# Computer Vision Assignment 2

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## Solution 2

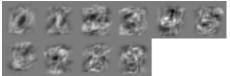
MNIST Data: 93-2-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-					
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## Solution 3(a)

Data= MNIST Training batch size = 1000 Testing batch size = 1000 Validation Batch size = 1000

#### Weights:



#### Output:

```
Started training!
train | epoch = 1 | lr = 0.1000 | loss: 24230.8342 | error: 642.0000 - valid | validloss: 6381.4538 | validerror: 361.0000 | s/iter:
0.2283
train | epoch = 2 | lr = 0.1000 | loss: 2192.4192 | error: 201.0000 - valid | validloss: 4167.5076 | validerror: 300.0000 | s/iter:
train | epoch = 3 | lr = 0.1000 | loss: 2763.5068 | error: 224.0000 - valid | validloss: 4796.0216 | validerror: 295.0000 | s/iter:
0.2055
train | epoch = 4 | lr = 0.1000 | loss: 1156.4391 | error: 130.0000 - valid | validloss: 1736.8518 | validerror: 189.0000 | s/iter:
0.2052
train | epoch = 5 | lr = 0.1000 | loss: 587.1516 | error: 89.0000 - valid | validloss: 1859.4947 | validerror: 216.0000 | s/iter:
0.2107
train | epoch = 6 | lr = 0.1000 | loss: 479.1976 | error: 81.0000 - valid | validloss: 1726.2918 | validerror: 195.0000 | s/iter:
0.2021
train | epoch = 7 | lr = 0.1000 | loss: 353.1795 | error: 79.0000 - valid | validloss: 1620.5536 | validerror: 192.0000 | s/iter:
train | epoch = 8 | lr = 0.1000 | loss: 301.1951 | error: 62.0000 - valid | validloss: 1391.0998 | validerror: 179.0000 | s/iter:
train | epoch = 9 | lr = 0.1000 | loss: 909.5289 | error: 97.0000 - valid | validloss: 2449.6014 | validerror: 237.0000 | s/iter:
0.2035
train | epoch = 10 | lr = 0.1000 | loss: 261.1198 | error: 54.0000 - valid | validloss: 1473.0624 | validerror: 168.0000 | s/iter:
0.2010
test | error: 172.0000
```

#### Solution 3(b)

Data= MNIST Training batch size = 1000 Testing batch size = Full Validation Batch size = Full

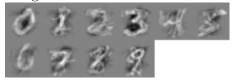
Weights: (Solution 3(a))

Output:

```
Started training!
train | epoch = 1 | lr = 0.1000 | loss: 24068.8428 | error: 633.0000 - valid | validloss: 6816.1372 | validerror: 3908.0000 | s/iter:
1.1765
train | epoch = 2 | lr = 0.1000 | loss: 2815.8436 | error: 220.0000 - valid | validloss: 2409.8042 | validerror: 2222.0000 | s/iter:
1.0915
train | epoch = 3 | lr = 0.1000 | loss: 2034.2651 | error: 181.0000 - valid | validloss: 1733.7340 | validerror: 1743.0000 | s/iter:
1.1065
train | epoch = 4 | lr = 0.1000 | loss: 849.8391 | error: 110.0000 - valid | validloss: 1670.8067 | validerror: 1813.0000 | s/iter:
1.1047
train | epoch = 5 | lr = 0.1000 | loss: 541.3584 | error: 83.0000 - valid | validloss: 1366.3635 | validerror: 1635.0000 | s/iter:
1,1023
train | epoch = 6 | lr = 0.1000 | loss: 859.5161 | error: 129.0000 - valid | validloss: 1411.4094 | validerror: 1575.0000 | s/iter:
1.0992
train | epoch = 7 | lr = 0.1000 | loss: 369.0440 | error: 82.0000 - valid | validloss: 1515.7540 | validerror: 1826.0000 | s/iter:
1.0971
train | epoch = 8 | lr = 0.1000 | loss: 560.5294 | error: 102.0000 - valid | validloss: 1863.3577 | validerror: 2077.0000 | s/iter:
1.1024
train | epoch = 9 | lr = 0.1000 | loss: 364.5681 | error: 81.0000 - valid | validloss: 1522.1837 | validerror: 1733.0000 | s/iter:
1.1118
train | epoch = 10 | lr = 0.1000 | loss: 347.1860 | error: 80.0000 - valid | validloss: 1597.3836 | validerror: 1707.0000 | s/iter:
1.1012
test | error: 1773.0000
```

Training batch size = 50 Testing batch size = Full Validation Batch size = Full

#### Weights:



#### Output:

```
Started training!
train | epoch = 1 | lr = 0.1000 | loss: 90.0954 | error: 50.0000 - valid | validloss: 31438.4139 | validerror: 8682.0000 | s/iter:
1.0458
train | epoch = 2 | lr = 0.1000 | loss: 23607.4596 | error: 37.0000 - valid | validloss: 34350.9191 | validerror: 7231.0000 | s/iter:
1.0100
train | epoch = 3 | lr = 0.1000 | loss: 37256.6338 | error: 32.0000 - valid | validloss: 36009.7375 | validerror: 7331.0000 | s/iter:
1.0060
train | epoch = 4 | lr = 0.1000 | loss: 31562.3642 | error: 26.0000 - valid | validloss: 23038.2053 | validerror: 5905.0000 | s/iter:
0.9959
train | epoch = 5 | lr = 0.1000 | loss: 17958.7962 | error: 23.0000 - valid | validloss: 18427.7558 | validerror: 5515.0000 | s/iter:
1.0025
train | epoch = 6 | lr = 0.1000 | loss: 7299.0775 | error: 19.0000 - valid | validloss: 10424.1505 | validerror: 5613.0000 | s/iter:
1.0031
train | epoch = 7 | lr = 0.1000 | loss: 2741.1831 | error: 11.0000 - valid | validloss: 6625.9933 | validerror: 3935.0000 | s/iter:
1.0044
train | epoch = 8 | lr = 0.1000 | loss: 414.9122 | error: 2.0000 - valid | validloss: 5901.6454 | validerror: 3944.0000 | s/iter:
0.9973
train | epoch = 9 | lr = 0.1000 | loss: 0.0000 | error: 0.0000 - valid | validloss: 5901.6454 | validerror: 3944.0000 | s/iter: 0.9968 train | epoch = 10 | lr = 0.1000 | loss: 0.0000 | error: 0.0000 - valid | validloss: 5901.6454 | validerror: 3944.0000 | s/iter:
1.0010
test | error: 4085.0000
```

The test error for Training Size=1000: 1773.00 The test error for Training Size=50: 4085.00

The test error has increased.

Small training size, results in less generalization, which can be seen while comparing the images of the weights.

We can se that the loss converges to 0, which means that there is overfitting of data.

So, the lack of sufficient training data and overfitting leads to higher error

#### Solution 4

Sequential Network Linear(1,1000) Tanh() Linear(1000,10)

Data= MNIST Training batch size = 1000 Testing batch size = 1000 Validation Batch size = 1000

Learning Rate=0.1

#### Output:

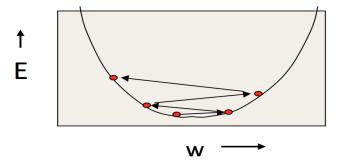
```
Started training!
train | epoch = 1 | lr = 0.1000 | loss: 5.8203 | error: 726.0000 - valid | validloss: 9.2654 | validerror: 808.0000 | s/iter: 0.3874
train | epoch = 2 | lr = 0.1000 | loss: 10.9501 | error: 735.0000 - valid | validloss: 11.8801 | validerror: 596.0000 | s/iter: 0.3717
train | epoch = 3 | lr = 0.1000 | loss: 12.0459 | error: 709.0000 - valid | validloss: 11.7269 | validerror: 674.0000 | s/iter: 0.3687
train | epoch = 4 | lr = 0.1000 | loss: 10.3445 | error: 671.0000 - valid | validloss: 9.6046 | validerror: 579.0000 | s/iter: 0.3662
train | epoch = 5 | lr = 0.1000 | loss: 10.5664 | error: 632.0000 - valid | validloss: 7.7937 | validerror: 570.0000 | s/iter: 0.3664
train | epoch = 6 | lr = 0.1000 | loss: 9.2159 | error: 616.0000 - valid | validloss: 8.6705 | validerror: 594.0000 | s/iter: 0.3663
train | epoch = 7 | lr = 0.1000 |
                                 loss: 6.9828 | error: 552.0000 - valid | validloss: 8.7377 |
                                                                                               validerror: 426.0000 |
                                                                                                                     s/iter: 0.3653
train | epoch = 8 | lr = 0.1000 | loss: 6.3810 | error: 557.0000 - valid | validloss: 9.7003 |
                                                                                               validerror: 674.0000 |
train | epoch = 9 | lr = 0.1000 | loss: 7.4764 | error: 559.0000 - valid | validloss: 6.6970 | validerror: 532.0000 | s/iter: 0.3609
train | epoch = 10 | lr = 0.1000 | loss: 5.7766 | error: 523.0000 - valid | validloss: 6.8547 | validerror: 546.0000 | s/iter: 0.3649
test | error: 543.0000
```

#### Learning Rate=10.0

#### Output:

```
Started training!
train | epoch = 1 | lr = 10.0000 | loss: 3037.5151 | error: 901.0000 - valid | validloss: 5228.1623 | validerror: 900.0000 | s/iter:
0.3725
train | epoch = 2 | lr = 10.0000 | loss: 3927.6720 | error: 906.0000 - valid | validloss: 5017.1181 | validerror: 795.0000 | s/iter:
0.3531
train | epoch = 3 | lr = 10.0000 | loss: 3842.2043 | error: 882.0000 - valid | validloss: 4554.0584 | validerror: 896.0000 | s/iter:
0.3558
train | epoch = 4 | lr = 10.0000 | loss: 4380.0806 | error: 905.0000 - valid | validloss: 4017.2982 | validerror: 813.0000 | s/iter:
0.3547
train | epoch = 5 | lr = 10.0000 | loss: 3584.1842 | error: 864.0000 - valid | validloss: 4413.3504 | validerror: 900.0000 | s/iter:
0.3566
train | epoch = 6 | lr = 10.0000 | loss: 4092.4456 | error: 885.0000 - valid | validloss: 4231.3322 | validerror: 900.0000 | s/iter:
train | epoch = 7 | lr = 10.0000 | loss: 3697.0259 | error: 867.0000 - valid | validloss: 4069.8637 | validerror: 798.0000 | s/iter: 0.3541
train | epoch = 8 | lr = 10.0000 | loss: 3089.1885 | error: 819.0000 - valid | validloss: 3480.3622 | validerror: 900.0000 | s/iter:
0.3565
train | epoch = 9 | lr = 10.0000 | loss: 3710.1879 | error: 873.0000 - valid | validloss: 3149.9053 | validerror: 897.0000 | s/iter:
0.3547
train | epoch = 10 | lr = 10.0000 | loss: 3133.2058 | error: 840.0000 - valid | validloss: 3676.1565 | validerror: 727.0000 | s/iter:
0.3597
test | error: 722.0000
```

Since the learning rate is big, gradient descent is not able to converge to the minima (as the step size overshoots the minima and increases the loss) The above scenario can be explained by the following image:



Therefore, we can see the training loss increase for learning rate=10 Since, the training loss is not minimized, the network is not optimally trained, resulting in higher test error( in comparison to learning rate=.1)

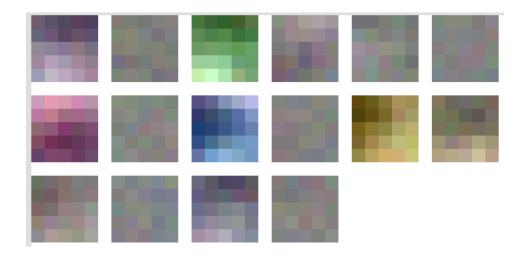
#### Solution 5

```
\begin{split} &\operatorname{CNN:} \\ &\operatorname{network} = \operatorname{nn.Sequential}() \\ &\operatorname{network} : \operatorname{add}(\operatorname{nn.SpatialConvolution}(3,16,5,5)) \\ &\operatorname{network} : \operatorname{add}(\operatorname{nn.Tanh}()) \\ &\operatorname{network} : \operatorname{add}(\operatorname{nn.SpatialMaxPooling}(2,2)) \\ &\operatorname{network} : \operatorname{add}(\operatorname{nn.SpatialConvolution}(16,128,5,5)) \\ &\operatorname{network} : \operatorname{add}(\operatorname{nn.Tanh}()) \\ &\operatorname{network} : \operatorname{add}(\operatorname{nn.SpatialMaxPooling}(2,2)) \\ &\operatorname{network} : \operatorname{add}(\operatorname{nn.View}(128*5*5)) \\ &\operatorname{network} : \operatorname{add}(\operatorname{nn.Linear}(128*5*5,64)) \\ &\operatorname{network} : \operatorname{add}(\operatorname{nn.Linear}(64,10)) \\ \end{split}
```

#### Output:

```
Started training!
train | epoch = 1 | lr = 0.1000 | loss: 2.2330 | error: 10220.0000 - valid | validloss: 2.0966 | validerror: 2441.0000 | s/iter:
        epoch = 2 | lr = 0.1000 | loss: 2.1084 | error: 9432.0000 - valid | validloss: 2.0924 | validerror: 2383.0000 | s/iter:
37.4676
        epoch = 3 | lr = 0.1000 | loss: 2.0472 | error: 9108.0000 - valid | validloss: 1.9477 | validerror: 2136.0000 | s/iter:
30.7322
train |
29.8809
        epoch = 4 | lr = 0.1000 | loss: 1.9404 | error: 8565.0000 - valid | validloss: 1.9124 | validerror: 2076.0000 | s/iter:
train | epoch = 5 | lr = 0.1000 | loss: 1.9045 | error: 8368.0000 - valid | validloss: 1.8570 | validerror: 2080.0000 | s/iter:
        epoch = 6 | lr = 0.1000 | loss: 1.7741 | error: 7715.0000 - valid | validloss: 1.8345 | validerror: 2050.0000 | s/iter:
train |
27.4241
train |
        epoch = 7 | lr = 0.1000 | loss: 1.7492 | error: 7610.0000 - valid | validloss: 1.7036 | validerror: 1852.0000 | s/iter:
27,1194
        epoch = 8 | lr = 0.1000 | loss: 1.7080 | error: 7399.0000 - valid | validloss: 1.7161 | validerror: 1896.0000 | s/iter:
27.1138
Train | epoch = 9 | lr = 0.1000 | loss: 1.6413 | error: 7142.0000 - valid | validloss: 1.6319 | validerror: 1790.0000 | s/iter: 27.3319
train | epoch = 10 | lr = 0.1000 | loss: 1.5848 | error: 6919.0000 - valid | validloss: 1.6063 | validerror: 1714.0000 | s/iter:
27.2203
train | epoch = 11 | lr = 0.1000 | loss: 1.5617 | error: 6779.0000 - valid | validloss: 1.6223 | validerror: 1750.0000 | s/iter:
28.1517
        epoch = 12 | lr = 0.1000 | loss: 1.5166 | error: 6601.0000 - valid | validloss: 1.6787 | validerror: 1830.0000 | s/iter:
28.8950
train | epoch = 13 | lr = 0.1000 | loss: 1.4574 | error: 6343.0000 - valid | validloss: 1.5087 | validerror: 1665.0000 | s/iter: 29.8077
train | epoch = 14 | lr = 0.1000 | loss: 1.3890 | error: 6057.0000 - valid | validloss: 1.5538 | validerror: 1711.0000 | s/iter:
31.171
train | epoch = 15 | lr = 0.1000 | loss: 1.3978 | error: 6056.0000 - valid | validloss: 1.6089 | validerror: 1761.0000 | s/iter:
28.1390
train | epoch = 16 | lr = 0.1000 | loss: 1.3397 | error: 5787.0000 - valid | validloss: 1.6520 | validerror: 1805.0000 | s/iter:
28.050
      | epoch = 17 | lr = 0.1000 | loss: 1.3394 | error: 5803.0000 - valid | validloss: 1.5286 | validerror: 1642.0000 | s/iter:
28.1142
train | epoch = 18 | lr = 0.1000 | loss: 1.3152 | error: 5668.0000 - valid | validloss: 1.5838 | validerror: 1686.0000 | s/iter: 32.8296
train | epoch = 19 | lr = 0.1000 | loss: 1.2492 | error: 5351.0000 - valid | validloss: 1.6582 | validerror: 1769.0000 | s/iter:
32.0069
train | epoch = 20 | lr = 0.1000 | loss: 1.2312 | error: 5296.0000 - valid | validloss: 1.5980 | validerror: 1668.0000 | s/iter:
31.501
test | error: 1731.0000
```

First layer weights:



### Solution 5(b)

Parameters for the CNN:

Layer 1 (convolution) = 
$$[(5x5x3 + 1(bias))x16]=1216$$

Layer 2 
$$(Tanh()) = 0$$

Layer 3 (Pooling) = 
$$0$$

Layer 4 (convolution) = 
$$[(5x5x16 + 1(bias))x128] = 51328$$

Layer 5 
$$(Tanh()) = 0$$

Layer 6 (Pooling) = 
$$0$$

Layer 7 (flatten) = 
$$0$$

Layer 8 (Linear) = 
$$[(5x5x128 + 1(bias))x64] = 204864$$

Layer 
$$9 (Tanh()) = 0$$

Layer 10 (Linear) = 
$$[(64 + 1(bias))x10] = 650$$

 ${\it Total Parameters=} 258{,}058$