

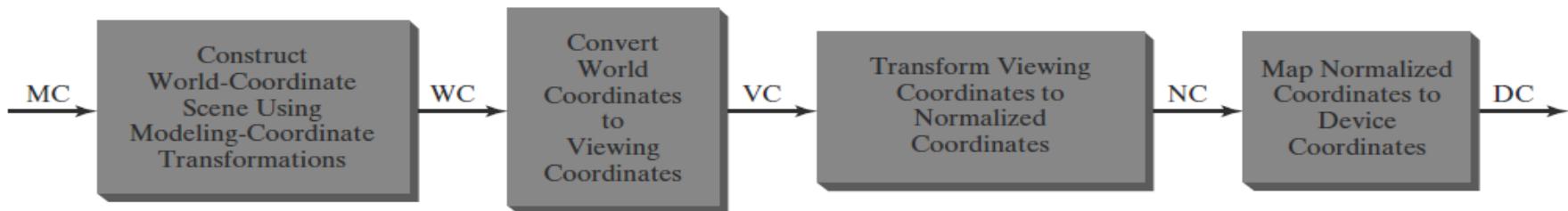
# **Computer Graphics**

**Unit 3 – Part 2**

**–By Manjula. S**

# Clipping Window

- ▶ The mapping of a two-dimensional, world-coordinate scene description to device coordinates is called a **two-dimensional viewing transformation**.
- ▶ This transformation is simply referred to as the *window-to-viewport transformation* or the *windowing transformation*.
- ▶ In analogy with three-dimensional viewing, we can describe the steps for two-dimensional viewing as indicated in Figure 2.



**FIGURE 2**  
Two-dimensional viewing-transformation pipeline.

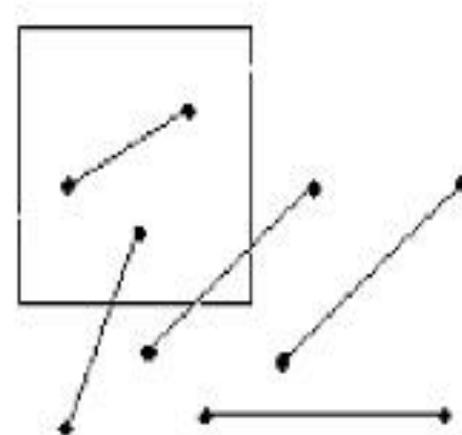
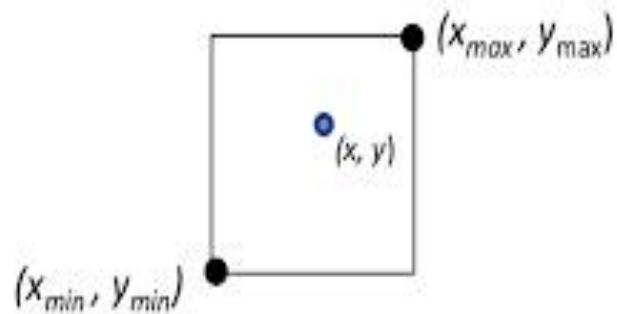
# Clipping Types

## Clipping Types:

- ▶ Point Clipping
- ▶ Line Clipping
- ▶ Polygon Clipping(Fill area Clipping)
- ▶ Curve Clipping
- ▶ Text Clipping

# Line Clipping

- Clipping a point  $(x, y)$ 
  - if  $(x_{min} < x < x_{max}) \&\& (y_{min} < y < y_{max})$
  - Then:  $(x, y)$  is inside
- For lines:
  - If both endpoints are in, do “trivial acceptance”
  - If one endpoint in, one endpoint out, must clip
  - If both endpoints out:
    - Could be out
    - Could be clipped
- Brute force clip: solve simultaneous equations using  $y = mx + b$  for the line, and the four edges (of the region)
  - Slope-intercept formula handles infinite line only
  - Doesn't handle vertical lines

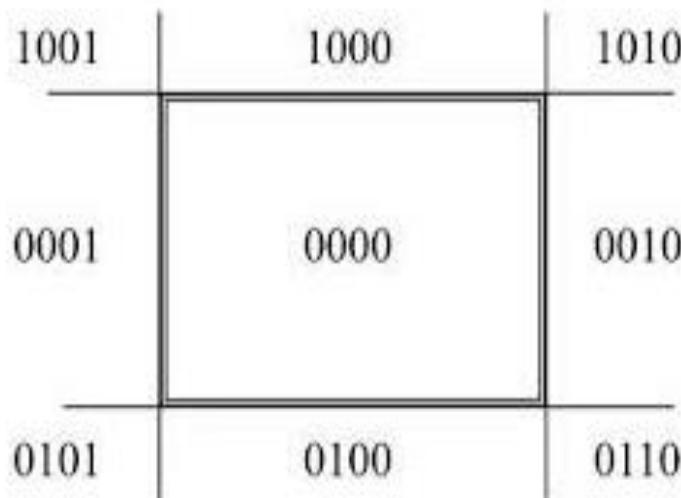


# Cohen-Sutherland line clipping: steps

- Calculate differences between endpoint coordinates and clipping boundaries
- Use the resultant sign bit of each difference to set the corresponding value in the region code
  - Bit 1 is the sign bit of  $x - xw_{min}$
  - Bit 2 is the sign bit of  $xw_{max} - x$
  - Bit 3 is the sign bit of  $y - yw_{min}$
  - Bit 4 is the sign bit of  $yw_{max} - y$
- Any lines that are completely inside have a region code 0000 for both endpoints (save the line segment)
- Any line that has a region code value of 1 in the same bit position for each endpoint is completely outside (eliminate the line segment)

# Cohen-Sutherland Clipping (cont.)

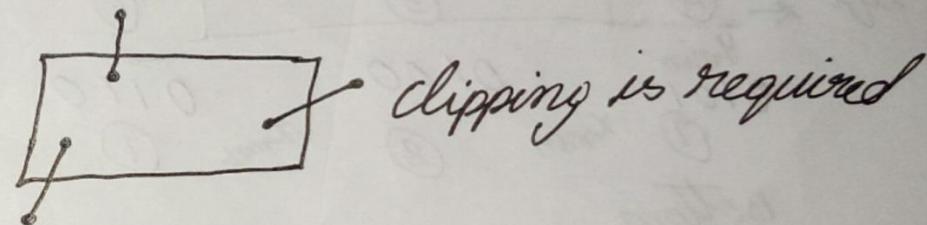
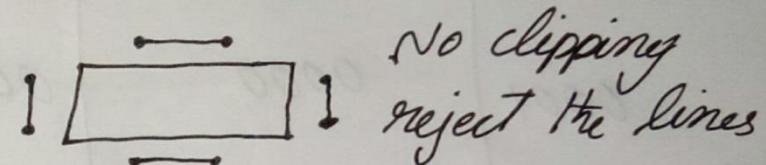
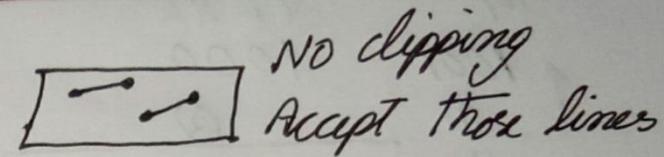
Bit 1: Above  
Bit 2: Below  
Bit 3: Right  
Bit 4: Left



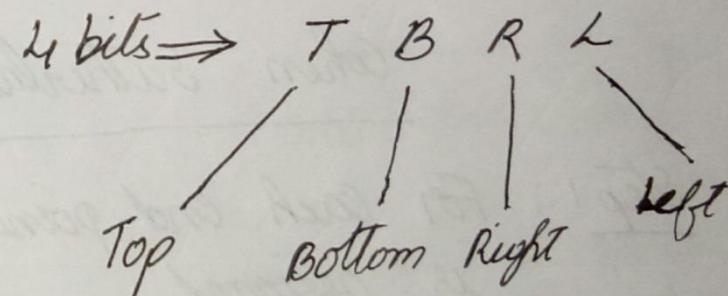
- A line can be trivially **accepted** if both endpoints have an outcode of 0000.
- A line can be trivially **rejected** if any corresponding bits in the two outcodes are both equal to 1. (This means that both endpoints are to the right, to the left, above, or below the window.)
- if  $(\text{outcode 1} \& \text{outcode 2}) \neq 0000$ , trivially reject!

# Cohen Gutherland Line Clipping

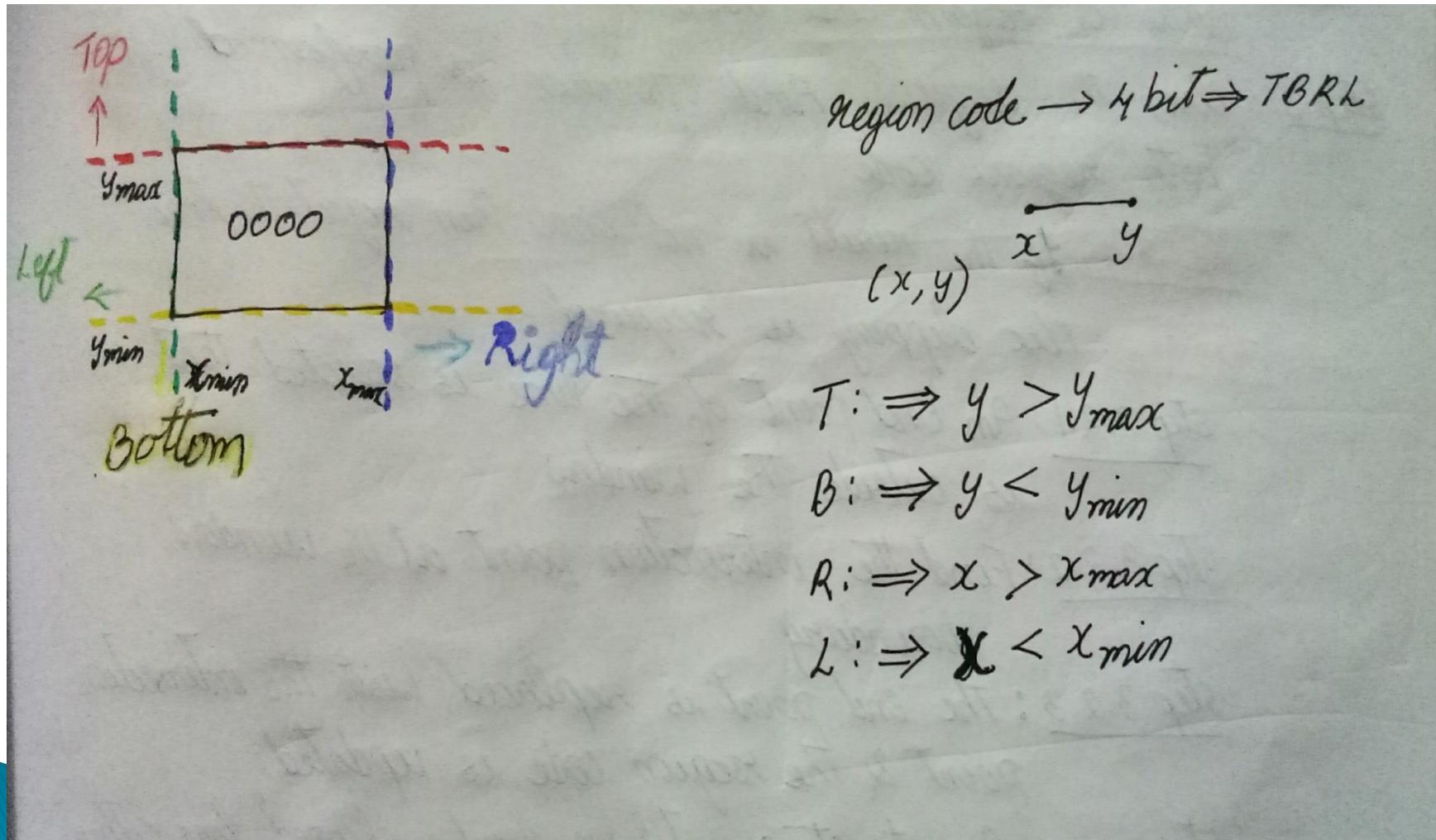
Line



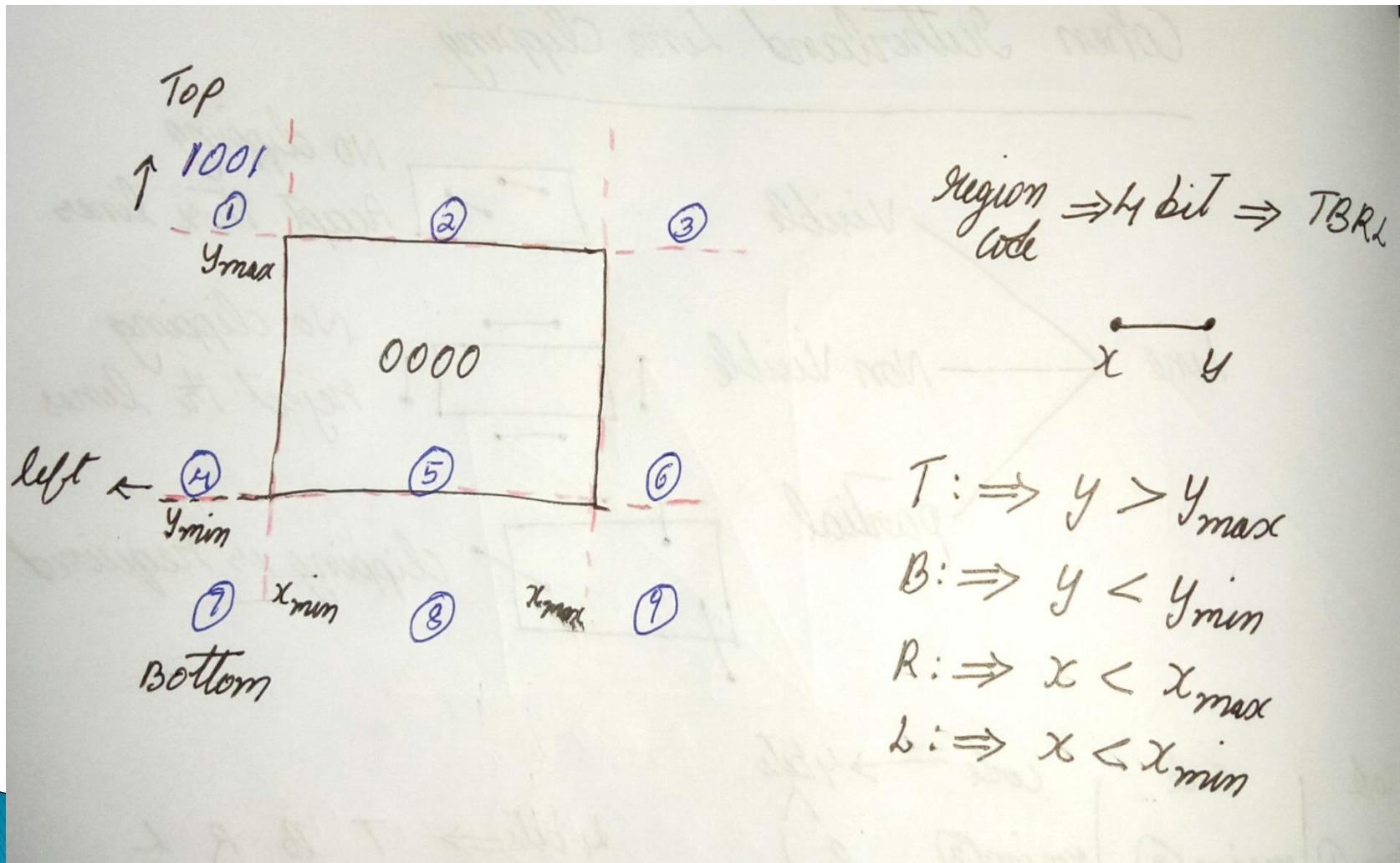
code	code	code	$\rightarrow$ 4 bits
region ①	region ②	region ③	0 1
code	code	code	
region ④	region ⑤	region ⑥	
code	code	code	
region ⑦	region ⑧	region ⑨	



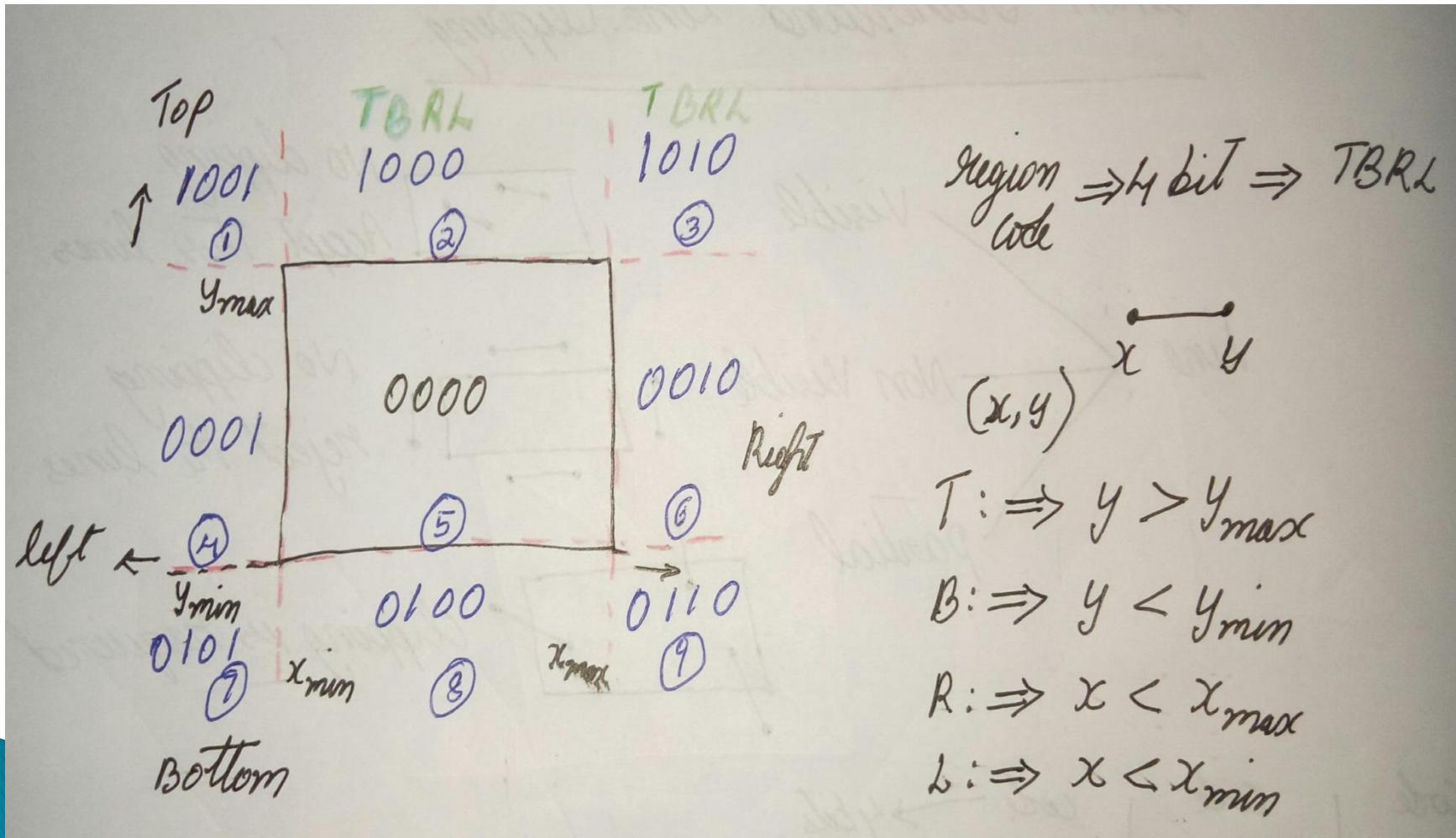
# Cohen Sutherland Line Clipping



# Cohen Sutherland Line Clipping



# Cohen Sutherland Line Clipping



## Cohen Sutherland Line Clipping Algorithm

Step 1: For each end points, a region code is assigned.

Step 2: The line is accepted if both end points have a region code 0000

Step 3: Else, the logical And operation is performed for both regions code.

Step 3.1: If the result is not 0000 then reject the line

Step 3.2: Else clipping is required.

Step 3.2.1: An End point of the line is selected that is outside the window

Step 3.2.2: Find the intersection point at the window boundary.

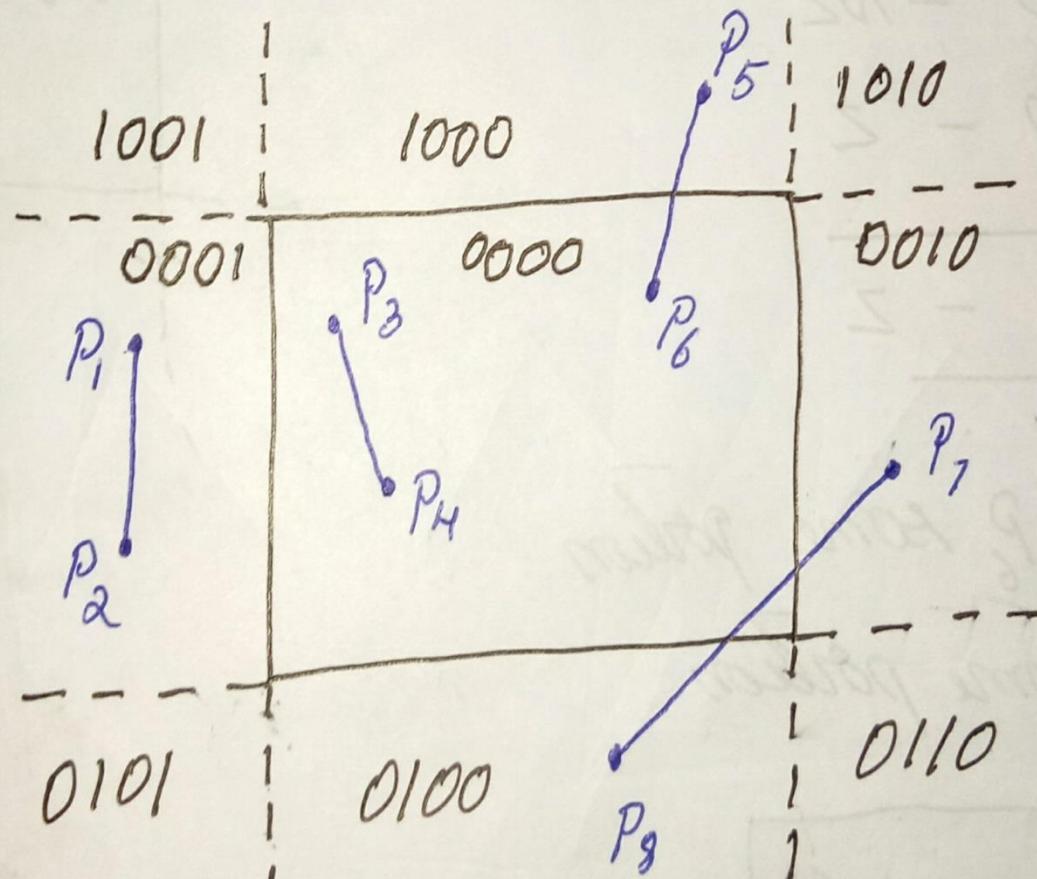
Step 3.2.3: The end point is replaced with the intersection point & the region code is updated.

Step 3.2.4: Repeat step 2 until we find a clipped line either trivially accepted or trivially rejected.

Step 4: Repeat step 1 for other lines.

# Cohen Sutherland Line Clipping

Example:



# Cohen Sutherland Line Clipping

Case ①:  $P_1$  &  $P_2$

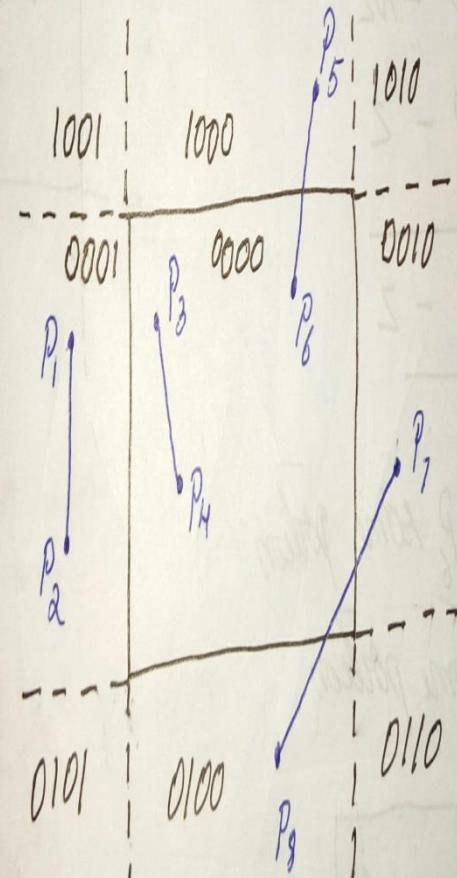
$$\begin{array}{l} P_1 - 0001 \quad \text{- Non zero (NZ)} \\ P_2 - 0001 \quad \text{- Non zero (NZ)} \\ \hline \text{AND operation} \quad 0001 \quad \text{- Non zero (NZ)} \end{array}$$

AND operation	
00	-0
01	-0
10	-0
11	-1

If all Non zeros are there, it indicates  
 $P_1$  &  $P_2$  are completely outside the window.

Reject line

Example:

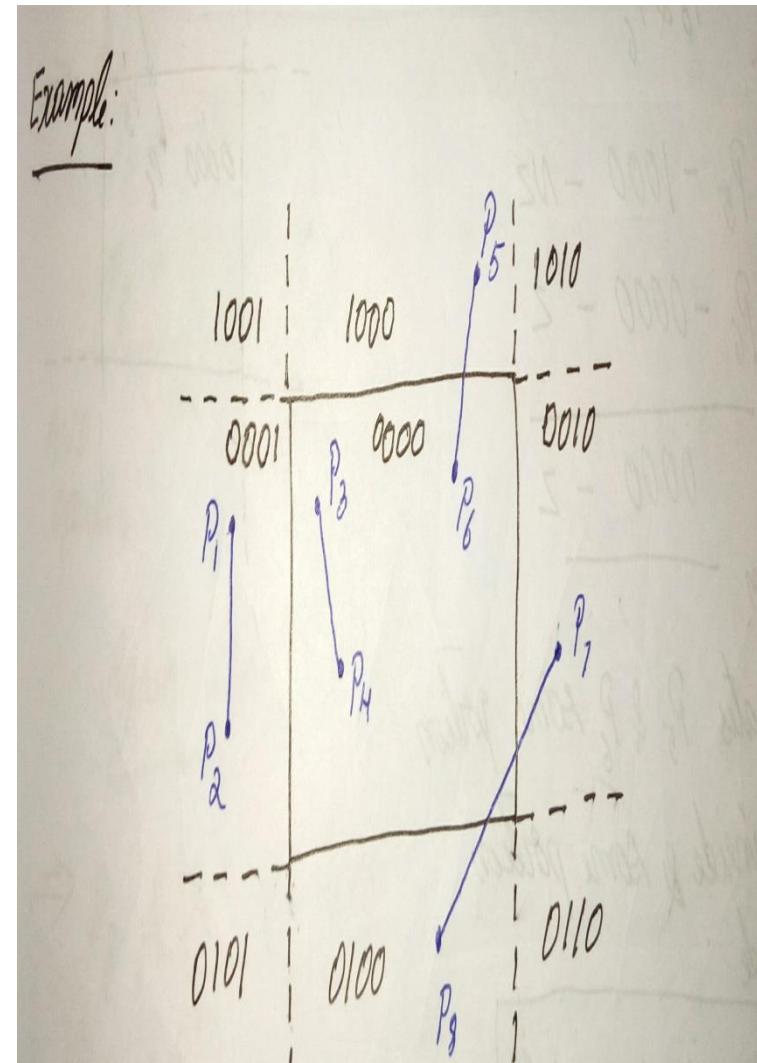


# Cohen Sutherland Line Clipping

case (ii):  $P_3 \& P_4$

$$\begin{array}{l} P_3 - 0000 \quad -\text{zero}(z) \\ P_4 - 0000 \quad -\text{zero}(z) \\ \hline \text{AND operation} \quad - 0000 \quad -\text{zero}(z) \end{array}$$

Accept the line



# Cohen Sutherland Line Clipping

case (iii) :  $P_5$  &  $P_6$

$$P_5 - 1000 - NZ$$

$$P_6 - 0000 - Z$$

$$\begin{array}{r} \text{AND} \\ \text{operation} \end{array} \quad \underline{0000 - Z}$$

It indicates  $P_5$  &  $P_6$  some portion lies inside & some portion outside.

clipping is required

$\Rightarrow P_5' \& P_6'$

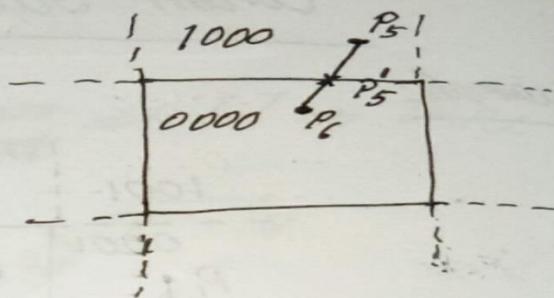
$$P_5' - 0000 - Z$$

$$P_6 - \underline{0000 - Z}$$

$$\begin{array}{r} \text{AND} \\ \text{operation} \end{array} \quad \underline{\underline{0000}}$$

Accept  $P_5' \& P_6'$

clip  $P_5 \& P_5'$



# Cohen Sutherland Line Clipping

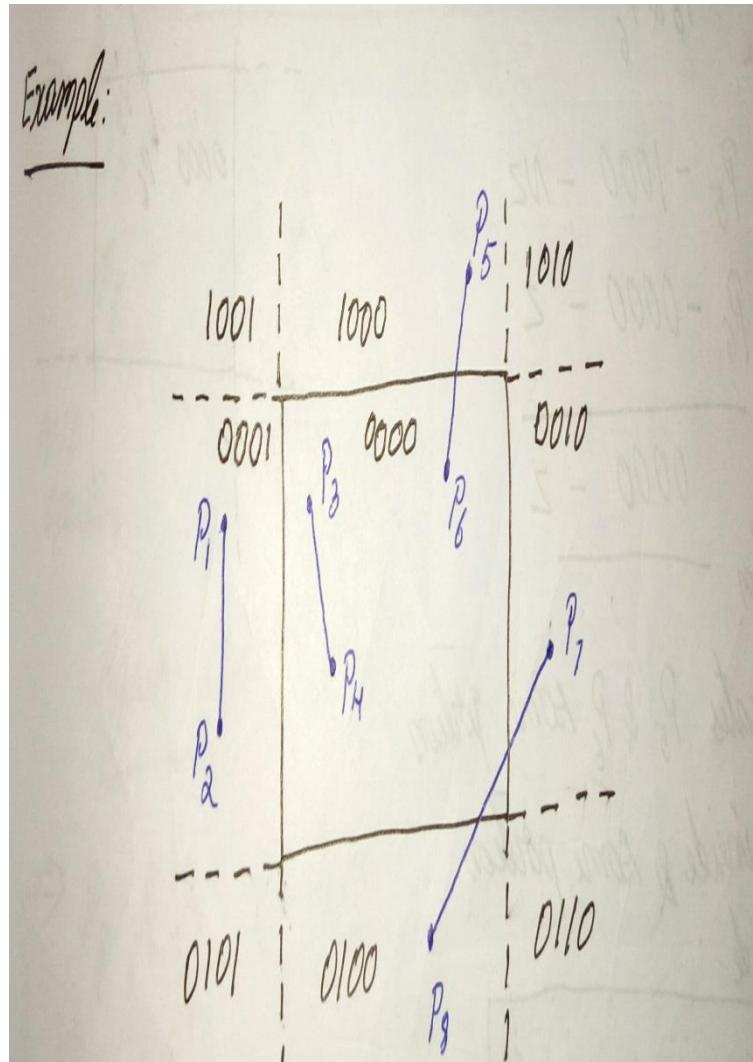
$\Rightarrow P_7 \& P_8$

$P_7 - 0100 - NZ$

$P_8 - 0010 - NZ$

AND - 0000 - Z  
operation

It indicates  $P_7 \& P_8$  need to clip.



# Cohen Sutherland Line Clipping

$\Rightarrow P_7 \& P_7' - \text{clipped}$

$\Rightarrow P_7' \& P_8' - 0000 Z$

$$\begin{array}{r} P_8 - 0010 NZ \\ \hline 0000 Z \end{array}$$

AND operation

Again clip

$\Rightarrow P_8 \& P_8' - \text{clipped}$

$\Rightarrow P_8' \& P_7'$

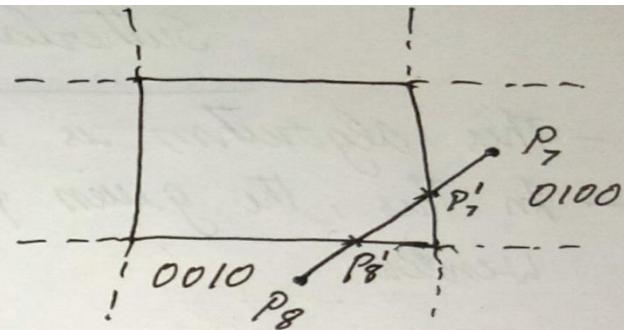
$$P_8' - 0000 Z$$

$$P_7' - 0000 Z$$

$$\hline 0000 Z$$

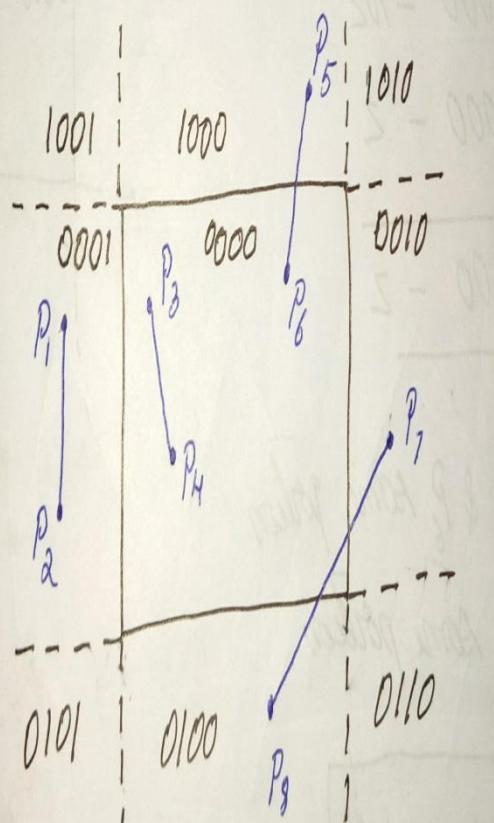
AND operation

Accept the line  $P_8'P_7'$

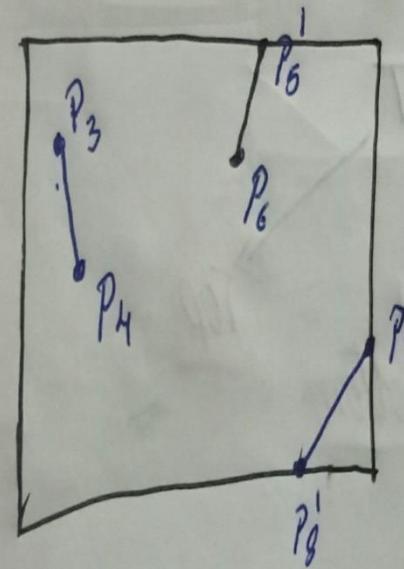


# Cohen Sutherland Line Clipping

Example:



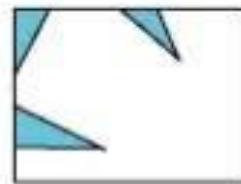
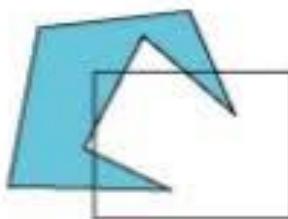
Output :





# Polygon Clipping

- Not as simple as line segment clipping
  - Clipping a line segment yields at most one line segment
  - Clipping a polygon can yield multiple polygons



- However, clipping a convex polygon can yield at most one other polygon



# Sutherland-Hodgman Clipping

## Rules to generate the Vertex list

- Apply the following rules for every pair of vertices
  - If the first vertex is outside and the second is inside, then move the first vertex to the clipping boundary and accept both vertices.
    - Calculate intersection point with the boundary
    - Replace the first vertex with the intersection point
    - Put the new first vertex and the second vertex in the output list
  - If both vertices are inside, put the second vertex in the output list.
  - If the first vertex is inside and the second is outside, then move the second to the clipping boundary and accept the second.
    - Calculate intersection point with the boundary
    - Replace the second vertex with the intersection point
    - Put the new second vertex in the output list
  - If both vertices are outside, reject both.

# Sutherland-Hodgman Clipping Algorithm

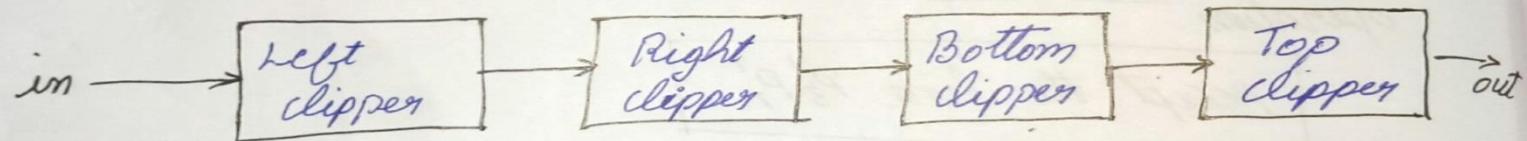
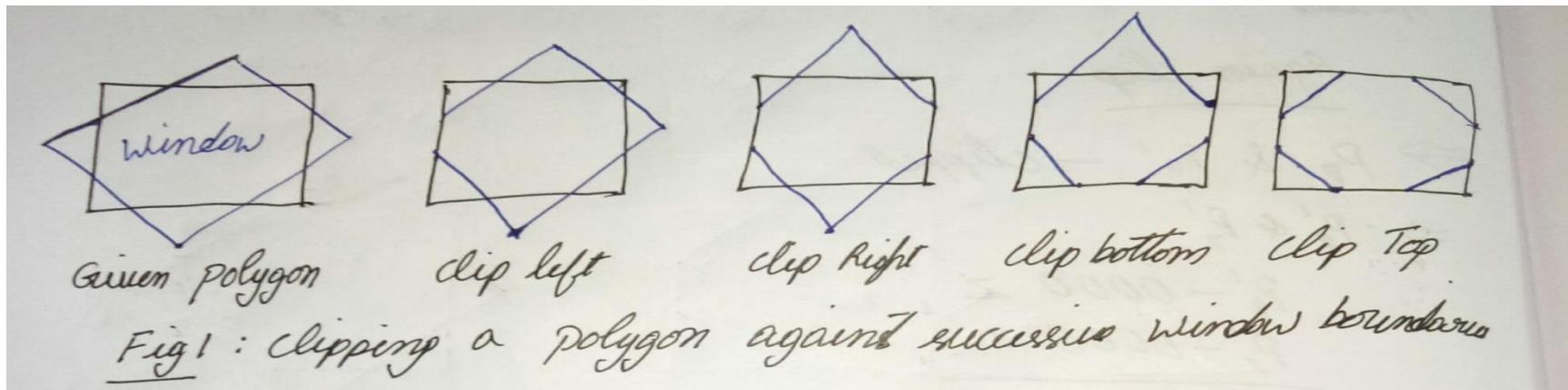
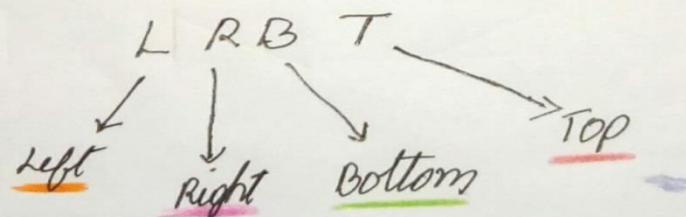


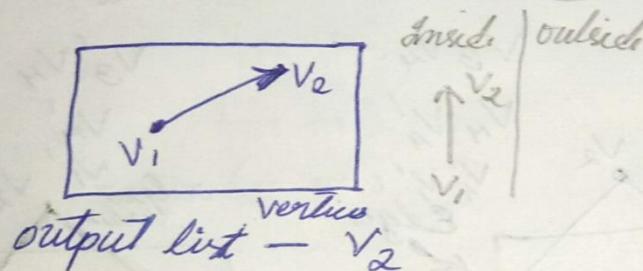
Fig 2 : processing the vertices of the polygon through boundary clippers



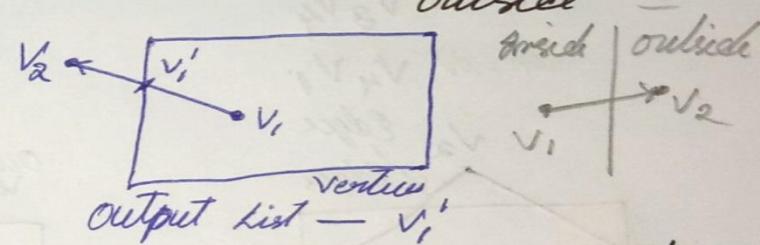
# Sutherland-Hodgman Clipping Algorithm

4 cases when processing vertices in sequence around the perimeter of polygon

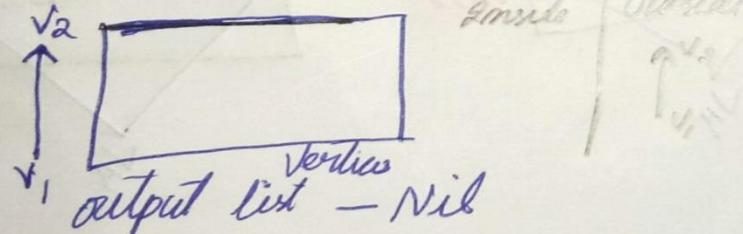
case I - Both input vertices are inside the WB



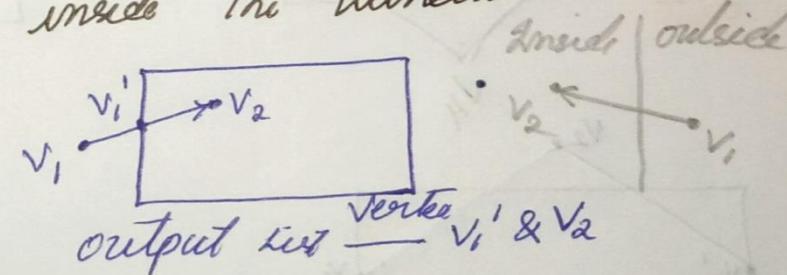
case II - First vertex is inside the WB & 2<sup>nd</sup> is outside



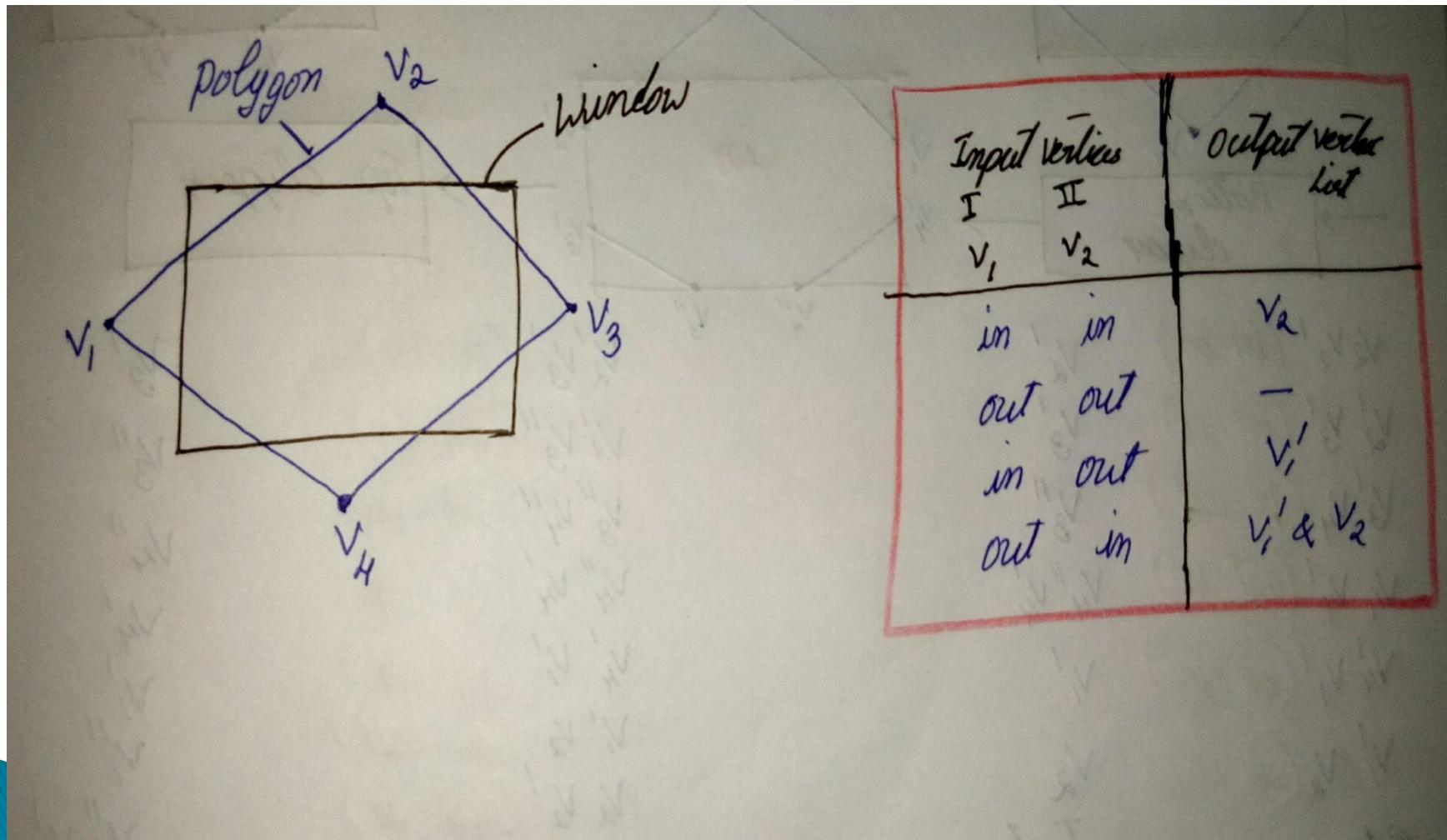
case III - If both input vertices are outside the WB



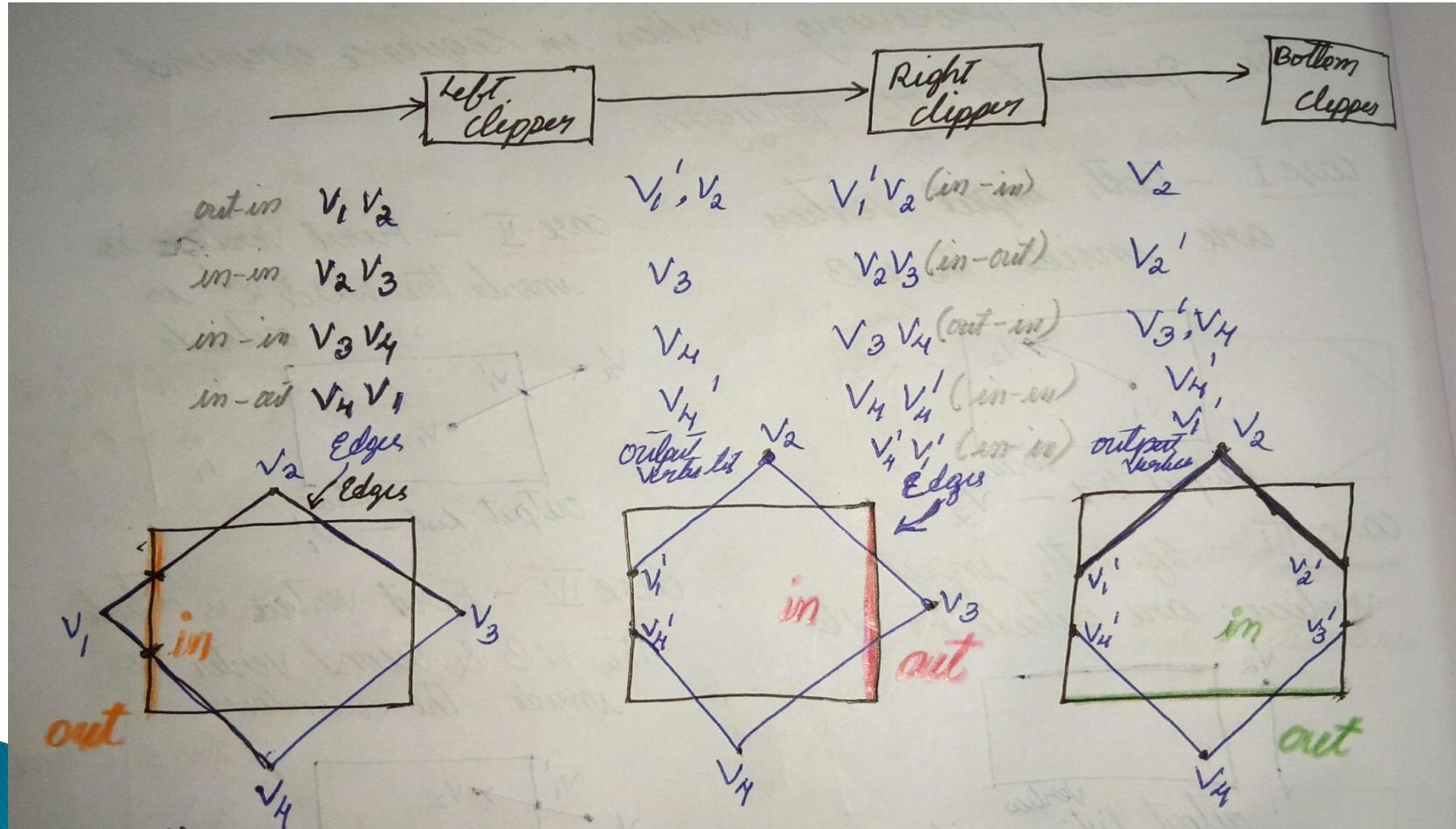
case IV - First vertex is outside the WB & second vertex is inside the window.



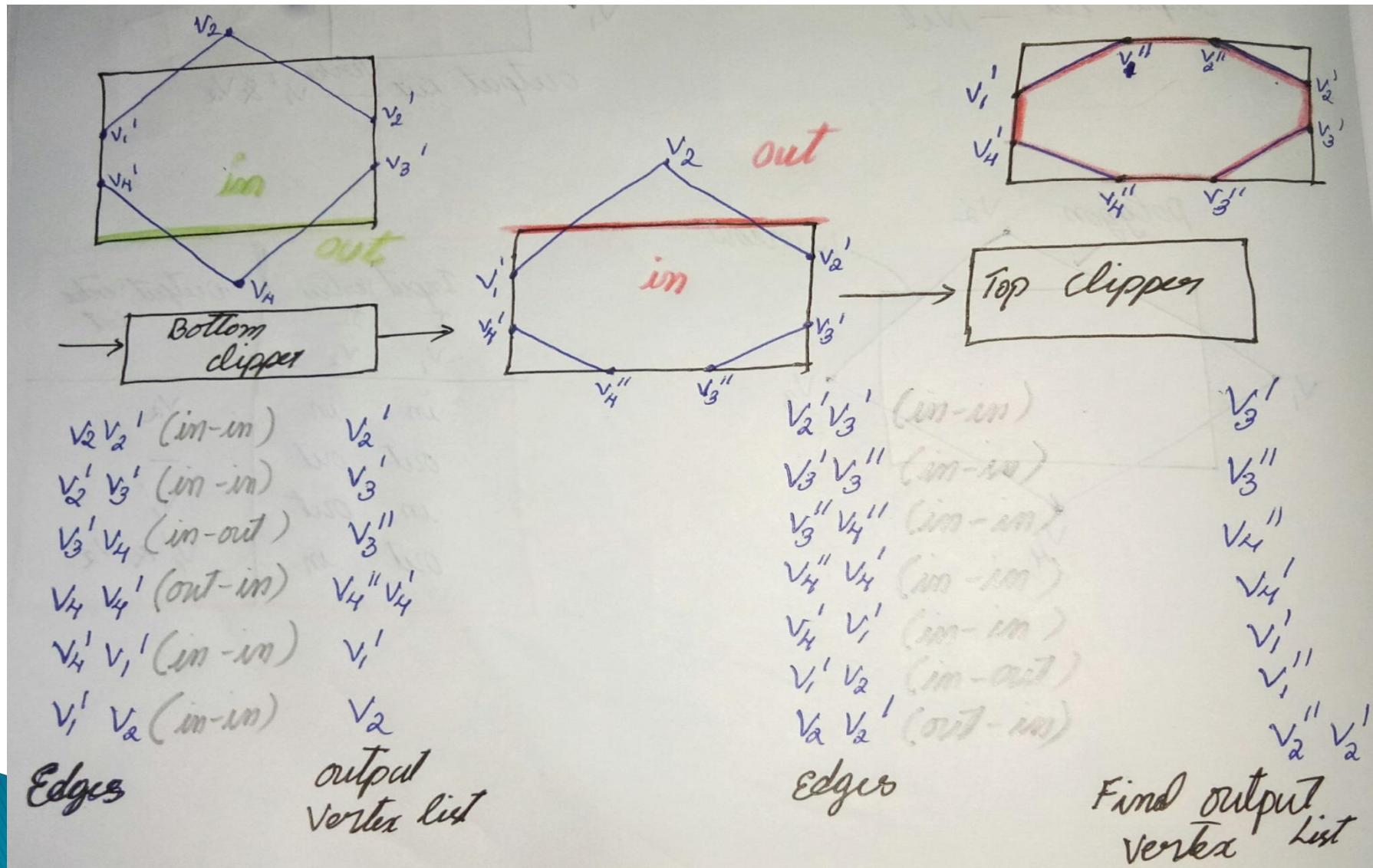
# Sutherland-Hodgman Clipping Algorithm



# Sutherland-Hodgman Clipping Algorithm

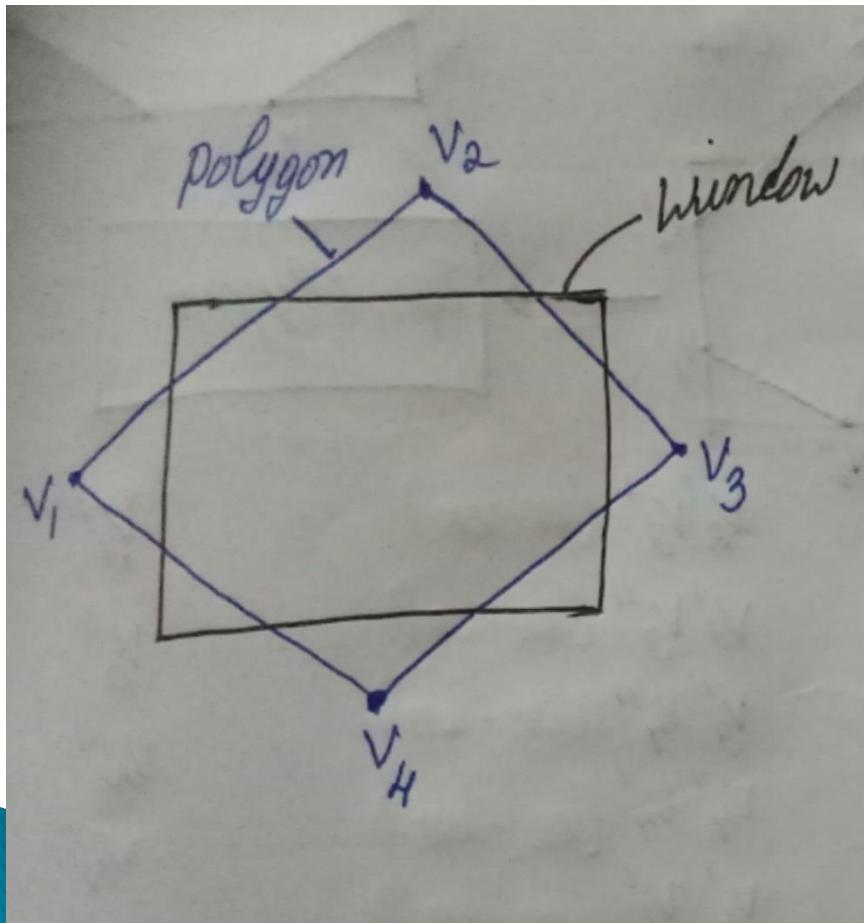


# Sutherland-Hodgman Clipping Algorithm

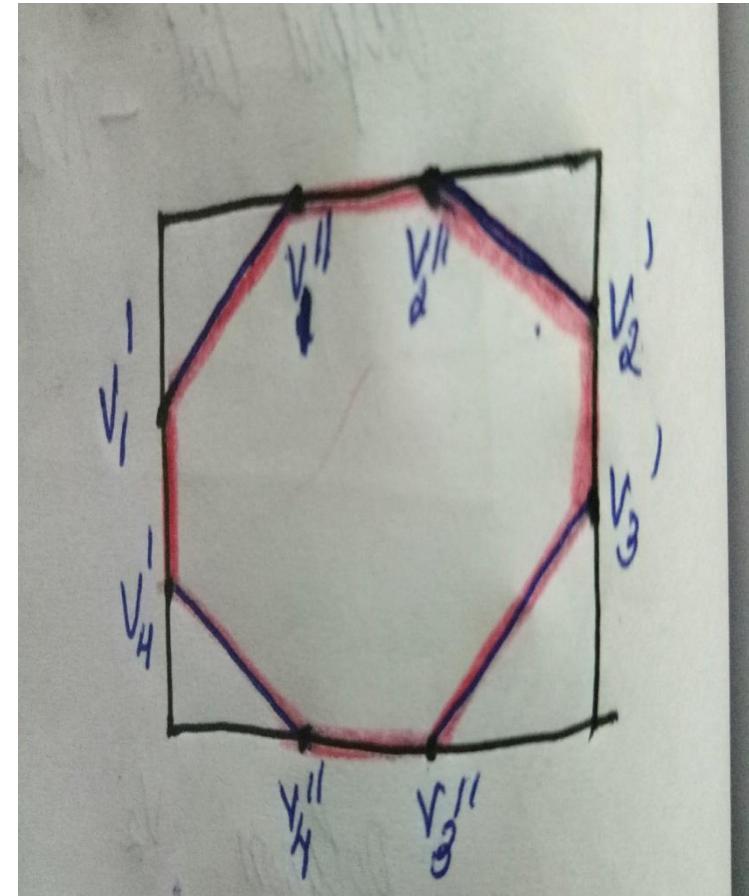


# Sutherland-Hodgman Clipping Algorithm

Input :



Output:



# Thank You

-By Manjula. S