

# notes

## 1 Foundations

### 1.1 The Role of Algorithms in Computing

#### 1.1.1 Algorithms

#### 1.1.2 Algorithms as a technology

#### 1.1.3 Problems

### 1.2 Getting Started

#### 1.2.1 Insertion sort

**Input:** A sequence of  $n$  numbers  $(a_1, a_2, \dots, a_n)$ .

**Output:** A permutation  $(a'_1, a'_2, \dots, a'_n)$  of the input sequence such that  $a'_1 \leq a'_2 \leq \dots \leq a'_n$ .

INSERTION-SORT( $A$ )

```
1  for  $j \leftarrow 2$  to  $\text{length}[A]$ 
2      do  $\text{key} \leftarrow A[j]$ 
3           $\triangleright$  Insert  $A[j]$  into the sorted sequence  $A[1..j-1]$ .
4           $i \leftarrow j - 1$ 
5          while  $i > 0$  and  $A[i] > \text{key}$ 
6              do  $A[i+1] \leftarrow A[i]$ 
7                   $i \leftarrow i - 1$ 
8           $A[i+1] \leftarrow \text{key}$ 
```

**loop invariant:** We use loop invariants to help us understand why an algorithm is correct. We must show three things about a loop invariant:

**Initialization:** It is true prior to the first iteration of the loop.

**Maintenance:** If it is true before an iteration of the loop, it remains true before the next iteration.

**Termination:** When the loop terminates, the invariant gives a useful property that helps show the algorithm is correct.

**1.2.2 Analyzing algorithms**

**1.2.3 Designing algorithms**

**1.2.4 Problems**