

```
clc;
clear all;
close all;
```

generate data

```
run ("Basics.m")
```

```
sys =
```

```

          1.3 s + 1.333
-----
s^4 + 3.967 s^3 + 8.41 s^2 + 10.62 s + 8.756
```

Continuous-time transfer function.

```
fb = 2.4327
```

```
sysd =
```

```

0.0004236 z^3 + 0.001167 z^2 - 0.000997 z - 0.0003069
-----
z^4 - 3.481 z^3 + 4.58 z^2 - 2.697 z + 0.5991
```

Sample time: 0.12914 seconds

Discrete-time transfer function.

```
c = 1x5
```

```
    0    0.0004    0.0012   -0.0010   -0.0003
```

```
d = 1x5
```

```
    1.0000   -3.4807    4.5802   -2.6968    0.5991
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
tfinal=200;
```

```
t = 0:T_s:tfinal;
```

```
u = gensig('sine' , tfinal/20 , tfinal ,T_s);%+gensig('sine' , tfinal/50 , tfinal ,T_s)+gensig('sine' , tfinal ,T_s)
```

```
Noise=[1:numel(t)];
```

```
Noise(1:10) = ones(1,10)';
```

```
for i=4:1:numel(t)
```

```
    Noise(i)=+0.6*Noise(i-1)+0.75*Noise(i-2)-0.35*Noise(i-3);
```

```
end
```

```
u=u+Noise';
```

```
y = lsim(sysd ,u ,t);
```

```
plot(t,u ,t , y , 'LineWidth',2) ;
```

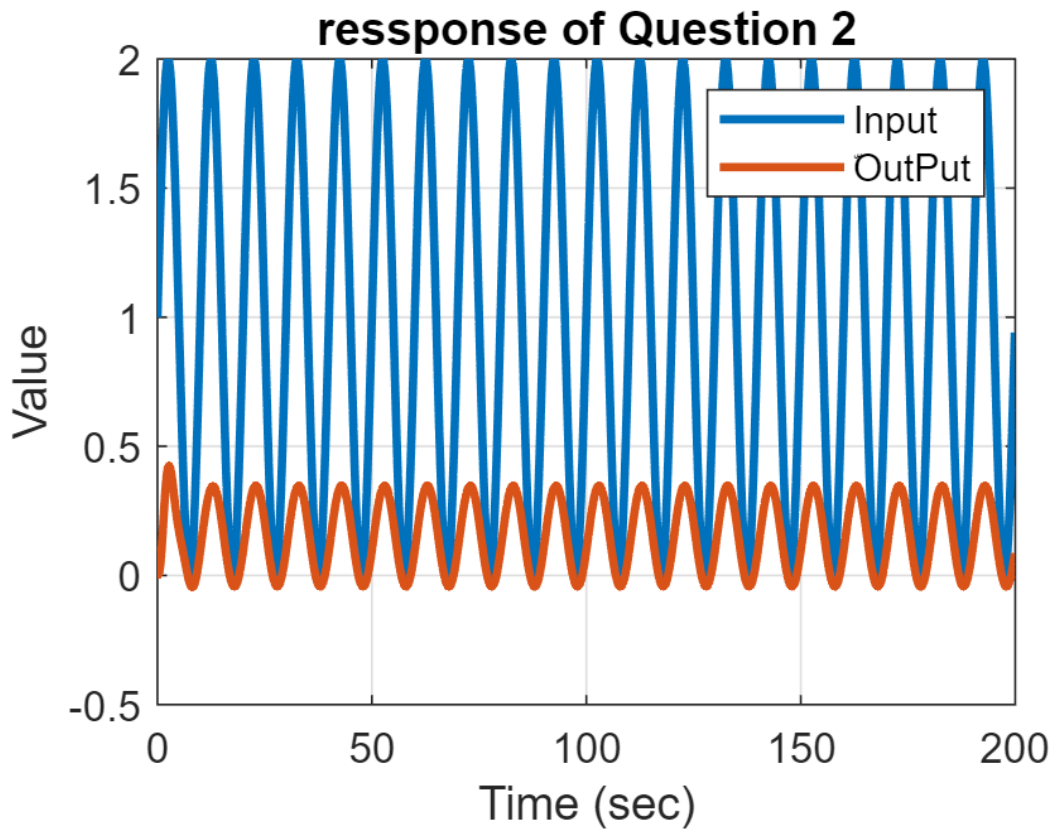
```
xlabel('Time (sec)') ;
```

```
ylabel('Value') ;
```

```
title('response of Question 2') ;
```

```
grid on
```

```
legend('Input' , 'OutPut') ;
```



recursive least esquare estimation

```
N = numel(y) ;  
%choose number of parameters  
Parameters_in_den=4
```

Parameters_in_den = 4

Parameters_in_num=4

Parameters_in_num = 4

$$N_v = \text{Parameters_in_num} + \text{Parameters_in_den}$$
$$N_v = 8$$

```
P = 1e12*eye(Nv) ;
theta=[Nv,N]
```

```
theta = 1x2
      8      1549
```

```
theta(1:Nv,1:30) = 5*ones(Nv,30) ;
```

```
phi=[];  
Error=zeros(1,N)
```

Error = 1×10^{-15}

```

tic
for i = (max(Parameters_in_num,Parameters_in_den))+1:N
    phi(:,i) = [[y(i-1:-1:i-Parameters_in_den)]' , [u(i-1:-1:i-Parameters_in_num)]']';
    K = P*phi(:,i)*(1+phi(:,i)'*P*phi(:,i))^( -1) ;
    P = (eye(Nv) - K*phi(:,i)')*P ;
    theta(:,i) = theta(:,i-1) + K*(y(i) - phi(:,i)'*theta(:,i-1));
    Error(i)=(Error(i-1)+(y(i)-phi(:,i)'*theta(:,i))^2);
end

```

Code

```

ident_dis = tf(theta((Parameters_in_num+1):end,end)' , [1 -theta(1:Parameters_in_num ,end)'] , T, 's');

```

```

ident_dis =

```

$$\frac{0.0005414 z^3 + 0.0005013 z^2 + 5.629e-05 z - 0.0007949}{z^4 - 3.471 z^3 + 4.554 z^2 - 2.674 z + 0.5925}$$

Sample time: 0.12914 seconds
Discrete-time transfer function.

```

ident_analog = d2c(ident_dis)

```

```

ident_analog =

```

$$\frac{0.003168 s^3 - 0.02925 s^2 + 1.336 s + 1.421}{s^4 + 4.053 s^3 + 8.692 s^2 + 11.03 s + 9.331}$$

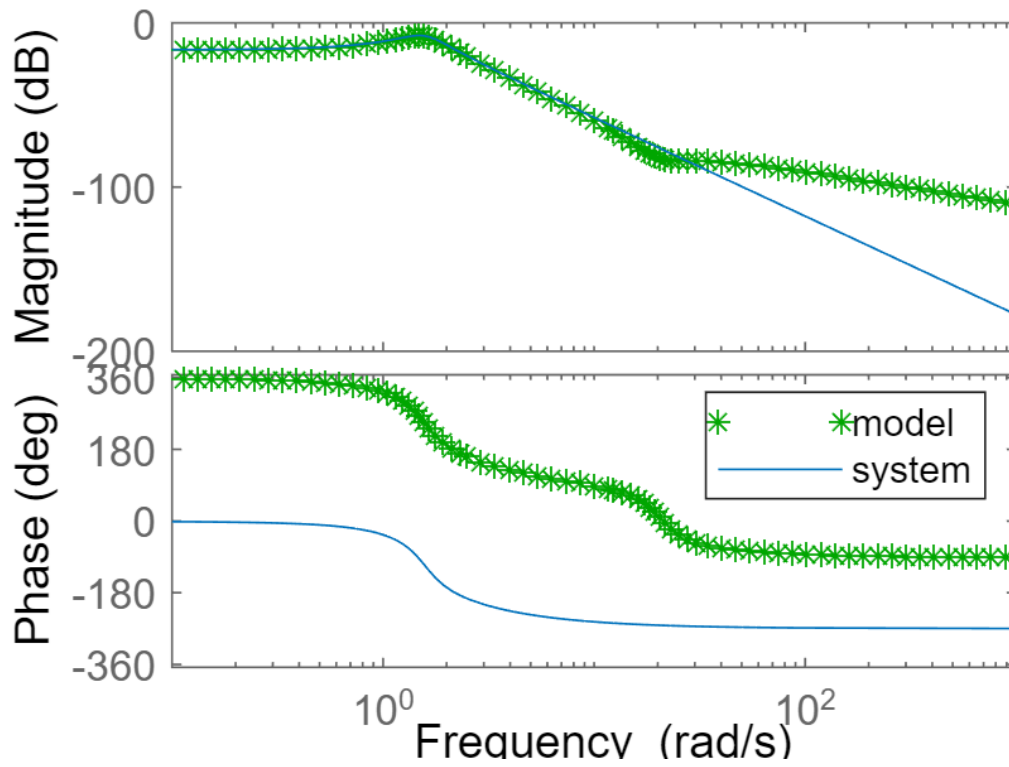
Continuous-time transfer function.

```

bode(ident_analog , 'g*',sys )
legend('model ', 'system')

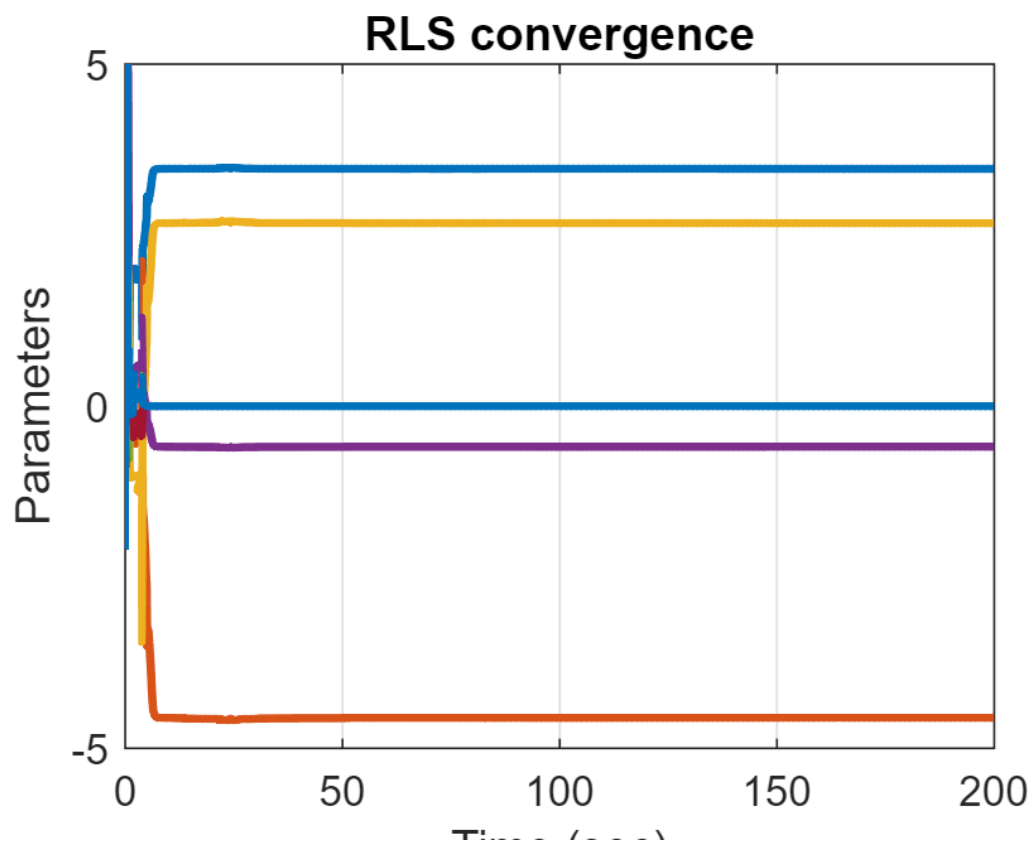
```

Bode Diagram



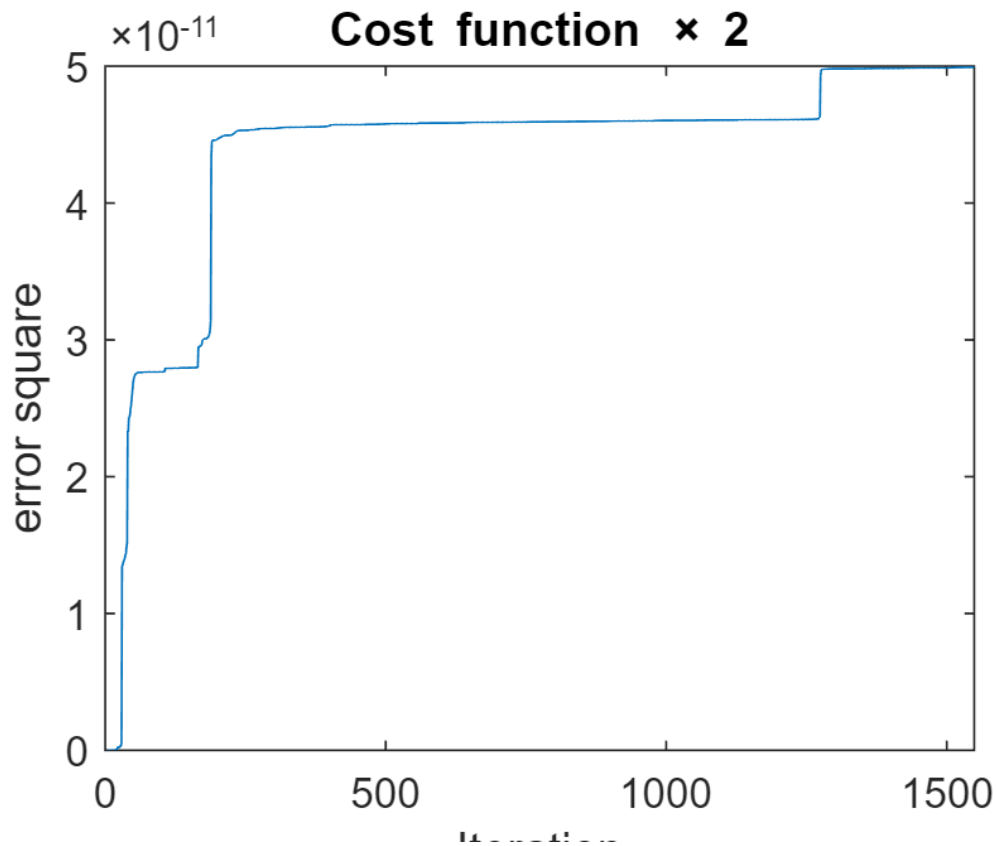
RLS Convergence

```
plot(t , theta(:,:) , 'LineWidth' , 2) ;  
xlabel('Time (sec)') ;  
ylabel('Parameters') ;  
title('RLS convergence') ;  
grid on
```



```

plot(1:1:N,Error)
xlabel('Iteration') ;
ylabel('error square') ;
title('Cost function \times 2') ;
  
```



```
tfinal=1000;
T_s=T_s
```

```
T_s = 0.1291
```

```
t = 0:T_s:tfinal;
u = gensig('square' , tfinal/20 , tfinal ,T_s);
u = u+rand(numel(t),1);
y = lsim(sysd,u ,t);

y_model = lsim(ident_dis ,u ,t);

plot(t,y_model , 'b*',t , y , 'LineWidth',1.25) ;
xlabel('Time (sec)') ;
ylabel('Value') ;
title('ressponse of Question 2') ;
grid on
legend('Under parameter Model' , 'System') ;
```

