

1.1.9.28

EE24BTECH11059 - Yellanki Siddhanth

Question:

If **A** and **B** are the points $(-6, 7)$ and $(-1, -5)$ respectively, then the distance **2AB** is equal to

Solution:

Variable	Description	Formula
A	A Point to be plotted	$A = \begin{pmatrix} -6 \\ 7 \end{pmatrix}$
B	A Point to be plotted	$B = \begin{pmatrix} -1 \\ -5 \end{pmatrix}$

TABLE 0

To calculate the distance AB,

$$\mathbf{A} - \mathbf{B} = \begin{pmatrix} -6 \\ 7 \end{pmatrix} - \begin{pmatrix} -1 \\ -5 \end{pmatrix} = \begin{pmatrix} -5 \\ 12 \end{pmatrix} \quad (0.1)$$

$$\|\mathbf{A} - \mathbf{B}\|^2 = (\mathbf{A} - \mathbf{B})^\top (\mathbf{A} - \mathbf{B}) \quad (0.2)$$

$$(\mathbf{A} - \mathbf{B})^\top (\mathbf{A} - \mathbf{B}) = \begin{pmatrix} -5 & 12 \end{pmatrix} \begin{pmatrix} -5 \\ 12 \end{pmatrix} = 169 \quad (0.3)$$

Thus the distance AB is,

$$\|\mathbf{A} - \mathbf{B}\| = \sqrt{169} = 13 \quad (0.4)$$

∴ Required value is:

$$\mathbf{2AB} = 26 \quad (0.5)$$

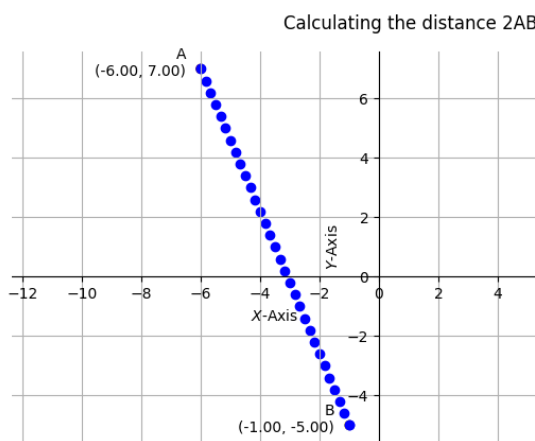


Fig. 0.1