

# 3D DENSE MAPPING AND LOCALIZATION WITH ICP

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*Max Lu*  
April 26 2016



# PROJECT OVERVIEW

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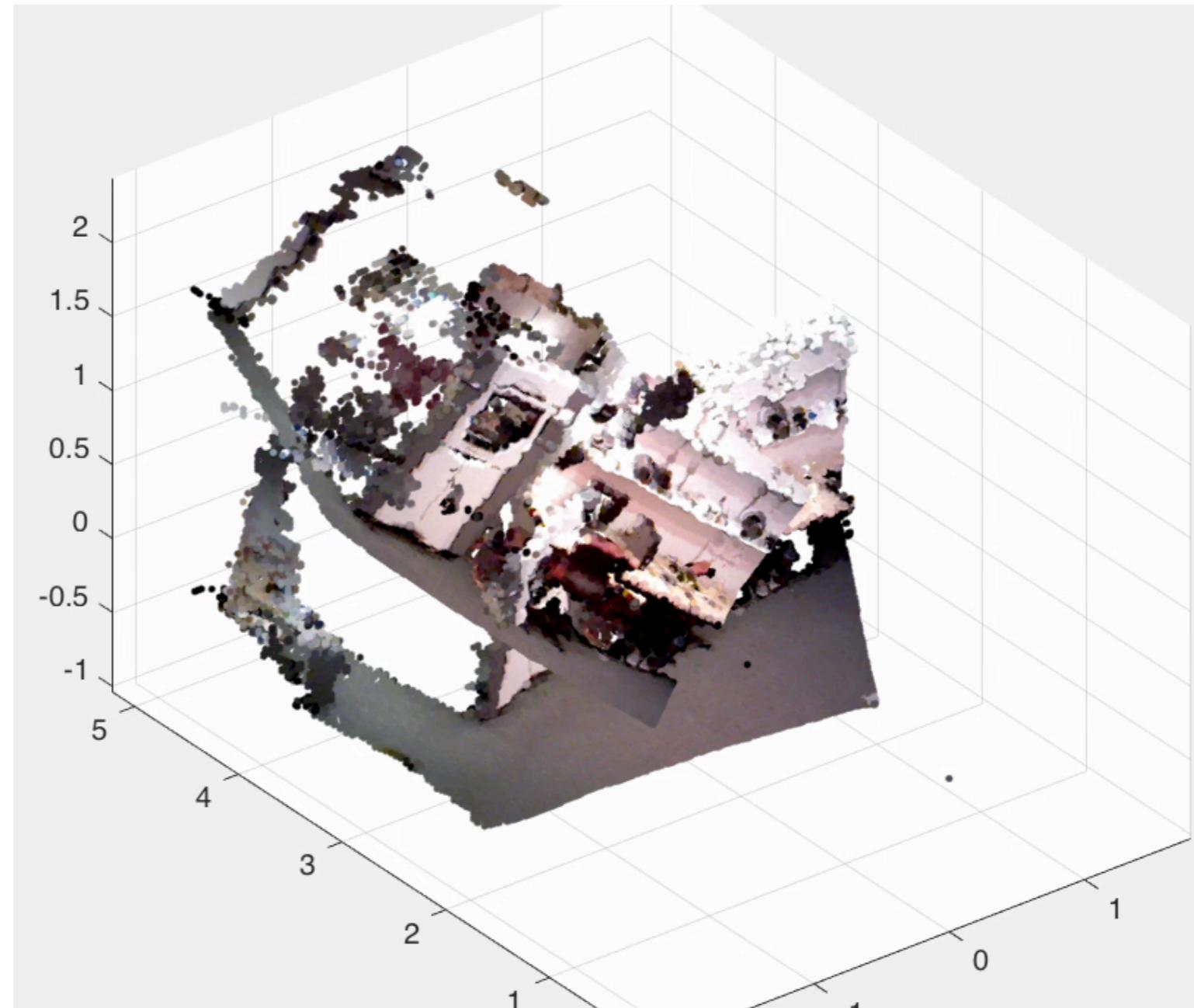
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- RGB-D Dataset
- Iterative Closest (Corresponding) Points
- Mapping and Localization



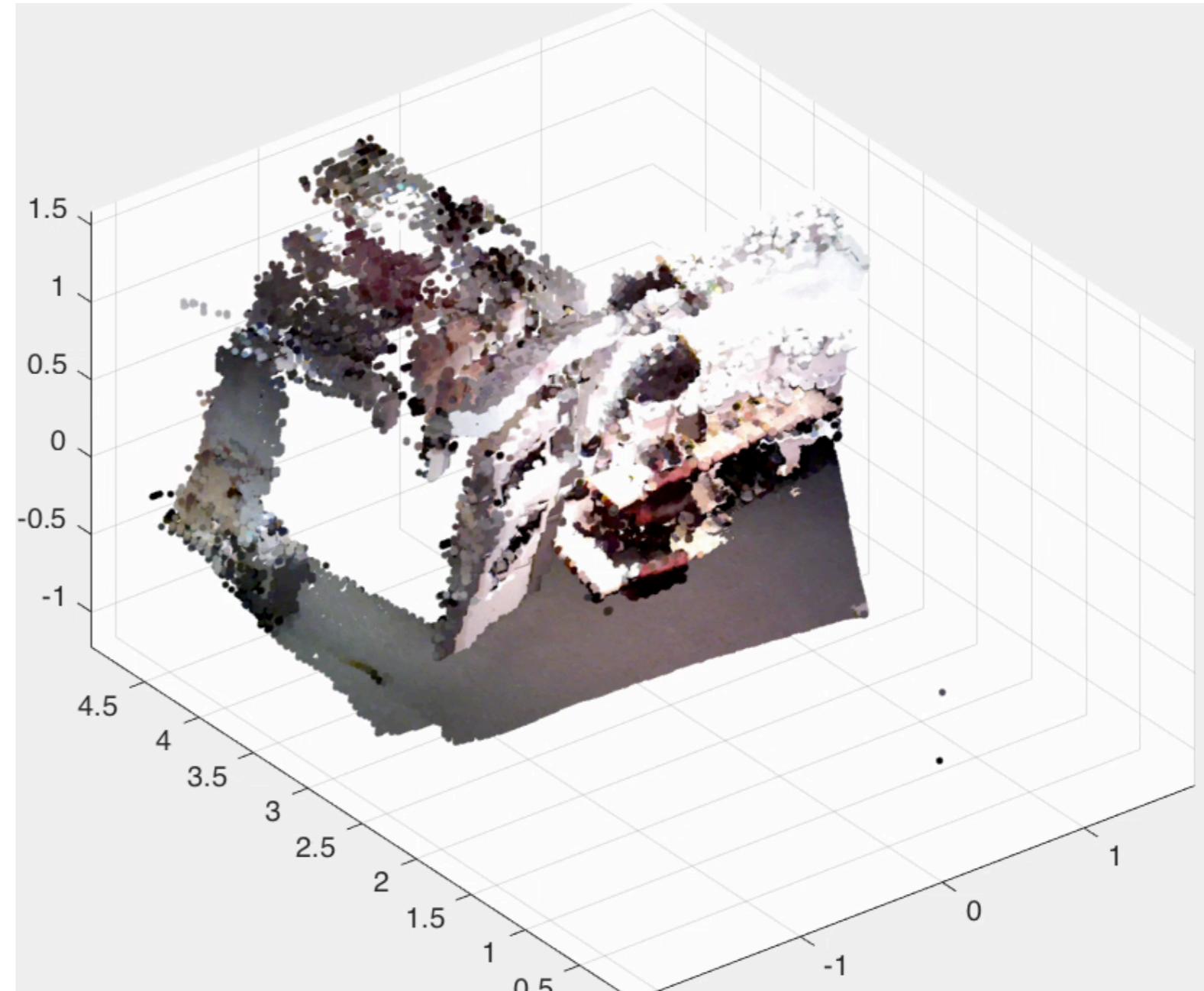
- .....  
• • • • •  
↓  
\* Sampling  
\* Matching  
\* Weighting  
\* Rejection  
\* Optimization  
• • • • •

*Frame 1 vs Frame 1*



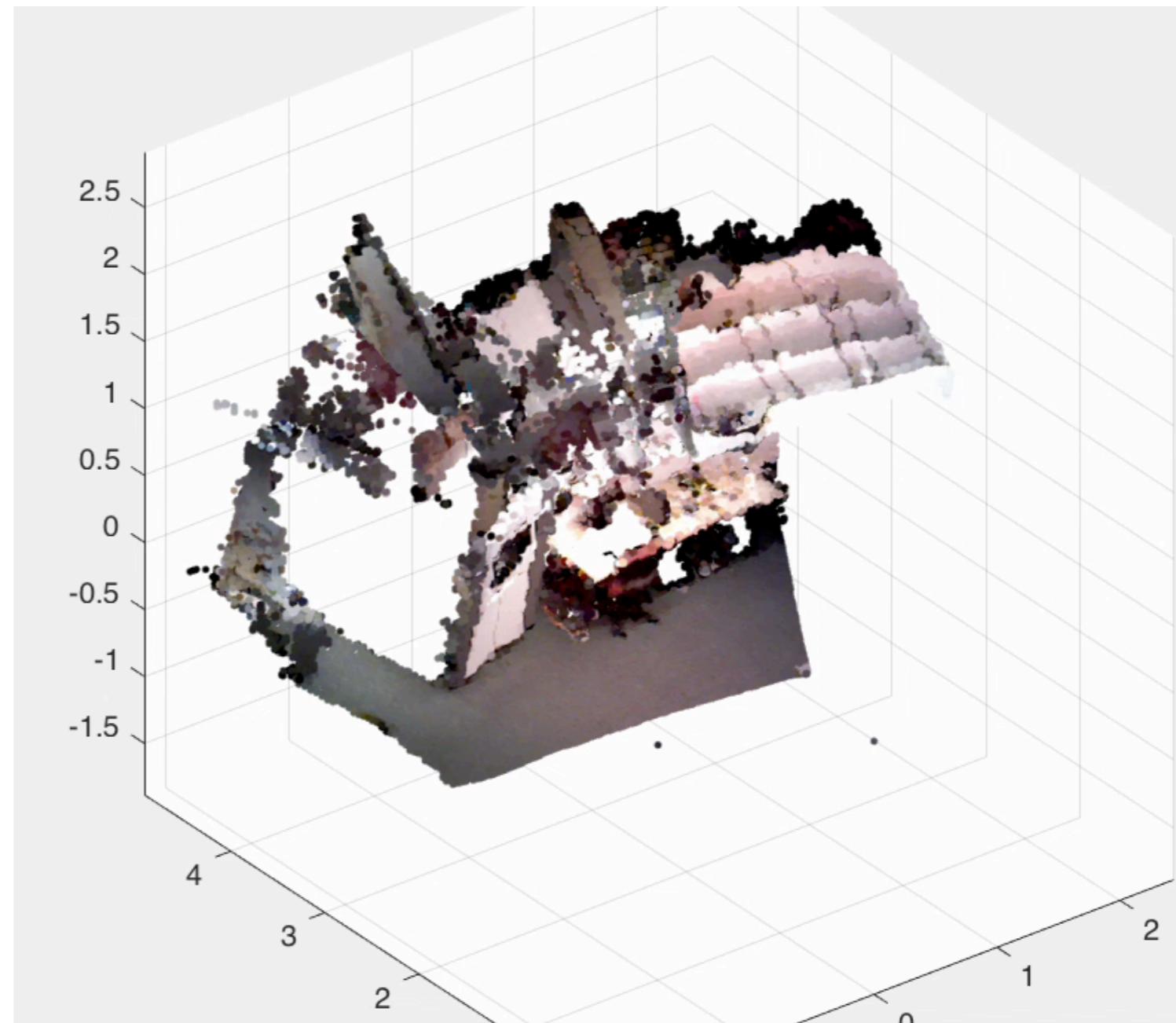
- \* *Sampling*
  - \* *Matching*
  - \* *Weighting*
  - \* *Rejection*
  - \* *Optimization*

## *Frame 1 vs Frame 50*



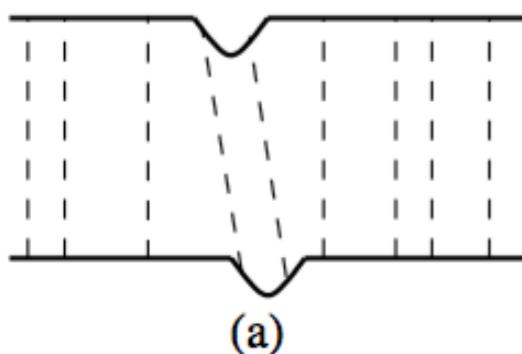
- • • • •
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- \* *Sampling*
- \* *Matching*
- \* *Weighting*
- \* *Rejection*
- \* *Optimization*
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*Frame 1 vs Frame 50*

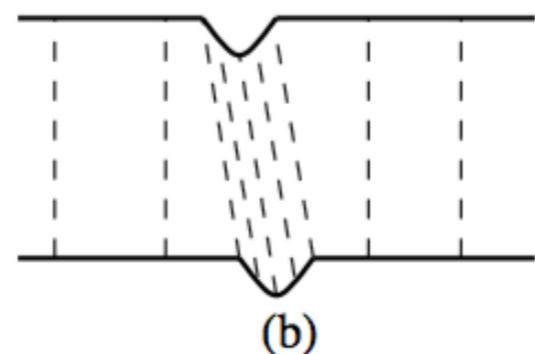


# ICP – SAMPLING

- Random Sampling (a)
- Normal-space Sampling (b)



(a)



(b)

Compute Normals

4-NN 3d points

PCA

*Sampling*

Convert 3d normals into 2d spherical coordinates

Binning all the normals

Uniform Sampling from bins

Efficient Variants of the ICP Algorithm

Szymon Rusinkiewicz  
Marc Levoy  
Stanford University

## Abstract

The ICP (Iterative Closest Point) algorithm is widely used for geometric alignment of three-dimensional models when an initial estimate of the relative pose is known. Many variants of ICP have been proposed, affecting all phases of the algorithm from the selection and matching of points to the minimization strategy. We enumerate and classify many of these variants, and evaluate their effect on the speed with which the correct alignment is reached. In order to improve convergence for nearly-flat meshes with small features, such as inscribed surfaces, we introduce a new variant based on uniform sampling of the space of normals. We conclude by proposing a combination of ICP variants optimized for high speed. We demonstrate an implementation that is able to align two range images in a few tens of milliseconds, assuming a good initial guess. This capability has potential application to real-time 3D model acquisition and model-based tracking.

consider the accuracy of the final answer and the ability of ICP to reach the correct solution given “difficult” geometry. Our comparisons suggest a combination of ICP variants that is able to align a pair of meshes in a few tens of milliseconds, significantly faster than most commonly-used ICP systems. The availability of such a real-time ICP algorithm may enable significant new applications in model-based tracking and 3D scanning.

In this paper, we first present the methodology used for comparing ICP variants, and introduce a number of test scenes used throughout the paper. Next, we summarize several ICP variants in each of the above six categories, and compare their convergence performance. As part of the comparison, we introduce the concept of normal-space-directed sampling, and show that it improves convergence in scenes involving sparse, small-scale surface features. Finally, we examine a combination of variants optimized for high speed.

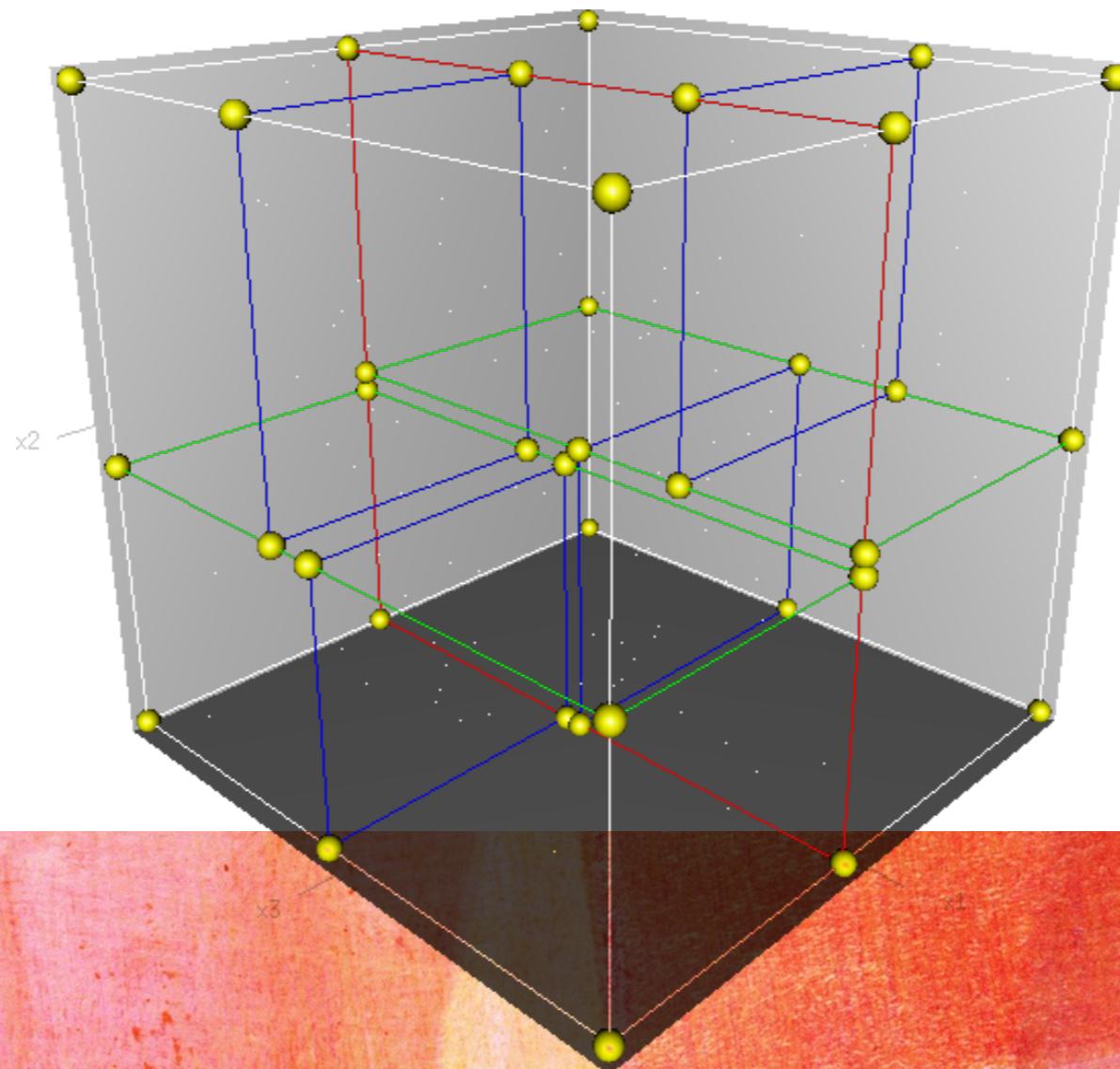
## 2 Comparison Methodology

Our goal is to compare the convergence characteristics of several ICP variants. In order to limit the scope of the problem, and avoid a combinatorial explosion in the number of possibilities, we adopt the methodology of choosing a *baseline* combination of variants, and examining performance as individual ICP stages are varied. The algorithm we will select as our baseline is essentially that of [Pulli 99], incorporating the following features:

- Random sampling of points on both meshes.
- Matching each selected point to the closest sample in the other mesh that has a normal within 45 degrees of the source normal.
- Uniform (constant) weighting of point pairs.
- Rejection of pairs containing edge vertices, as well as a percentage of pairs with the largest point-to-point distances.
- Point-to-plane error metric.
- The classic “select-match-minimize” iteration, rather than some other search for the alignment transform.

We pick this algorithm because it has received extensive use in a production environment [Levoy 00], and has been found to be

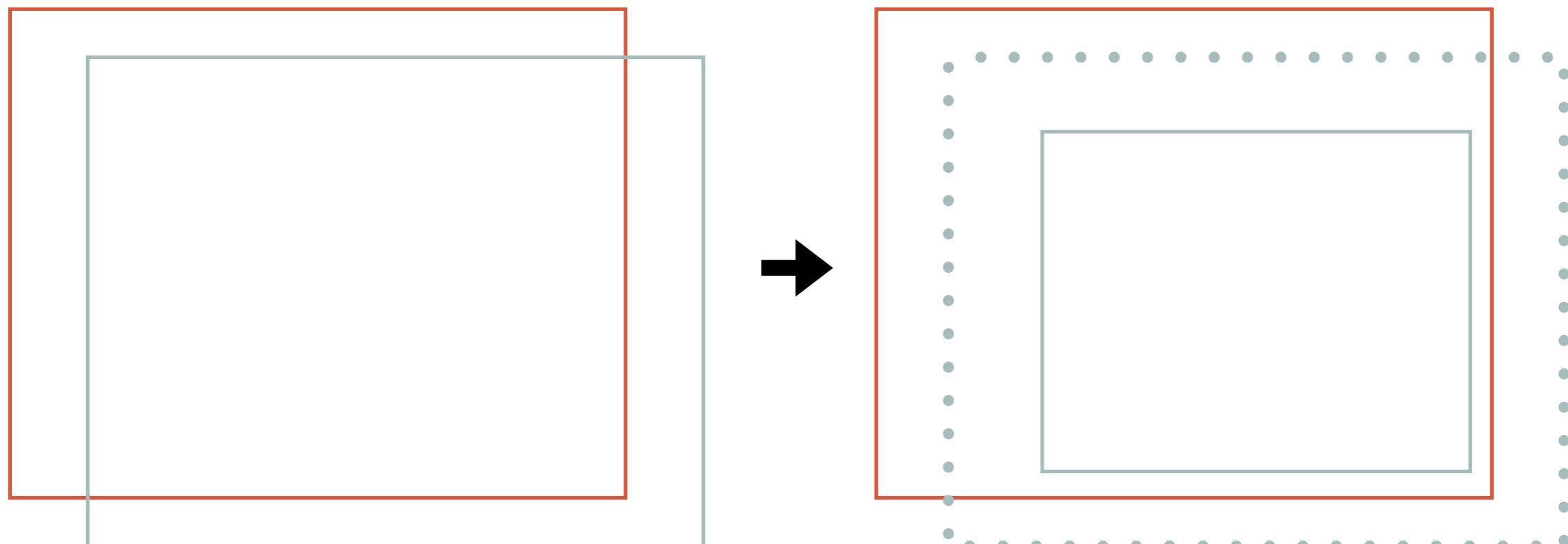
- Nearest Neighbor
- XYZ-RGB space
- K-d tree to accelerate the computation (Faster than KNN!)



# ICP - REJECTION

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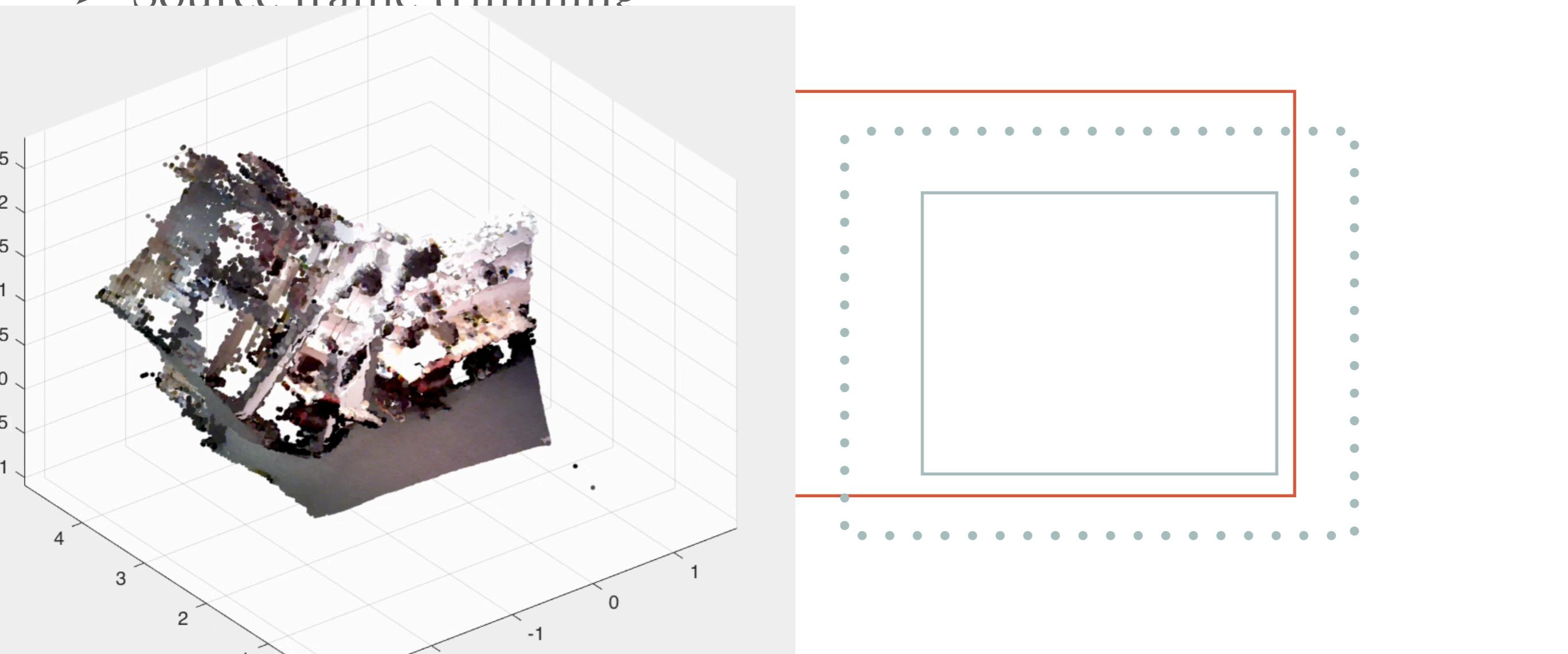
- Normal incompatibility (angle between normals  $> 45$  degree)
- Source frame trimming



# ICP - REJECTION

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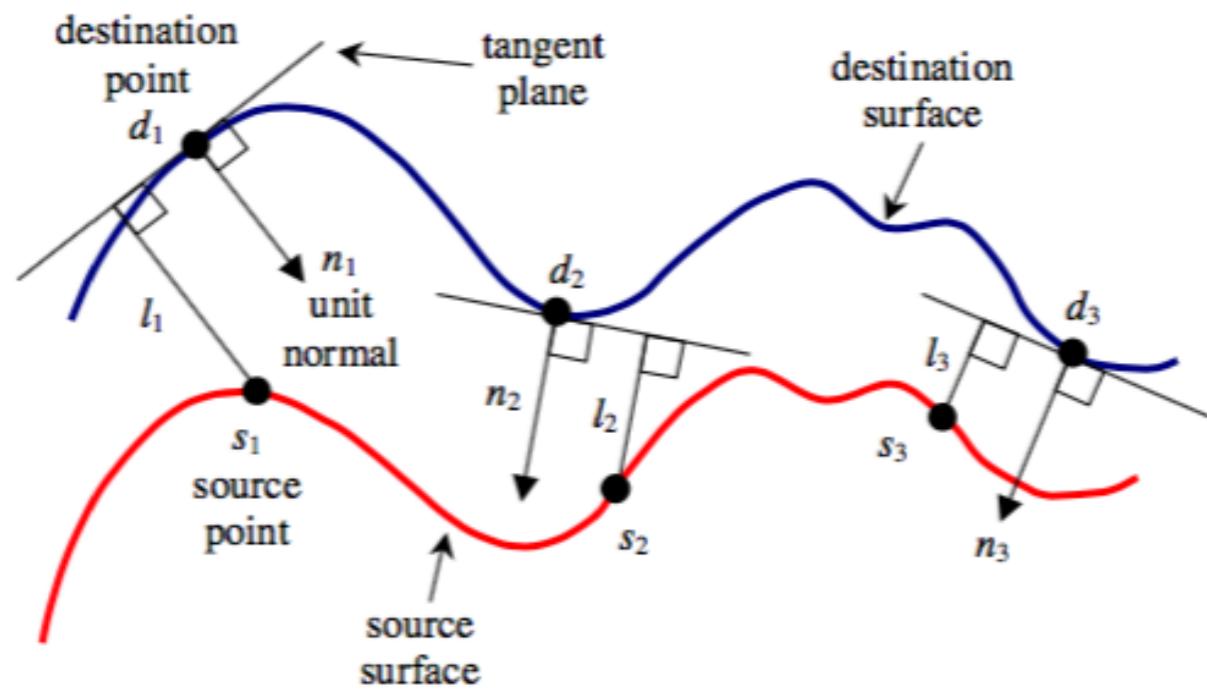
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# ICP – OPTIMIZATION METRIC

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- Least Squares
- Point 2 Plane



**Figure 1:** Point-to-plane error between two surfaces.

Technical Report TR04-004, Department of Computer Science, University of North Carolina at Chapel Hill

## Linear Least-Squares Optimization for Point-to-Plane ICP Surface Registration

Kok-Lim Low

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### ABSTRACT

The Iterative Closest Point (ICP) algorithm that uses the point-to-plane error metric has been shown to converge much faster than one that uses the point-to-point error metric. At each iteration of the ICP algorithm, the change of relative pose that gives the minimal point-to-plane error is usually solved using standard nonlinear least-squares methods, which are often very slow. Fortunately, when the relative orientation between the two input surfaces is small, we can approximate the nonlinear optimization problem with a linear least-squares one that can be solved more efficiently. We detail the derivation of a linear system whose least-squares solution is a good approximation to that obtained from a nonlinear optimization.

### 1 INTRODUCTION

3D shape alignment is an important part of many applications. It is used for object recognition in which newly acquired shapes in the environment are fitted to model shapes in the database. For reverse engineering and building real-world models for virtual reality, it is used to align multiple partial range scans to form models that are more complete. For autonomous range acquisition, 3D registration is used to accurately localize the range scanner, and to align data from multiple scans for view-planning

In [Rusinkiewicz01], it was suggested that the relative orientation (rotation) between the two input surfaces can be approximated by a linear least-squares one, so as to speed up the iterative optimization process. This approximation is simply done by replacing the rotation matrix  $R$  in the rotation matrix  $R\mathbf{t}$  by a unitary matrix  $U$ .

In this technical report, we describe how to derive a linear system of linear equations to approximate the nonlinear optimization problem, and demonstrate how the linear system can be obtained (via singular value decomposition). A 3D rigid-body transformation is derived from the linear least-squares solution.

### 2 POINT-TO-PLANE ICP ALGORITHM

Given a source surface and a destination surface, the ICP algorithm first establishes correspondence between points in the source surface and the destination surface. For example, for each point  $s$  in the source surface, the nearest point on the destination surface is found. Correspondence [Besl92] (see [Rusinkiewicz01] for a survey) is used to find point correspondences. The ICP iteration is a 3D rigid-body transformation that moves the source points such that the total error is minimized.

# ICP - OPTIMIZATION

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- Least Squares
- Point 2 Plane

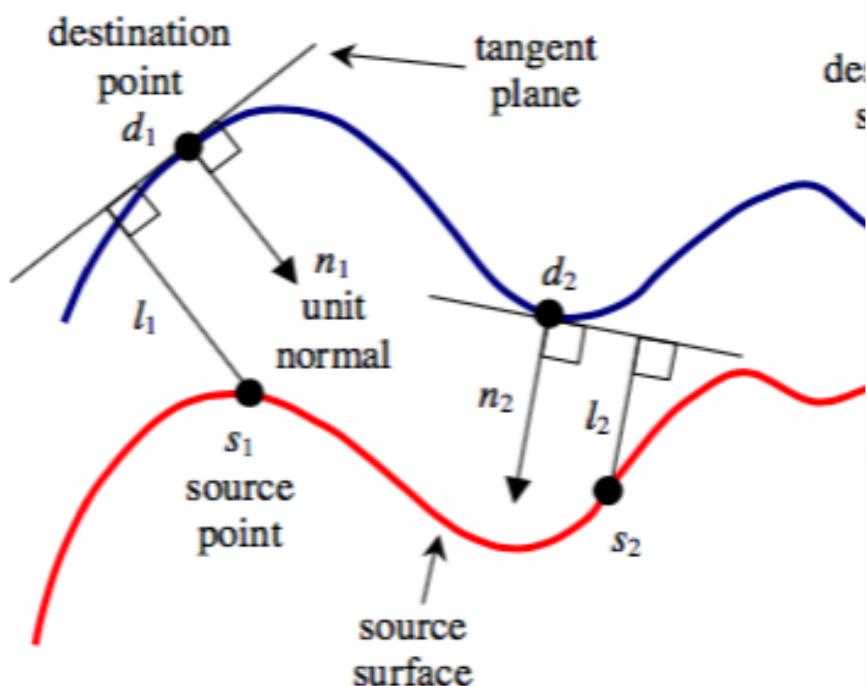
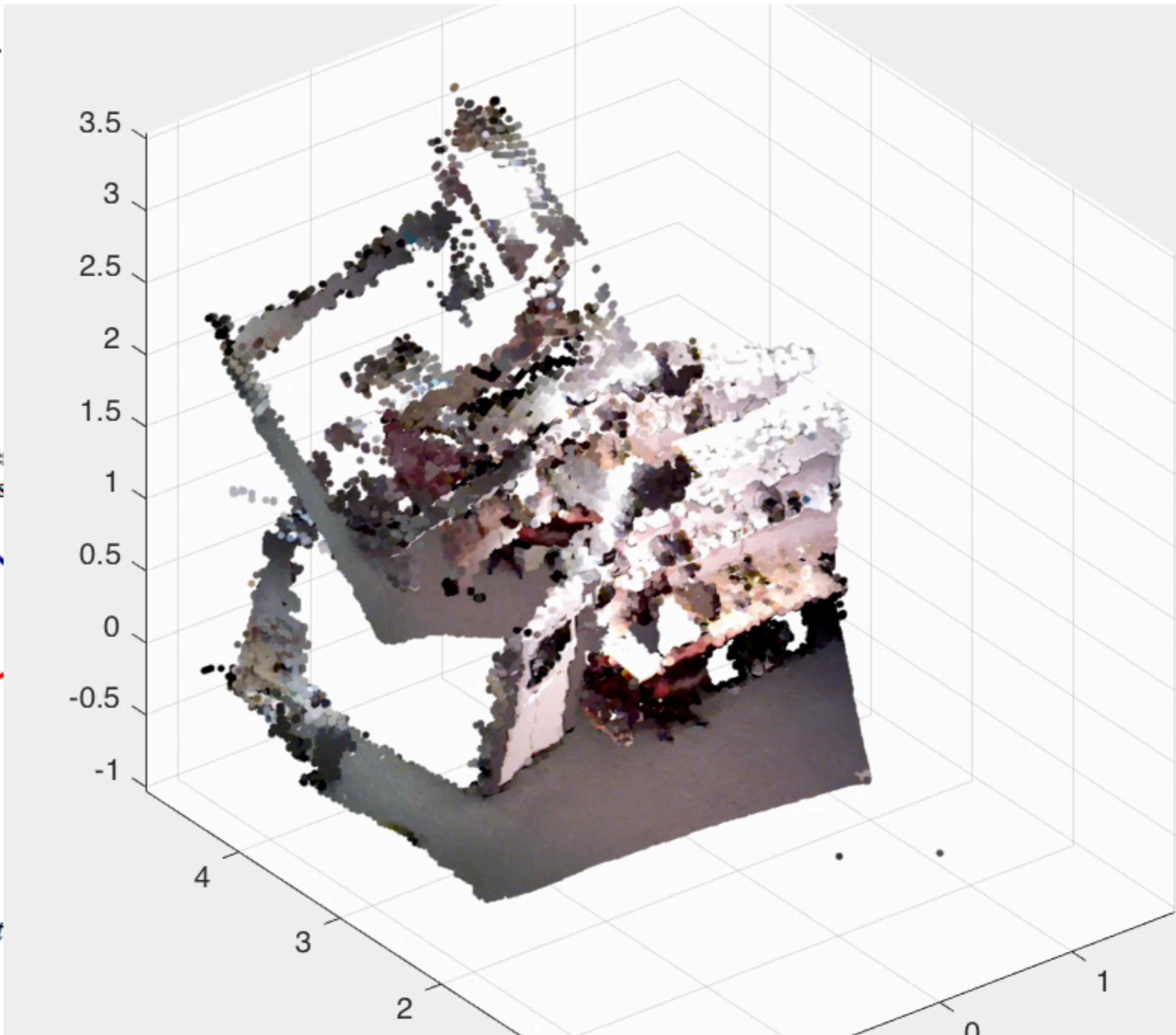


Figure 1: Point-to-plane error between two surfaces.



# MAPPING & LOCALIZATION

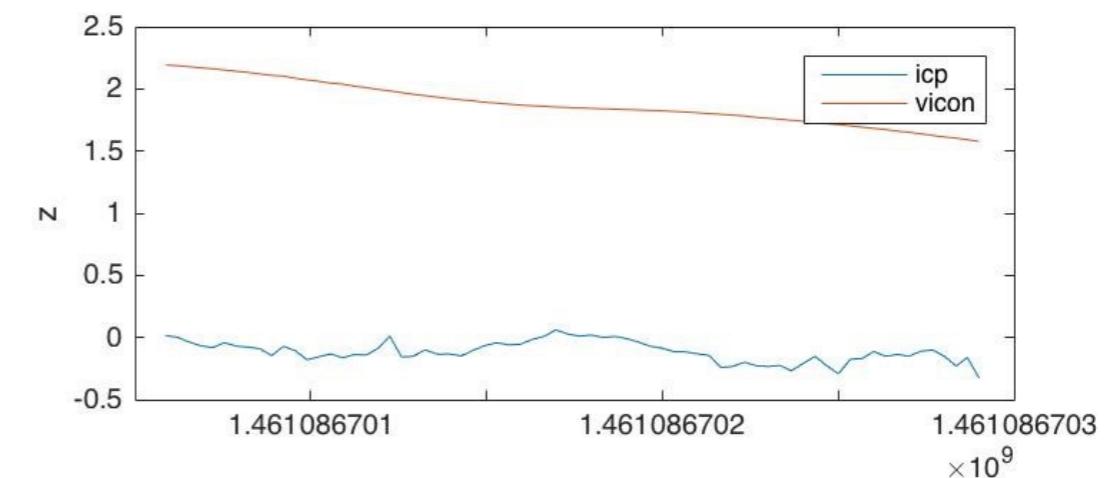
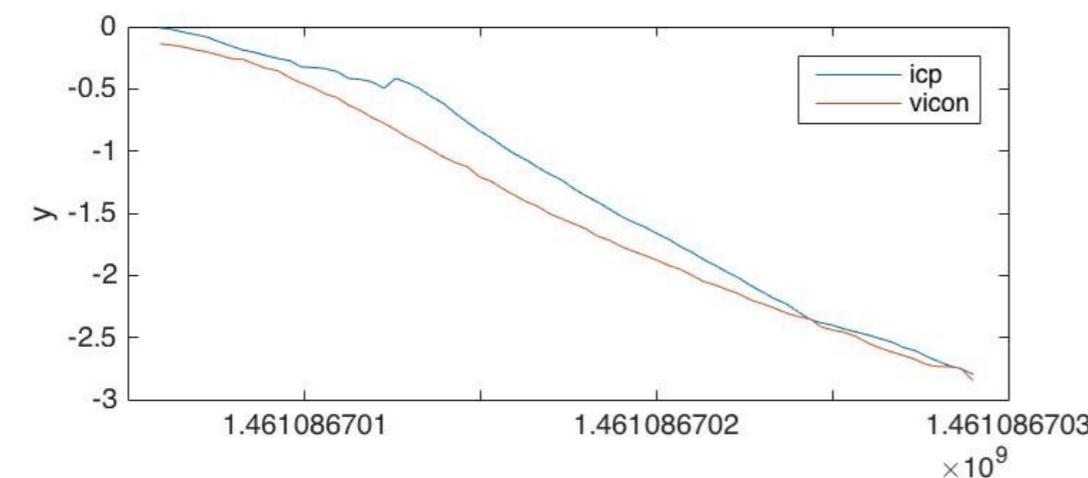
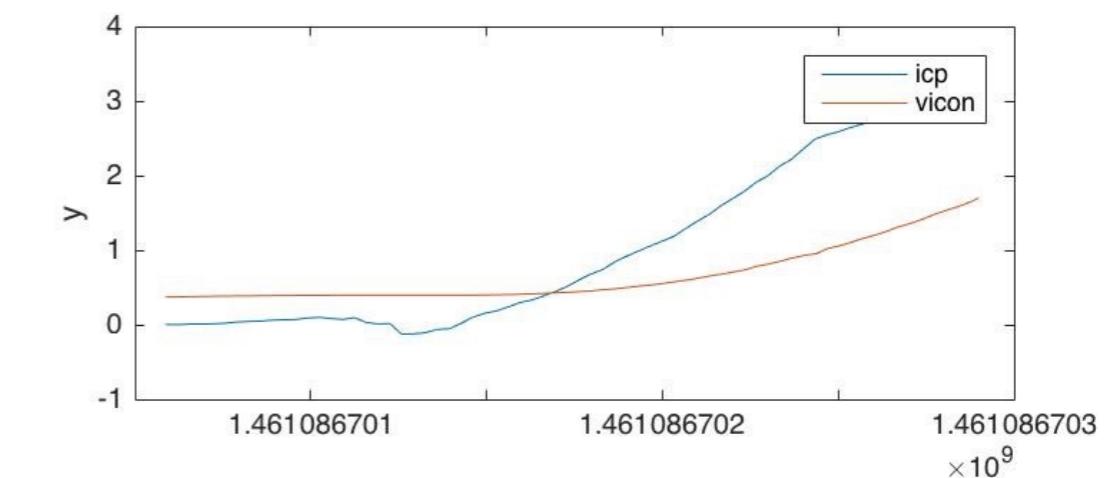
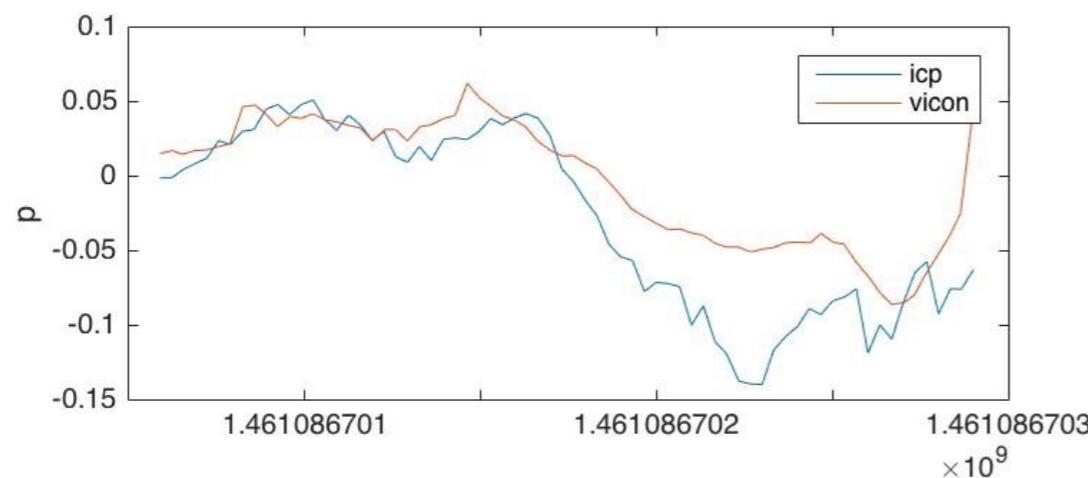
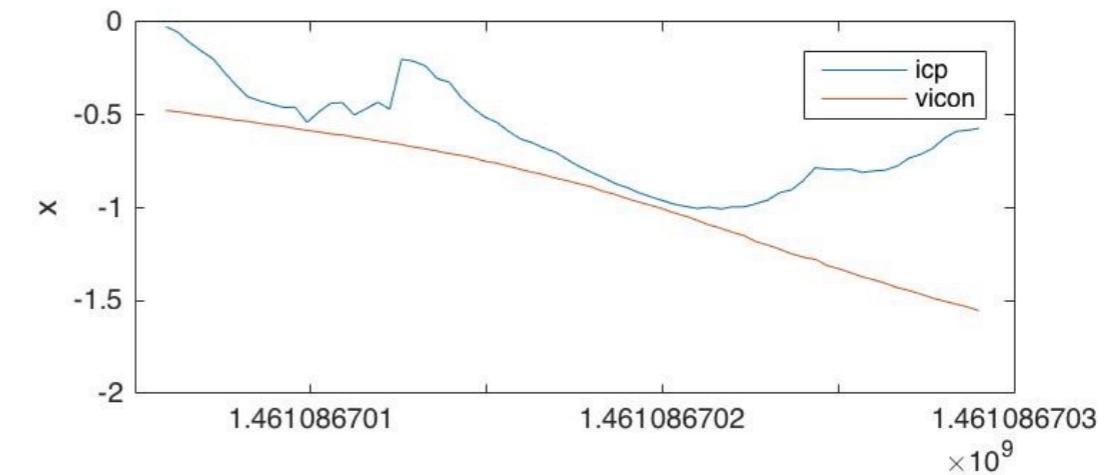
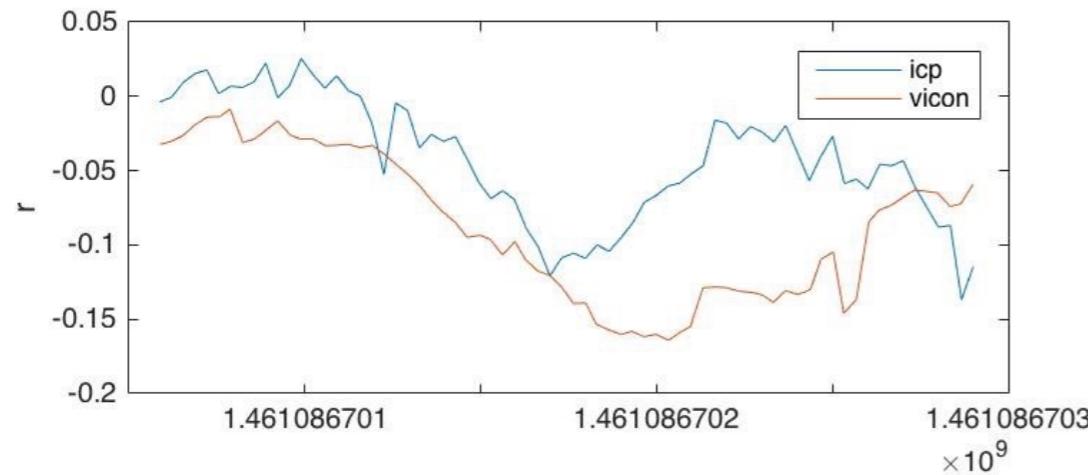
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- Vicon data
- Camera distortion & Noise
- Live Demo

# MAPPING & LOCALIZATION

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# NEXT STEP

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- Global registration
- Feature-based sampling, matching, & Rejection (Plane estimation, etc)
- Model de-noising and smoothing
- Merge Vicon data (EKF etc. ?)

# THANK YOU!

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