DUBAI INTERNATIONAL ACADEMIC CITY, DUBAI SECOND SEMESTER 2020 – 2021 ACADEMIC-UNDERGRADUATE STUDIES DIVISION DEPARTMENT OF COMPUTER SCIENCE

Questions: 6 Pages: 2

COURSE: Design and Analysis of Algorithms (CS F364)

COMPONENT : Test -1 (Closed Book) **WEIGHTAGE :** 20% (40 Marks)

DATE: 11-Mar-2021, Thursday **DURATION:** 50 Minutes (08:30 am - 09:20 am)

Note: Scan and upload only between (09:20 am to 09:30 am).

Submissions beyond 09:30 am will not be accepted.

Q. 1			-	ing recursion the form give		hod an	d find	the co	mplexity.	6
	T(N)=a T(N T(1)=1	V/b) + f(r	1)							
Q. 2	conquer ap following the	series of reproach. And way in livision of	As you so which the	ort them on t them, wri divide and n erging opera	te a sequence ope	ience i	number takes p	r (1, 2 place.	2 ,3) Write the	8(5+3)
	Nos: 14	12	100 20		2 8	3	6	10	18	
Q.3	modified as manner that m and p-1, a) Write the b) For the ModifiedPa	e modifie : within a : if initiall a[k] >t for e algorithm given ar rtition with	d Partition [m],a[m+ y t = a[m], r m <=k < c n for the M ray show th pivot ele	algorithm r 1],,a[p-1] then after c q and a[k] <= IodifiedParti the stepwis ement as the difiedPartition	the element ompletion et for q < li>tion se single first element	ents are n a[q] = k <p. comp="" ent="" of="" q="" t<="" th=""><th>e rearra t for s is retu</th><th>anged some or rned.</th><th>in such a petween on of the</th><th>7(4+3)</th></p.>	e rearra t for s is retu	anged some or rned.	in such a petween on of the	7(4+3)
Q. 4	[23, 18, 6, 1] Consider a l	1, 90, 5, 1 knapsack j	120, 33, 29 problem. V	0, 2] Ve have give	n a knaps	ack of			nd objects	
ν. τ	correspondi	ng to it. I om set A to knapsa al object s	However, to then an object problem is delection is	he objects a ject from set n using Gree	re selecte B and th	ed in se is orde	equence er is rep	e orde eated.	and profit r. At first . Provide	6
ψ. τ	correspondi an object fr the solution the fraction	ng to it. I om set A to knapsa al object s the knaps	However, to then an object probler selection is sack is 25,	he objects a ject from sen n using Gree allowed.	re selecte B and the dy metho	ed in se is orde	equence er is rep he follo	e orde eated.	and profit r. At first . Provide	6
۳ ۰۷	corresponding an object from the solution the fraction Capacity of Set A: Object	ng to it. I om set A to knapsa al object set the knaps	However, to then an object problem is election is each is 25,	he objects a ject from set in using Gree allowed.	re selecte B and the dy metho	ed in se is orde	equence er is rep he follo	e orde eated.	and profit r. At first . Provide	6
Ψ. τ	corresponding an object from the solution the fraction Capacity of Set A:	ng to it. I om set A to knapsa al object s the knaps	However, to then an object probler selection is sack is 25,	he objects a ject from sen n using Gree allowed.	re selecte B and the dy metho	ed in se is orde	equence er is rep he follo	e orde eated.	and profit r. At first . Provide	6

	Set B:							
	Object	B1	B2	B3	B4	B5		
	Weight	7	15	2	31	14		
	Profit	90	4	55	200	41		
					•		•	
	Represent th		_	•	wing which	all objects a	re selected	
	into it. Com	pute the ma	ximum prof	it achieved.				
Q. 5	There are se	ven jobs and	d, their dead	llines and a	ssociated pr	ofits as show	vn-	7(3+2+2)
		T = 2	T ==	1	T = .	Г	T = - T	
	Jobs	J1	J2	J3	J4	J5	J6	
	Profits	3	5	20	18	0	6	
	Deadlines	1	3	4	3	2	1	
	Answer the	following q	uestions-					
	a) Weit	a tha antime	al aabadula (that airrag m	avinavna na	£:4		
	,	e the optima		_				
	,	all the jobs o			al schedule?			
	c) Wha	t is the max	<u>imum earne</u>	ed profit?				
Q. 6	What is the	problem wit	h Dijkstra A	Algorithm in	n greedy pro	gramming.	Explain the	6(3+3)
	problem and	l how the pr	oblem has b	een handle	d using dyna	amic prograi	nming.	
	Explain ther				2 3	1 0	C	

***** ALL THE BEST ******

DUBAI INTERNATIONAL ACADEMIC CITY, DUBAI SECOND SEMESTER 2020 – 2021 ACADEMIC-UNDERGRADUATE STUDIES DIVISION DEPARTMENT OF COMPUTER SCIENCE

Questions: 5 Pages: 2 SET A

COURSE: Design and Analysis of Algorithms (CS F364)

COMPONENT: Test -2 (Open Book)

WEIGHTAGE: 20% (40 Marks)

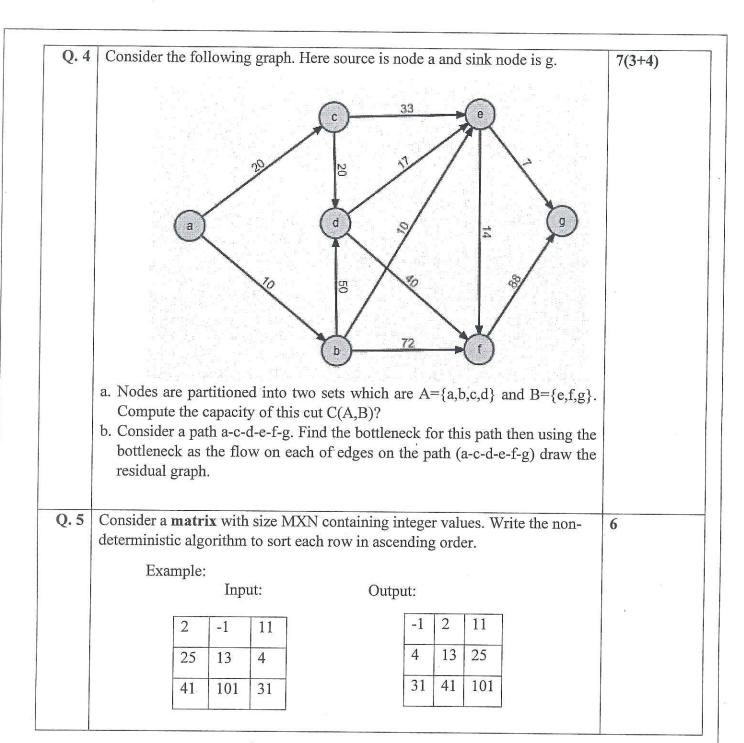
DATE: 20-Apr-2021, T2

DURATION: 50 Minutes (08:30 am - 09:20 am)

Note: Scan and upload only between (09:20 am to 09:25 am).

Submissions beyond 09:25 am will not be accepted.

	WE AND DISCOURTS AND	
Q. 1	A) Write a pseudo code to print all the possible permutations for the given array with duplicates using Backtracking. B) Draw the recursion tree for the problem.	13(5+5+2+1)
	C) What will be the complexity of the approach followed. D) What will be output of the following problem.	
	Input: nums[] = { 2, 1, 2 }	
Q. 2	Think of solution which solves problems of this kind? Recorded advertisement videos have to be packed into fixed lengths breaks. These would be telecasted on the television. The playback time (mins) of 8 advertisements are given to be A(10), B(14), C(1), D(13), E(7), F(2), G(5), H(6). The break duration is a constant time of 15 mins.	6(1+4+1)
	 a. Calculate the minimum number of breaks to pack these advertisements using brute force method? b. Apply First Fit, Best Fit and First Fit Decreasing and find the pattern of allocating the advertisements to different breaks? c. Identify the method which plays advertisement G earlier, and also identify the one which plays together the advertisements D and F. 	
Q. 3	Solve the graph given below using TSP-BB technique and find the optimal path from A to C (Run the TSP-BB for one iteration only). Draw the state space tree. Follow the reduction procedure and write the upper bound values obtained for each node. A B C D A B 2 ∞ 1 B 2 ∞ 2 A D 1 B 2 ∞ 4 D 1 3 4	8



***** ALL THE BEST *****

DUBAI INTERNATIONAL ACADEMIC CITY, DUBAI SECOND SEMESTER 2020 – 2021 ACADEMIC-UNDERGRADUATE STUDIES DIVISION DEPARTMENT OF COMPUTER SCIENCE

Questions: 5 Pages: 2 SET B

COURSE: Design and Analysis of Algorithms (CS F364)

COMPONENT: Test -2 (Open Book)

WEIGHTAGE: 20% (40 Marks)

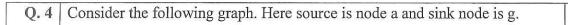
DATE: 20-Apr-2021, T2

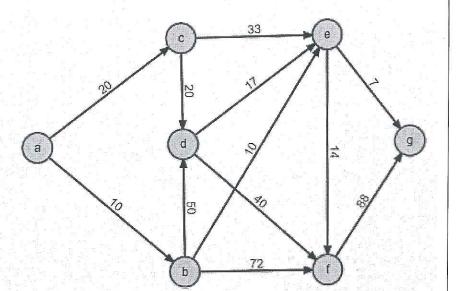
DURATION: 50 Minutes (08:30 am - 09:20 am)

Note: Scan and upload only between (09:20 am to 09:25 am).

Submissions beyond 09:25 am will not be accepted.

Q. 1	A)Write a pseudo code to print all the possible permutations for the given array using Backtracking.	13(5+5+2+1)
	B)Draw the state space tree for the problem.	
	C) What will be the complexity of the approach suggested?	(40)
	D)What will be output of the following problem.	
	Input: nums[] = { 3, 2, 1 }	
Q. 2	Think of solution which solves problems of this kind? Recorded advertisement	6(1+4+1)
V	videos have to be packed into fixed lengths breaks. These would be telecasted on the television. The playback time (mins) of 8 advertisements are given to be A(11), B(13), C(2), D(13), E(6), F(2), G(8), H(3). The break duration is a constant time of 15 mins.	0(1:1:1)
et.	a. Calculate the minimum number of breaks to pack these advertisements using brute force method?b. Apply First Fit, Best Fit and First Fit Decreasing and find the pattern of	1
1	allocating the advertisements to different breaks?	
	c. Identify the method which plays advertisement G earlier, and also identify the one which plays together the advertisements D and F.	
Q. 3	Solve the graph given below using TSP-BB technique and find the optimal path from A to C (Run the TSP-BB for one iteration only). Draw the state space tree. Follow the reduction procedure and write the upper bound values obtained for each node.	8
	A B C D	
	A \infty 3 \infty 2	
	B 3 \infty 3 4	
	C \omega 3 \omega 5	
	D 2 4 5 \infty	
	B — C	
į.		





7(3+4)

- a. Nodes are partitioned into two sets which are A={a,c,e,d} and B={b,f,g}. Compute the capacity of this cut C(A,B)?
- b. Consider a path a-b-d-e-g . Find the bottleneck for this path then using the bottleneck as the flow on each of edges on the path (a-b-d-e-g) draw the residual graph.
- Q. 5 Consider a **matrix** with size MXN containing integer values. Write the non-deterministic algorithm to sort each row in descending order.

Example:

Input:

2	-1	11
25	13	4
41	101	31

Output:

11	2	-1
25	13	4
101	41	31

****** ALL THE BEST ******

DUBAI INTERNATIONAL ACADEMIC CITY, DUBAI SECOND SEMESTER 2020 – 2021 ACADEMIC-UNDERGRADUATE STUDIES DIVISION DEPARTMENT OF COMPUTER SCIENCE

Questions: 3 Pages: 2

COURSE: Design and Analysis of Algorithms (CS F364)

COMPONENT: COMPRE EXAM- SET A - WEIGHTAGE: 13.5% (27 Marks)

SECTION 1(Open Book)

DATE: 02-June-2021 -AN **DURATION**: (50 mins) 12:30 PM - 01:20 PM

Note: Scan and upload only between 01:20 PM - 01:25 PM

Submissions beyond 01:25 PM will not be accepted.

Q. 1	B jobs are executed on A machines and B=2*A+1. Each job is of length as given in the sequence (2*A-1, 2*A-2, 2*A-2, 2*A-3, 2*A-3,, A, A) and the very last job is of length A again.	10 (4+4+ 2)
	a. Apply Longest Processing Time by taking A value as 6 and calculate the finish time \rightarrow (F^(I)) b. Applying brute force find the optimal solution and calculate the finish time \rightarrow (F*(I)) c. Prove that $\frac{4}{3} - \frac{1}{3*A} > = \frac{F*(I)}{F^{(I)}}$	
Q.2	Given four cities A, B, C and D. Apply the Branch and Bound approach to find the shortest path from source node B to destination node B. Follow the principles of Travelling salesman problem. 1. Draw the state space tree for one complete iteration . Derive the upper bound values for each node in the traversing path and mention the same in the state space tree. 2. Write the path obtained after first iteration. What is the cost of the path. 3. How would you proceed, if you come to know that the path you obtained in the first iteration is not the shortest path? CITY D CITY D CITY D CITY D	10 (6+4)

Q.3	Multithreading plays	a major role	in parallel	computing.
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(2.5+2)

- 1. Assume you frame a recursive Algorithm A for a problem P and its Directed Acyclic Graph (DAG) is drawn. The total time taken to execute 'A' in one processor is 20 time units. The longest path in the DAG is 8 time units. Calculate the parallelism. Also, calculate the parallel slackness using 2 processors.
- 2. Assume you frame a different recursive Algorithm B for a same problem P and its Directed Acyclic Graph (DAG) is drawn. The total time taken to execute 'B' in one processor is 24 time units. The longest path in the DAG is 12 time units. Calculate the parallelism. Also, calculate the parallel slackness using 2 processors. Compare and contrast the slackness value vs perfect linear speedup.
- 3. Justify the algorithm A or B, which you prefer and mention why?

Compare and contrast the slackness value vs perfect linear speedup.

DUBAI INTERNATIONAL ACADEMIC CITY, DUBAI SECOND SEMESTER 2020 - 2021 ACADEMIC-UNDERGRADUATE STUDIES DIVISION DEPARTMENT OF COMPUTER SCIENCE

Questions: 3 Pages: 2

COURSE: Design and Analysis of Algorithms (CS F364)

COMPONENT: COMPRE EXAM-SET A-

WEIGHTAGE: 13.5% (27 Marks)

SECTION 2(Open Book)

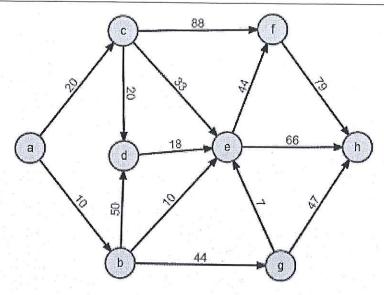
DATE: 02-June-2021 -AN

DURATION: (55 mins) 01:30 PM - 02:25 PM

Note: Scan and upload only between 02:25 PM - 02:30 PM

Submissions beyond 02:30 PM will not be accepted.

Q. 1	Consider the following objective function and constraints	10(2+2
	Minimization $x1 - 10x2 + 13x3$	+2+4)
	Constraints	
	$-2x1 - 12x2 \ge -4$	
	$23x1 - 2x3 \le 15$	
	$6x1 + 12x2 \ge -3$	
	$x1, x2, x3 \geq 0$	
	 i. Convert the above linear optimization problem to standard form ii. Represent the linear optimization problem into slack form iii. Provide the basic solution and value of each variable for basic solution iv. Consider variable x2. Perform exchange (pivot) operation of exchanging the role of non-basic to basic variable for x2. what is the 	
Q.2	objective value after this operation? In the proof of CNF-satisfiability reduces to clique decision problem, provide the details with suitable notation and equations how to make graph from a CNF. Construct the graph representation for the CNF and write at least two cliques from this graph. $F = (X1\sqrt{X3})\Lambda(X2\sqrt{X4})\Lambda(X2\sqrt{X3}\sqrt{X4})$	7(2+3+2)
Q.3	Consider the following network. In this network node 'a' is source and node 'h' is the sink.	10(4+2 +4)



- a. Construct a path such that it not passing through node d and node e with minimum flow 10. Write the residual graph for this path.
- b. Consider two sets A={a,b,g} and B={c,d,e,f,h} what is the capacity of this cut?
- c. Consider node e. The inflow from each incoming edge to e are
 - i. (c,e) flow is 12
 - ii. (d,e) flow is 9
 - iii. (b,e) flow is 10
 - iv. (g,e) flow is 6

The outflow from each edges are:

- v. (e,f) flow is 20
- vi. (e,h) flow is 26

Is conservation condition satisfied at the node e? if not adjust the new values for outgoing flow to satisfy conservation condition.

DUBAI INTERNATIONAL ACADEMIC CITY, DUBAI SECOND SEMESTER 2020 – 2021 ACADEMIC-UNDERGRADUATE STUDIES DIVISION DEPARTMENT OF COMPUTER SCIENCE

Questions: 3 Pages: 2

COURSE: Design and Analysis of Algorithms (CS F364)

COMPONENT : COMPRE EXAM- SET A - WEIGHTAGE : 13% (26 Marks)

SECTION 3(Open Book)

DATE: 02-June-2021 -AN **DURATION**: (50 mins) 02:35 PM -03:25 PM

Note: Scan and upload only between 03:25 PM – 03:30 PM

Submissions beyond 03:30 PM will not be accepted.

Q. 1	Assume the partition in the quick sort is done on the basis of second last element of the given input below. Assume, there are n distinct elements from the set [1n] which needs to be sorted. The input to this example is 10, 3, 5, 9, 14, 4. A) What is the complexity of the problem in big 'O' notation. B) Derive the recurrence relation of the above problem. C) Write the complete working of all the iterations in the quick sort including the pivot element and array obtained with the input given.	8(2+1+5)
Q.2	There is a set of 4 non-negative integers (x1, x2, x3, and x4) and variable Y. The non-negative integers are single-digit prime number. The task is to determine whether there exists a subset of the given set sum equal to a given variable Y. Here the value of the variable Y is 8. A) Identify the value for non-negative integers (x1, x2, x3, and x4). B) Solve the problem using back tracking technique. Show the state space tree for the values identified in part (a). C) Write the algorithm for approach to solve this problem.	9(3+3+3)
Q3.	Consider the graph given below: 5 7 1 8 2 4	9(2+2+5)

- A) Write the initial cost matrix.
- B) What is the complexity of the all pair shortest path algorithm.
 C) and show the results along with the complete steps how the values are computed for all the iterations till A⁴.

Each step carries marks, so please mention all the steps how results has been computed.

DUBAI INTERNATIONAL ACADEMIC CITY, DUBAI SECOND SEMESTER 2020 – 2021 ACADEMIC-UNDERGRADUATE STUDIES DIVISION DEPARTMENT OF COMPUTER SCIENCE

Questions: 3 Pages: 2

COURSE: Design and Analysis of Algorithms (CS F364)

COMPONENT : COMPRE EXAM-SET B - WEIGHTAGE : 13.5% (27 Marks)

SECTION 1(Open Book)

DATE: 02-June-2021 -AN **DURATION**: 50 Minutes (12:30 PM - 01:20 PM)

Note: Scan and upload only between 01:20 PM - 01:25 PM

Submissions beyond 01:25 PM will not be accepted.

Q. 1	Assume there are X machines.	10
. 32	Y jobs are executed on X machines and Y=2*X+1.	(4+4+2
	Each job is of length as given in the sequence (2*X-1, 2*X-1, 2*X-2, 2*X-2, 2*X-3,)
	2*X-3,, X, X) and the very last job is of length X again.	
	a. Apply Longest Processing Time by taking X value as 7 and calculate the finish	
	$time \rightarrow (F^{\wedge}(I))$	
	b. Applying brute force find the optimal solution and calculate the finish time \rightarrow (F*(I))	
	c. Prove that $\frac{4}{3} - \frac{1}{3*A} > = \frac{F*(I)}{F^{(I)}}$.
Q. 2	Given nodes W, X, Y and Z. Apply the Branch and Bound approach to find the	10
	shortest path from source node X to destination node X. Follow the principles of	(6+4)
	Travelling salesman problem.	(0 1)
	1. Draw the state space tree for one complete iteration . Derive the upper bound	
- 1	values for each node in the traversing path and mention the same in the state space	
	tree.	
	2. Write the path obtained (NODE W) (NODE Y)	
	after first iteration. What	
	is the cost of the path.	
	$\frac{8}{3}$ $\frac{2}{5}$ $\frac{4}{1}$	
	3. How would you	
	proceed, if you come to	
	know that the path you $\setminus (NODE X)_1 \setminus (NODE Z)$	
	obtained in the first	
	iteration is not the shortest	
	path?	

Q. 3	Multithreading plays a major role in parallel computing.
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(2.5+2. 5+2)

- 1. Assume you frame a recursive Algorithm A for a problem P and its Directed Acyclic Graph (DAG) is drawn. The total time taken to execute 'A' in one processor is 40 time units. The longest path in the DAG is 20 time units. Calculate the parallelism. Also the parallel slackness using 2 processors. Compare and contrast the slackness value vs perfect linear speedup.
- 2. Assume you frame a different recursive Algorithm B for a same problem P and its Directed Acyclic Graph (DAG) is drawn. The total time taken to execute 'B' in one processor is 48 time units. The longest path in the DAG is 22 time units Calculate the parallelism. Also the parallel slackness using 2 processors. Compare and contrast the slackness value vs perfect linear speedup.
- 3. Justify the algorithm which you prefer and mention why?

DUBAI INTERNATIONAL ACADEMIC CITY, DUBAI SECOND SEMESTER 2020 – 2021 ACADEMIC-UNDERGRADUATE STUDIES DIVISION DEPARTMENT OF COMPUTER SCIENCE

Questions: 3 Pages: 2

COURSE: Design and Analysis of Algorithms (CS F364)

COMPONENT: COMPRE EXAM- SET B -

WEIGHTAGE: 13.5% (27 Marks)

SECTION 2(Open Book)

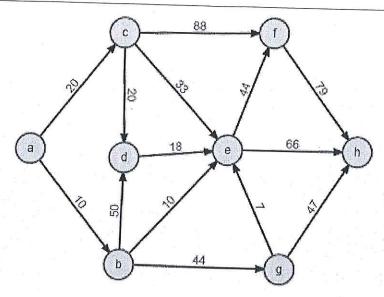
DATE: 02-June-2021 -AN

DURATION: (55 mins) 01:30 PM – 02:25 PM

Note: Scan and upload only between 02:25 PM - 02:30 PM

Submissions beyond 02:30 PM will not be accepted.

Q. 1	1 O	10(2+2 +2+4)
	$2x1 - 22x3 \le 5$ $15x1 - 7x2 \ge -21$ $x1, x2, x3 \ge 0$	
	 i. Convert the above linear optimization problem to standard form ii. Represent the linear optimization problem into slack form iii. Provide the basic solution and value of each variable for basic solution iv. Consider variable x2. Perform exchange (pivot) operation of exchanging the role of non-basic to basic variable for x2. what is the objective value after this operation? 	. 0
Q.2	In the proof that CNF-satisfiability reduces to clique decision problem, provide the details with suitable notation and equations how to make graph from a CNF. Construct the graph representation for the CNF and write at least two cliques from this graph.	-/
Q. 3	$F = (X1\sqrt{X2})\Lambda(\overline{X1}\sqrt{X3})\Lambda(X1\sqrt{X2}\sqrt{X3})$ Consider the following network. In this network node 'a' is source and node 'h' is the sink.	10(4++4)



- a. Consider the path (a—c—d—e—h) with flow 18. Write the residual graph for this path.
- b. Consider two sets $A=\{a,c,d,e\}$ and $b=\{b,f,g,h\}$ what is the capacity of this cut?
- c. Consider node e. The inflow from each incoming edge to e are
 - i. (c,e) flow is 10
 - ii. (d,e) flow is 7
 - iii. (b,e) flow is 6
 - iv. (g,e) flow is 4

The outflow from each edges are:

- v. (e,f) flow is 17
- vi. (e,h) flow is 13

Is conservation condition satisfied at the node e? if not adjust the new values for outgoing flow to satisfy conservation condition.

DUBAI INTERNATIONAL ACADEMIC CITY, DUBAI SECOND SEMESTER 2020 – 2021 ACADEMIC-UNDERGRADUATE STUDIES DIVISION DEPARTMENT OF COMPUTER SCIENCE

Questions: 3 Pages: 2

COURSE: Design and Analysis of Algorithms (CS F364)

COMPONENT : COMPRE EXAM- SET B – WEIGHTAGE : 13% (26 Marks)

SECTION 3 (Open Book)

DATE: 02-June-2021 -AN **DURATION**: (50 mins)02:35 PM -03:25 PM

Note: Scan and upload only between 03:25 PM - 03:30 PM

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Q. 1	Assume the partition in the quick sort is done on the basis of second last element of the given input below. Assume, there are n distinct elements from the set [1n] which needs to be sorted. The input to this example is 11, 4, 6, 10, 15, 5. A) What is the complexity of the problem in big 'O' notation. B) Derive the recurrence relation of the above problem. C) Write the complete working of all the iterations in the quick sort including the pivot element and array obtained with the input given.	8(2+1+5)
Q.2	 There is a set of 4 non-negative integers (x1, x2, x3, x4) and variable Y. The non-negative integers are first four double-digit prime number less than 20. The task is to determine whether there exists a subset of the given set sum equal to given variable Y. Here the value of the variable Y is 30. A) Identify the value for non-negative integers (x1, x2, x3, and x4). B) Solve the problem using back tracking technique. Show the state space tree for the values identified in part (a). C) Write the algorithm for approach to solve this problem. 	9(3+3+3)
Q3.	Consider the graph given below: 1 7 5 8 2 4	9(2+2+5)

- A) Write the initial cost matrix.
- B) What is the complexity of the all pair shortest path algorithm.
- C) and show the results along with the complete steps how the values are computed for all the iterations till A⁴.

Each step carries marks, so please mention all the steps how results has been computed.