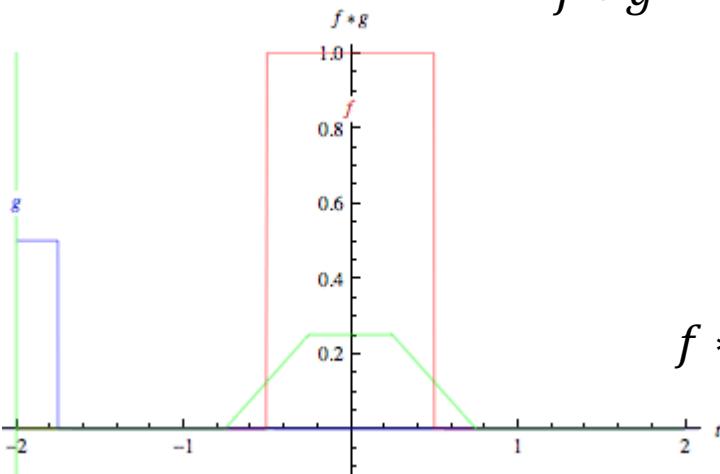


# Lecture 9 Recap

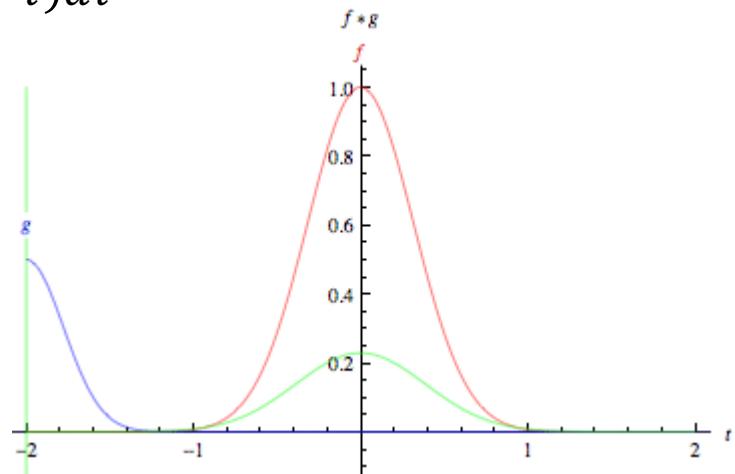
# What are Convolutions?

$$f * g = \int_{-\infty}^{\infty} f(\tau)g(t - \tau)d\tau$$



Convolution of two box functions

$f$  = red  
 $g$  = blue  
 $f * g$  = green



Convolution of two Gaussians

application of a filter to a function  
the 'smaller' one is typically called the filter kernel

# What are Convolutions?

Discrete case: box filter

4	3	2	-5	3	5	2	5	5	6
---	---	---	----	---	---	---	---	---	---

1/3	1/3	1/3
-----	-----	-----

??	3	0	0	1	10/3	4	4	16/3	??
----	---	---	---	---	------	---	---	------	----

*What to do at boundaries?*

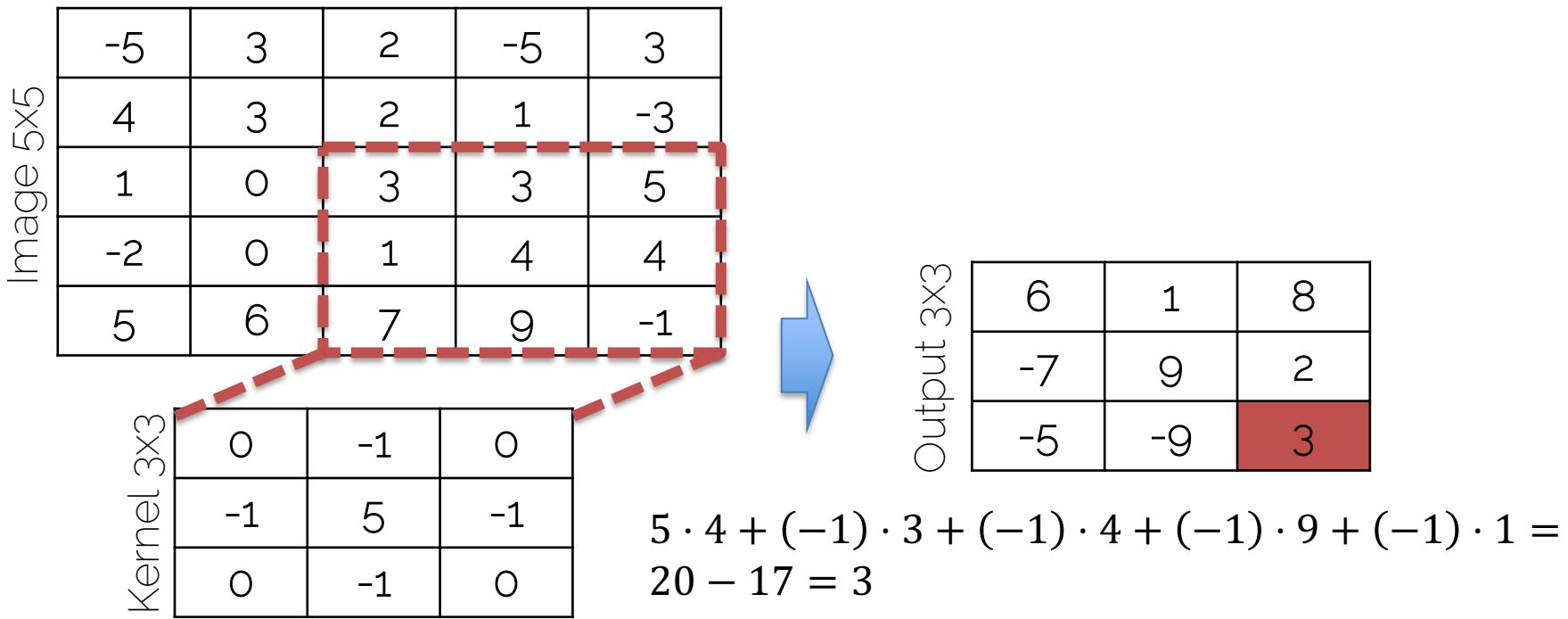
1) Shrink

3	0	0	1	10/3	4	4	16/3
---	---	---	---	------	---	---	------

2) Pad  
often '0'

7/3	3	0	0	1	10/3	4	4	16/3	11/3
-----	---	---	---	---	------	---	---	------	------

# Convolutions on Images



# Image Filters

- Each kernel gives us a different image filter

Input



Edge detection

$$\begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$



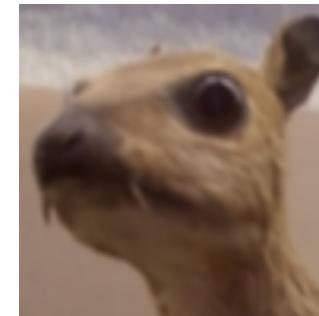
Box mean

$$\frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$



Sharpen

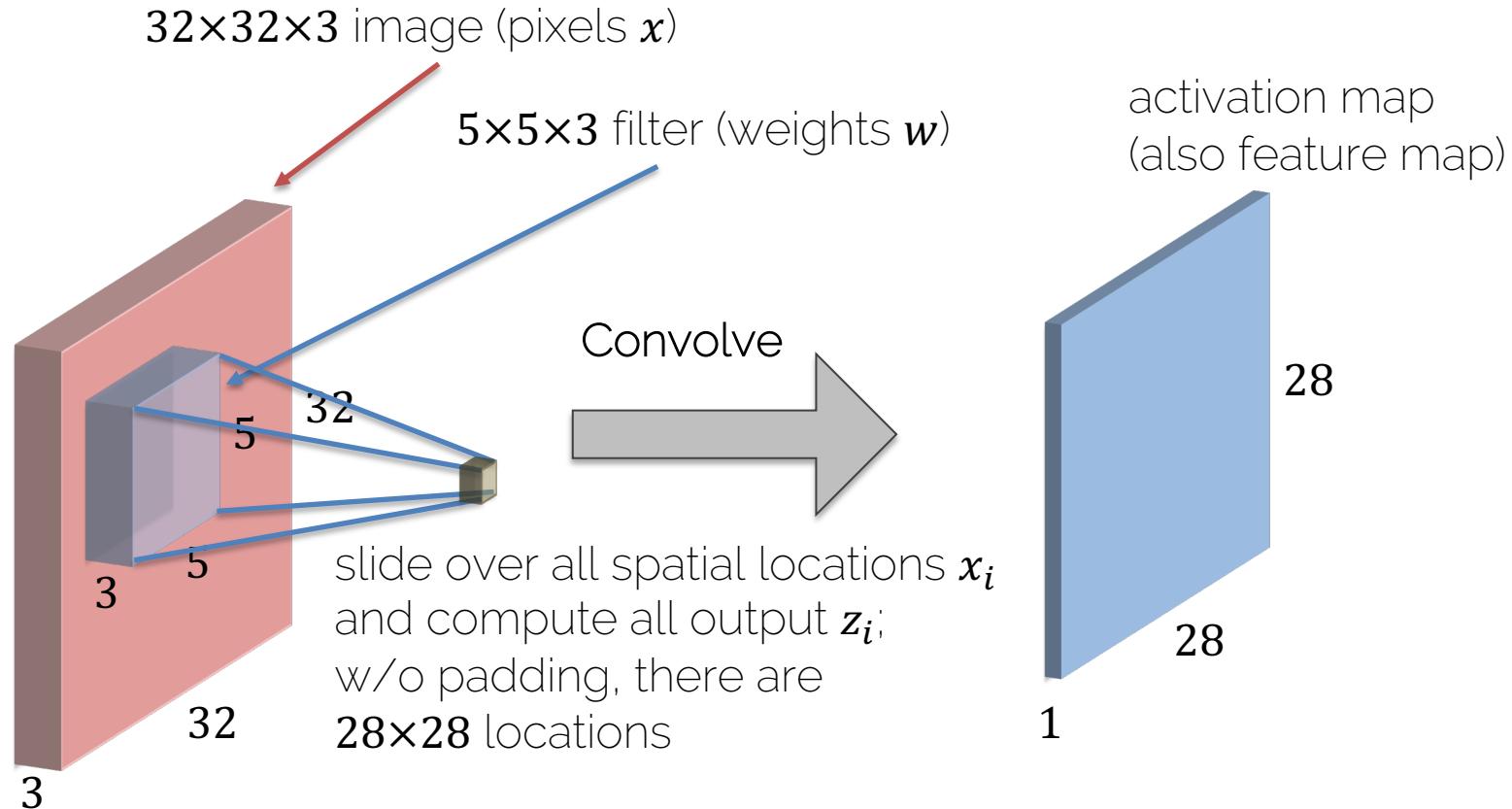
$$\begin{bmatrix} 0 & -1 & 0 \\ -1 & 5 & -1 \\ 0 & -1 & 0 \end{bmatrix}$$



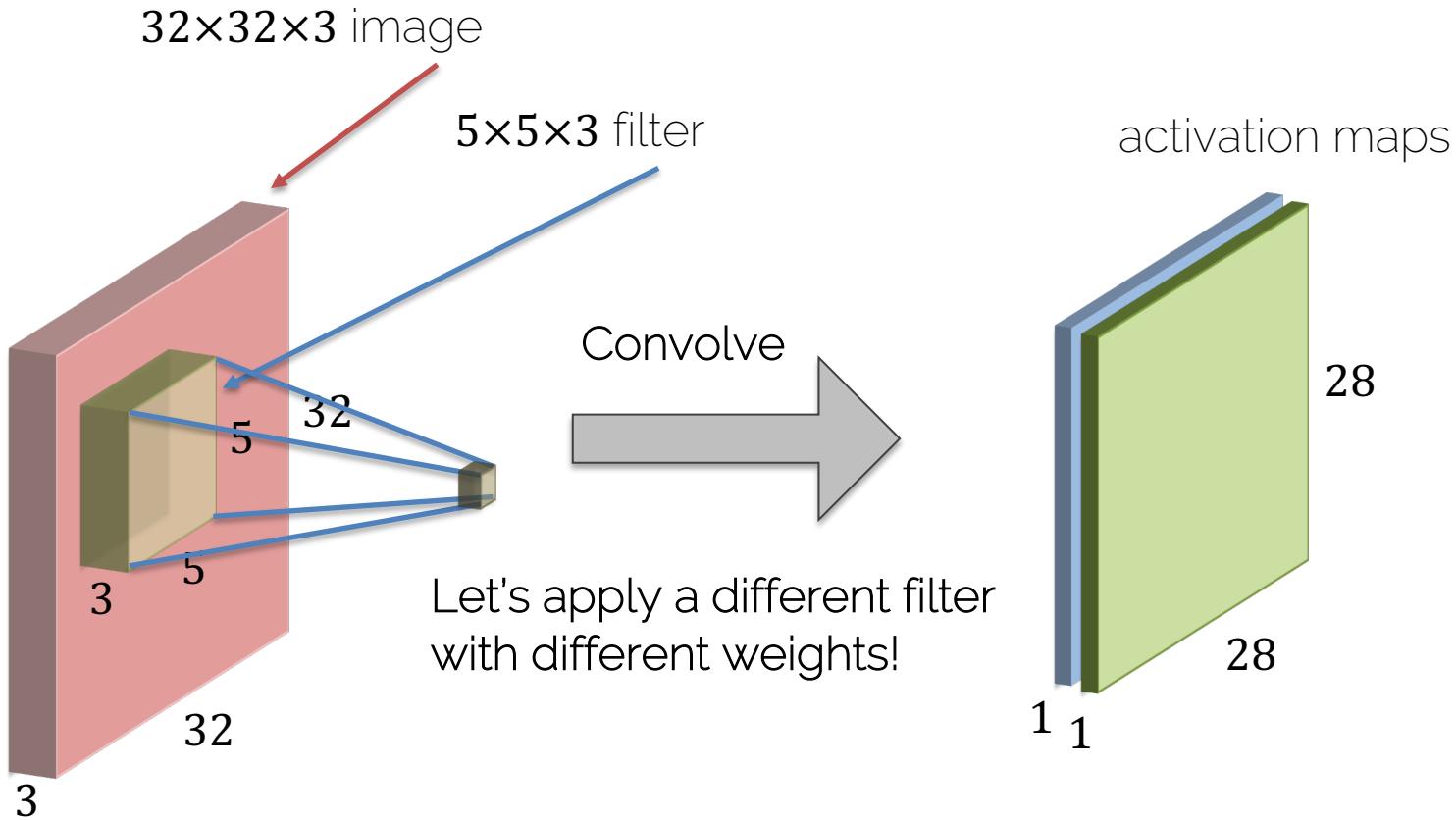
Gaussian blur

$$\frac{1}{16} \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$$

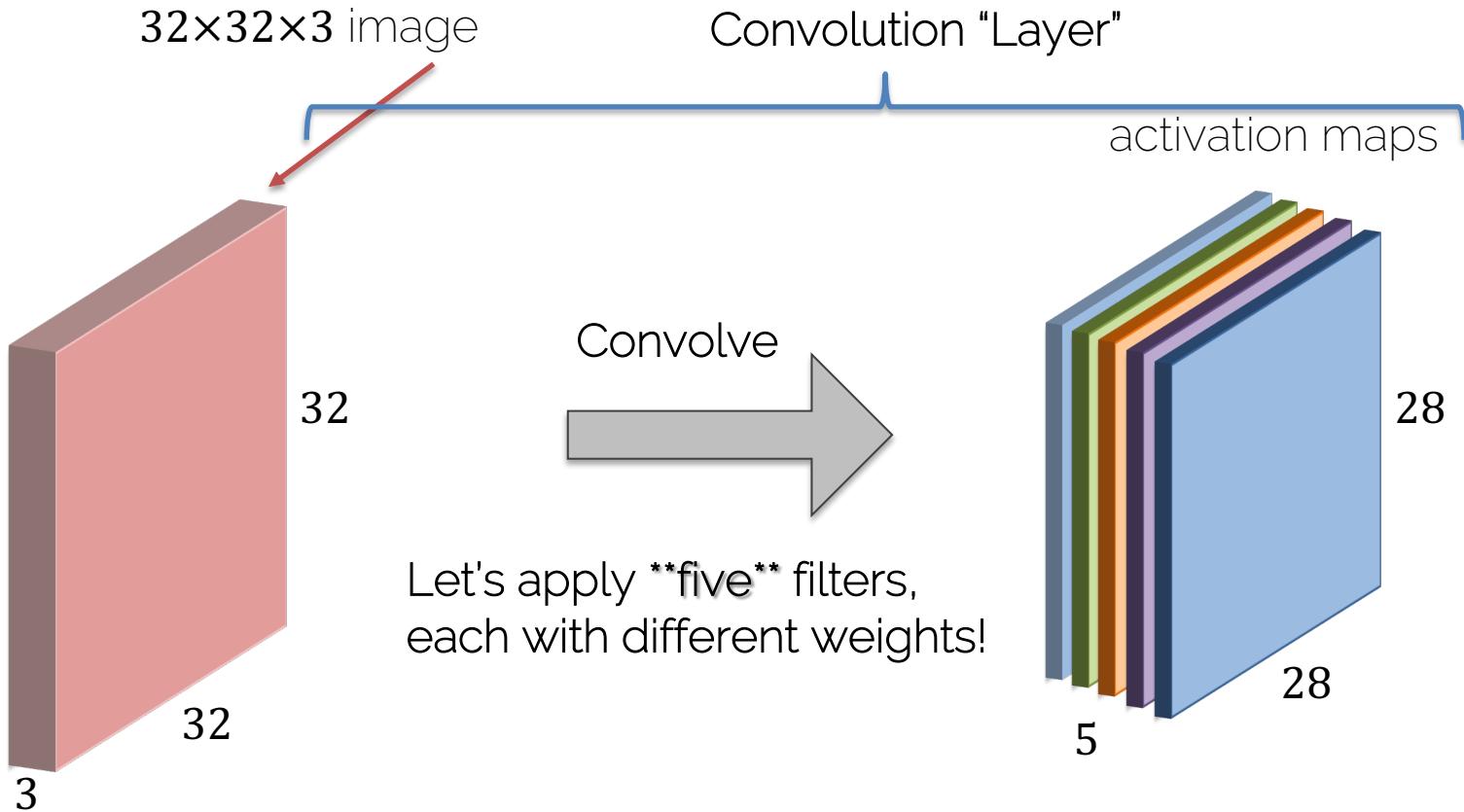
# Convolutions on RGB Images



# Convolution Layer

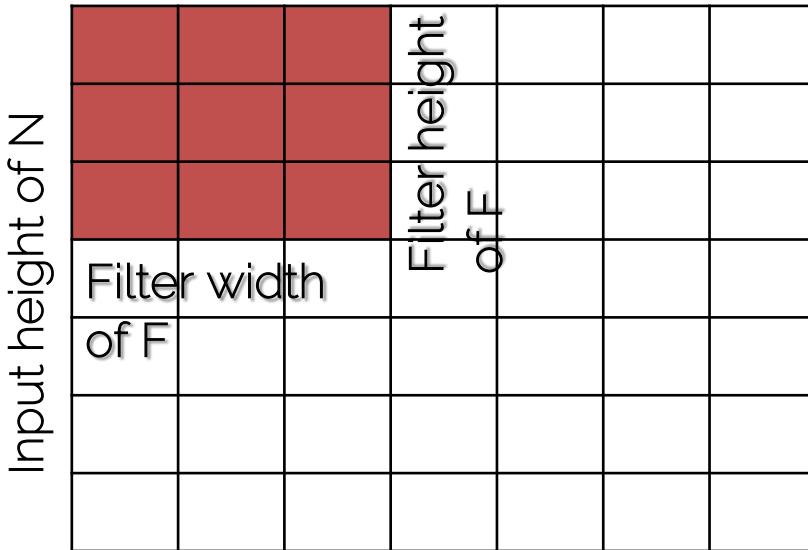


# Convolution Layer



# Convolution Layers: Dimensions

Input width of  $N$



Input:  $N \times N$

Filter:  $F \times F$

Stride:  $S$

Output:  $(\frac{N-F}{S} + 1) \times (\frac{N-F}{S} + 1)$

$$N = 7, F = 3, S = 1: \quad \frac{7-3}{1} + 1 = 5$$

$$N = 7, F = 3, S = 2: \quad \frac{7-3}{2} + 1 = 3$$

$$N = 7, F = 3, S = 3: \quad \frac{7-3}{3} + 1 = 2.3333$$



Fractions are illegal

# Convolution Layers: Padding

Image 7x7 + zero padding

o	o	o	o	o	o	o	o	o
o								o
o								o
o								o
o								o
o								o
o								o
o								o
o	o	o	o	o	o	o	o	o

Types of convolutions:

- Valid convolution: using no padding
- Same convolution: output=input size

$$\text{Set padding to } P = \frac{F-1}{2}$$

# Convolution Layers: Dimensions

Remember: Output =  $\left(\frac{N+2\cdot P-F}{S} + 1\right) \times \left(\frac{N+2\cdot P-F}{S} + 1\right)$

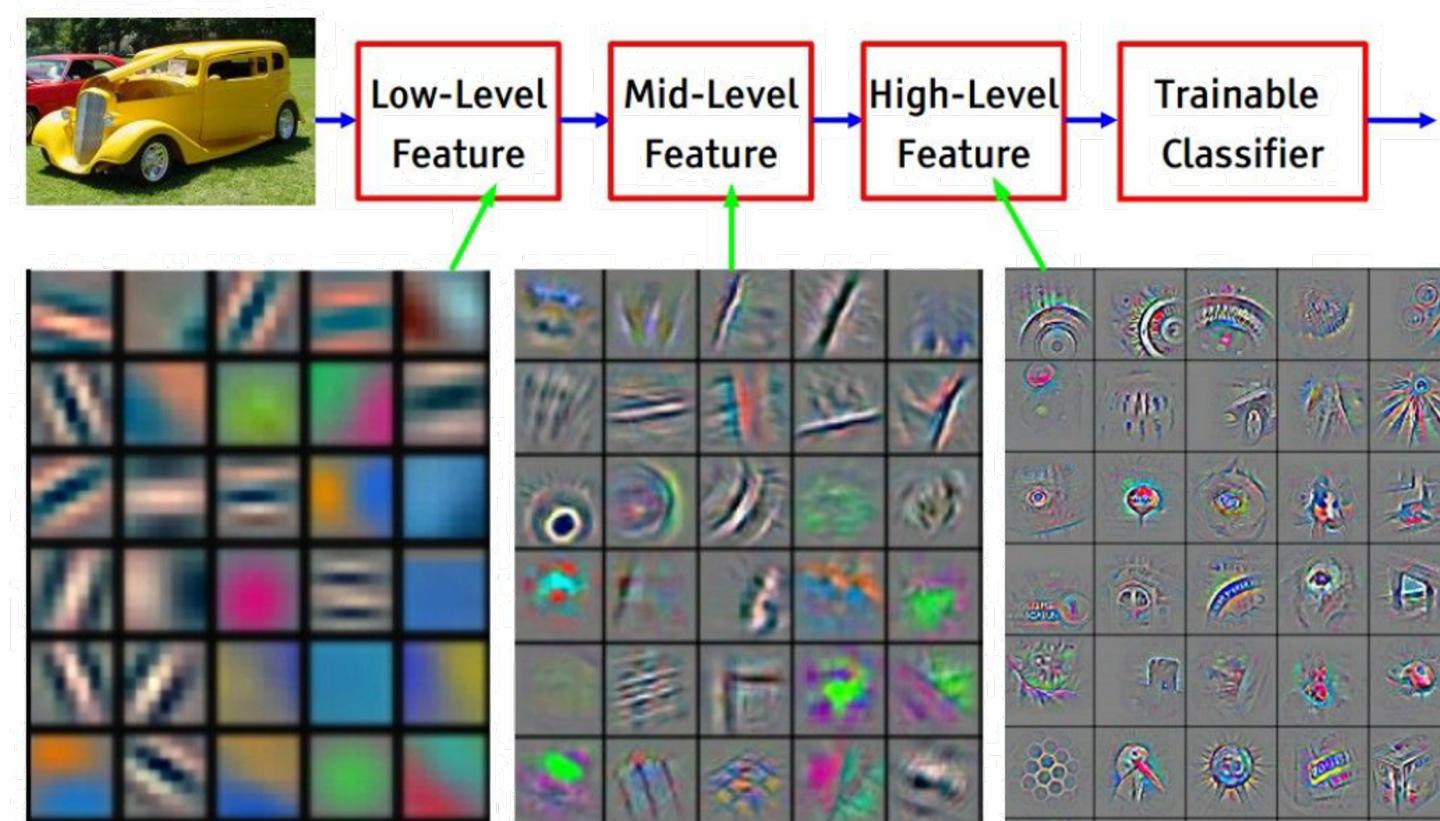


**REMARK:** in practice, typically **integer division** is used  
(i.e., apply the **floor-operator!**)

*Example:* 3x3 conv with same padding and strides of 2  
on an 64x64 RGB image ->  $N = 64$ ,  $F = 3$ ,  $P = 1$ ,  $S = 2$

$$\begin{aligned}\text{Output: } & \left(\frac{64+2\cdot 1-3}{2} + 1\right) \times \left(\frac{64+2\cdot 1-3}{2} + 1\right) \\ &= \textcolor{brown}{floor}(32.5) \times \textcolor{brown}{floor}(32.5) \\ &= 32 \times 32\end{aligned}$$

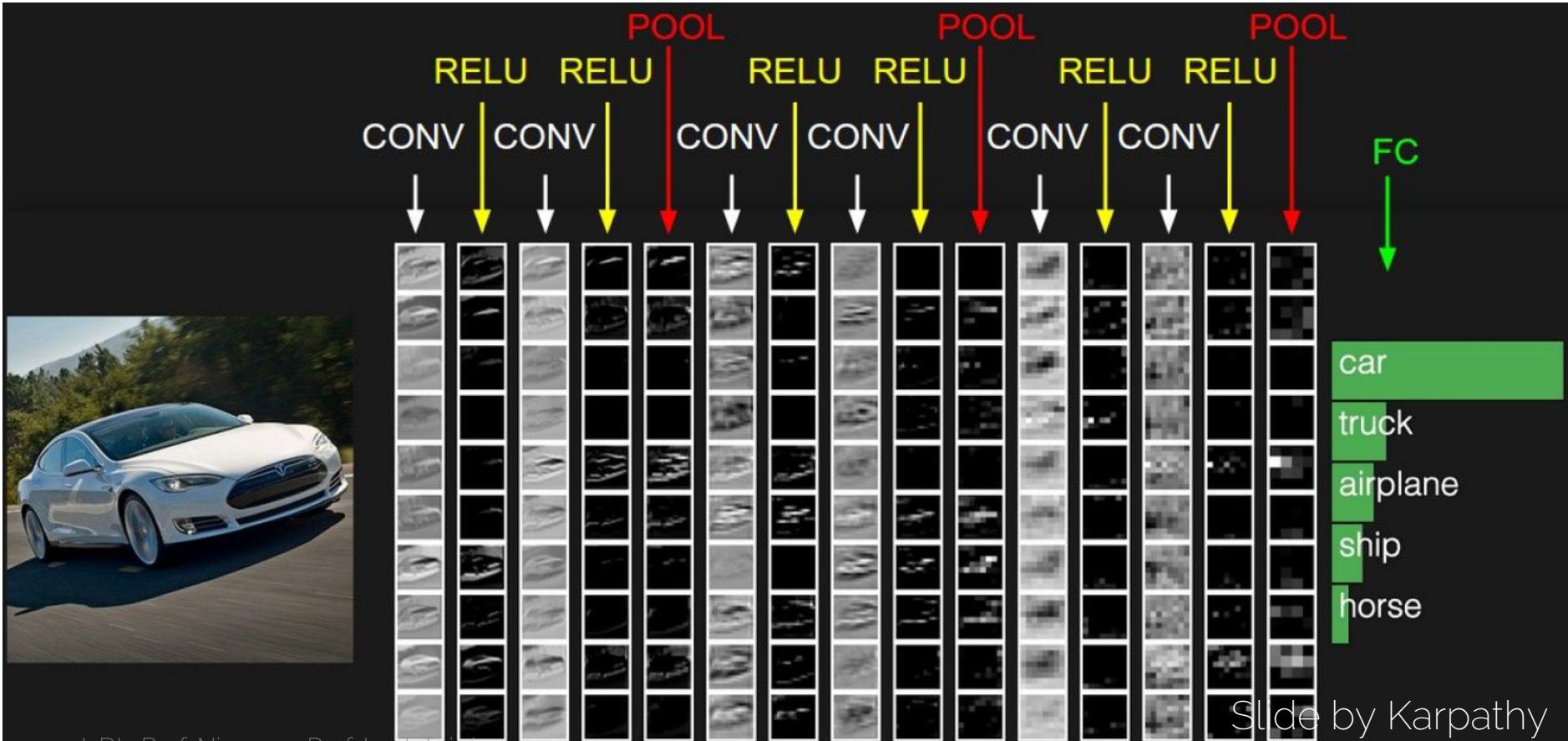
# CNN Learned Filters



Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]

I2DL: Prof. Niessner, Prof. Leal-Taixe

# CNN Prototype

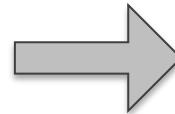


# Pooling Layer: Max Pooling

Single depth slice of input

3	1	3	5
6	0	7	9
3	2	1	4
0	2	4	3

Max pool with  
**2×2** filters and stride 2

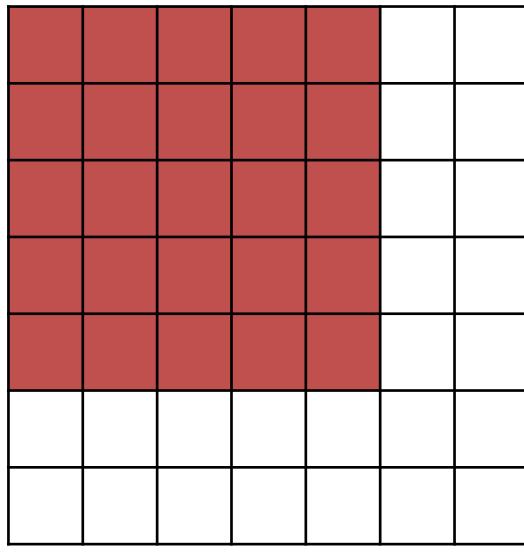


'Pooled' output

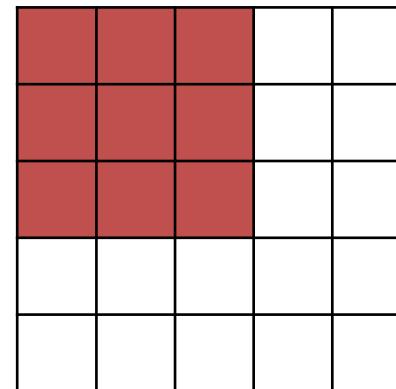
6	9
3	4

# Receptive Field

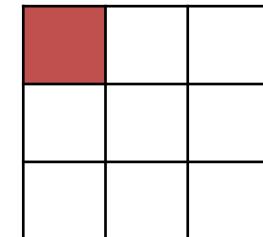
- Spatial extent of the connectivity of a convolutional filter



7x7 input



3x3 output



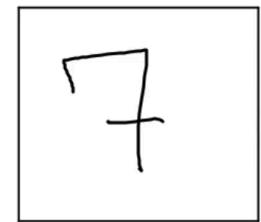
5x5 receptive field on the original input:  
one output value is connected to 25 input pixels

# Lecture 10 – CNNs (part 2)

# Classic Architectures

# LeNet

- Digit recognition: 10 classes



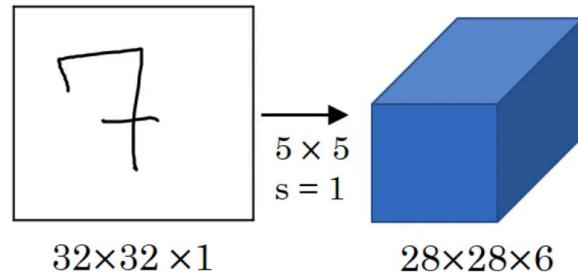
$32 \times 32 \times 1$

Input:  $32 \times 32$  grayscale images

*This one: Labeled as class "7"*

# LeNet

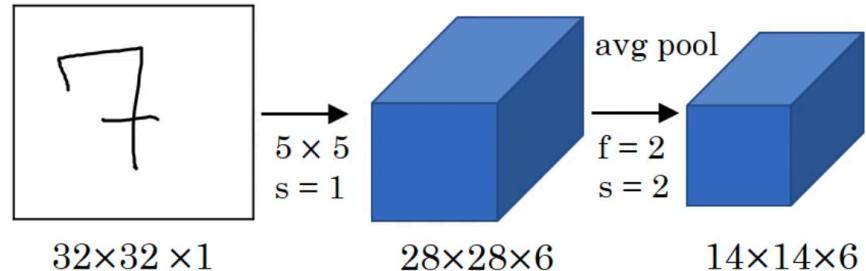
- Digit recognition: 10 classes



- Valid convolution: size shrinks
- How many conv filters are there in the first layer? 6

# LeNet

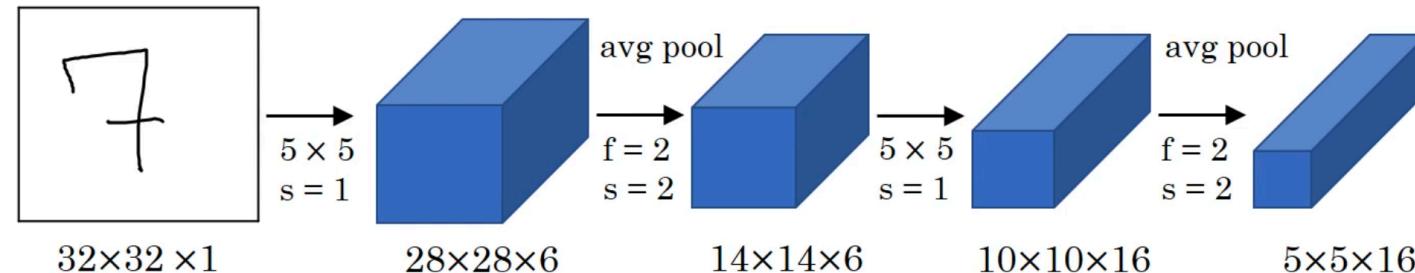
- Digit recognition: 10 classes



- At that time average pooling was used, now max pooling is much more common

# LeNet

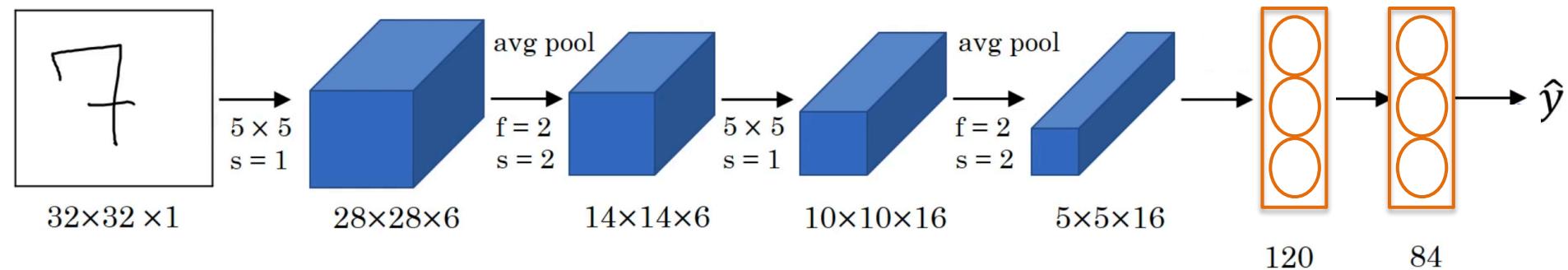
- Digit recognition: 10 classes



- Again valid convolutions, how many filters?

# LeNet

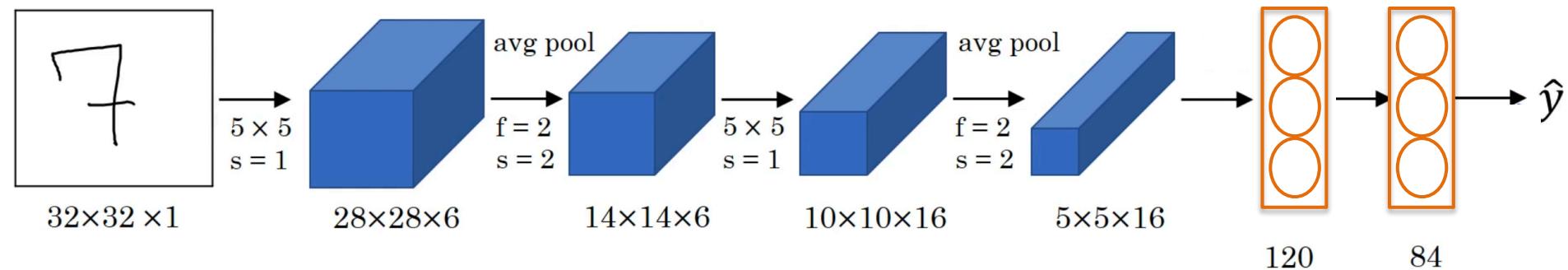
- Digit recognition: 10 classes



- Use of tanh/sigmoid activations → not common now!

# LeNet

- Digit recognition: 10 classes

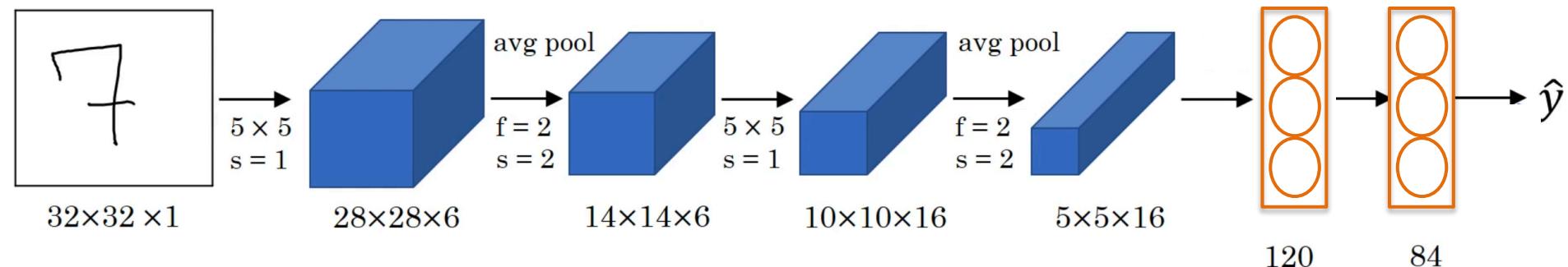


- Conv -> Pool -> Conv -> Pool -> Conv -> FC

# LeNet

- Digit recognition: 10 classes

60k parameters

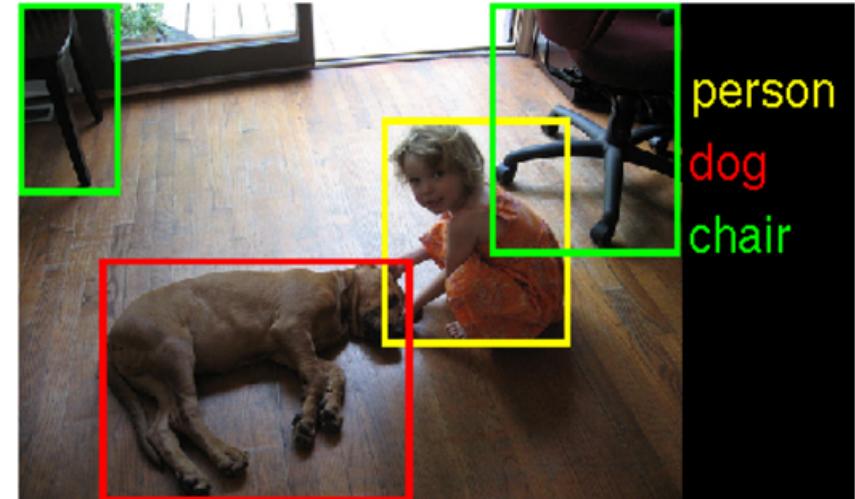
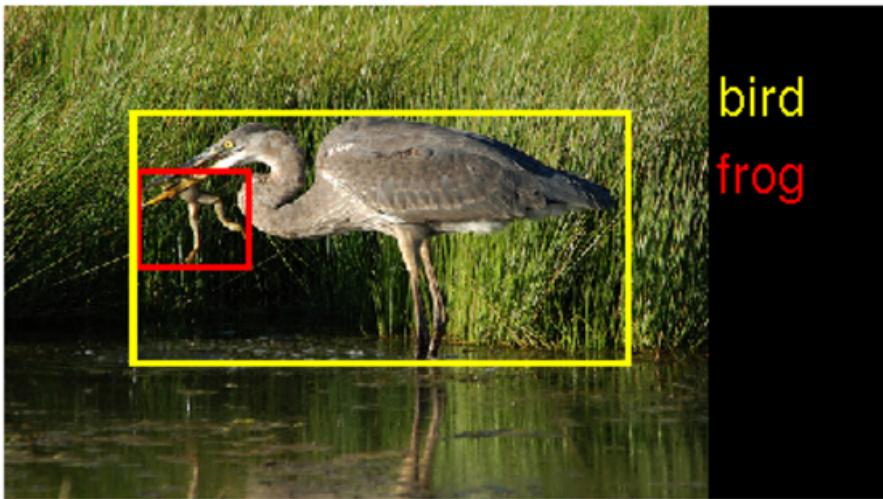


- Conv -> Pool -> Conv -> Pool -> Conv -> FC
- As we go deeper: Width, Height  $\downarrow$  Number of Filters  $\uparrow$

# Test Benchmarks

- ImageNet Dataset:

*ImageNet Large Scale Visual Recognition Competition (ILSVRC)*



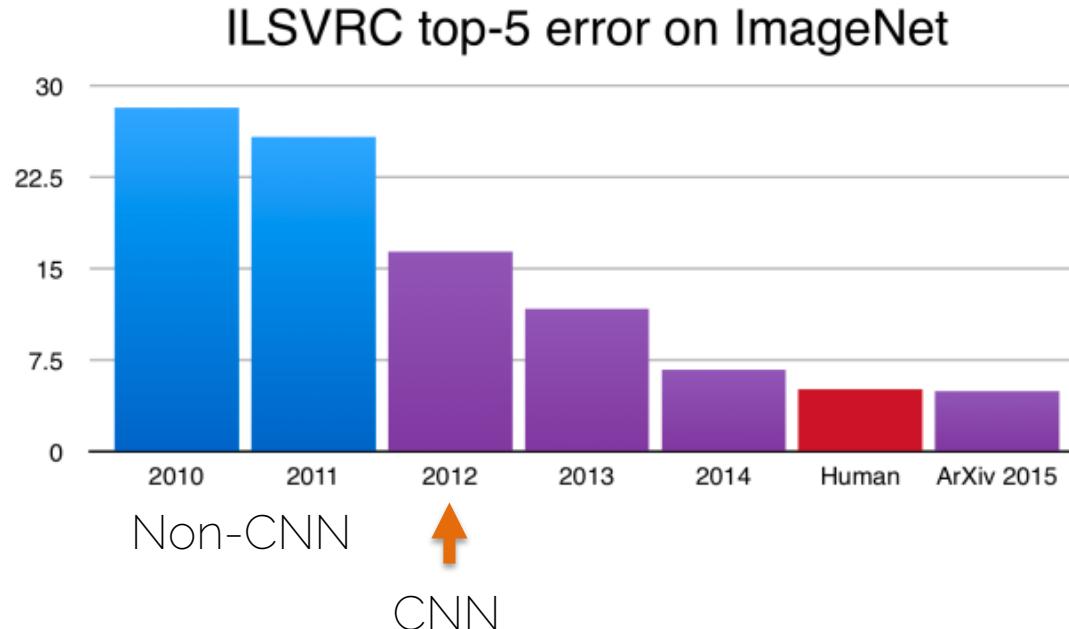
[Russakovsky et al., IJCV'15] "ImageNet Large Scale Visual Recognition Challenge."

# Common Performance Metrics

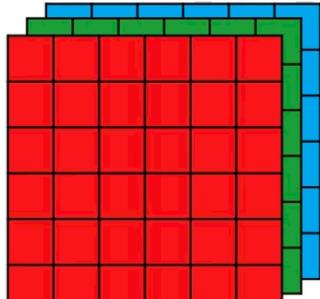
- **Top-1 score:** check if a sample's top class (i.e. the one with highest probability) is the same as its target label
- **Top-5 score:** check if your label is in your 5 first predictions (i.e. predictions with 5 highest probabilities)
- → **Top-5 error:** percentage of test samples for which the correct class was not in the top 5 predicted classes

# AlexNet

- Cut ImageNet error down in half



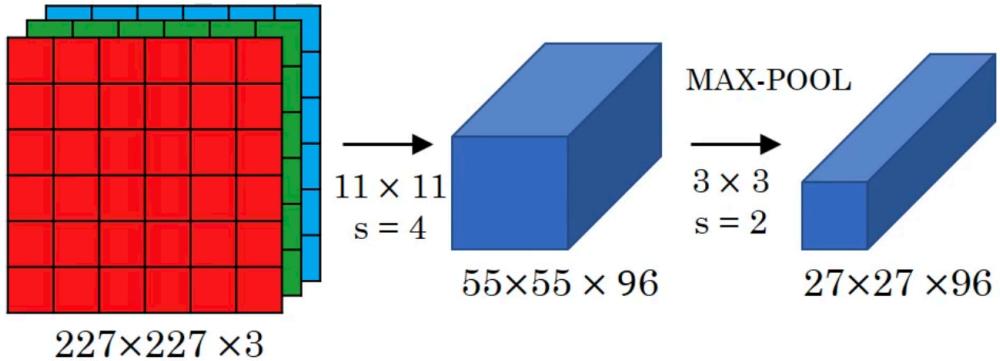
# AlexNet



227×227 ×3

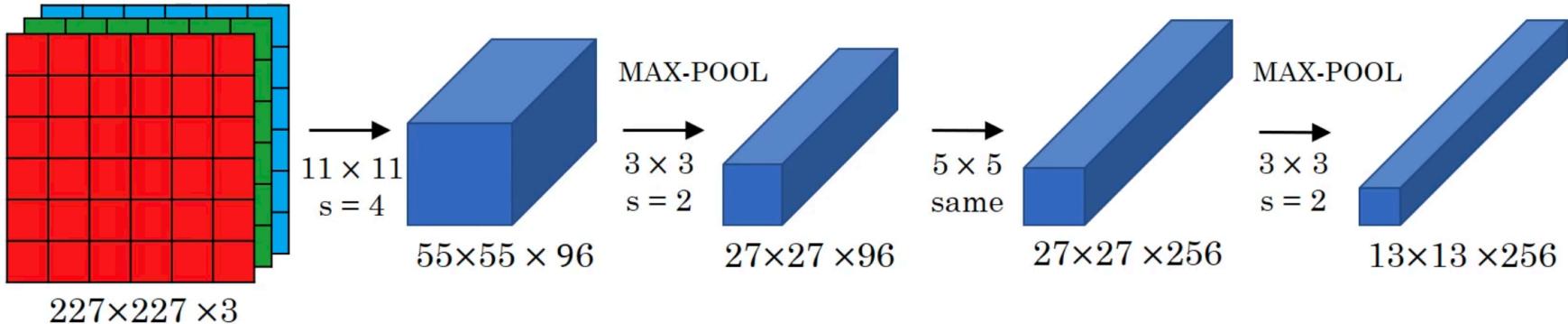
[Krizhevsky et al. NIPS'12] AlexNet

# AlexNet



[Krizhevsky et al. NIPS'12] AlexNet

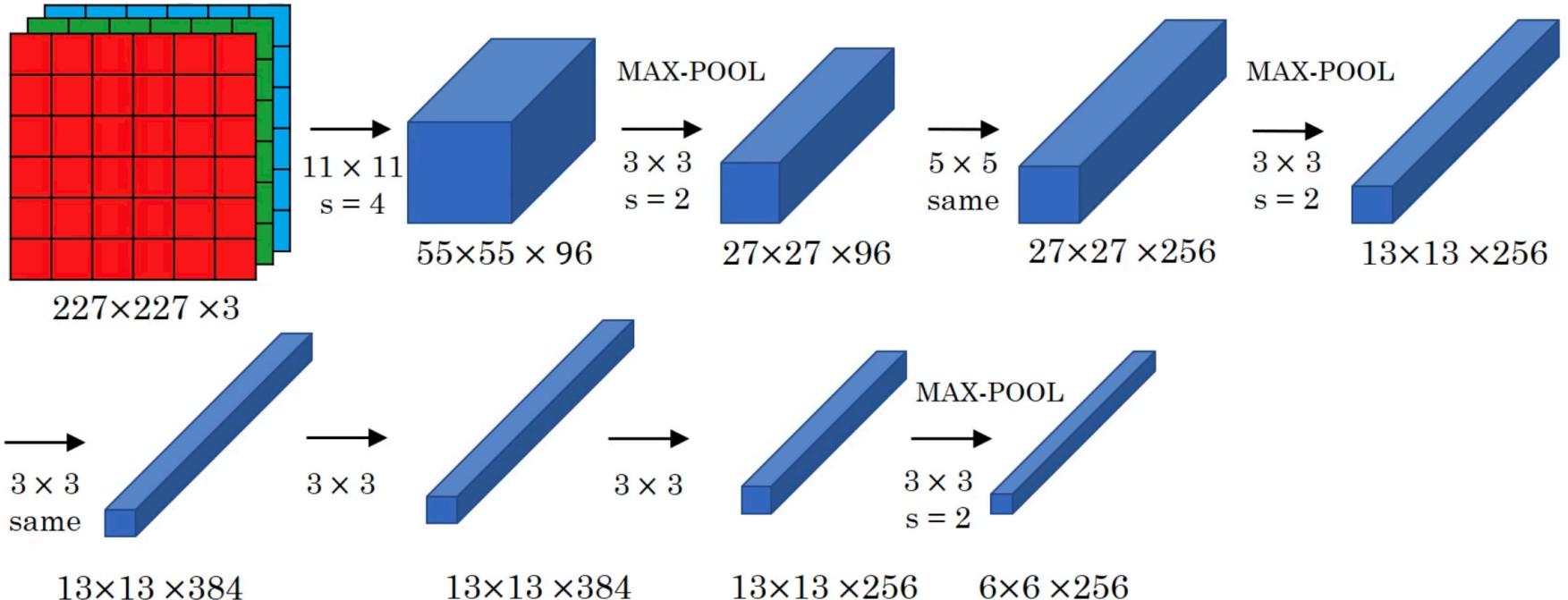
# AlexNet



- Use of same convolutions
- As with LeNet: Width, Height  $\downarrow$  Number of Filters  $\uparrow$

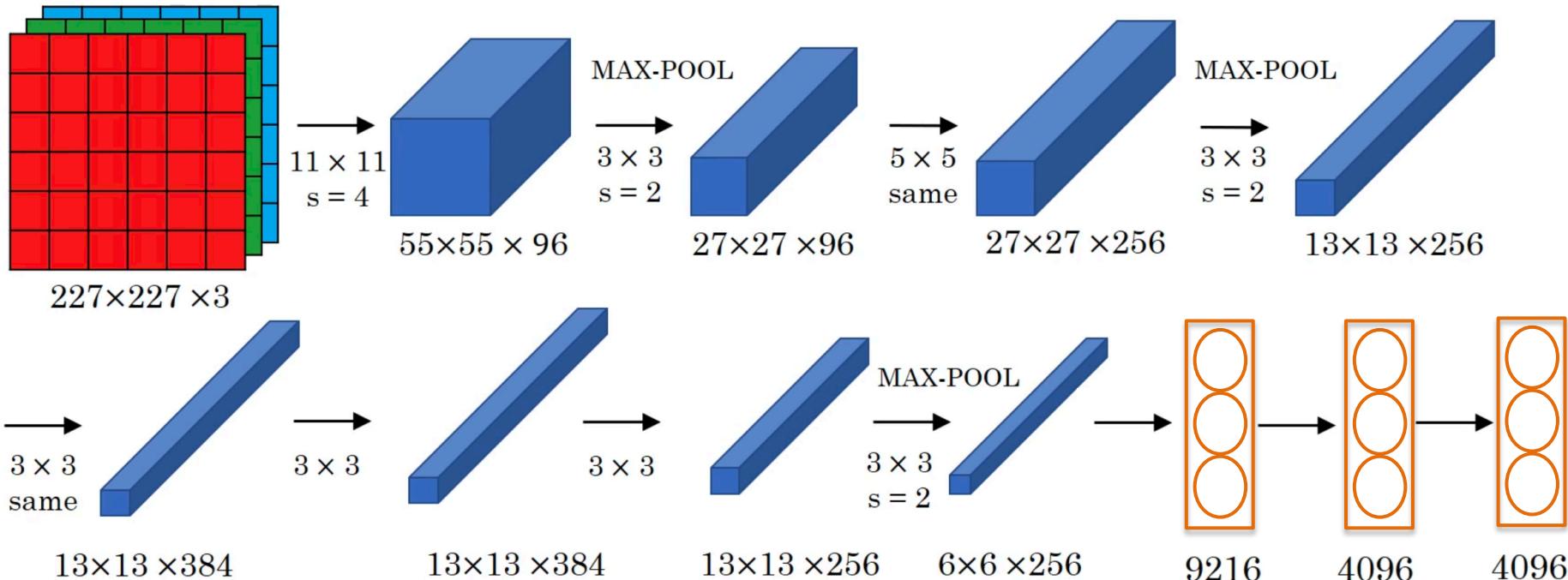
[Krizhevsky et al. NIPS'12] AlexNet

# AlexNet



[Krizhevsky et al. NIPS'12] AlexNet

# AlexNet



- Softmax for 1000 classes

[Krizhevsky et al. NIPS'12] AlexNet

# AlexNet

- Similar to LeNet but much bigger (~1000 times)
- Use of ReLU instead of tanh/sigmoid

60M parameters

[Krizhevsky et al. NIPS'12] AlexNet

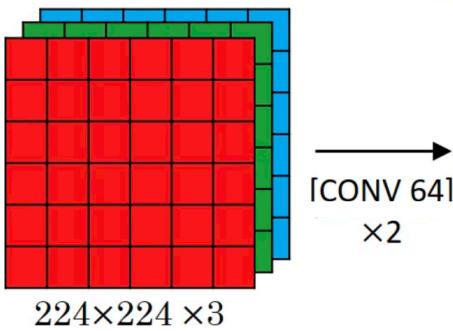
# VGGNet

- Striving for simplicity
- CONV =  $3 \times 3$  filters with stride 1, same convolutions
- MAXPOOL =  $2 \times 2$  filters with stride 2

[Simonyan and Zisserman ICLR'15] VGGNet

# VGGNet

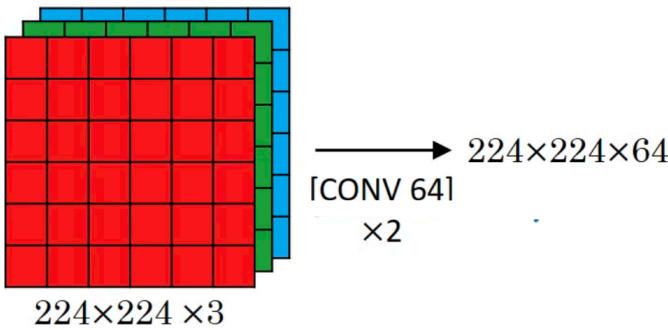
Conv=3x3,s=1,same  
Maxpool=2x2,s=2



[Simonyan and Zisserman ICLR'15] VGGNet

# VGGNet

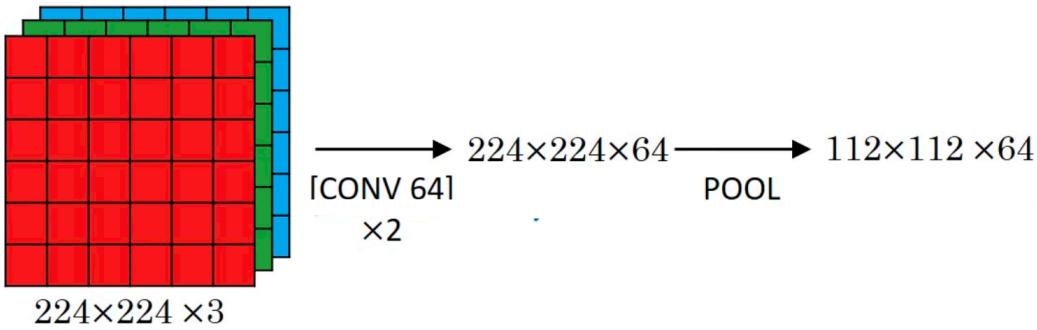
Conv=3x3,s=1,same  
Maxpool=2x2,s=2



[Simonyan and Zisserman ICLR'15] VGGNet

# VGGNet

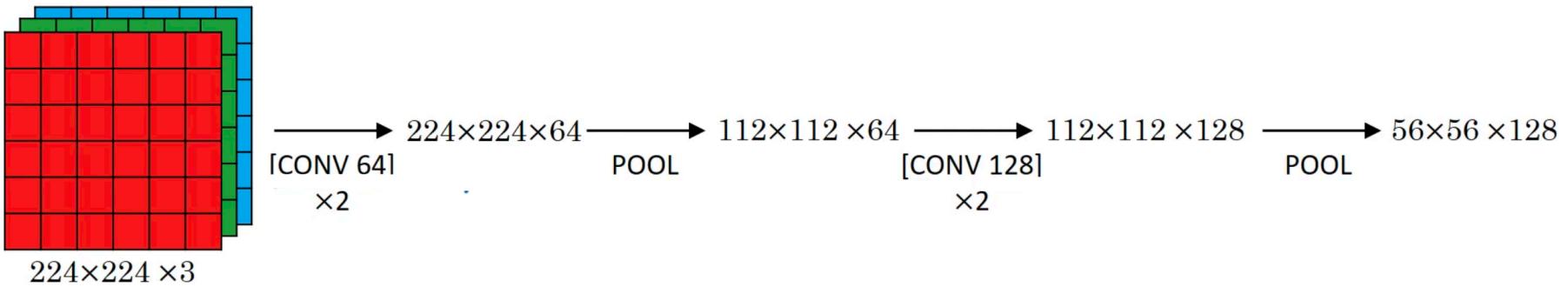
Conv=3x3,s=1,same  
Maxpool=2x2,s=2



[Simonyan and Zisserman ICLR'15] VGGNet

# VGGNet

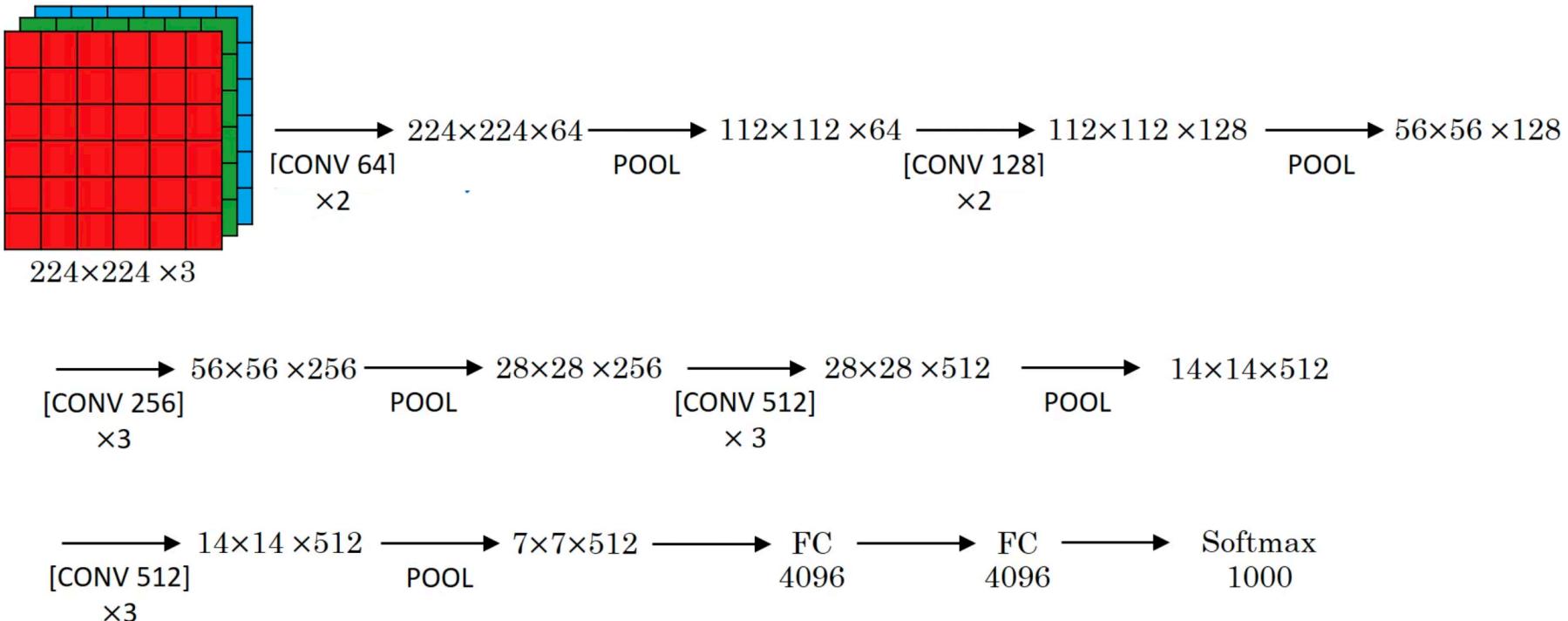
Conv=3x3,s=1,same  
Maxpool=2x2,s=2



[Simonyan and Zisserman ICLR'15] VGGNet

# VGGNet

Conv=3x3,s=1,same  
Maxpool=2x2,s=2



[Simonyan and Zisserman ICLR'15] VGGNet

# VGGNet

- Conv -> Pool -> Conv -> Pool -> Conv -> FC
- As we go deeper: Width, Height  Number of Filters 
- Called VGG-16: 16 layers that have weights
  - 138M parameters
- Large but simplicity makes it appealing

[Simonyan and Zisserman ICLR'15] VGGNet

# VGGNet

- A lot of architectures were analyzed

ConvNet Configuration					
A	A-LRN	B	C	D	E
11 weight layers	11 weight layers	13 weight layers	16 weight layers	16 weight layers	19 weight layers
input (224 × 224 RGB image)					
conv3-64	conv3-64 <b>LRN</b>	conv3-64 <b>conv3-64</b>	conv3-64 conv3-64	conv3-64 conv3-64	conv3-64 conv3-64
maxpool					
conv3-128	conv3-128	conv3-128 <b>conv3-128</b>	conv3-128 conv3-128	conv3-128 conv3-128	conv3-128 conv3-128
maxpool					
conv3-256	conv3-256	conv3-256 conv3-256	conv3-256 conv3-256	conv3-256 conv3-256 <b>conv1-256</b>	conv3-256 conv3-256 <b>conv3-256</b> <b>conv3-256</b>
maxpool					
conv3-512	conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512 <b>conv1-512</b>	conv3-512 conv3-512 <b>conv3-512</b>	conv3-512 conv3-512 conv3-512 <b>conv3-512</b>
maxpool					
conv3-512	conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512 <b>conv1-512</b>	conv3-512 conv3-512 <b>conv3-512</b>	conv3-512 conv3-512 conv3-512 <b>conv3-512</b>
maxpool					
FC-4096					
FC-4096					
FC-1000					
soft-max					

[Simonyan and Zisserman 2014]

Table 2: Number of parameters (in millions).

Network	A,A-LRN	B	C	D	E
Number of parameters	133	133	134	138	144

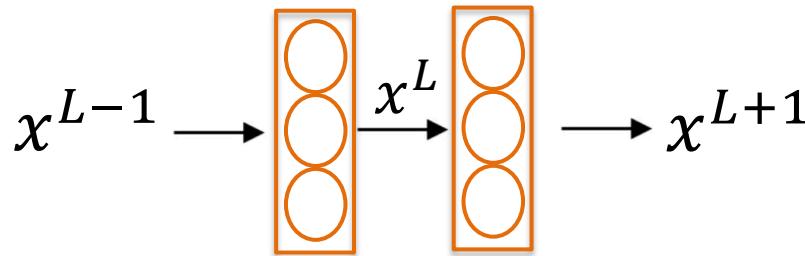
# Skip Connections

# The Problem of Depth

- As we add more and more layers, training becomes harder
- Vanishing and exploding gradients
- How can we train very deep nets?

# Residual Block

- Two layers



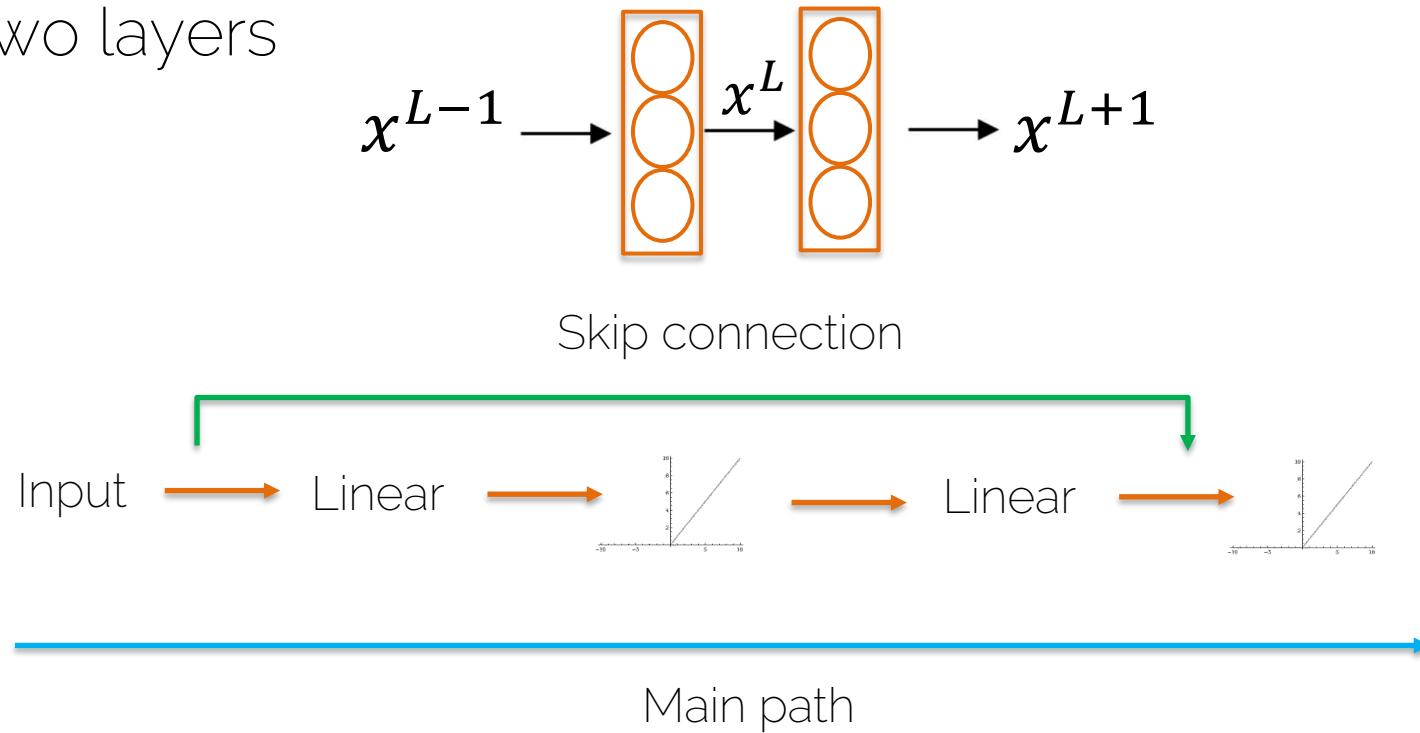
Input  $\longrightarrow W^L x^{L-1} + b^L \xrightarrow{\text{Linear}} x^L = f(W^L x^{L-1} + b^L) \xrightarrow{\text{Non-linearity}}$

A graph showing a straight line passing through the origin (0,0) with a positive slope, representing the linear function  $f(x) = x$ . The x-axis ranges from -10 to 10, and the y-axis ranges from -10 to 10.

$\longrightarrow x^{L+1} = f(W^{L+1} x^L + b^{L+1})$

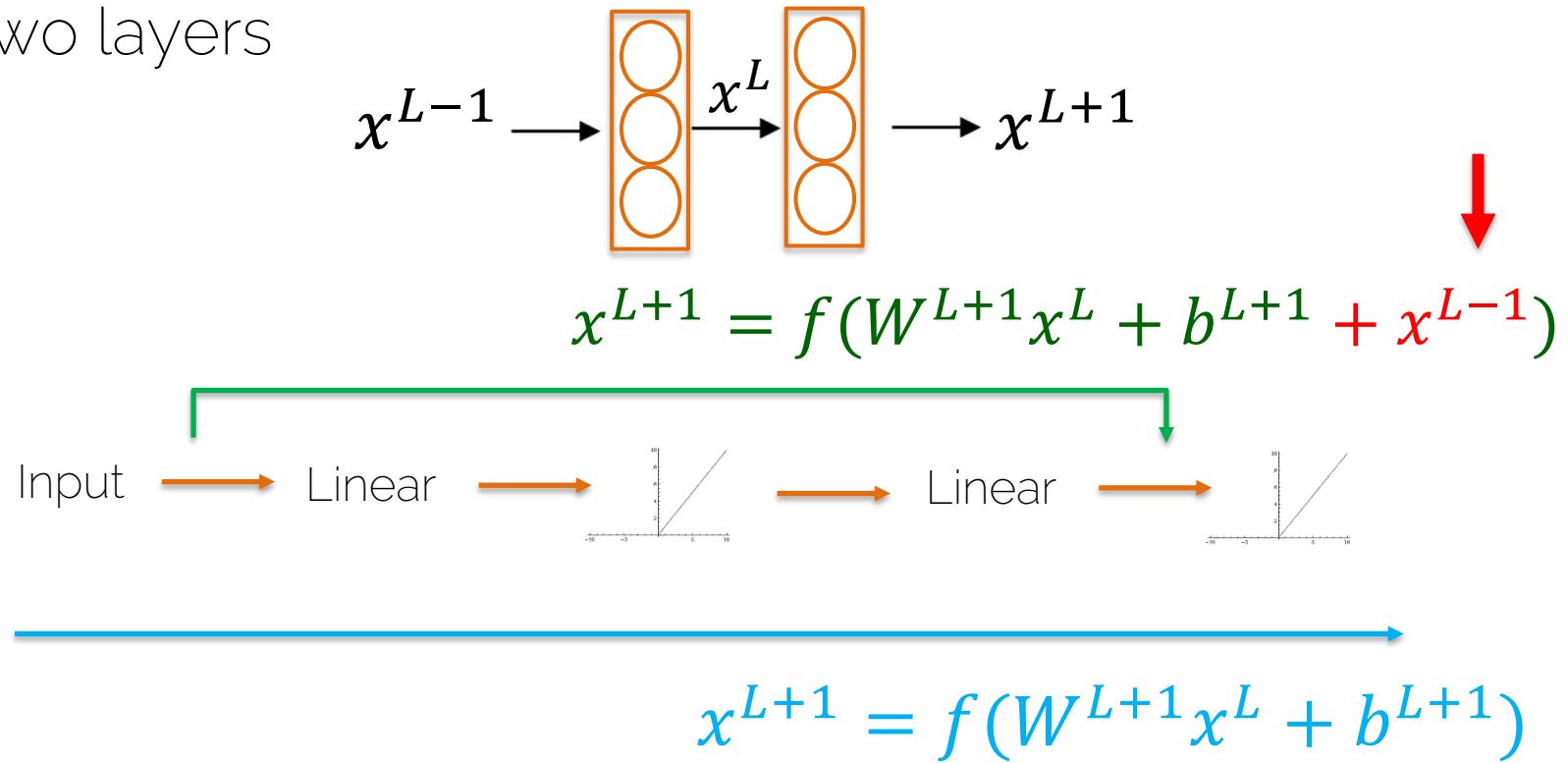
# Residual Block

- Two layers



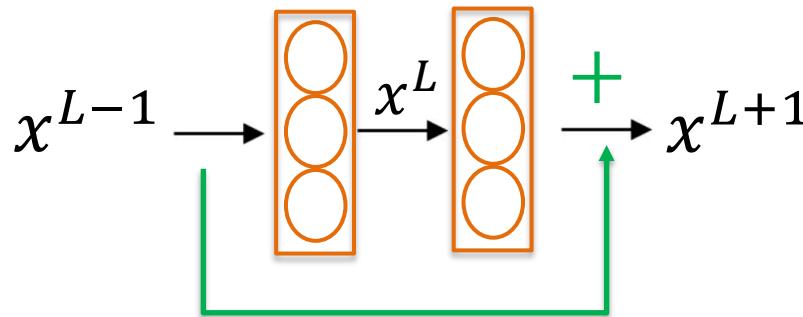
# Residual Block

- Two layers



# Residual Block

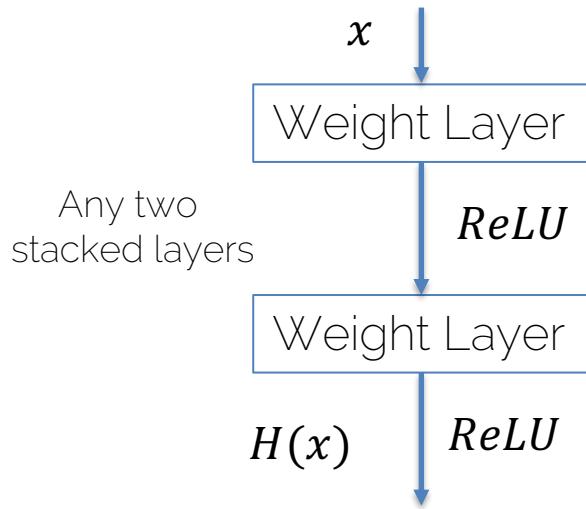
- Two layers



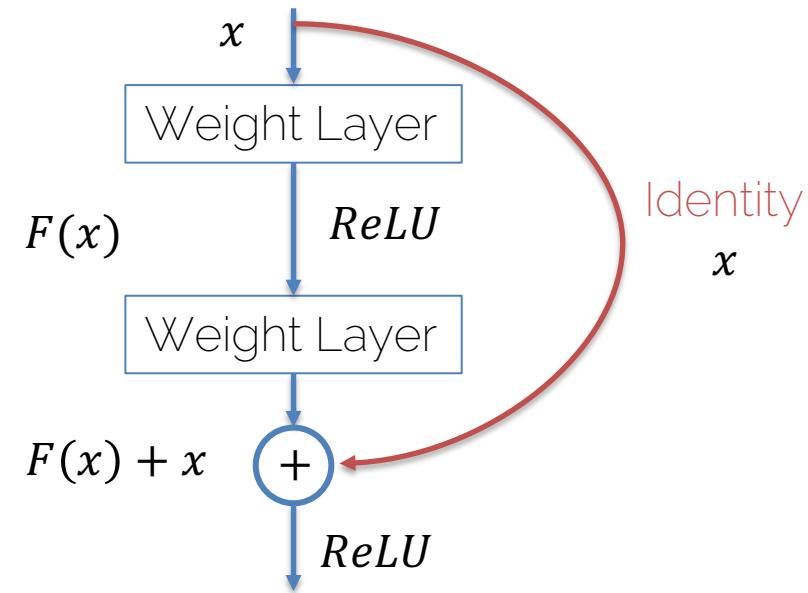
- Usually use a same convolution since we need same dimensions
- Otherwise we need to convert the dimensions with a matrix of learned weights or zero padding

# ResNet Block

Plain Net



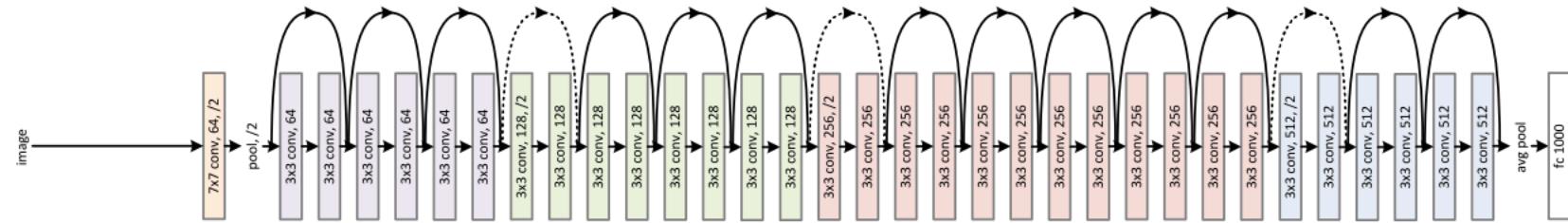
Residual Net



[He et al. CVPR'16] ResNet

# ResNet

34-layer residual

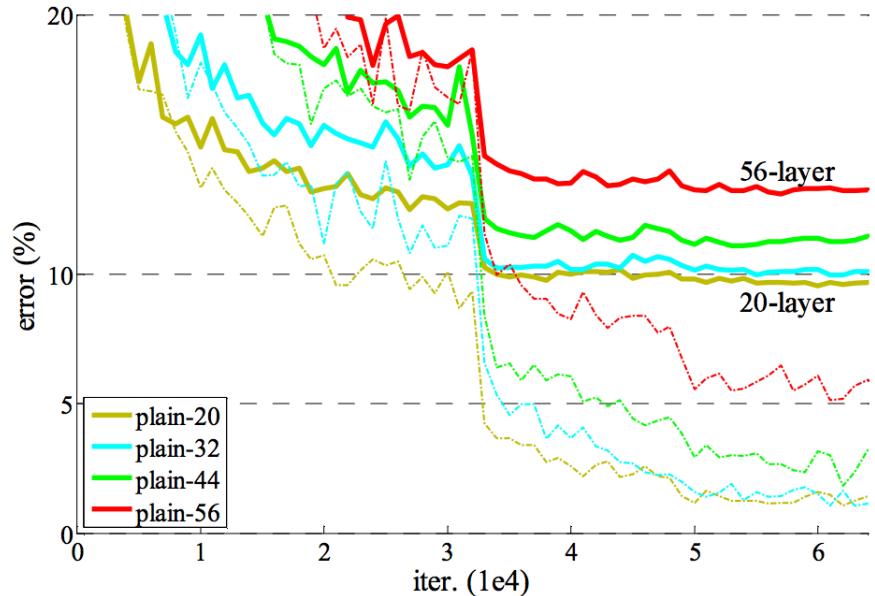


- Xavier/2 initialization
- SGD + Momentum (0.9)
- Learning rate 0.1, divided by 10 when plateau
- Mini-batch size 256
- Weight decay of 1e-5
- No dropout

ResNet-152:  
60M parameters

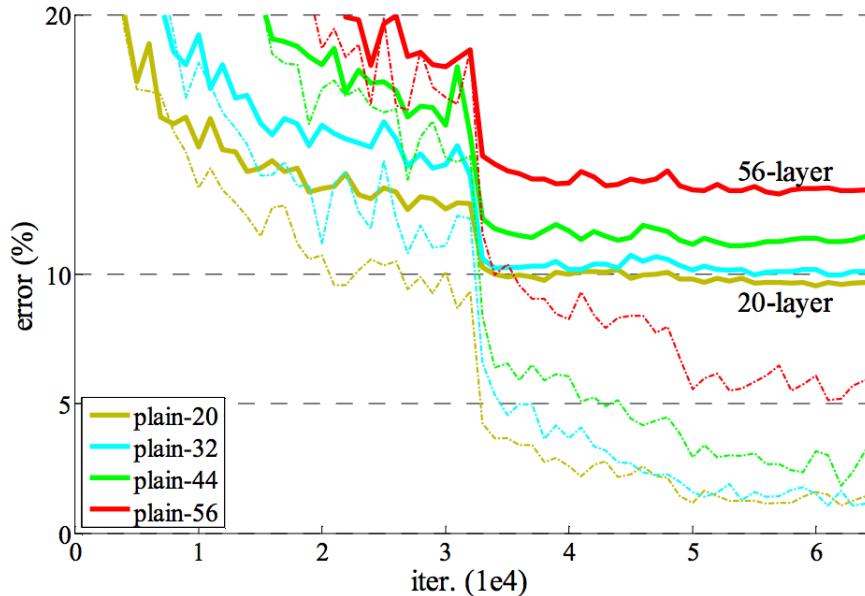
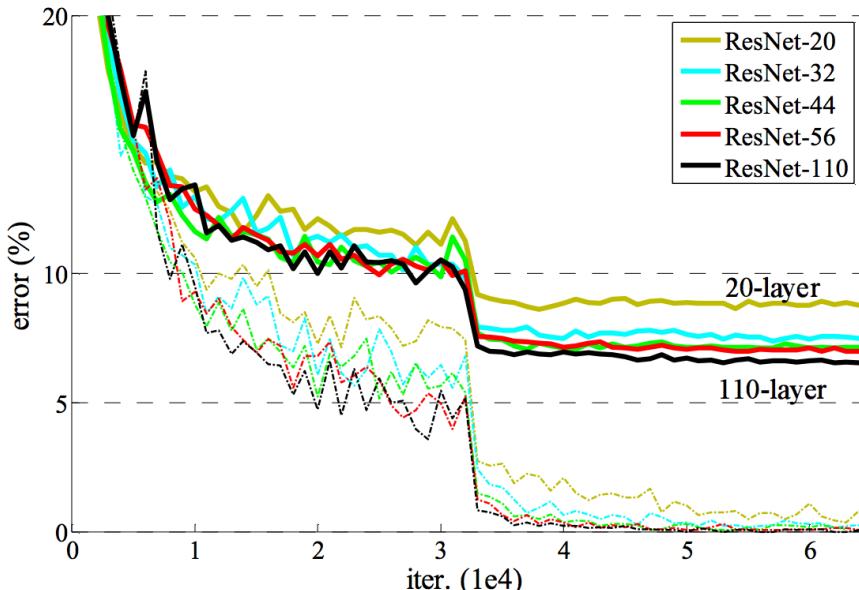
# ResNet

- If we make the network deeper, at some point performance starts to degrade

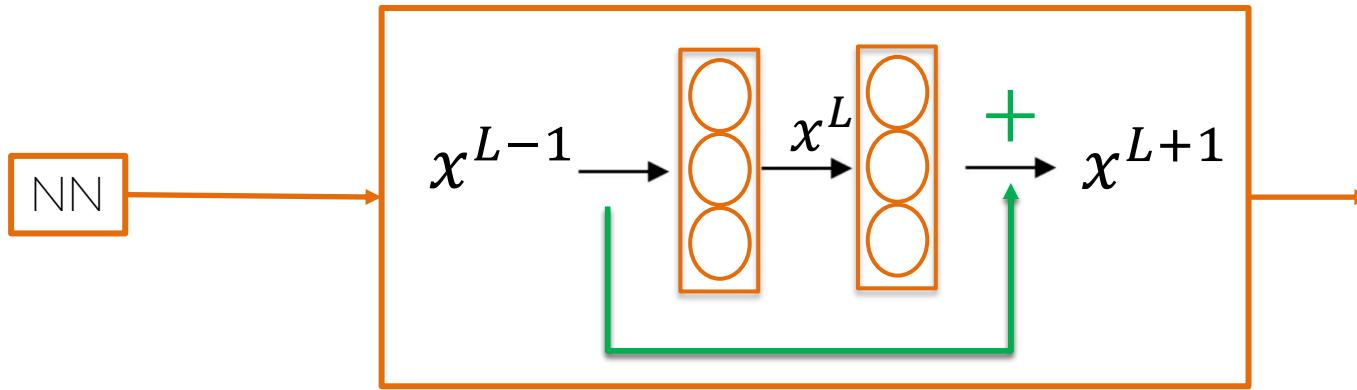


# ResNet

- If we make the network deeper, at some point performance starts to degrade

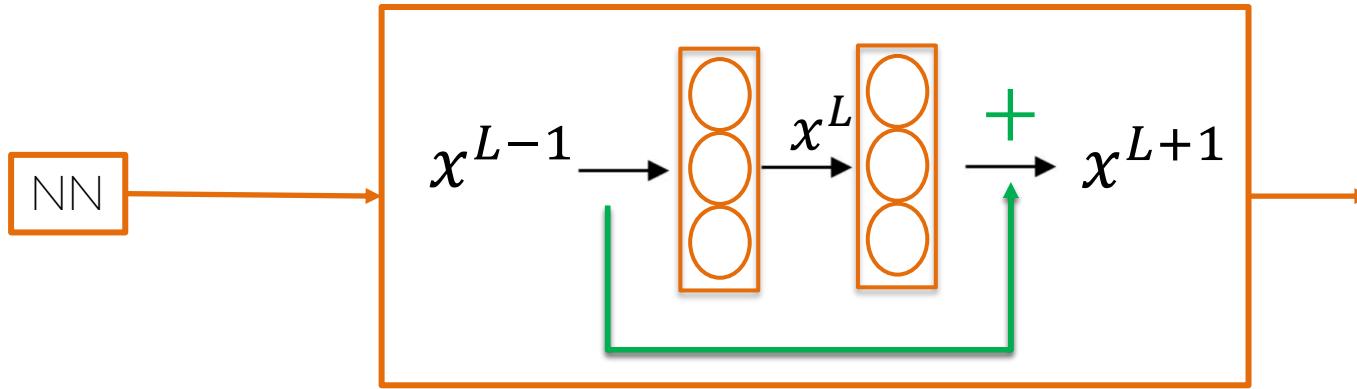


# Why do ResNets Work?



- How is this block really affecting me?

# Why do ResNets Work?

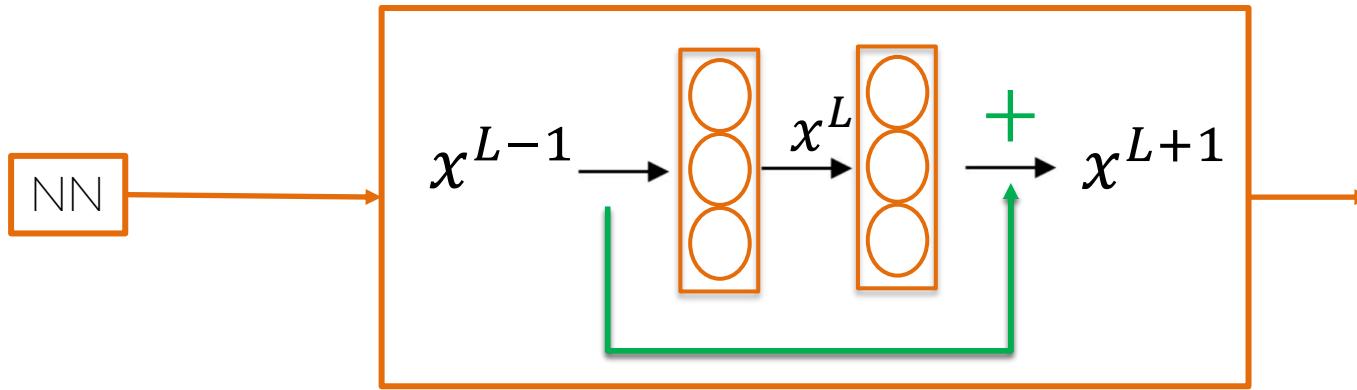


$$x^{L+1} = f(W^{L+1}x^L + b^{L+1} + x^{L-1})$$

~zero              ~zero

$$x^{L+1} = f(x^{L-1})$$

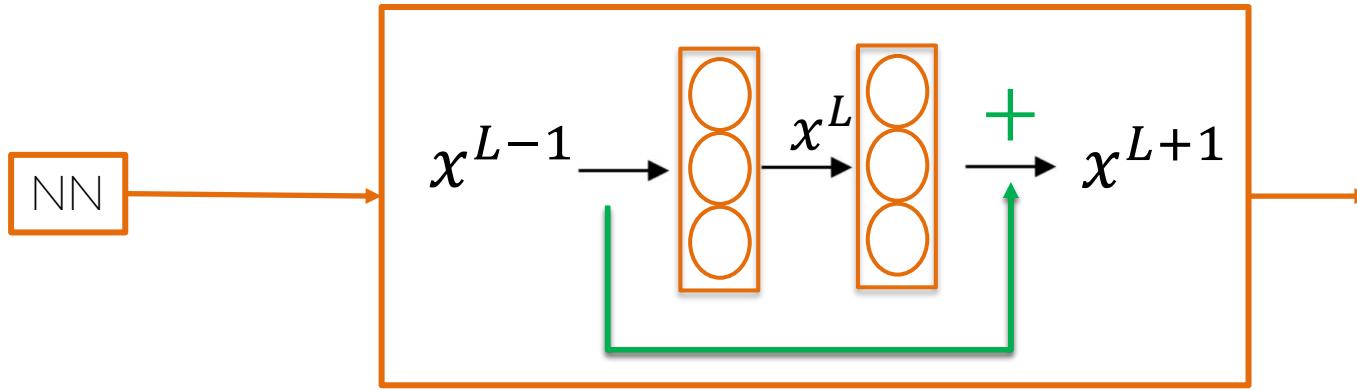
# Why do ResNets Work?



- We kept the same values and added a non-linearity

$$x^{L+1} = f(x^{L-1})$$

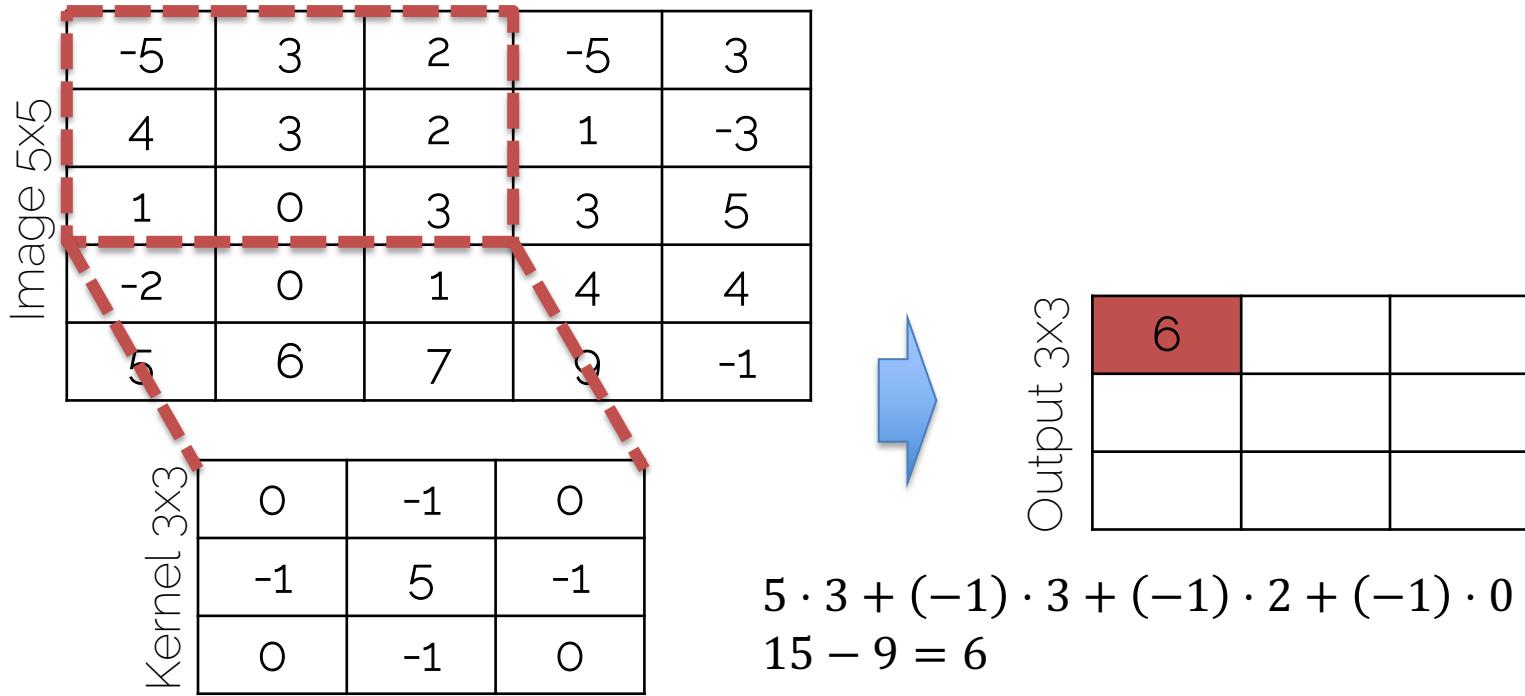
# Why do ResNets Work?



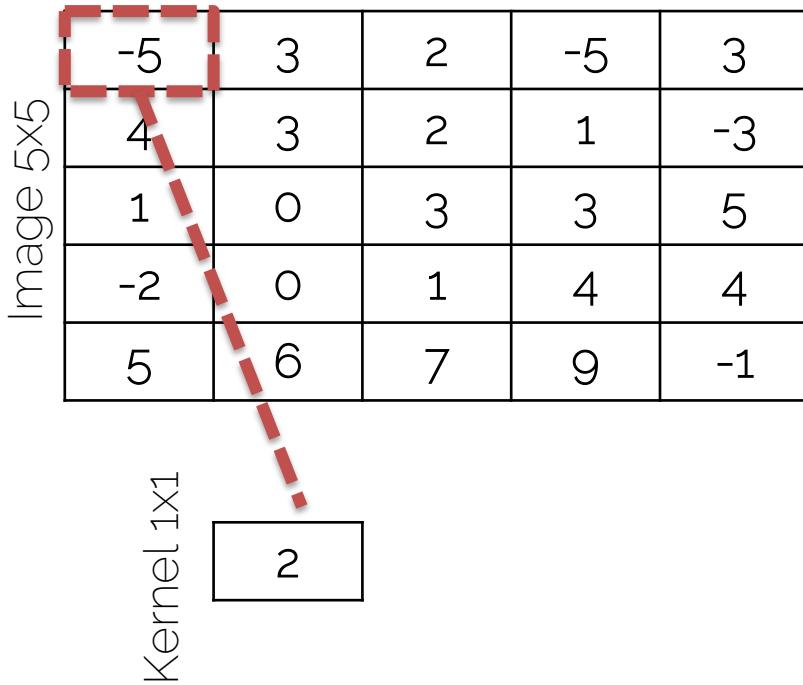
- The identity is easy for the residual block to learn
- Guaranteed it will not hurt performance, can only improve

# 1x1 Convolutions

# Recall: Convolutions on Images

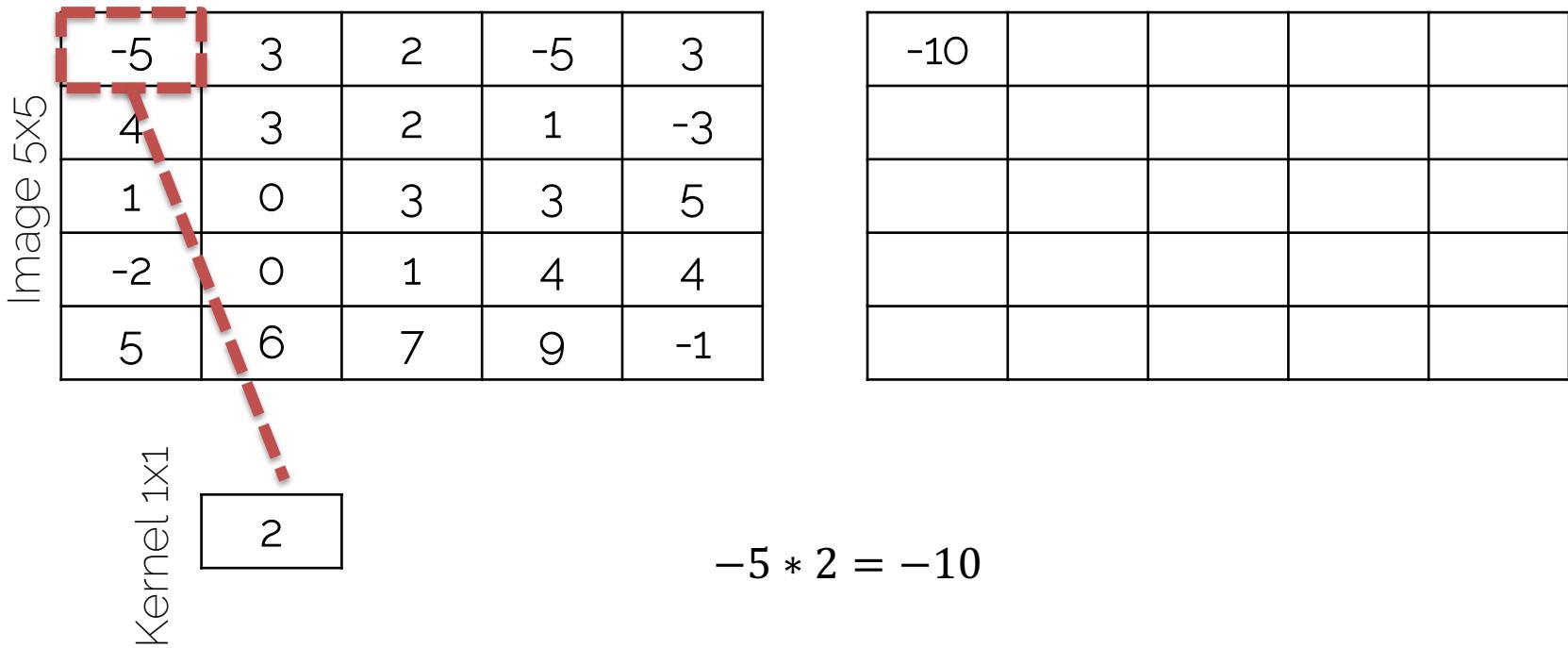


# 1x1 Convolution



What is the output size?

# 1x1 Convolution



# 1x1 Convolution

Image 5x5

-5	3	2	-5	3
4	3	2	1	-3
1	0	3	3	5
-2	0	1	4	4
5	6	7	9	-1

Kernel 1x1

2
---

$$-1 * 2 = -2$$

-10	6	4	-10	6
8	6	4	2	-6
2	0	6	6	10
-4	0	2	8	8
10	12	14	18	-2

# 1x1 Convolution

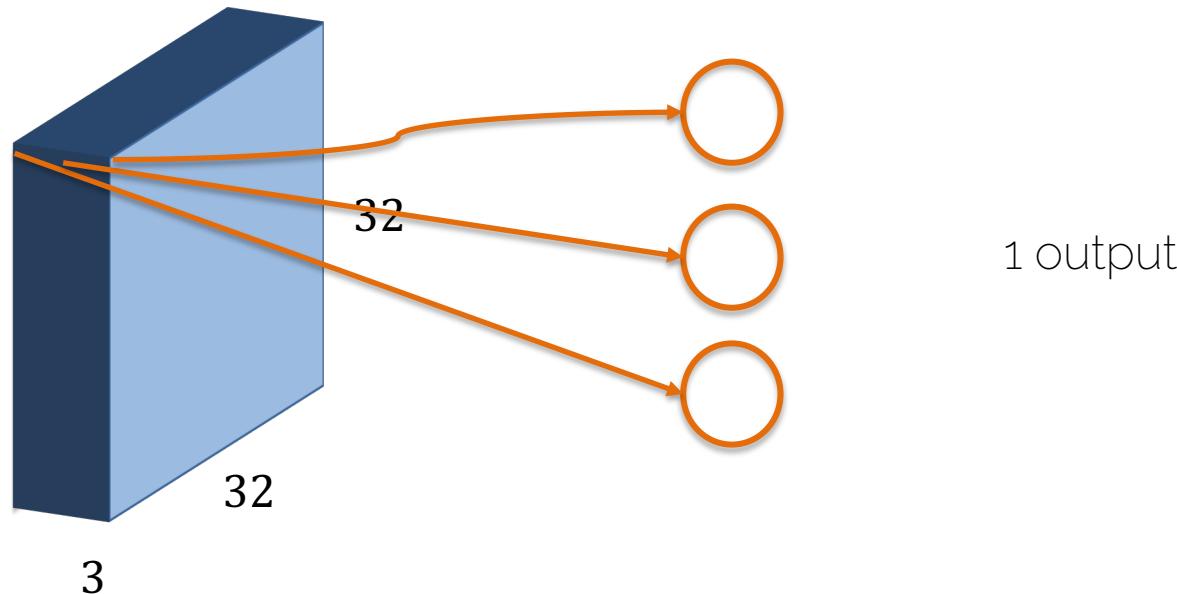
Image 5x5

-5	3	2	-5	3
4	3	2	1	-3
1	0	3	3	5
-2	0	1	4	4
5	6	7	9	-1

-10	6	4	-10	6
8	6	4	2	-6
2	0	6	6	10
-4	0	2	8	8
10	12	14	18	-2

- 1x1 kernel: keeps the dimensions and scales input

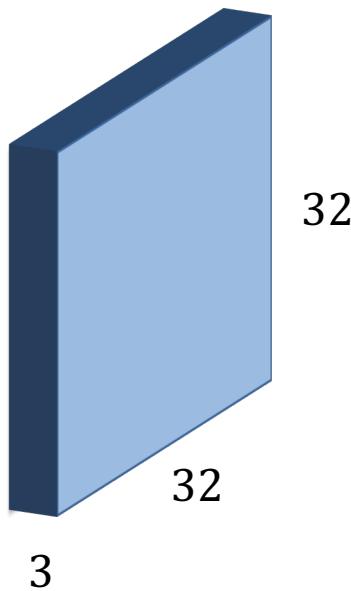
# 1x1 Convolution



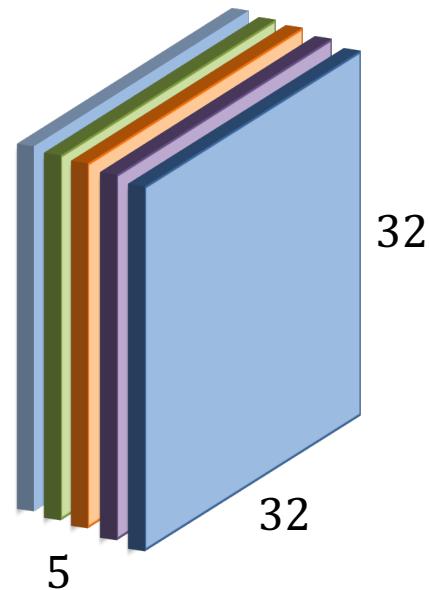
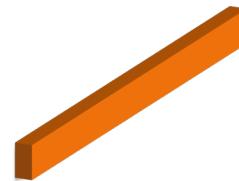
- Same as having a 3 neuron fully connected layer

# 1x1 Convolution

[Li et al. 2013]



*5 filters 1x1x3*



- As always we use more convolutional filters

# Using 1x1 Convolutions

- Use it to shrink the number of channels
- Further adds a non-linearity → one can learn more complex functions



# Inception Layer

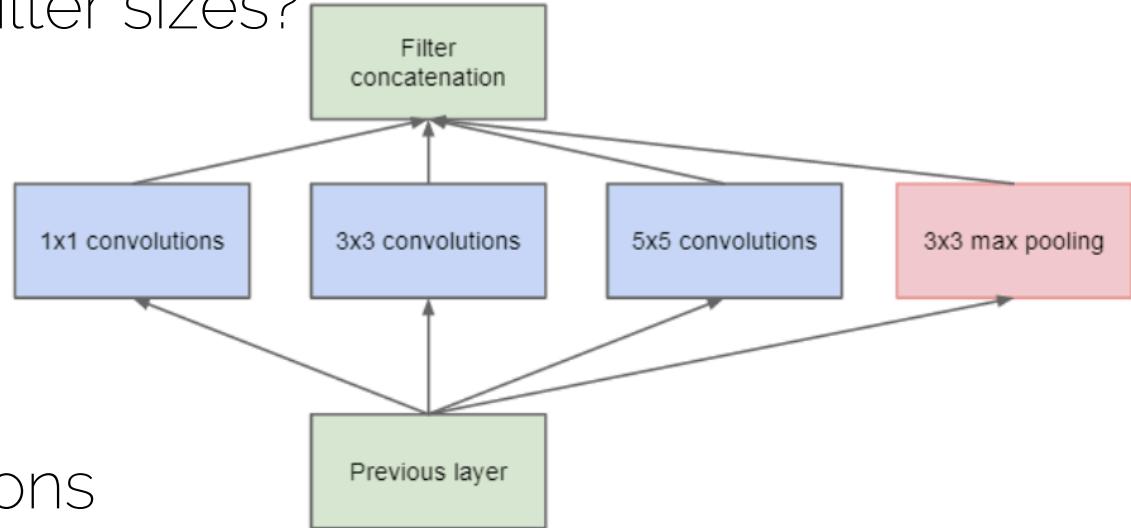
# Inception Layer

- Tired of choosing filter sizes?

- Use them all!

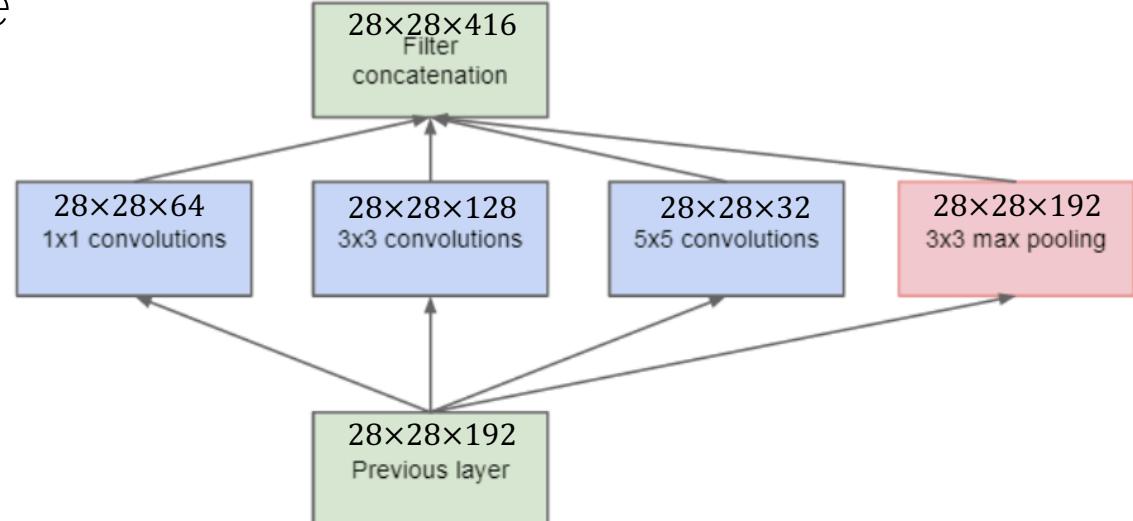
- All same convolutions

- 3x3 max pooling is with stride 1



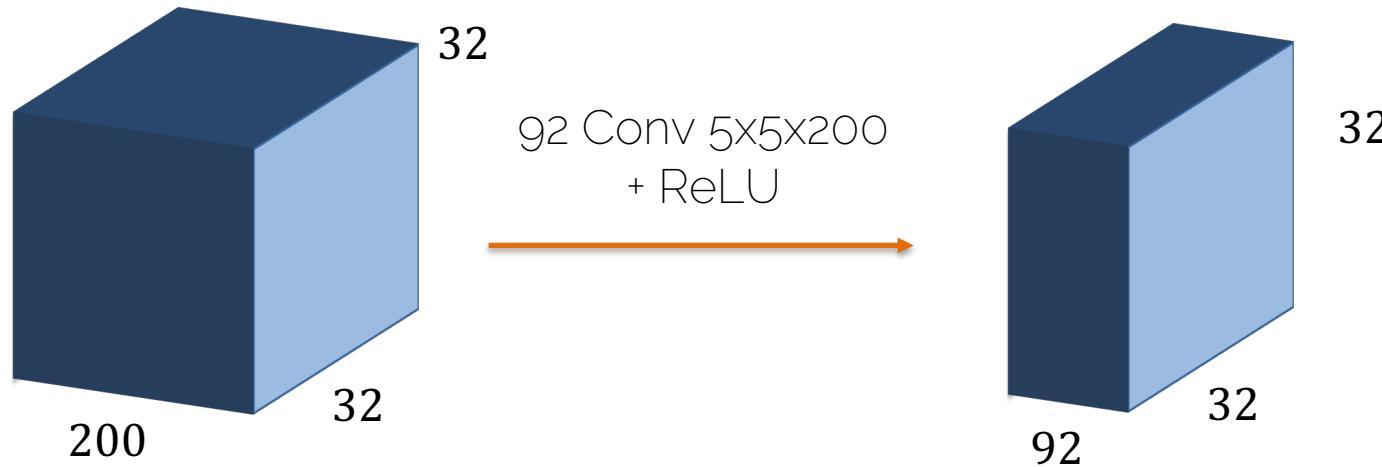
# Inception Layer

- Possible size of the output



- Not sustainable!

# Inception Layer: Computational Cost

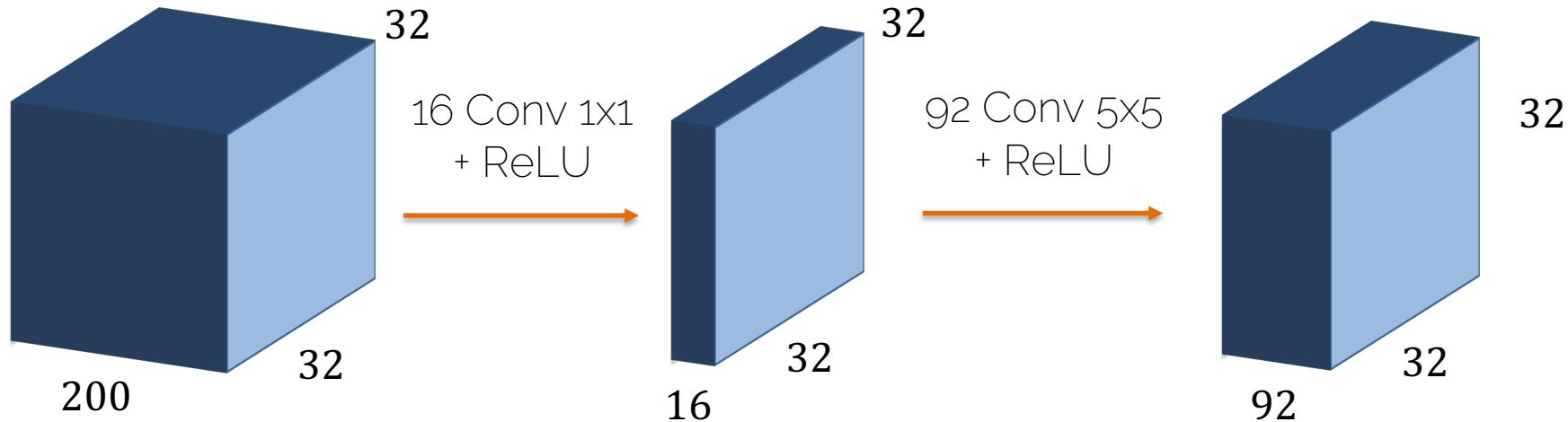


Multiplications:  $5 \times 5 \times 200 \times 32 \times 32 \times 92 \sim 470 \text{ million}$



1 value of the output volume

# Inception Layer: Computational Cost



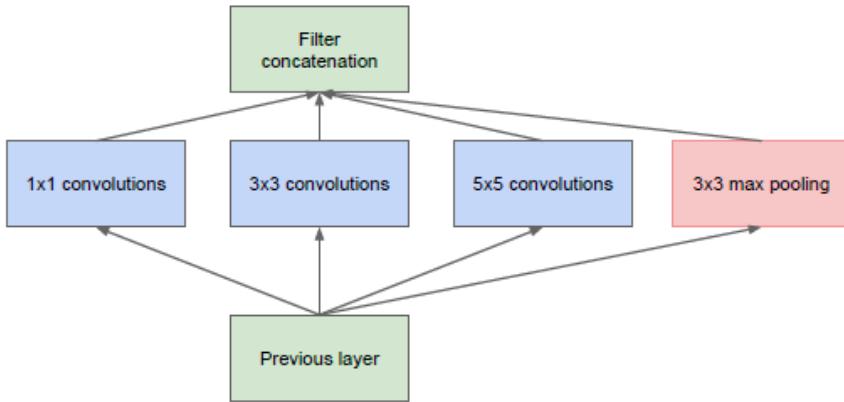
Multiplications:  $1 \times 1 \times 200 \times 32 \times 32 \times 16$

$5 \times 5 \times 16 \times 32 \times 32 \times 92$

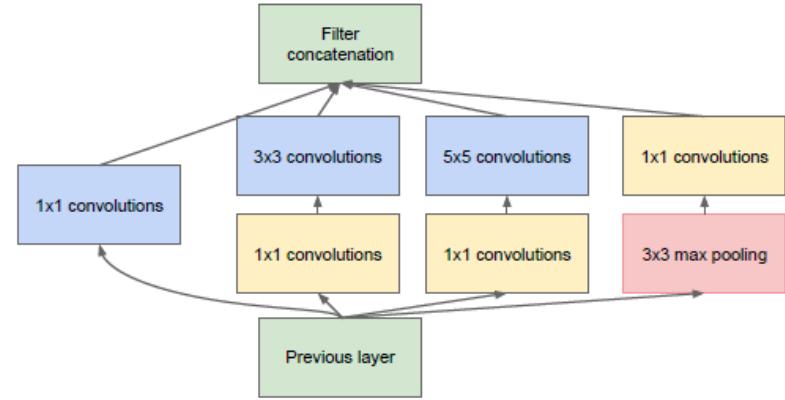
~ 40 million

Reduction of multiplications by 1/10

# Inception Layer



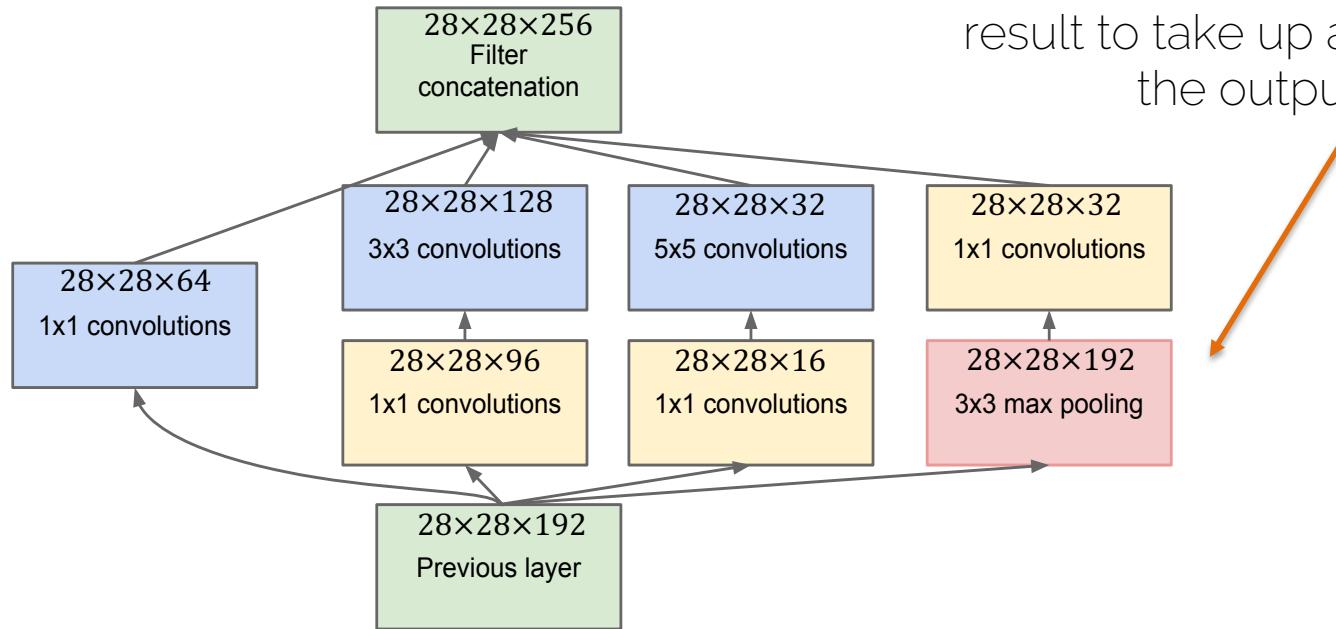
(a) Inception module, naïve version



(b) Inception module with dimensionality reduction

[Szegedy et al CVPR'15] GoogLeNet

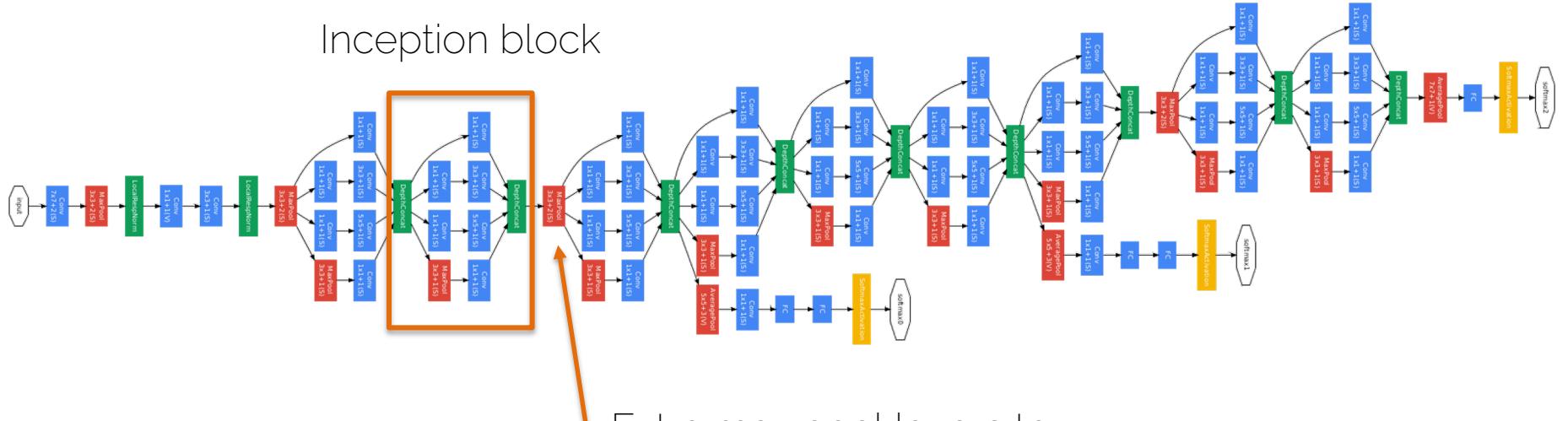
# Inception Layer: Dimensions



[Szegedy et al CVPR'15] GoogLeNet

# GoogLeNet: Using the Inception Layer

Inception block



Extra max pool layers to  
reduce dimensionality

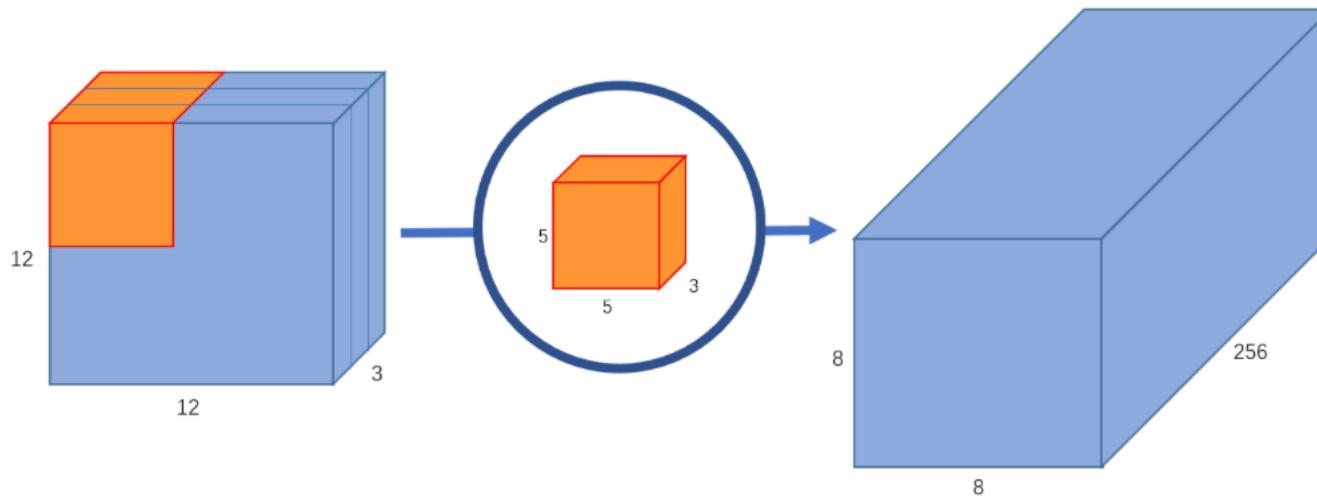
[Szegedy et al CVPR'15] GoogLeNet

# Xception Net

- „Extreme version of Inception“: applying (modified) Depthwise Separable Convolutions instead of normal convolutions
- 36 conv layers, structured into several modules with skip connections
- outperforms Inception Net V3

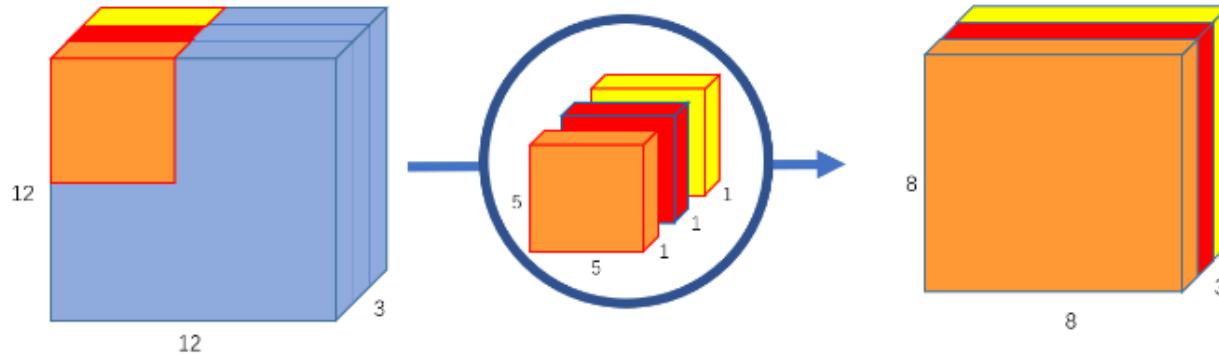
[Chollet CVPR'17] Xception

# Depth-wise separable convolutions



Normal convolutions act on all channels.

# Depth-wise separable convolutions

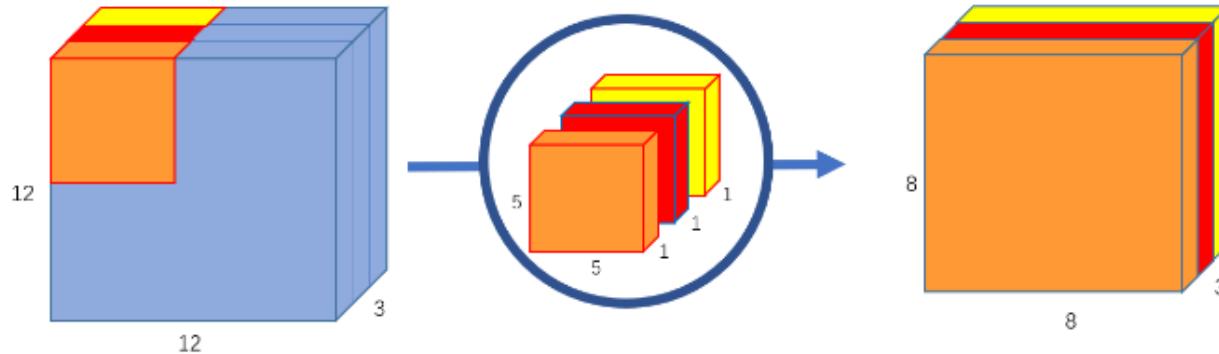


Filters are applied only at certain depths of the features.  
Normal convolutions have groups set to 1, the convolutions used in this image have groups set to 3.

`class torch.nn.Conv2d(in_channels, out_channels, kernel_size, stride=1, padding=0, groups=3)`

`class torch.nn.ConvTranspose2d(in_channels, out_channels, kernel_size, stride=1, padding=0, groups=3)`

# Depth-wise separable convolutions

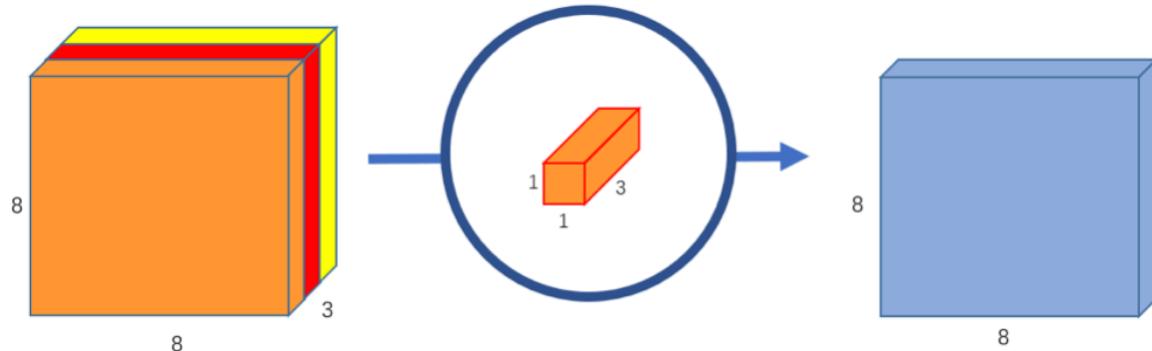
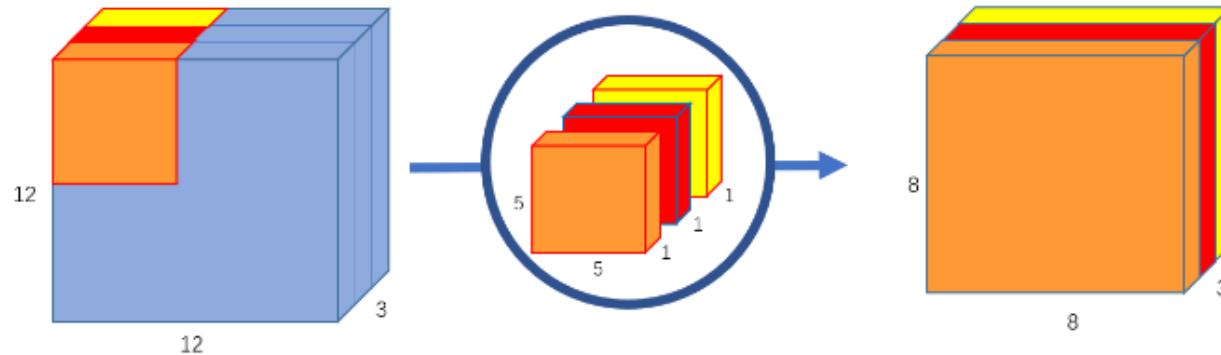


But the depth size is always the same!

```
class torch.nn.Conv2d(in_channels, out_channels, kernel_size, stride=1, padding=0, groups=3)
```

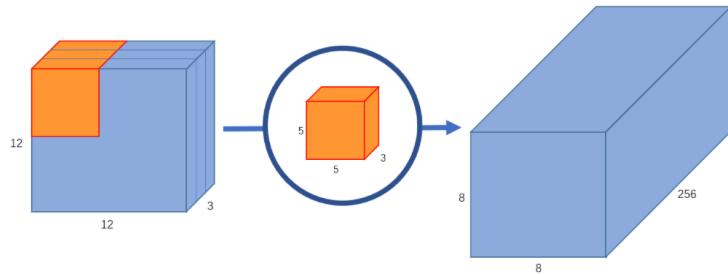
```
class torch.nn.ConvTranspose2d(in_channels, out_channels, kernel_size, stride=1, padding=0, groups=3)
```

# Depth-wise separable convolutions



Solution:  
1x1 convs!

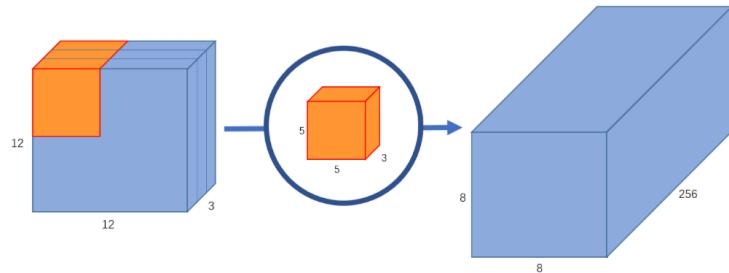
# But why?



Original convolution  
256 kernels of size 5x5x3

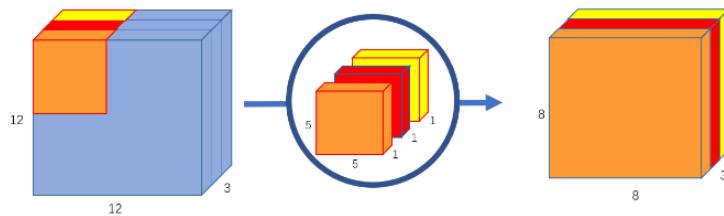
Multiplications:  
 $256 \times 5 \times 5 \times 3 \times (8 \times 8 \text{ locations}) = 1.228.800$

# But why?



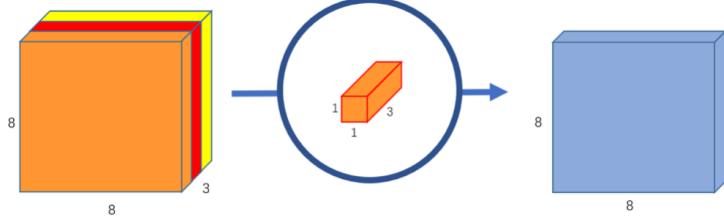
Original convolution  
256 kernels of size  $5 \times 5 \times 3$

Multiplications:  
 $256 \times 5 \times 5 \times 3 \times (8 \times 8 \text{ locations}) = 1.228.800$



Depth-wise convolution  
3 kernels of size  $5 \times 5 \times 1$

Multiplications:  
 $5 \times 5 \times 3 \times (8 \times 8 \text{ locations}) = 4800$

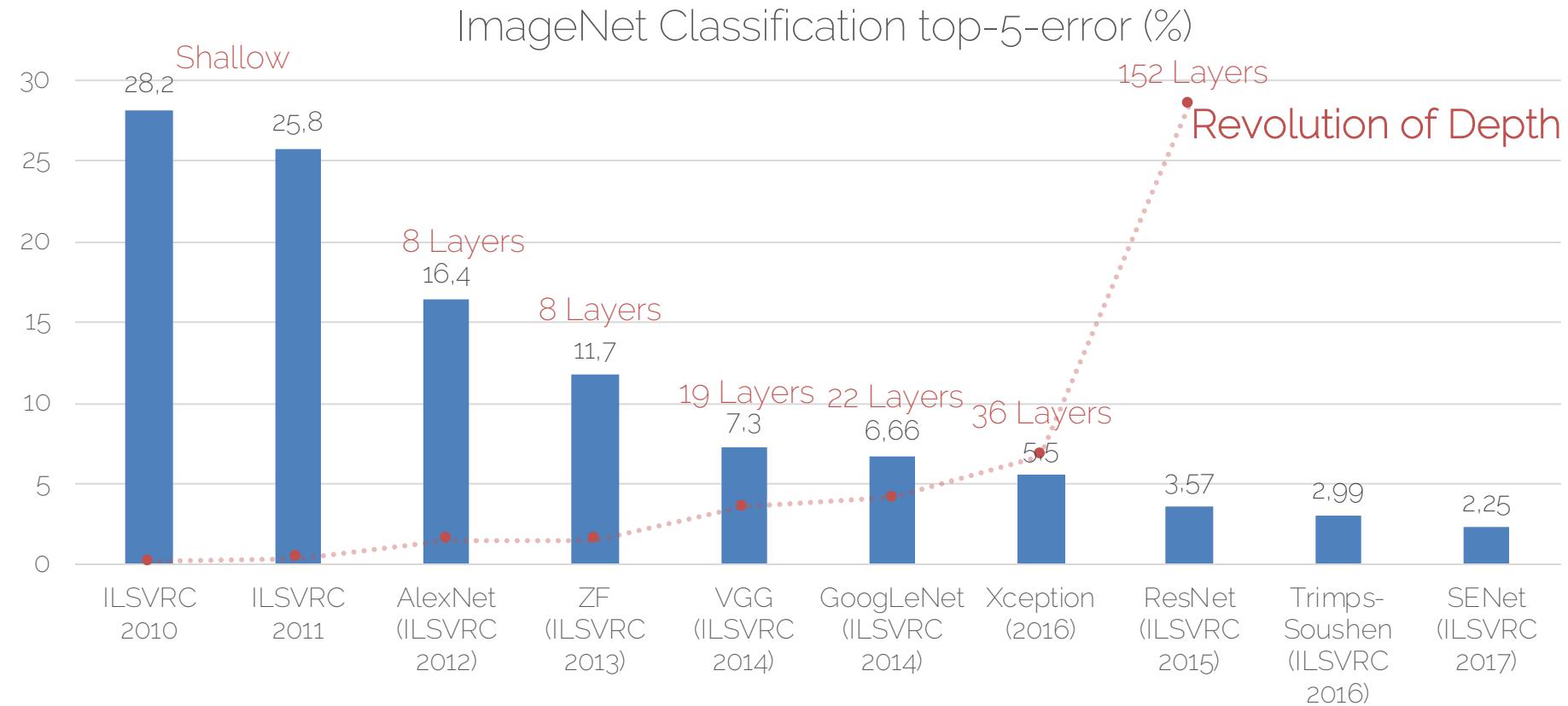


1x1 convolution  
256 kernels of size  $1 \times 1 \times 3$

Multiplications:  
 $256 \times 1 \times 1 \times 3 \times (8 \times 8 \text{ locations}) = 49152$

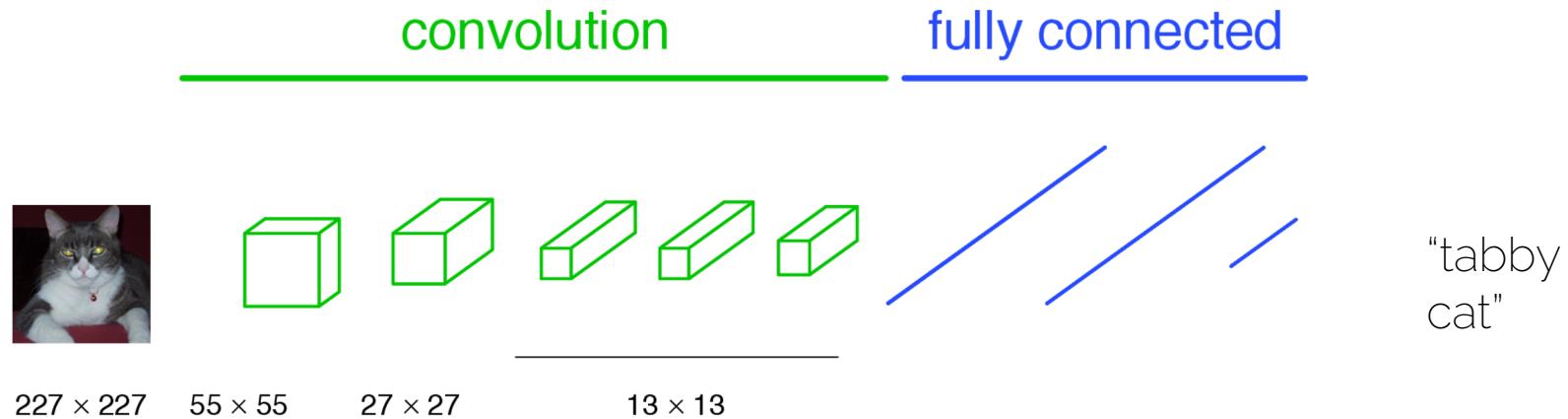
Less computations!

# ImageNet Benchmark

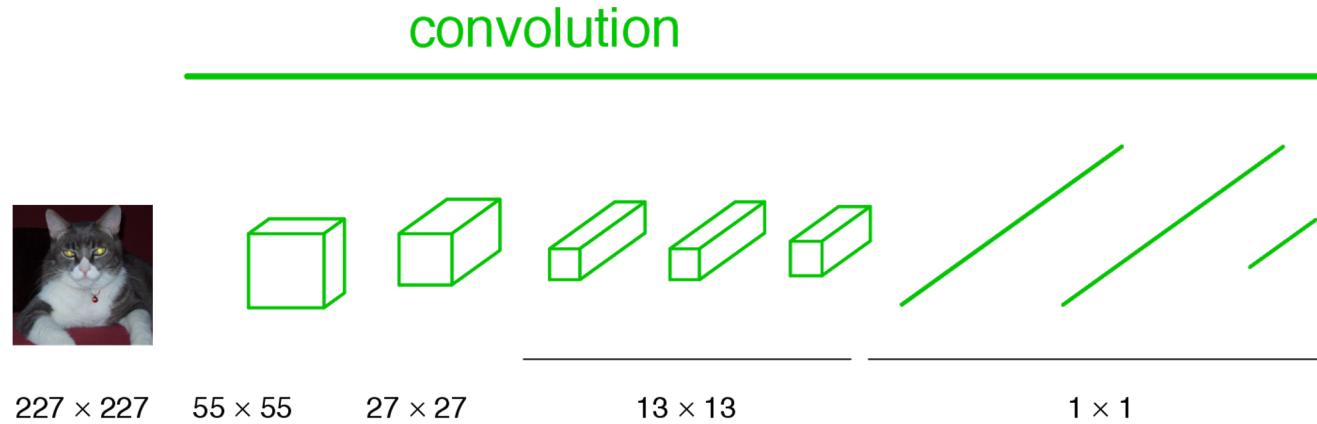


# Fully Convolutional Network

# Classification Network

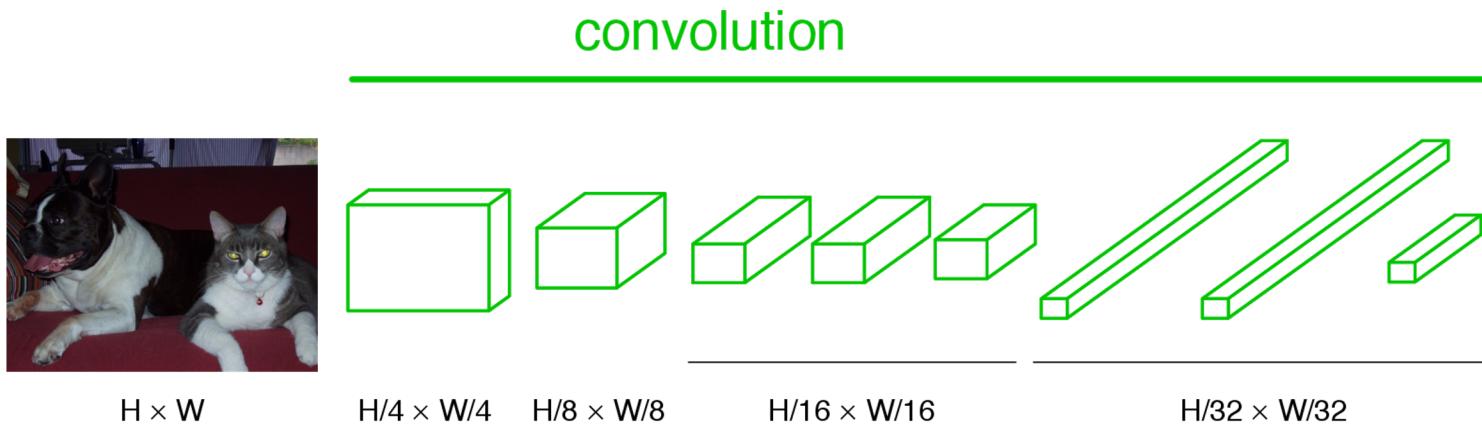


# FCN: Becoming Fully Convolutional

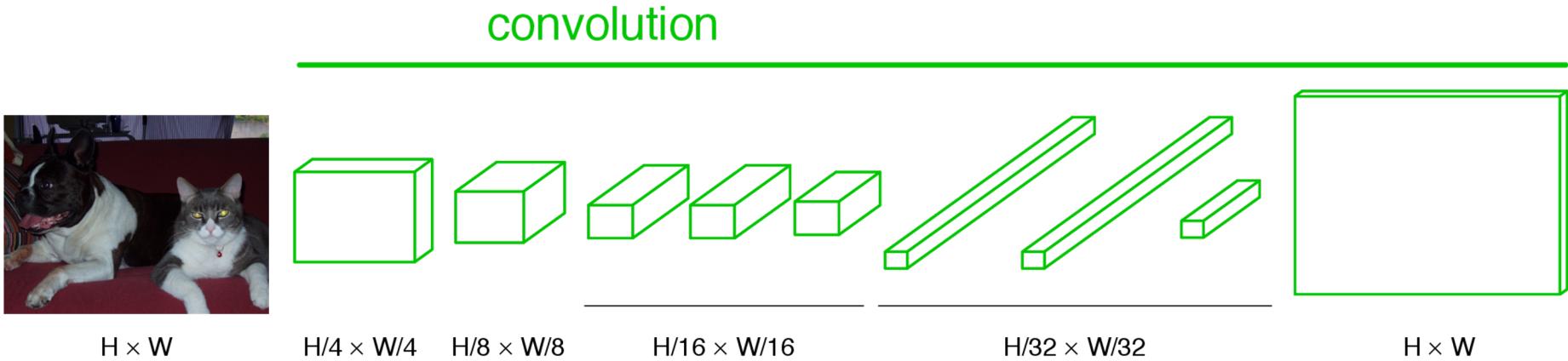


Convert fully connected layers to convolutional layers!

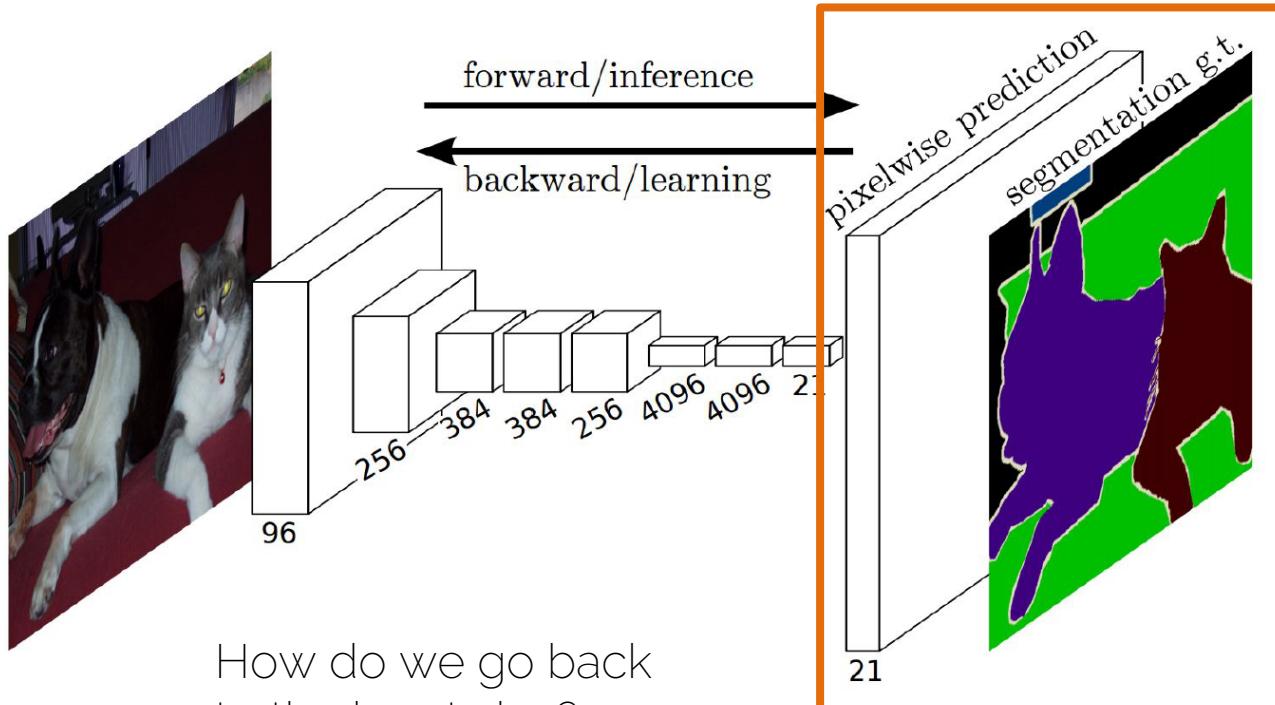
# FCN: Becoming Fully Convolutional



# FCN: Upsampling Output

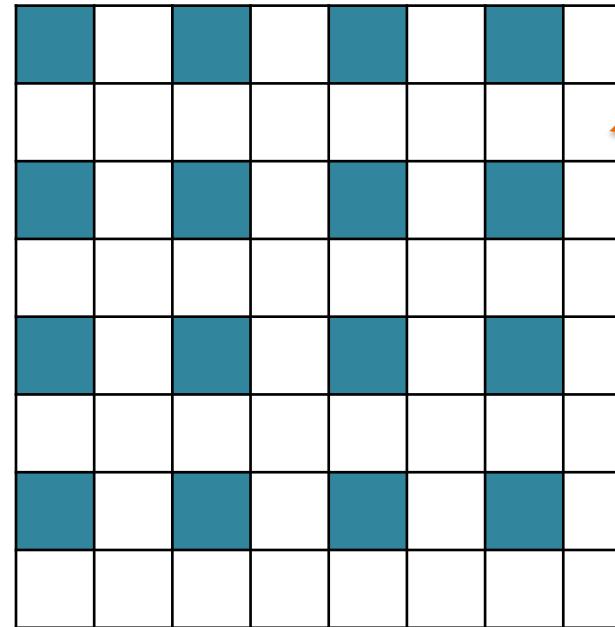
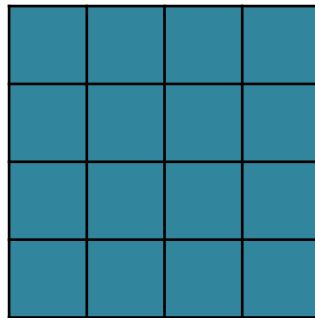


# Semantic Segmentation (FCN)



# Types of Upsampling

- 1. Interpolation



# Types of Upsampling

- 1. Interpolation

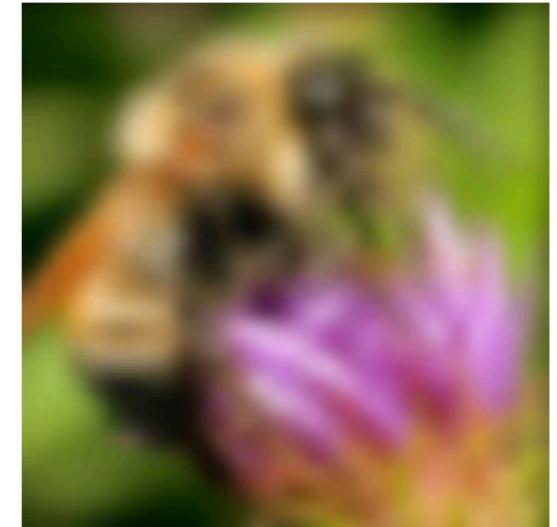
Original image  **x 10**



Nearest neighbor interpolation



Bilinear interpolation



Bicubic interpolation

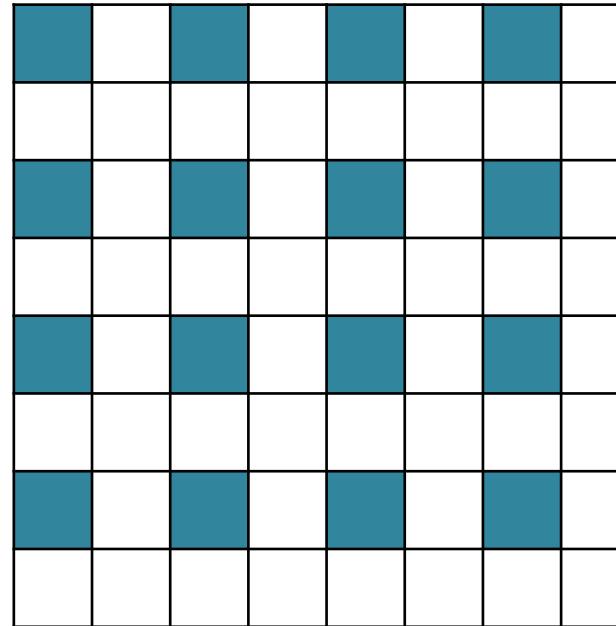
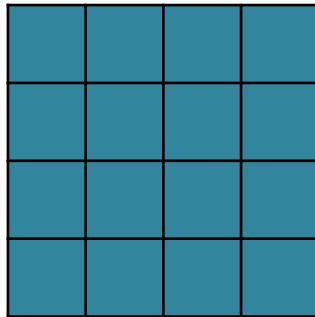
# Types of Upsampling

- 1. Interpolation

Few artifacts

# Types of Upsampling

- 2. Transposed conv



+ CONVS

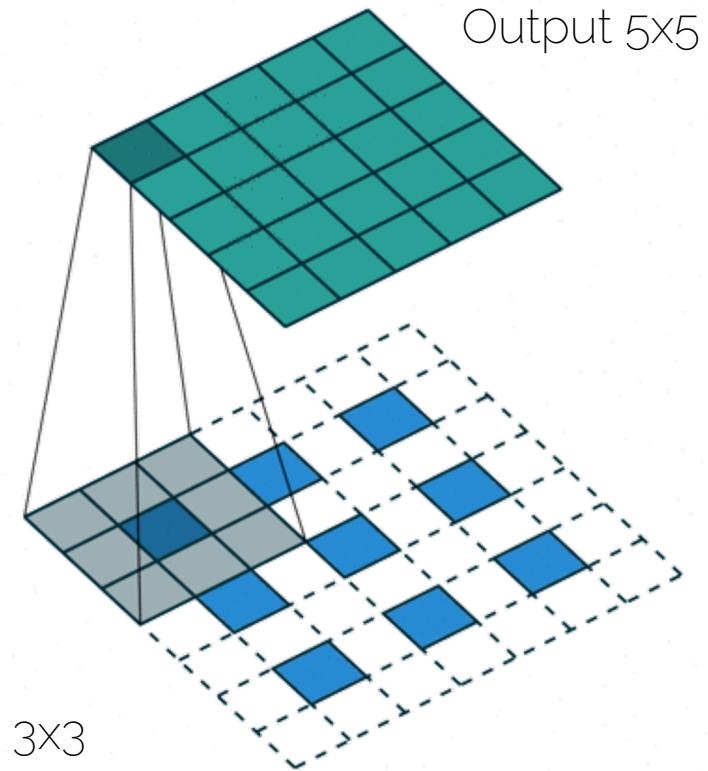
efficient

[A. Dosovitskiy, TPAMI 2017] "Learning to Generate Chairs, Tables and Cars with Convolutional Networks"

# Types of Upsampling

- 2. Transposed convolution

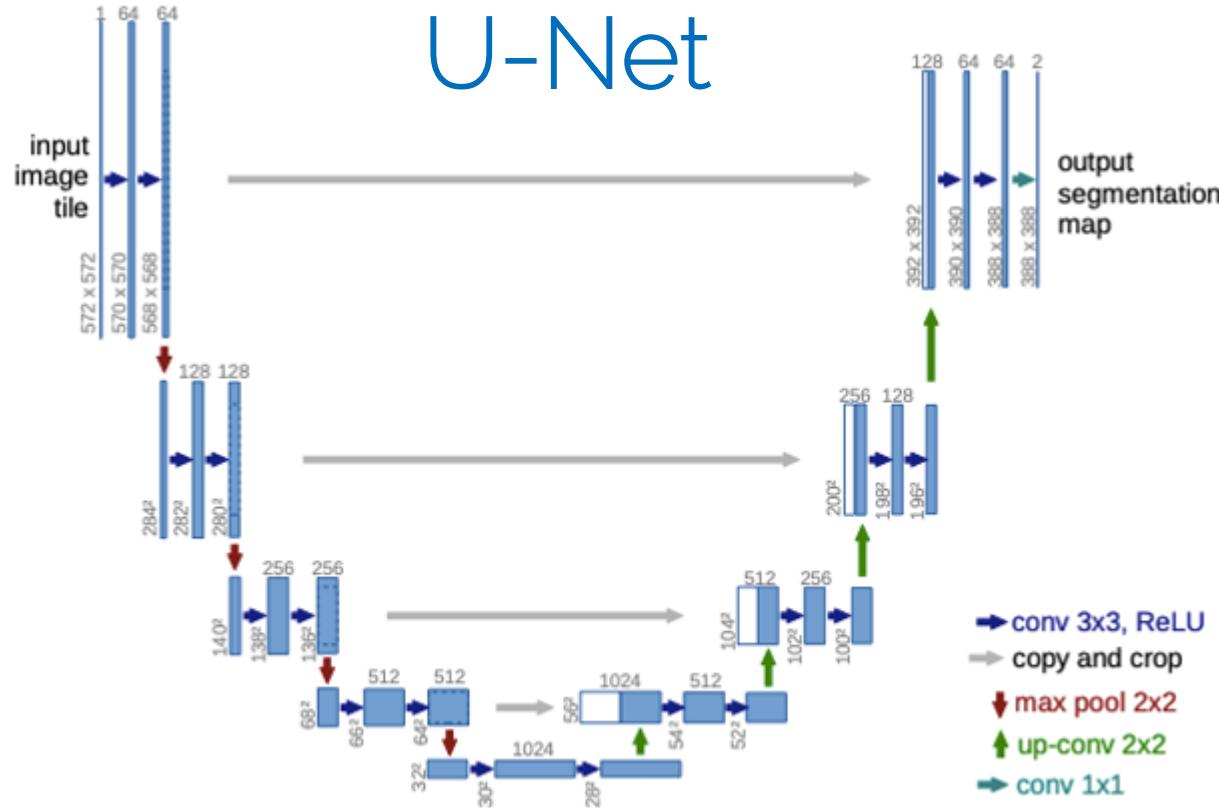
- Unpooling
  - Convolution filter (learned)
- Also called up-convolution  
**(never deconvolution)**



# Refined Outputs

- If one does a cascade of unpooling + conv operations, we get to the encoder-decoder architecture
- Even more refined: Autoencoders with skip connections (aka U-Net)

# U-Net



U-Net architecture: Each blue box is a multichannel feature map. Number of channels denoted at the top of the box. Dimensions at the top of the box. White boxes are the copied feature maps.

# U-Net: Encoder

Left side: Contraction Path (Encoder)

- Captures context of the image
- Follows typical architecture of a CNN:
  - Repeated application of 2 unpadded 3x3 convolutions
  - Each followed by ReLU activation
  - 2x2 maxpooling operation with stride 2 for downsampling
  - At each downsampling step, # of channels is doubled

→ as before: Height, Width  Depth: 

[Ronneberger et al. MICCAI'15] U-Net

# U-Net: Decoder

Right Side: Expansion Path (Decoder):

- Upsampling to recover spatial locations for assigning class labels to each pixel
  - 2x2 up-convolution that halves number of input channels
  - **Skip Connections:** outputs of up-convolutions are concatenated with feature maps from encoder
  - Followed by 2 ordinary 3x3 convs
  - final layer: 1x1 conv to map 64 channels to # classes
- Height, Width:       Depth: 

[Ronneberger et al. MICCAI'15] U-Net

See you next time!

# References

*We highly recommend to read through these papers!*

- [AlexNet](#) [Krizhevsky et al. 2012]
- [VGGNet](#) [Simonyan & Zisserman 2014]
- [ResNet](#) [He et al. 2015]
- [GoogLeNet](#) [Szegedy et al. 2014]
- [Xception](#) [Chollet 2016]
- [Fast R-CNN](#) [Girshick 2015]
- [U-Net](#) [Ronneberger et al. 2015]
- [EfficientNet](#) [Tan & Le 2019]