

BITS PILANI, DUBAI CAMPUS
DUBAI INTERNATIONAL ACADEMIC CITY, DUBAI

SECOND SEMESTER 2023 – 2024

COURSE: BITS F464 (Machine Learning)

COMPONENT: Practice Tutorial 3

DATE: 23rd October 2023

Q1: Consider a below dataset of 14 training examples of the target concept “Buys_computer”, where each instance is described as attributes Age, Income, Student, Credit_rating.

Age	Income	Student	Credit_rating	Buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31 to 40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31 to 40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31 to 40	medium	no	excellent	yes
31 to 40	high	yes	fair	yes
>40	medium	no	excellent	no

Apply Navie Bayes Classifier on given training data to classify the novel instance $X = (\text{age} \leq 30, \text{Income} = \text{medium}, \text{Student} = \text{yes}, \text{Credit_rating} = \text{fair})$ in a correct class. Show the steps by step procedure of calculating all posterior and prior probabilities to classify the instance in a correct class (Training and Testing Phase).

Answer:

Training Phase:

$P(C_i): P(\text{buys_computer} = \text{"yes"}) = 9/14 = 0.643$

$P(\text{buys_computer} = \text{"no"}) = 5/14 = 0.357$

Compute $P(X|C_i)$ for each class

$P(\text{age} = \text{"<=30"} | \text{buys_computer} = \text{"yes"}) = 2/9 = 0.222$

$P(\text{age} = \text{"<= 30"} | \text{buys_computer} = \text{"no"}) = 3/5 = 0.6$

$P(\text{income} = \text{"medium"} | \text{buys_computer} = \text{"yes"}) = 4/9 = 0.444$

$P(\text{income} = \text{"medium"} | \text{buys_computer} = \text{"no"}) = 2/5 = 0.4$

$P(\text{student} = \text{"yes"} | \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667$

$P(\text{student} = \text{"yes"} | \text{buys_computer} = \text{"no"}) = 1/5 = 0.2$

$P(\text{credit_rating} = \text{"fair"} | \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667$

$P(\text{credit_rating} = \text{"fair"} | \text{buys_computer} = \text{"no"}) = 2/5 = 0.4$

Testing Phase:

X = (age <= 30 , income = medium, student = yes, credit_rating = fair)

$P(X|C_i) : P(X|\text{buys_computer} = \text{"yes"}) = 0.222 \times 0.444 \times 0.667 \times 0.667 = 0.044$

$P(X|\text{buys_computer} = \text{"no"}) = 0.6 \times 0.4 \times 0.2 \times 0.4 = 0.019$

$P(X|C_i) \cdot P(C_i) : P(X|\text{buys_computer} = \text{"yes"}) \cdot P(\text{buys_computer} = \text{"yes"}) = 0.028$

$P(X|\text{buys_computer} = \text{"no"}) \cdot P(\text{buys_computer} = \text{"no"}) = 0.007$

Therefore, X belongs to class ("buys_computer = yes")

Q2: Consider the following set of training examples,

Instance	Classification	A1	A2
1	+	T	T
2	+	T	T
3	-	T	F
4	+	F	F
5	-	F	T
6	-	F	T

What is the information gain of A2 relative to these training examples?

Answer:

$\text{Gain}(S, A2) = 0$

Q3: Given a following observed datapoints ($X: x_i$) with two classes A and B,

Class A	Class B
10	14
11	11
8	9
10	13

The prior probabilities of class A and B are 0.4 and 0.6 respectively. What will be the class of following unlabelled data points (x_1 and x_2) using Gaussian for classification? (Show all steps of calculations)

i. $X_1 = 5$

ii. $X_2 = 12$

Answer:

i. X_1 belongs to class B

ii. X_2 belongs to class B

Q4: Consider a following dataset which shows willingness of certain customer to eat a chocolate of certain manufactures with specific flavor,

Manufacturer	Flavor	Willingness to eat
Lindt	Strawberry	Yes
Lindt	Milk	Yes
Cadbury	Strawberry	Yes
Cadbury	Milk	No
Milka	Strawberry	No
Milka	Milk	No

- In above dataset, which feature (Manufacturer or flavor) has the larger information gain with willingness to eat?
- Also draw the decision tree for predicting willingness to eat which maximizes the information gain?

Answer:

i. Manufacture have larger information gain than flavor.

ii. Decision tree

