GATE: IN - 50.2023

EE23BTECH11224 - Sri Krishna Prabhas Yadla*

Question: The phase margin of the transfer function $G(s) = \frac{2(1-s)}{(1+s)^2}$ is _____ degrees. (rounded off to the nearest integer). (GATE IN 2023)

Solution:

| Parameters | Description |
|-----------------------|--------------------------------------|
| ω_c | crossover frequency |
| $\angle G(j\omega_c)$ | phase angle of the transfer function |
| PM | Phase Margin |

TABLE 1

$$G(j\omega_c) = \frac{2(1 - j\omega_c)}{(1 + j\omega_c)^2} \tag{1}$$

$$|G(j\omega_c)| = \left| \frac{2(1 - j\omega_c)}{(1 + j\omega_c)^2} \right|$$

$$= \frac{2}{\sqrt{1 + \omega_c^2}} = 1$$
(2)

$$=\frac{2}{\sqrt{1+\omega_c^2}}=1\tag{3}$$

$$\implies \omega_c = \sqrt{3} \tag{4}$$

$$G(j\omega) = \frac{2(1 - j\omega)^3}{(1 + \omega^2)^2}$$
 (5)

$$\angle G(j\omega) = 3 \tan^{-1}(-\omega) \tag{6}$$

$$\implies \angle G(j\omega_c) = -180^{\circ} \tag{7}$$

$$PM = \angle G(j\omega_c) + 180^{\circ} \tag{8}$$

$$=0^{\circ} \tag{9}$$

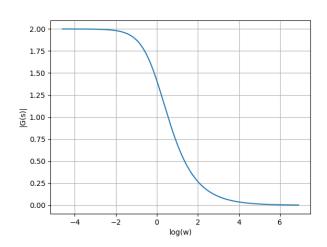


Fig. 1. Plot of $|G(j\omega)|$ vs $\log \omega$

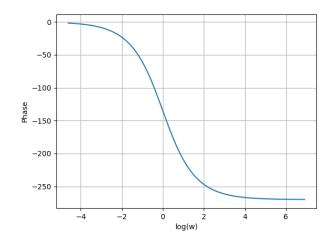


Fig. 2. Plot of $\angle G(j\omega)$ vs $\log \omega$