

notes

1 Foundations

1.1 The Role of Algorithms in Computing

1.1.1 Algorithms

1.1.2 Algorithms as a technology

1.1.3 Problems

1.2 Getting Started

1.2.1 Insertion sort

Input: A sequence of n numbers (a_1, a_2, \dots, a_n) .

Output: A permutation $(a'_1, a'_2, \dots, a'_n)$ of the input sequence such that $a'_1 \leq a'_2 \leq \dots \leq a'_n$.

INSERTION-SORT(A)

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1  for  $j \leftarrow 2$  to  $\text{length}[A]$ 
2      do  $\text{key} \leftarrow A[j]$ 
3           $\triangleright$  Insert  $A[j]$  into the sorted sequence  $A[1..j-1]$ .
4           $i \leftarrow j - 1$ 
5          while  $i > 0$  and  $A[i] > \text{key}$ 
6              do  $A[i+1] \leftarrow A[i]$ 
7                   $i \leftarrow i - 1$ 
8           $A[i+1] \leftarrow \text{key}$ 
```

loop invariant: We use loop invariants to help us understand why an algorithm is correct. We must show three things about a loop invariant:

Initialization: It is true prior to the first iteration of the loop.

Maintenance: If it is true before an iteration of the loop, it remains true before the next iteration.

Termination: When the loop terminates, the invariant gives a useful property that helps show the algorithm is correct.

Pseudocode conventions

1.2.2 Analyzing algorithms

1.2.3 Designing algorithms

1.2.4 Problems