

Person

Rating 1 (X)

Rating 2 (Y)

A

4

3

B

2

4

C

3

2

D

5

5

E

1

3

F

3

1

⇒ Step 1:

X	Y	XY	X ²
4	3	12	16
2	4	8	4
3	2	6	9
5	5	25	25
1	3	3	1
3	1	3	9
$\Sigma x = 18$		$\Sigma y = 18$	$\Sigma xy = 57$
			$\Sigma x^2 = 64$

$$\text{Here, } \bar{x} = \frac{18}{6} = 3$$

$$\bar{y} = \frac{18}{6} = 3$$

Step 2: Calculate value of 'a' (n=6)

$$a = \frac{n \Sigma xy - \Sigma x \Sigma y}{n \Sigma x^2 - (\Sigma x)^2} = \frac{6(57) - (18 \times 18)}{6(64) - (18)^2}$$

$$= \frac{342 - 324}{384 - 324} = \frac{18}{60} = 0.3 \quad \boxed{a = 0.3}$$

Step 2: Calculate of value of 'b'.

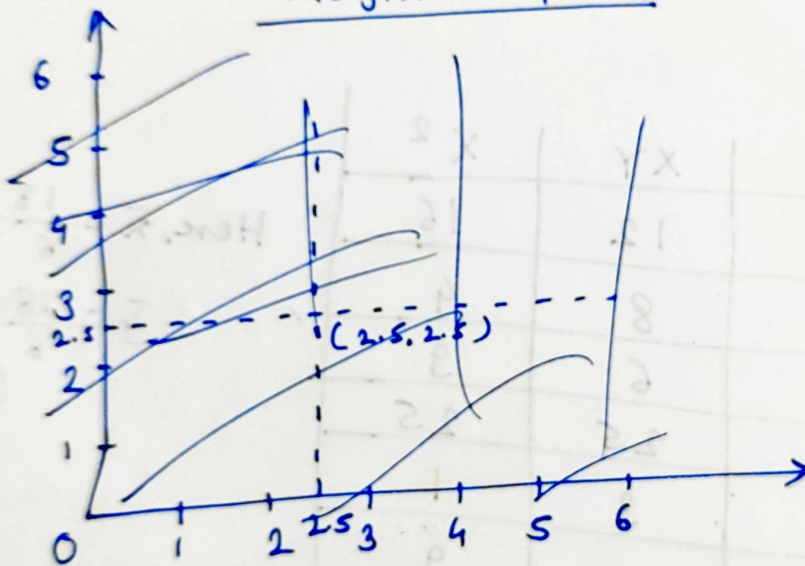
$$b = \frac{1}{n} [\Sigma y - a \Sigma x] = \frac{1}{6} [18 - (0.3)(18)]$$

$$= \frac{1}{6} [18 - 5.4] = \frac{1}{6} [12.6] = 2.1$$

$$\therefore y = ax + b$$

$$\hat{y} = (0.3)x + 2.1$$

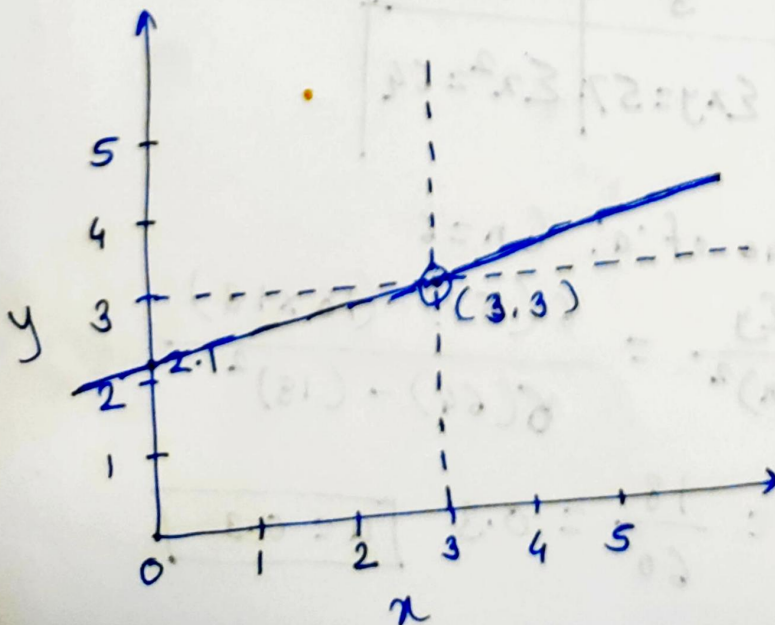
Find regression line that best fit
the given sample data.



Regression line which is best fit, always passes through dense data.

Regression line passes through mean values of 'x' & 'y' intercept.

Her, 'b' is 'y' intercept & 'a' is slope.



Line of best fit, for given sample data.

Interpret & explain equation of regression line.

⇒ For it we need to find standard error of estimate.

$$\text{Standard error of estimate} = \sqrt{\frac{\sum (\hat{y} - y)^2}{n-2}}$$

We have, $\hat{y} = 2.1 + 0.3(x)$

Now, we will calculate different values of \hat{y} , for different values of 'x'.

x	\hat{y}	$(\hat{y} - y)$	$(\hat{y} - y)^2$
4	3.3	0.3	0.9
2	2.7	1.3	1.69
3	3.0	1	1
5	3.6	-1.4	1.96
1	2.4	-0.6	0.36
3	3.0	2	4
			$\sum (\hat{y} - y)^2$ = 9.91

Generally standard error of estimate should be less than '1' to have good regression solution.

$$\text{Standard error of estimate} = \sqrt{\frac{9.91}{6-2}} = \sqrt{\frac{9.91}{4}}$$

$$= \sqrt{2.47} \approx 1.5 < 1 \quad \left(\begin{array}{l} \text{Ideally it} \\ \text{should be less} \\ \text{than '1'} \end{array} \right)$$

Here, $\hat{y} = 2.1 + 0.3(x)$ is not good equation of regression.

line as standard error of estimate.

So, we can have ^(or need) more sample data to get better regression line.