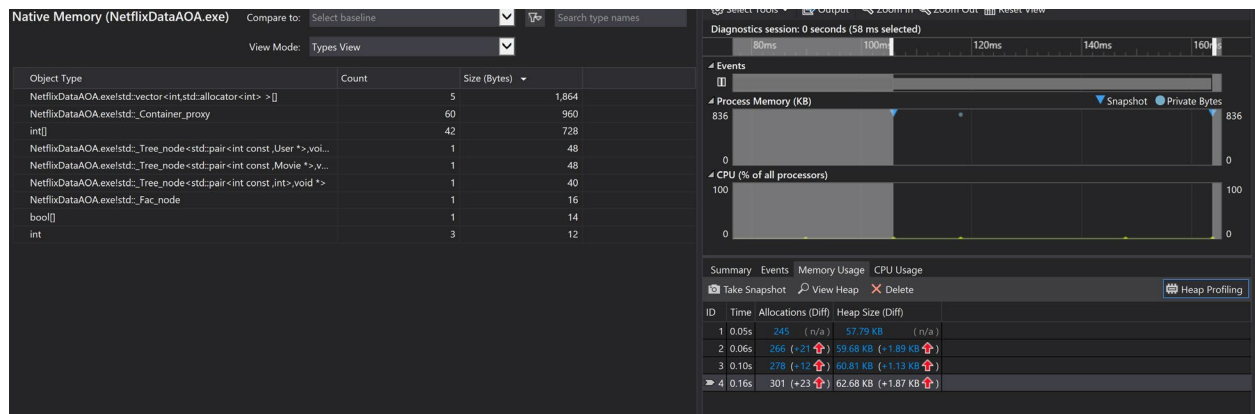
The distance from node 1 to node 6 is: 2 and the path is 1 - 10 - 6

The distance from node 1 to node 7 is: 2 and the path is 1 - 3 - 7

The distance from node 1 to node 8 is: 2 and the path is 1 - 3 - 8

The distance from node 1 to node 9 is: 2 and the path is 1 - 4 - 9

The distance from node 1 to node 10 is: 1 and the path is 1 - 10



// A truncated heap: The vertices are integers from m through $n - 1$. The edge relationship is the same as for the heap. There are $n - 1 - 2m$ edges, $m + 1$ connected components, and no cycles. The paths, when they exist, are short

-----testing with truncated heap -----

Adjacency list of vertex 0

head

Adjacency list of vertex 1

head

Adjacency list of vertex 2

head

Adjacency list of vertex 3

head

Adjacency list of vertex 4

head -> 10-> 9-> 10

Adjacency list of vertex 5

head -> 10

Adjacency list of vertex 6

head -> 10

Adjacency list of vertex 7

head -> 10

Adjacency list of vertex 8

head -> 10

Adjacency list of vertex 9

head -> 4-> 10

Adjacency list of vertex 10

head -> 4-> 5-> 6-> 7-> 8-> 9-> 4-> 10-> 10

Following are connected components

0

1

2

3

4 10 5 6 7 8 9

finding cycle

Cycle found: 4 9 10 4

-----shortest path-----

Getting the shortest path from 6 to all other nodes.

Printing the shortest paths for node 6.

There is no path from 6 to node 0

There is no path from 6 to node 1

There is no path from 6 to node 2

There is no path from 6 to node 3

The distance from node 6 to node 4 is: 2 and the path is 6 - 10 - 4

The distance from node 6 to node 5 is: 2 and the path is 6 - 10 - 5

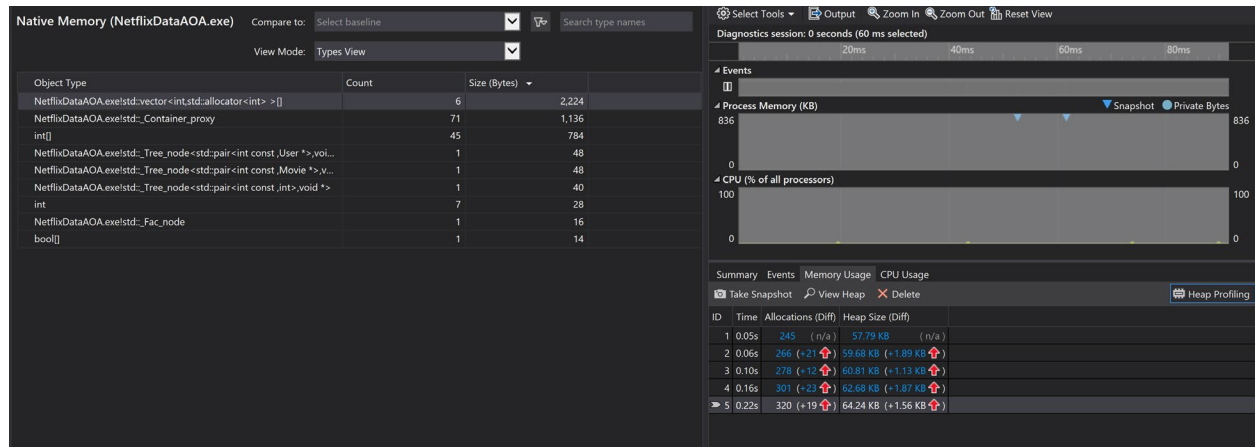
The distance from node 6 to node 6 is: 0 and the path is 6

The distance from node 6 to node 7 is: 2 and the path is 6 - 10 - 7

The distance from node 6 to node 8 is: 2 and the path is 6 - 10 - 8

The distance from node 6 to node 9 is: 2 and the path is 6 - 10 - 9

The distance from node 6 to node 10 is: 1 and the path is 6 - 10



// Equivalence mod k: The vertices are integers from 0 to $n - 1$, where $k \leq n$. The vertices u and v are connected by an edge if $u - v$ is evenly divisible by k . There are k components, and each component is a complete graph.

-----testing with EquivalenceModKGraph -----

Adjacency list of vertex 0

head -> 4-> 8

Adjacency list of vertex 1

head -> 5-> 9

Adjacency list of vertex 2

head -> 6-> 10

Adjacency list of vertex 3

head -> 7

Adjacency list of vertex 4

head -> 0-> 8

Adjacency list of vertex 5

head -> 1-> 9

Adjacency list of vertex 6

head -> 2-> 10

Adjacency list of vertex 7

head -> 3

Adjacency list of vertex 8

head -> 0-> 4

Adjacency list of vertex 9

head -> 1-> 5

Adjacency list of vertex 10

head -> 2-> 6

Following are connected components

0 4 8

1 5 9

2 6 10

3 7

finding cycle

Cycle found: 0 8 4 0

-----shortest path-----

Getting the shortest path from 6 to all other nodes.

Printing the shortest paths for node 6.

There is no path from 6 to node 0

There is no path from 6 to node 1

The distance from node 6 to node 2 is: 1 and the path is 6 - 2

There is no path from 6 to node 3

There is no path from 6 to node 4

There is no path from 6 to node 5

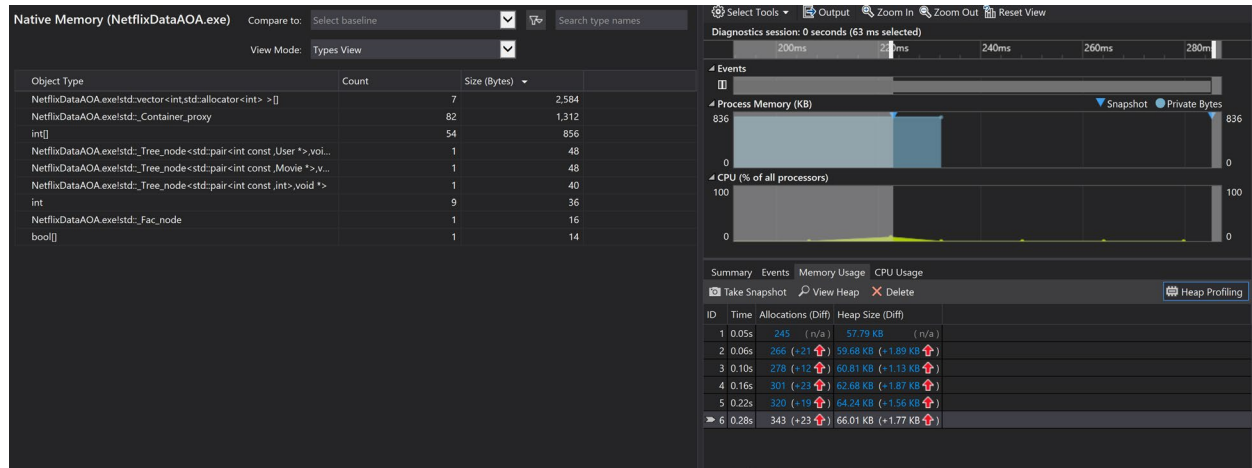
The distance from node 6 to node 6 is: 0 and the path is 6

There is no path from 6 to node 7

There is no path from 6 to node 8

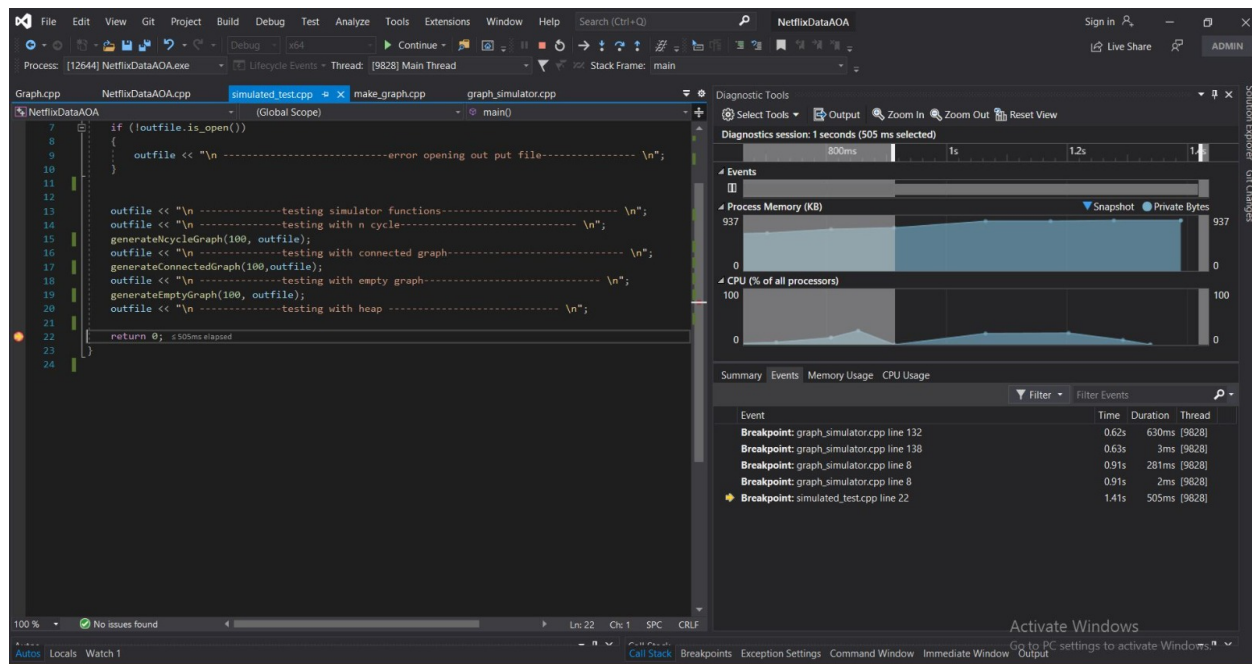
There is no path from 6 to node 9

The distance from node 6 to node 10 is: 1 and the path is 6 - 10

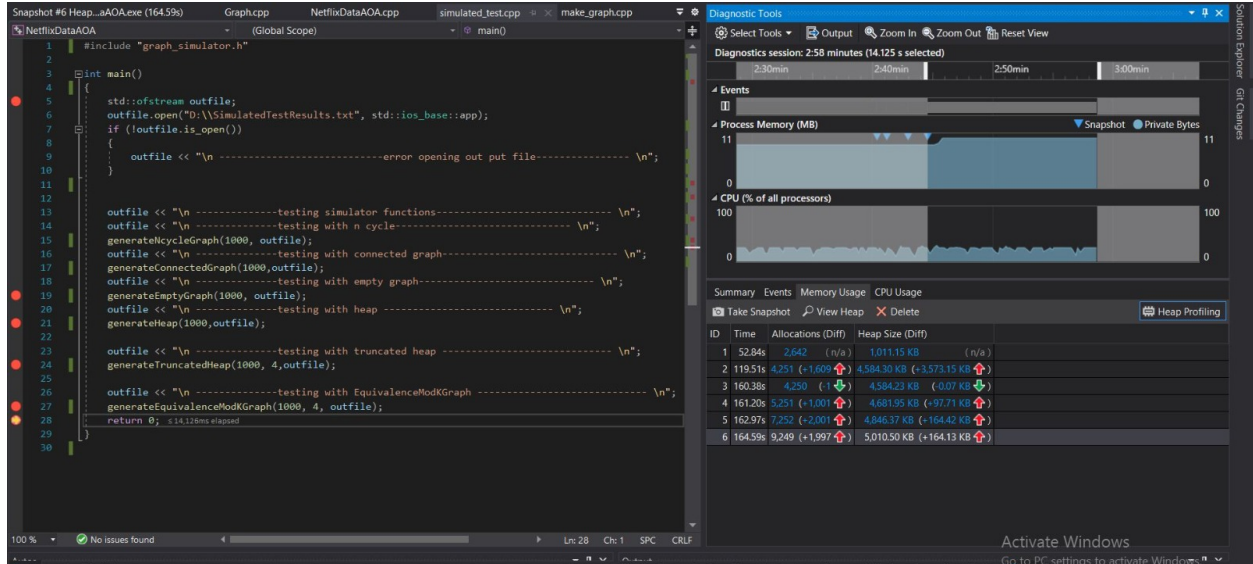


Simulated runtime and peak memory analysis:

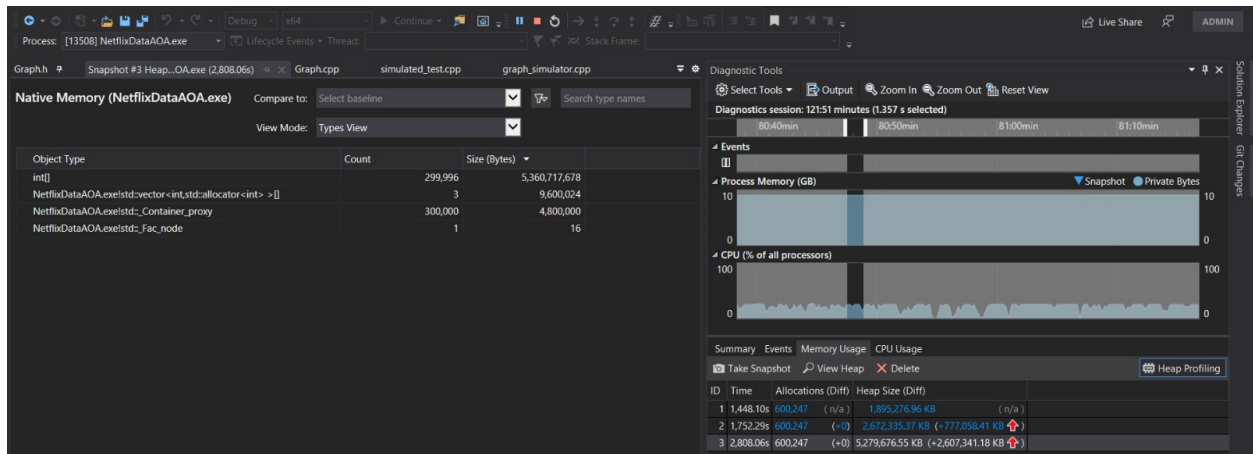
When n=100 -- 505 ms



When n=1000 - 2.58 mins



N=10000: 121.51 mins



Make_graph.cpp

This file contains the construction of graph based on the adjacency criteria.

Criteria1:

Our first criteria is to say that 2 customers have a relationship/similar taste when both of them liked at least 4 videos in the recent time

Assumptions: we assume that if the customer have given rating at least 4 then he must have liked the movie and considering movie ratings in the recent year (i.e, took after 2004)

For this to implement, while reading the data files for a movie if the customer gives more than 4 rating in the recent year (2005 or above) we store the movieid+rating as unique key against the customer key.

So at the end we will have customer map where each customer points to all the movies satisfying the above conditions.

And then we iterate over each customer to find the intersection of those unique keys at least 4 in common and for those we call ADD_EDGE API and after constructing graph we are printing the graph(adj list) and connected components in graph , finding the cycle path and finding shortest path from 1st customer to all.

Data structure used is: each customer pointer holds userid and unique review keys.

All the customers reviews are stored in a map whose key is customer_id and contains the unique review keys.

```
class User {
public:
    int user_id;
    vector<int> reviews;

}
```

Output is printed in **netflixtest1.txt** including in the zip file.

Sample output:

Adjacency list of vertex 0

```
head -> 1-> 11-> 12-> 17-> 3->.....->247-> 254-> 258-> 260-> 286-> 293-> 323-> 332-> 347-> 351-> 376-> 384-> 418-> 442-> 446-> 468-> 483->
486-> 501-> 505-> 506-> 507-> 528-> 541-> 622-> 630-> 632-> 671-> 679-> 693-> 707-> 709-> 722-> 724-> 737-> 745-> 765-> 770-> 771-> 844->
849-> 864-> 868-> 887-> 889-> 915-> 918-> 924-> 932-> 938-> 963-> 966-> 971-> 975-> 981-> 983-> 988-> 998-> 414585-> 414600-> 414624->
414629-> 414631-> 414632-> 414638-> 414660-> 414668-> 414675-> 414681-> 414691-> 414694-> 414702-> 414708-> 414710-> 414723
```

Adjacency list of vertex 1

```
head -> 0-> 2-> 7-> 10-> 11->.....
```

```
.
```

finding cycle

Cycle found: 0 11 2 1 0

-----shortest path-----

Getting the shortest path from 1 to all other nodes.

Printing the shortest paths for node 1.

Getting the shortest path from 1 to all other nodes.

Printing the shortest paths for node 1.

The distance from node 1 to node 0 is: 1 and the path is 1 - 0

The distance from node 1 to node 1 is: 0 and the path is 1

The distance from node 1 to node 2 is: 1 and the path is 1 - 2

The distance from node 1 to node 3 is: 2 and the path is 1 - 31 - 3

The distance from node 1 to node 4 is: 2 and the path is 1 - 1246 - 4

The distance from node 1 to node 5 is: 2 and the path is 1 - 41 - 5

The distance from node 1 to node 6 is: 2 and the path is 1 - 17 - 6

The distance from node 1 to node 7 is: 1 and the path is 1 - 7

.

.

.There is no path from 1 to node 414730

The distance from node 1 to node 414731 is: 1 and the path is 1 - 414731

The distance from node 1 to node 414732 is: 2 and the path is 1 - 54 - 414732

The distance from node 1 to node 414733 is: 2 and the path is 1 - 135 - 414733

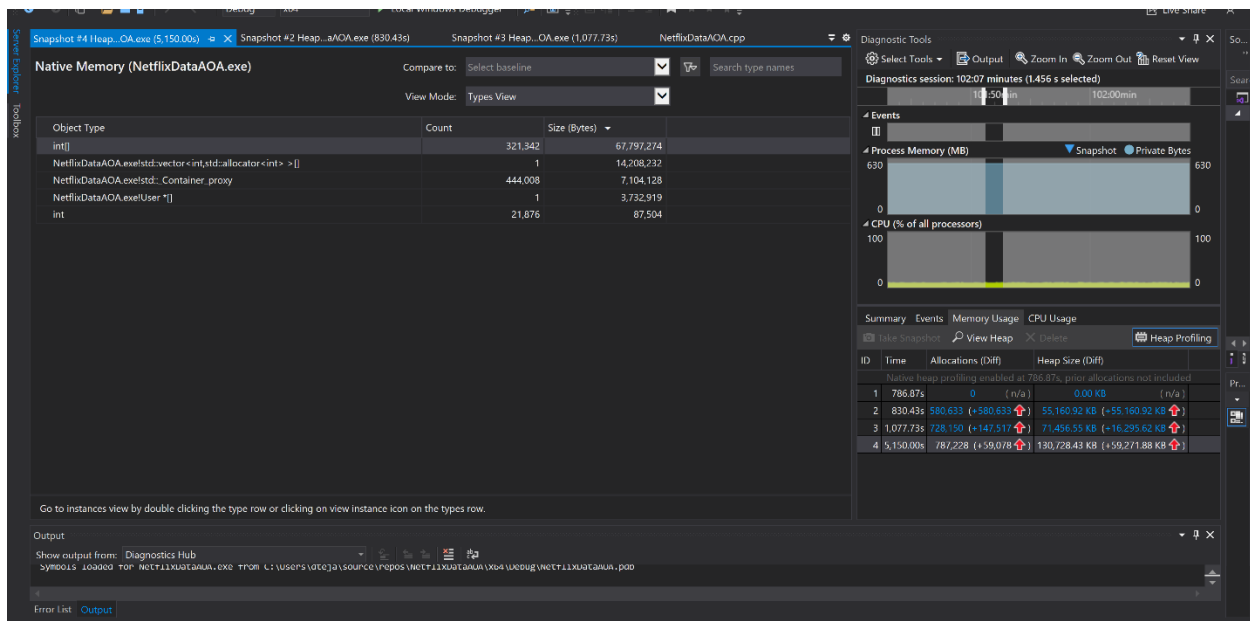
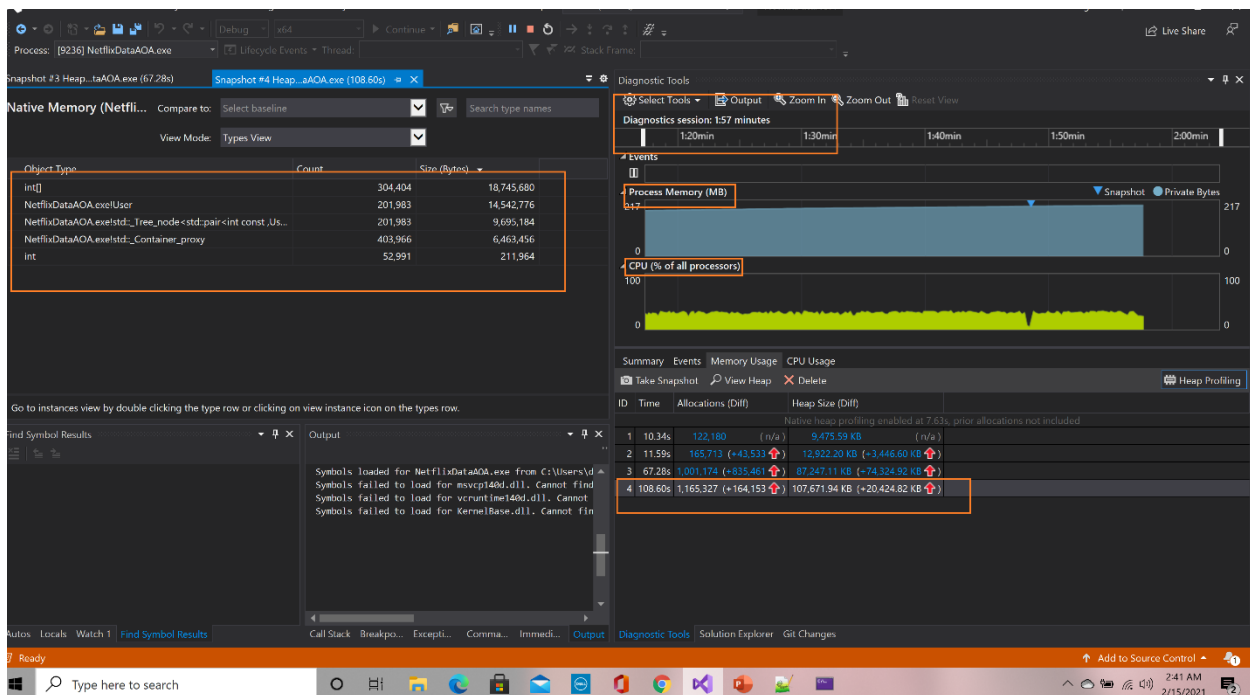
The distance from node 1 to node 414734 is: 2 and the path is 1 - 13 - 414734

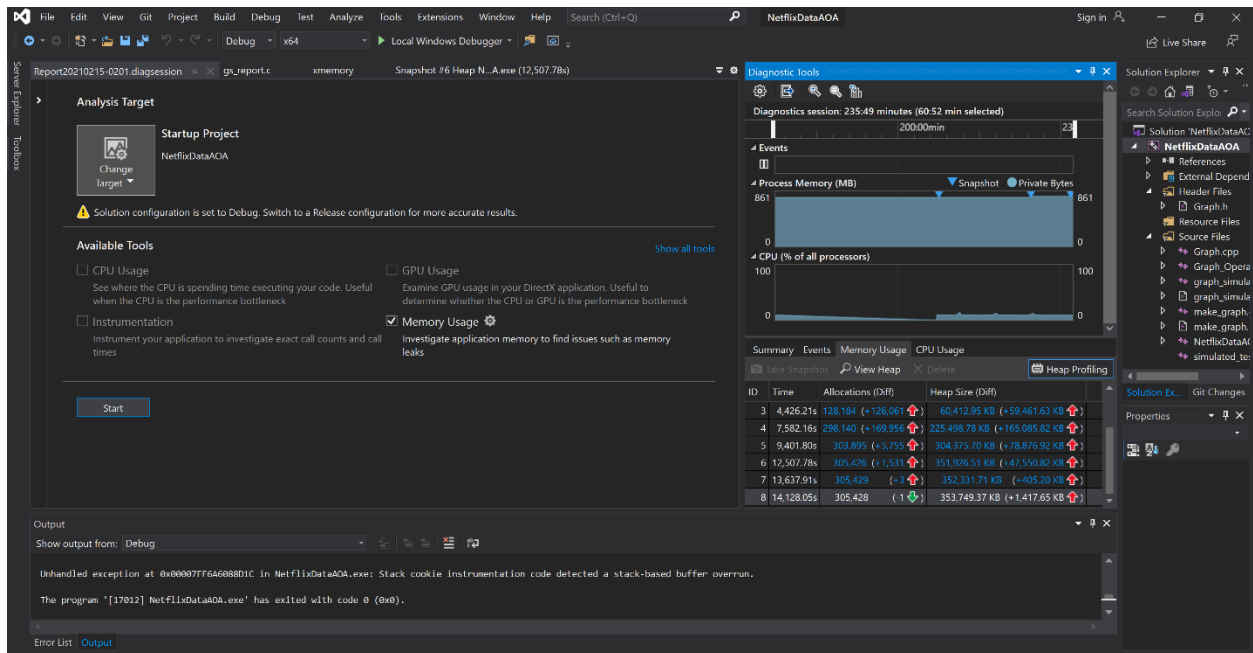
The distance from node 1 to node 414735 is: 1 and the path is 1 - 414735

****→** Here in graph we printed customer indexes and not customer IDS if we want to display as customerIDs graphs while printing we just access V[index] which gives the customerIDs

And for runtime and peak memory analysis we used the visual studio profiling tool

For this criteria it took 235.49 mins and the heap size and objects allocations are shown in below screenshot.





Adjacency criteria 2:

Criteria2:

Our second criteria is to say that 2 customers have a relationship/similar taste when both of them liked at least a movie.

Assumptions: we assume that if the customer have given rating 5 then he must have liked the movie.

For this to implement, while reading the data files for a movie if the customer gives rating 5 then we add that customer in the movie liked users list.

So at the end we will have movies map which says which customers have liked a particular movie.

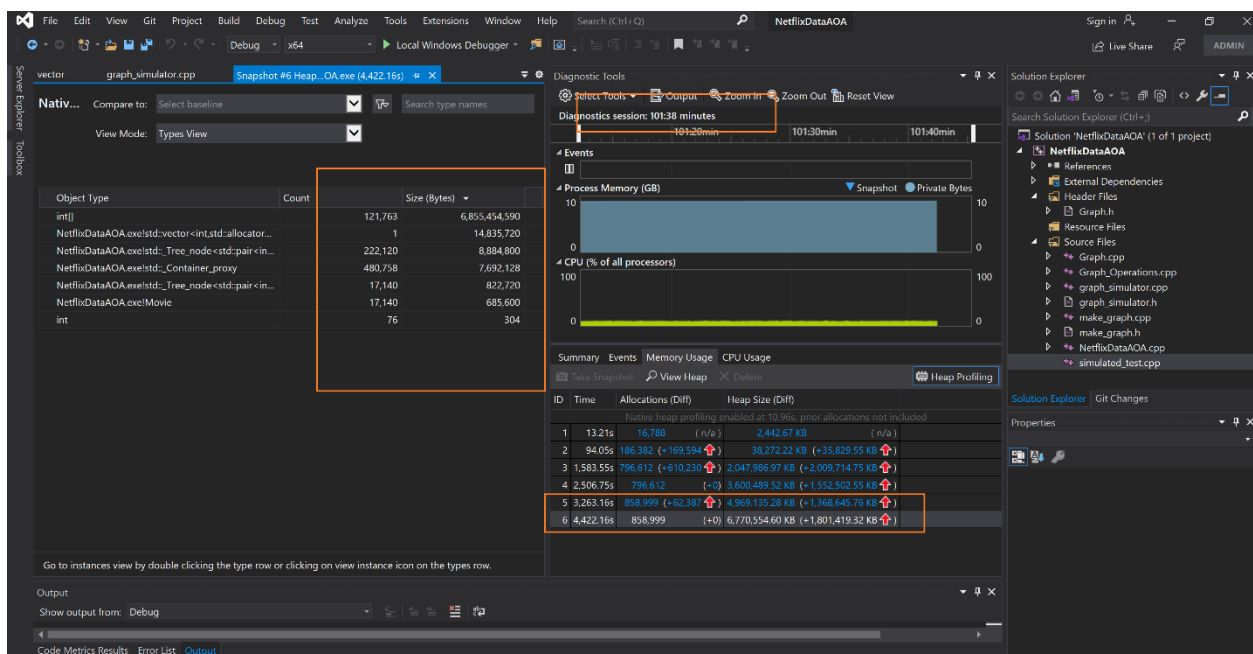
And then we iterate over each movie to map all the customers in that movie as we can add edge (if there is one movie in common we will add edge).

Output is printed in **netflixtest2.txt** file. Uploaded in the zip file.

Data structure:

```
class Movie {
public:
    int movie_id;
    vector<int> users;
    Movie(int id) {
        movie_id = id;
    }

    void add_user(int userid)
    {
        users.push_back(userid);
    }
};
```



Adjacency criteria 3:

Criteria3:

Our third criteria is to say that 2 customers have a relationship/similar taste when both of them liked at least 4 movies with same rating and on same date and he should have given rating recently.

Assumptions: we assume that

- i) if the customer have given rating at least 4 then he must have liked the movie and
- ii) also considering ratings given only in the recent year (i.e, ratings given after 2004)

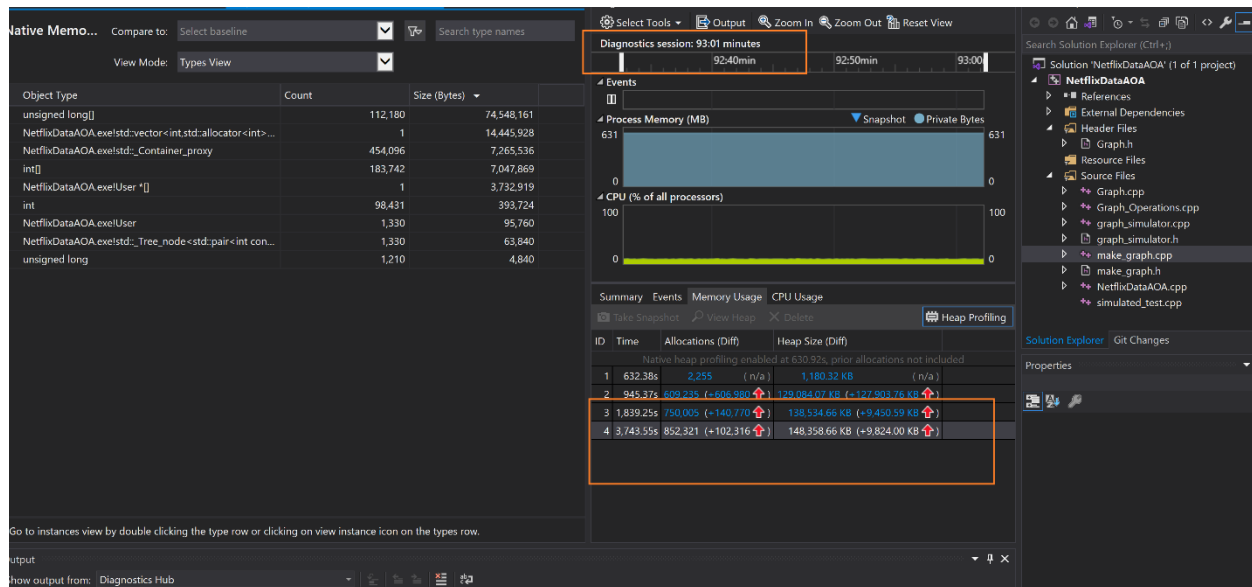
For this to implement, while reading the data files for a movie if the customer gives more than 4 rating in the recent year (2005 or above) we store the **date+movieid** as unique key against the customer key.

So at the end we will have customer map where each customer points to all the movies satisfying the above conditions.

And then we iterate over each customer to find the intersection of those unique keys at least 4 in common and for those we call ADD_EDGE API to construct graph.

For that graph, we are printing the graph (adj list) and connected components in graph , finding the cycle path and finding shortest path from 1st customer to all customers.

- Using same data structure as criteria_1.



****It took around 340mins but profiling tool ran out of memory after 90 mins of execution**

real_test.cpp:

It contains the function calls to adjacency criteria.

In order to test 3 criteria's separately for runtime and memory usage, called the functions individually.

SUMMARY

For simulated data:

For n=100 it took 550ms and memory is 5kb

For n=1000 it took 2.58 mins and memory is 5010.5kb

For n=10000 it took 125 mins and memory is 2607341.18kb

Observed that heap is taking very less time 16 mins for n=10000 and other graphs are taking $O(n^2)$ time.

All of them are n^2 loops adding edges with mathematical conditions.

For Netflix data :

Each criteria took minimum of 240 mins and minimum memory of 5 mb for filtered data in memory.

Each criteria of ours takes $o(n^3)$ time to process.