## JEE ASSIGNMENT 3

1

(2021 - 4 Marks)

## EE1030 : Matrix Theory Indian Institute of Technology Hyderabad

## Yellanki Siddhanth (EE24BTECH11059)

1) Let the system of linear equations  $4x + \lambda y + 2z = 0, 2x - y + z = 0, \mu x + 2y + 3z = 0, \lambda, \mu \in \mathbb{R}$  Has a non-trivial solution. Then which of the following is true?

2) A pole stands vertically inside a triangular park *ABC*. Let the angle of elevation of the top of the pole from each corner of the park be  $\frac{\pi}{3}$ . If the radius of the circumcircle

of  $\triangle ABC$  is 2, then the height of the pole is equal to

c)  $\lambda = 3, \mu \in \mathbb{R}$ 

d)  $\mu = -6, \lambda \in \mathbb{R}$ 

## 2021 Feb 25 Shift 2 1 to 15

a)  $\mu = 6, \lambda \in \mathbb{R}$ 

b)  $\lambda = 2, \mu \in \mathbb{R}$ 

	_				
a) $\frac{1}{\sqrt{3}}$	b) $\sqrt{3}$	c) $2\sqrt{3}$	d) $\frac{2\sqrt{3}}{3}$		
half are equal mean and stan	to $-a$ . Also by adding	half of them are equal g a constant b in each new set become 5 and	of these observatio	ns, the	
a) 250	b) 925	c) 650	d) 425		
		ntinuous function in $[0, t \in (1, 3]$ . The largest		which	
a) [1,3]	b) $\left[-1, -\frac{1}{2}\right]$	c) $\left[ -\frac{3}{2}, -1 \right]$	d) $\left[\frac{1}{3}, 2\right]$		
5) If $15 \sin^4 \theta + 1$ equal to:	$10\cos^4\theta = 6$ , for some	$\theta \in \mathbb{R}$ , then the value	e of $27 \sec^6 \theta + 8 \csc^6 \theta$ (2021 - 4 I		
a) 250	b) 400	c) 500	d) 350		
6) Let $f: \mathbb{R} - \{3\} \to \mathbb{R} - \{1\}$ be defined by $f(x) = \frac{x-2}{x-3}$ . Let $g: \mathbb{R} \to \mathbb{R}$ be given as $g(x) = 2x - 3$ . Then, the sum of all the values of $x$ for which $f^{-1}(x) + g^{-1}(x) = \frac{13}{2}$ is equal to					
is equal to			(2021 - 4 1	Marks)	

(2021 - 4 Marks)

d) 3

d) 1000

			(2021 - 4 Marks)		
a) $\left(\frac{1}{2}, \pm \frac{\sqrt{5}}{2}\right)$	b) $(2, \pm \frac{3}{2})$	c) (1, ±2)	d) $\left(0, \pm \sqrt{3}\right)$		
9) Let the centroid of an equilateral triangle $ABC$ be at the origin. Let one of the sides of the equilateral triangle be along the straight line $x + y = 3$ . If $R$ and $r$ be the radius of circumcircle and incircle respectively of $\Delta ABC$ , then $(R + r)$ is equal to (2021 - 4 Marks)					
a) $2\sqrt{2}$	b) $3\sqrt{2}$	c) $7\sqrt{2}$	d) $\frac{9}{\sqrt{2}}$		
10) In a triangle $ABC$ , if vector $\overrightarrow{BC} = 8$ , $\overrightarrow{CA} = 7$ , $\overrightarrow{AB} = 10$ , then the projection of the vector $AB$ on $AC$ is equal to: (2021 - 4 Marks)					
a) $\frac{25}{4}$	b) $\frac{85}{14}$	c) $\frac{127}{20}$	d) $\frac{115}{16}$		
11) Let in a Binomial distribution, consisting of 5 independent trials, probabilities of exactly 1 and 2 successes be 0.4096 and 0.2048 respectively. Then the probability of getting exactly 3 successes is equal to: (2021 - 4 Marks)					
a) $\frac{80}{243}$	b) $\frac{32}{625}$	c) $\frac{128}{625}$	d) $\frac{40}{243}$		
12) Let $a$ and $b$ be two non-zero vectors perpendicular to each other and $ a  =  b $ . If $ a \times b  =  a $ , then the angle between the vectors $(a + b + (a \times b))$ and $a$ is equal to: (2021 - 4 Marks)					
a) $\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$	b) $\cos^{-1}\left(\frac{1}{\sqrt{3}}\right)$	c) $\sin^{-1}\left(\frac{1}{\sqrt{6}}\right)$	d) $\cos^{-1}\left(\frac{1}{\sqrt{2}}\right)$		
13) Let a complex number be $w = 1 - \sqrt{3}i$ . Let another complex number $z$ be such that $ zw  = 1$ and $\arg(z) - \arg(w) = \frac{\pi}{2}$ . Then the area of the triangle with vertices origin, $z$ and $w$ is equal to:					
z ana // is eque			(2021 - 4 Marks)		

b) 5

b) 7000

c) 2

c) 5000

7) Let  $S_1$  be the sum of the first 2n terms of an arithmetic progression. Let  $S_2$  be the sum of the first 4n terms of the same arithmetic progression. If  $(S_2 - S_1)$  is 1000,

8) Let  $S_1 = x^2 + y^2 = 9$  and  $S_2 = (x - 2)^2 + y^2 = 1$ . Then the locus of the centre of a variable circle S which touches  $S_1$  internally and  $S_2$  externally always passes

then the sum of the first 6n terms of the arithmetic progression is equal to:

a) 7

a) 3000

through the points:

d)  $\frac{1}{4}$ 

14) The area bour	nded by the curve 4y	$x^2 = x^2 (4 - x)(x - 2)$ is	equal to: (2021 - 4 Marks)
a) $\frac{3\pi}{2}$	b) $\frac{\pi}{16}$	c) $\frac{\pi}{8}$	d) $\frac{3\pi}{8}$

c) 2

- 15) Define a relation R over a class of  $n \times n$  real matrices A and B as ARB if there exists a non-singular matrix P such that  $PAP^{-1} = B$ . Then which of the following is true? (2021 4 Marks)
  - a) R is reflexive, symmetric but not transitive

b) 4

- b) R is symmetric, transitive but not reflexive
- c) R is an equivalence relation

a)  $\frac{1}{2}$ 

d) R is reflexive, transitive but not symmetric