

HW2 Report

I. Implementation (Part 1 – Part 4)

```
class n:
    def __init__(self, End, distance, limit): # define a class to store the data of an edge
        self.End = End # including the end, the distance, and the speed limit
        self.distance = distance
        self.limit = limit
```

1. BFS

```
def bfs(start, end):
    # Begin your code (Part 1)

    # read the data
    EdgeFile = open(edgeFile) # open 'edges.csv'
    lines = EdgeFile.readlines() # read them as separate lines
    # create a dictionary to store the edges from the same start
    graph = defaultdict(list)
    # create a dictionary to see which has been visited
    visited = defaultdict(str)

    for line in lines:
        data = line.split(",") # store the data from csv file
        Node = n(data[1], data[2], data[3].replace("\n", ""))
        graph[data[0]].append(Node)
        visited[data[0]] = False # set all elements to not visited
    # bfs
    q = [] # create a queue for bfs
    q.append(start) # push the start node inside
    visited[str(start)] = True # mark the start as visited
    parent = defaultdict(str) # create a dictionary to store the previous node
    parent[str(start)] = None # start with no previous node
    num_visited = 0
    while len(q) != 0: # while the queue is not empty
        # set the current node to the top element of the queue (FIFO)
        current = str(q.pop(0))
        # for every edge starting from the current node
        for i in range(len(graph[current])):
            next = graph[current][i].End # set the next node
            if visited[next] == False: # if the next node is not visited
                # set the previous of the next to current
                parent[next] = current
                visited[str(next)] = True # visited
                num_visited += 1 # so the number of visited nodes increases
                q.append(next) # push the next node into the queue
                if next == str(end): # if this edge reaches the end
                    del q[:] # break the loop
                    break
```

```

path = [] # create a queue for storing the path
path.append(str(end)) # push the end node inside
dist = 0 # initialize the distance to 0
# now = end # set the current node to 'end'
turn = 0 # the first iteration
while parent[path[turn]] != None: # while the current node is not 'start'
    # print(parent[path[turn]])
    # for edges starting from the previous node
    for i in range(len(graph[parent[path[turn]]])):
        if graph[parent[path[turn]]][i].End == path[turn]: # if the End is the current node
            # add up the distance
            dist += float(graph[parent[path[turn]]][i].distance)
    turn += 1 # next iteration
    path.append(parent[path[turn-1]]) # add the previous node to the path
    # now = parent[now] # set the current node to the previous

path.reverse() # reverse because it was stored backwards
for i in range(len(path)): # change all the elements in the path to integers
    path[i] = int(path[i])

return path, dist, num_visited # return

raise NotImplementedError("To be implemented")
# End your code (Part 1)

```

2. DFS_stack

```

def dfs(start, end):
    # Begin your code (Part 2)

    # read the data
    EdgeFile = open(edgeFile) # open 'edges.csv'
    lines = EdgeFile.readlines() # read them as separate lines
    # create a dictionary to store the edges from the same start
    graph = defaultdict(list)
    # create a dictionary to see which has been visited
    visited = defaultdict(str)

    for line in lines:
        data = line.split(",") # store the data from csv file
        Node = Node(data[1], data[2], data[3].replace("\n", ""))
        graph[data[0]].append(Node)
        visited[data[0]] = False # set all elements to not visited
    # dfs
    q = [] # create a queue for dfs
    q.append(start) # push the start node inside
    visited[str(start)] = True # mark the start as visited
    parent = defaultdict(str) # create a dictionary to store the previous node
    parent[str(start)] = None # start with no previous node
    num_visited = 0

```

```

while len(q) != 0: # while the queue is not empty
    # set the current node to the last element of the queue (FILO)
    current = str(q.pop())
    # for every edge starting from the current node
    for i in range(len(graph[current])):
        next = graph[current][i].End # set the next node
        if visited[next] == False: # if the next node is not visited
            # set the previous of the next to current
            parent[next] = current
            visited[str(next)] = True # visited
            num_visited += 1 # so the number of visited nodes increases
            q.append(next) # push the next node into the queue
            if next == str(end): # if this edge reaches the end
                del q[:] # break the loop
                break

path = [] # create a queue for storing the path
path.append(str(end)) # push the end node inside
dist = 0 # initialize the distance to 0
# now = end # set the current node to 'end'
turn = 0 # the first iteration
while parent[path[turn]] != None: # while the current node is not 'start'
    # print(parent[path[turn]])
    # for edges starting from the previous node
    for i in range(len(graph[parent[path[turn]]])):
        if graph[parent[path[turn]]][i].End == path[turn]: # if the End is the current
            # add up the distance
            dist += float(graph[parent[path[turn]]][i].distance)
    turn += 1 # next iteration
    path.append(parent[path[turn-1]]) # add the previous node to the path
    # now = parent[now] # set the current node to the previous

path.reverse() # reverse because it was stored backwards
for i in range(len(path)): # change all the elements in the path to integers
    path[i] = int(path[i])

return path, dist, num_visited # return

raise NotImplementedError("To be implemented")
# End your code (Part 2)

```

3. UCS

```

def ucs(start, end):
    # Begin your code (Part 3)

    # read data
    EdgeFile = open('edges.csv') # open 'edges.csv'
    lines = EdgeFile.readlines() # read them as separate lines
    # create a dictionary to store the edges from the same start
    graph = defaultdict(list)
    # create a dictionary to see which has been visited
    visited = defaultdict(str)

```

```

for line in lines:
    data = line.split(",") # store the data from csv file
    Node = Node(data[1], data[2], data[3].replace("\n", ""))
    graph[data[0]].append(Node)
    graph[data[0]].sort(key=lambda Node: Node.End)
    visited[data[0]] = False # set all elements to not visited

# ucs
q = [] # create a list for ucs
q.append(start) # push the start node inside
visited[str(start)] = True # mark the start as visited
# create a dictionary to store the distance from 'start'
distance = defaultdict(float)
distance[start] = 0 # the distace from 'start' to 'start' is 0
parent = defaultdict(str) # create a dictionary to store the previous node
parent[start] = None # start with no previous node
num_visited = 0

while len(q) != 0: # while the queue is not empty
    min = float("inf") # set the minimum to infinity
    for i in range(len(q)): # for the distances to the ends in current queue
        if distance[q[i]] < min: # if it is smaller than the minimum
            min = distance[q[i]] # update the minimum
            m_index = i # record the index
    # set current node to the one with minimum distance
    current = str(q.pop(m_index))
    visited[current] = True # mark as visited
    num_visited += 1 # so the number of visited nodes increases
    if current == str(end): # if the node is 'end'
        del q[:] # break the loop
        # set the total distance to the distance to 'end'
        dist = distance[str(end)]
        break
    # for every edge starting from current node
    for i in range(len(graph[current])):
        # set the end of this edge to the next node
        next = graph[current][i].End
        if visited[next] == False: # if the next is not visited
            if next not in q: # and if it is not in the queue yet
                q.append(next) # add it to the queue
            if next in distance: # if it already has a distance
                if distance[next] > distance[current] + float(graph[current][i].distance):
                    # and if there exists smaller distance, update
                    parent[next] = current
                    distance[next] = distance[current] + \
                        float(graph[current][i].distance)
            else: # if next does not have a recorded distance yet
                parent[next] = current # do the same as above
                distance[next] = distance[current] + \
                    float(graph[current][i].distance)
        # set the used distance back to infinity
        distance[m_index] = float("inf")

```

```

path = [] # create a queue for storing the path
path.append(str(end)) # push the end node inside
turn = 0 # the first iteration
while path[turn] != str(start): # while the current node is not 'start'
    path.append(parent[path[turn]]) # add the previous node to the path
    turn += 1 # next iteration

path.reverse() # reverse because it was stored backwards
for i in range(len(path)): # change all the elements in the path to integers
    path[i] = int(path[i])

return path, dist, num_visited # return

raise NotImplementedError("To be implemented")
# End your code (Part 3)

```

4. A*

```

def astar(start, end):
    # Begin your code (Part 4)

    # read data
    EdgeFile = open('edges.csv') # open 'edges.csv'
    lines = EdgeFile.readlines() # read them as separate lines
    # create a dictionary to store the edges from the same start
    graph = defaultdict(list)
    # create a dictionary to see which has been visited
    visited = defaultdict(str)

    for line in lines:
        data = line.split(",") # store the data from csv file
        Node = Node(data[1], data[2], data[3].replace("\n", ""))
        graph[data[0]].append(Node)
        graph[data[0]].sort(key=lambda Node: Node.End)
        visited[data[0]] = False # set all elements to not visited

    # read heuristic
    Hfile = open('heuristic.csv') # open 'heuristic.csv'
    Lines = Hfile.readlines() # read them as separate lines
    # create three dictionaries for three possible values
    val1 = defaultdict(float)
    val2 = defaultdict(float)
    val3 = defaultdict(float)

    for line in Lines:
        data = line.split(",") # store the data from csv file
        val1[data[0]] = data[1]
        val2[data[0]] = data[2]
        val3[data[0]] = data[3].replace("\n", "")

```

```

# A*
q = [] # create a list for A*
q.append(start) # push the start node inside
visited[str(start)] = True # mark the start as visited
# create a dictionary to store the distance from 'start'
distance = defaultdict(float)
distance[start] = 0 # the distance from 'start' to 'start' is 0
parent = defaultdict(str) # create a dictionary to store the previous node
parent[start] = None # start with no previous node
add = defaultdict(float) # create a dictionary to store the addition
num_visited = 0

if str(end) == '1079387396': # check which value should be used
    value = val1
elif str(end) == '1737223506':
    value = val2
elif str(end) == '8513026827':
    value = val3


while len(q) != 0: # while the queue is not empty
    min = float("inf") # set the minimum to infinity
    for i in range(len(q)): # for the additions to the ends in current queue
        if add[q[i]] < min: # if it is smaller than the minimum
            min = add[q[i]] # update the minimum
            m_index = i # record the index
    # set current node to the one with minimum distance
    current = str(q.pop(m_index))
    visited[current] = True # mark as visited
    num_visited += 1 # so the number of visited nodes increases
    if current == str(end): # if the node is 'end'
        del q[:] # break the loop
        # set the total distance to the addition to 'end'
        dist = add[str(end)]
        break
    # for every edge starting from current node
    for i in range(len(graph[current])):
        # set the end of this edge to the next node
        next = graph[current][i].End
        if visited[next] == False: # if the next is not visited
            if next not in q: # and if it is not in the queue yet
                q.append(next) # add it to the queue
            if next in distance: # if already exists
                if distance[next] > distance[current] + float(graph[current][i].distance):
                    # and if there exists smaller distance, update
                    parent[next] = current
                    distance[next] = distance[current] + \
                        float(graph[current][i].distance)
            else: # if next does not have a recorded distance yet
                parent[next] = current # do the same as above
                distance[next] = distance[current] + \
                    float(graph[current][i].distance)
        add[next] = distance[next] + float(value[int(next)]) # add up the value and the distance
    add[m_index] = float("inf") # set the used addition back to infinity
    distance[m_index] = float("inf") # set the used distance back to infinity

```

```

path = [] # create a queue for storing the path
path.append(str(end)) # push the end node inside
turn = 0 # the first iteration
while path[turn] != str(start): # while the current node is not 'start'
    path.append(parent[path[turn]]) # add the previous node to the path
    turn += 1 # next iteration

path.reverse() # reverse because it was stored backwards
for i in range(len(path)): # change all the elements in the path to integers
    path[i] = int(path[i])

return path, dist, num_visited # return

raise NotImplementedError("To be implemented")
# End your code (Part 4)

```

II. Results and Analysis (Part 5)

- From National Yang Ming Chiao Tung University (ID: 2270143902) to Big City Shopping Mall (ID: 1079387396)

BFS



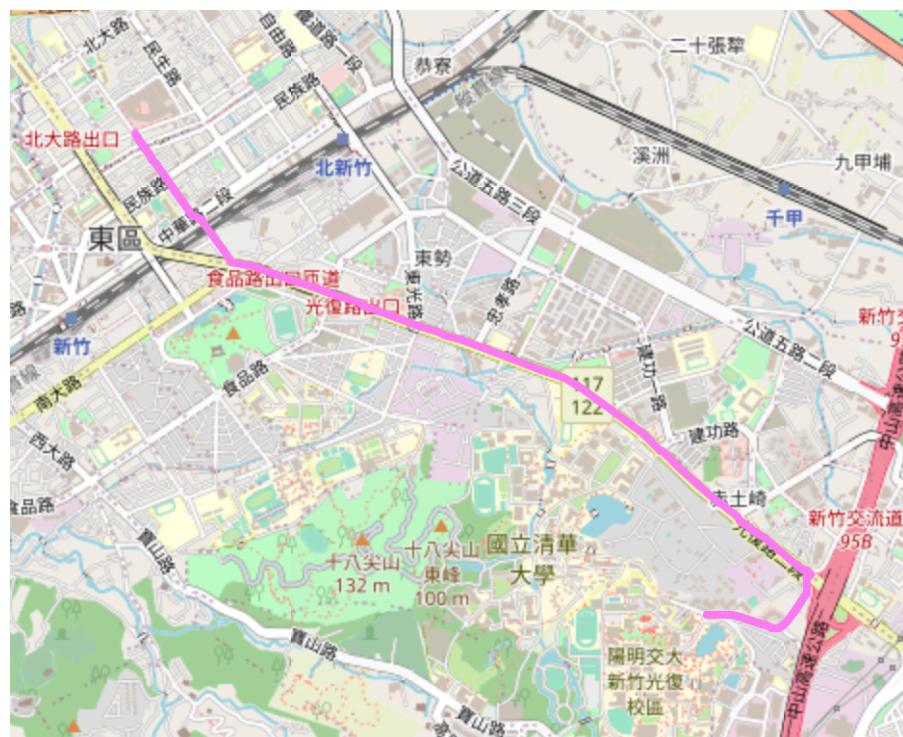
The number of nodes in the path found by BFS: 88
 Total distance of path found by BFS: 4978.881999999998 m
 The number of visited nodes in BFS: 4266

DFS_stack



The number of nodes in the path found by DFS: 1718
Total distance of path found by DFS: 75504.3150000001 m
The number of visited nodes in DFS: 5227

UCS



The number of nodes in the path found by UCS: 89
Total distance of path found by UCS: 4367.881 m
The number of visited nodes in UCS: 5077

A*



The number of nodes in the path found by A* search: 89

Total distance of path found by A* search: 4367.881 m

The number of visited nodes in A* search: 5077

2. From Hsinchu Zoo (ID: 426882161) to COSTCO Hsinchu Store (ID: 1737223506)

BFS

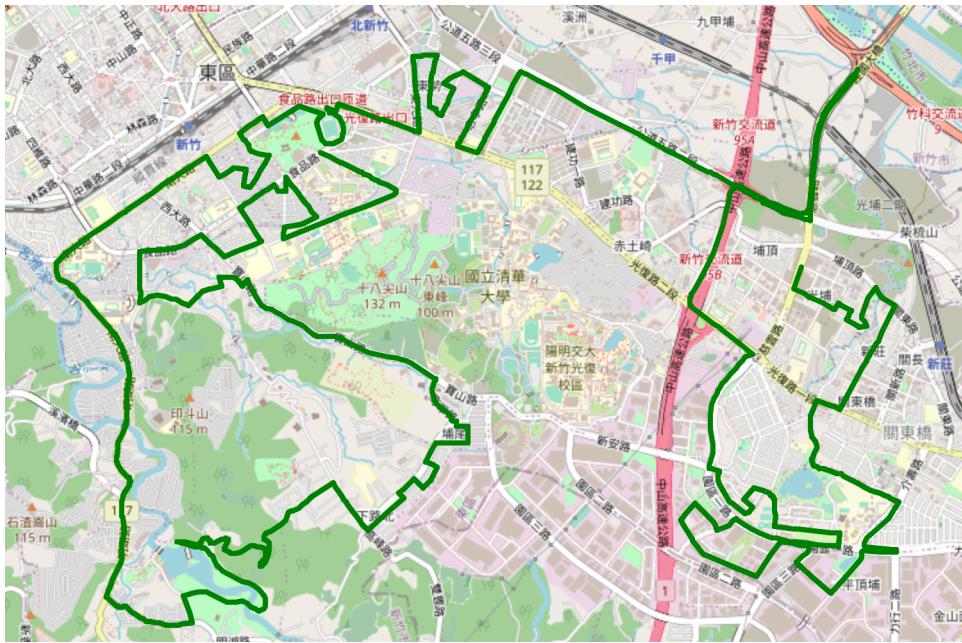


The number of nodes in the path found by BFS: 60

Total distance of path found by BFS: 4215.521000000001 m

The number of visited nodes in BFS: 4603

DFS_Stack

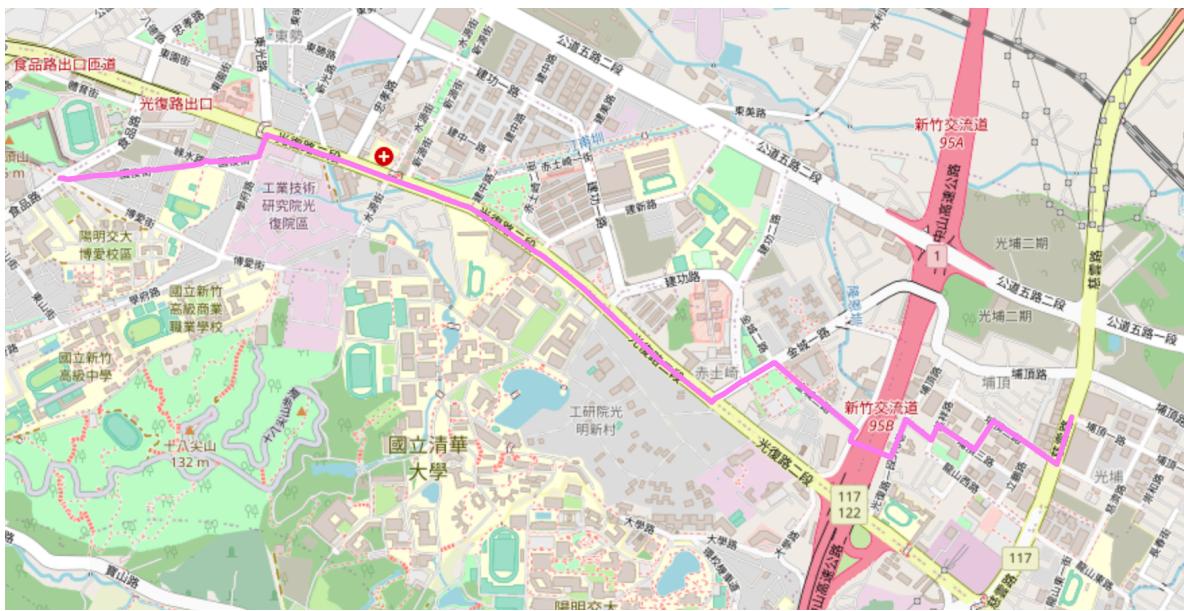


The number of nodes in the path found by DFS: 930

Total distance of path found by DFS: 38752.307999999895 m

The number of visited nodes in DFS: 9599

UCS

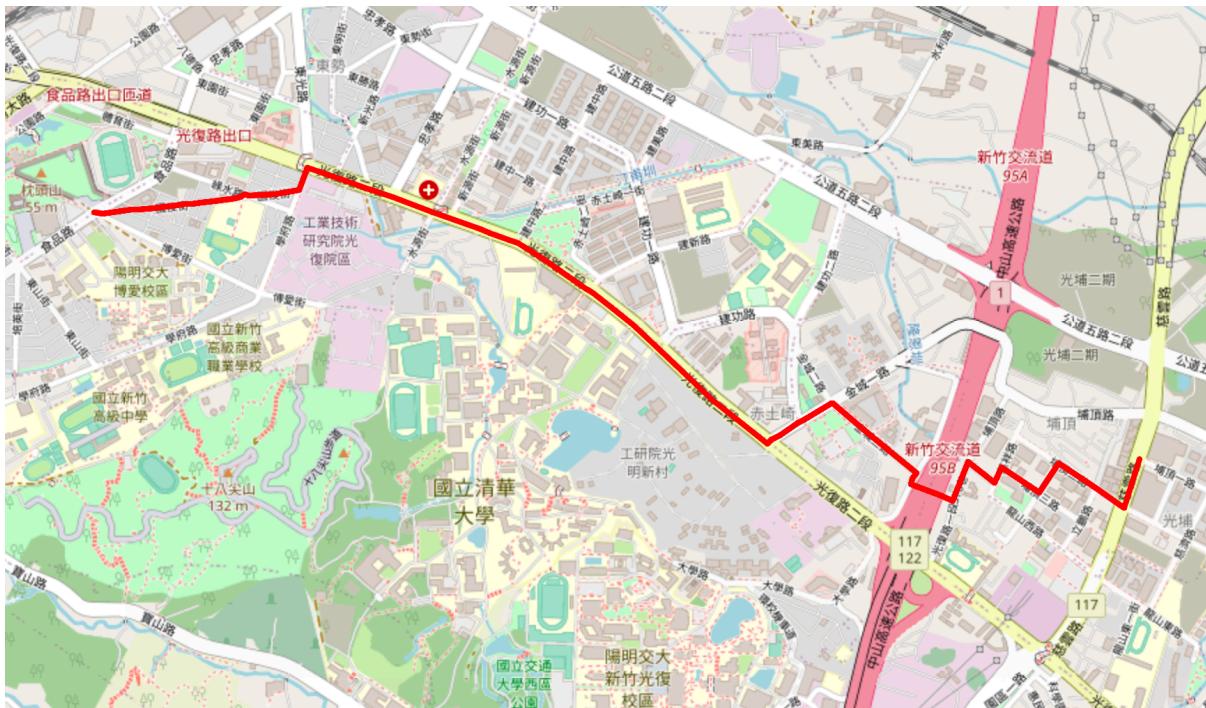


The number of nodes in the path found by UCS: 63

Total distance of path found by UCS: 4101.84 m

The number of visited nodes in UCS: 7207

A*



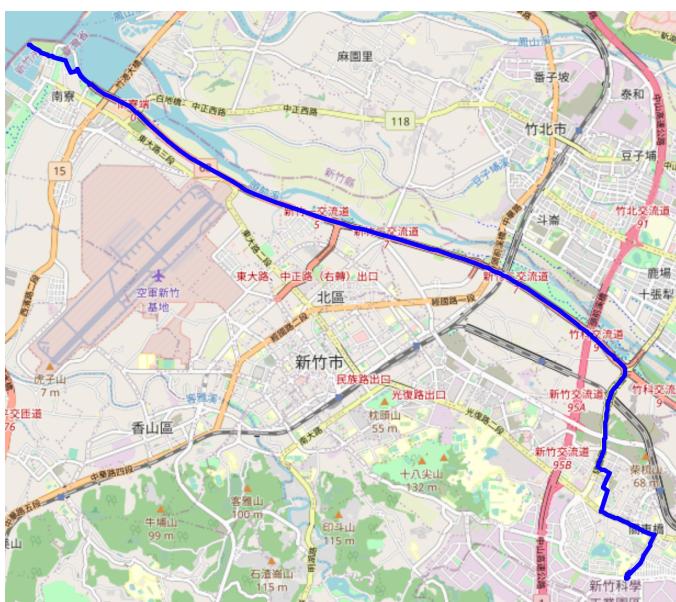
The number of nodes in the path found by A* search: 63

Total distance of path found by A* search: 4101.84 m

The number of visited nodes in A* search: 7207

3. From National Experimental High School At Hsinchu Science Park (ID: 1718165260) to Nanliao Fishing Port (ID: 8513026827)

BFS

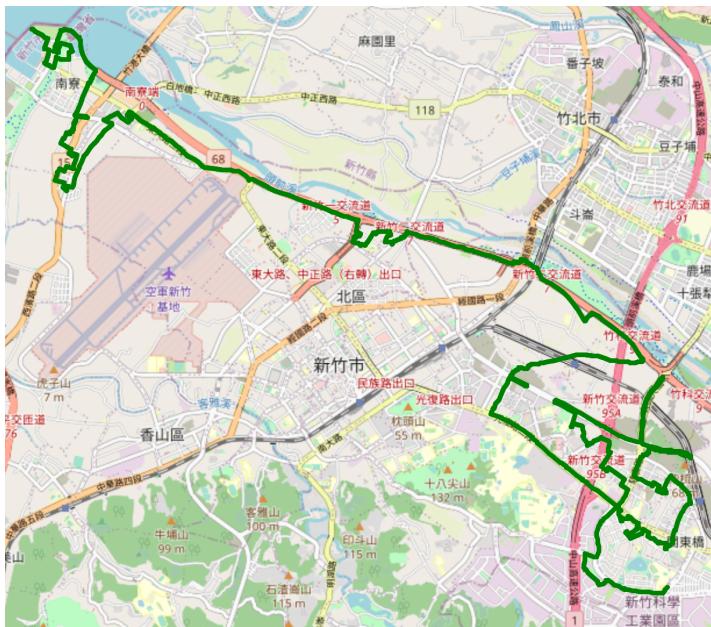


The number of nodes in the path found by BFS: 183

Total distance of path found by BFS: 15442.394999999995 m

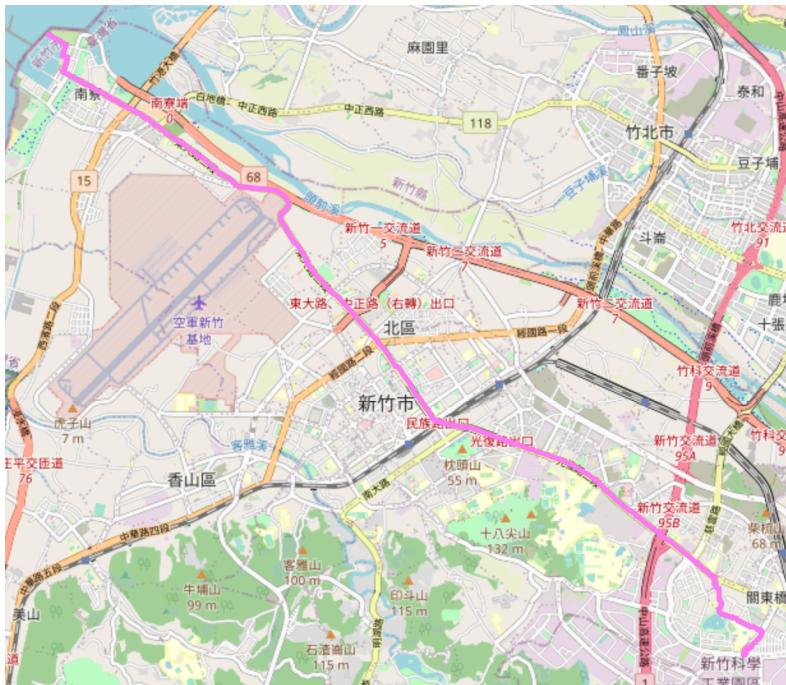
The number of visited nodes in BFS: 11226

DFS_stack



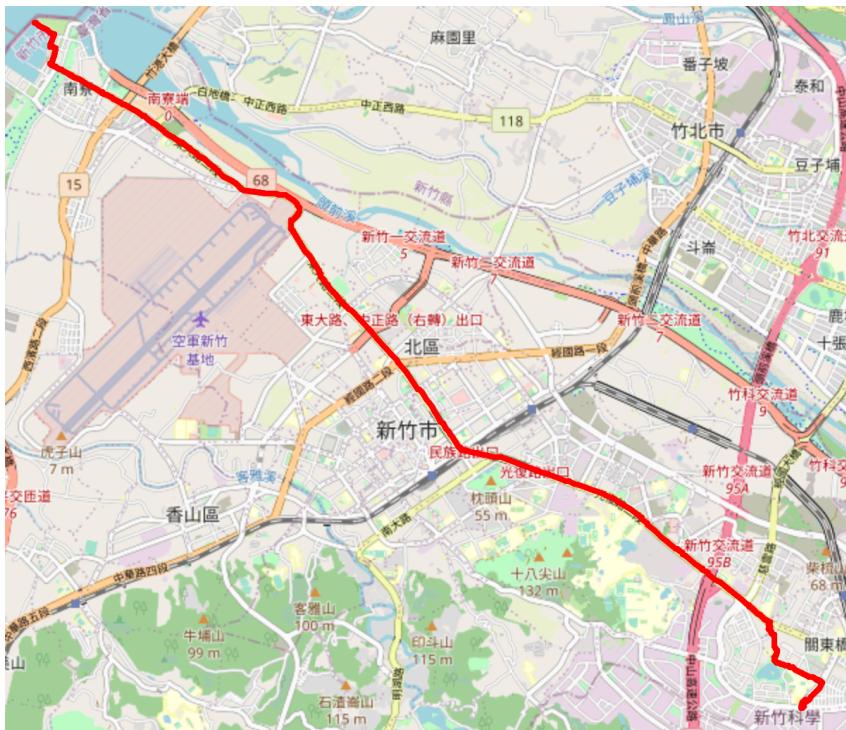
The number of nodes in the path found by DFS: 900
 Total distance of path found by DFS: 39219.993000000024 m
 The number of visited nodes in DFS: 2488

UCS



The number of nodes in the path found by UCS: 288
 Total distance of path found by UCS: 14212.412999999997 m
 The number of visited nodes in UCS: 11909

A*



The number of nodes in the path found by A* search: 288

Total distance of path found by A* search: 14212.412999999997 m

The number of visited nodes in A* search: 11909

Comparison

| Route 1 | BFS | DFS_stack | UCS | A* |
|-----------------------------|---------|-----------|----------|----------|
| Number of nodes in the path | 88 | 1718 | 89 | 89 |
| Total distance | 4978.88 | 75504.31 | 4367.881 | 4367.881 |
| Number of visited nodes | 4266 | 5667 | 5077 | 5077 |
| Route 2 | BFS | DFS_stack | UCS | A* |
| Number of nodes in the path | 60 | 930 | 63 | 63 |
| Total distance | 4215.52 | 38752.30 | 4101.84 | 4101.84 |
| Number of visited nodes | 4603 | 9599 | 7207 | 7207 |

| Route 3 | BFS | DFS_stack | UCS | A* |
|-----------------------------|----------|-----------|----------|----------|
| Number of nodes in the path | 183 | 900 | 288 | 288 |
| Total distance | 15442.39 | 39219.99 | 14212.41 | 14212.41 |
| Number of visited nodes | 11226 | 2488 | 11909 | 11909 |

Discussion:

1. For each route, BFS takes the least number of node in the final path, and visits the least nodes during traversal.
2. For each route, UCS and A* share the same final path and therefore has the same number of nodes in the path and the same total distance. For all 4 algorithms, they take the shortest total distance. However, UCS should visit way more nodes than A* does during traversal, which I didn't successfully implement.
3. For each route, DFS using stack takes the most number of node in the final path, the largest total distance. For the first and the second route, it also visits the most nodes during traversal.

III. Question Answering

1. Problem Encountered:

(1) For the previous lab, I used Anaconda as my programming environment, so this is my first time using Google Colab, and I don't really enjoy coding with it, you have to upload all the files to your drive and run the block for saving it every time or else it doesn't record your progress, also, the terminal wasn't really understandable for me. So I switched my environment to Visual Studio Code, then I encountered another problem that the version of Python in my VSCode was Python2 instead of Python3, so it couldn't compile several functions in my code. I tried to update it but it was helpless. At last, I tried to enter commands like "python3 bfs.py" in the terminal but not simply pressing the run button to ensure that it runs in python3, and it worked.

(2) I think that after the first lab, I wasn't so sure about how Python works, however after this assignment, I feel like I'm starting to embrace the advantages of Python. For example, when I write BFS and DFS in C++, I always

have to include the header files of queue and stack separately, while in Python, I need neither of them because I can simply use a list (which is in a format of a queue) and pop the thing I want to decide if it is first-in-first-out or first-in-last-out. Also, I learned how to use the sorting function and the delete function, which I believe would be really helpful in the future.

2. Besides speed limit and distance, I think the other attribute that is essential for route finding is the traffic flow of each road.
3. For mapping, it means to construct a graph with all the places as nodes and the roads as edges. For each road, record its length and the start and end node of it. For localization, you record the starting point, then estimate the possible speed of the vehicle by knowing the speed limit of each road, the traffic flow of it, and the traffic signs located there.
4. $h(x) = \text{the total of all roads divided by its own speed limit} \rightarrow$ This gives the fastest estimated time by expecting all the drivers would drive fast enough to meet the speed limit.