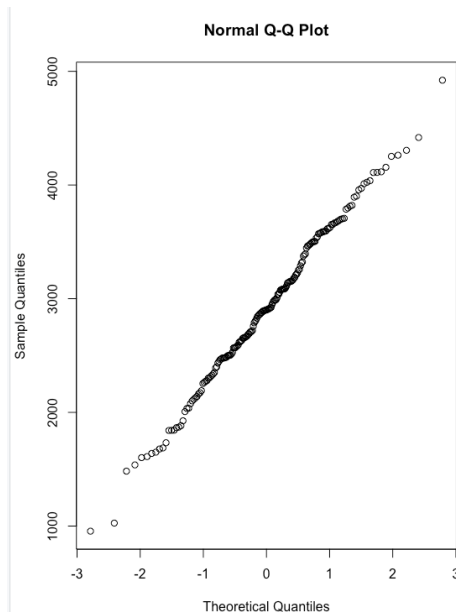


SSO Assignment 1

Q1

- A QQ-plot and Shapiro-Wilk test show that the data is normally distributed, with the QQ-plot (1) points being in a relatively straight line and the Shapiro-Wilk test outcome of 0.9 (2).
- The bounded 90% confidence interval for μ is between 2829.2 and 2997.4 (3).
- A t-test was performed using $H_0: \mu \leq 2800$ and $H_1: \mu > 2800$ (4). The outcome of this test showed a p-value of 0.013, which is smaller than the alpha of 0.05, meaning that H_0 is rejected and H_1 is assumed to be true.
- The confidence interval for (b) is a two-sided interval, meaning that we have boundaries for the interval at both sides of the true mean. This makes sense, because we want to know *where* the true mean is. In (c), all we want to know is whether the true mean is *bigger* than 2800. Therefore, it is one sided and we get the same left value, but no specified right value, as anything bigger than this value will also satisfy H_1 .



```
> #90% confidence interval for mu
> n=length(weights)
> m = mean(weights); m
[1] 2913.293
> s = sd(weights); s
[1] 697.5002
> t = qt(0.95,df=n-1); t
[1] 1.653043
> ci = c(m-t*s/sqrt(n),m+t*s/sqrt(n))
> ci
[1] 2829.202 2997.384
```

3

1

Shapiro-Wilk normality test

```
data: weights
W = 0.99595, p-value = 0.8995
```

2

```
data: weights
t = 2.2271, df = 187, p-value = 0.01357
alternative hypothesis: true mean is greater than 2800
95 percent confidence interval:
 2829.202      Inf
sample estimates:
mean of x
 2913.293
```

4

Q2

a. $\hat{p} = x/n$, so $140/200=0.7$

b. 99% confidence interval for $p = 0.7$

$p=0.7$

$q=0.3$

$n=200$

$z_{\alpha/2} = 1-0.005=0.995$ so $qnorm(0.995)$

$qnorm(0.995)*sqrt((0.7*0.3)/200)0.0834$

$0.7 \pm 0.08 = 0.6166$

$0.7 + 0.0834 = 0.7834$

So, CI is between 0.6166 and 0.7834

c. $H_0: p=0.75$

$H_1: p \neq 0.75$

number of successes = $0.75 \times 200 = 150$

$\alpha = 0.1$ `qnorm(0.95)`

Exact binomial test

data: 140 and 200

number of successes = 140, number of trials = 200, p-value = 0.103

alternative hypothesis: true probability of success is not equal to 0.75

95 percent confidence interval:

0.6313501 0.7626104

sample estimates:

probability of success
0.7

p-value is 0.103, so H_0 is not rejected.

Different confidence intervals:

$\alpha = 0.01$

Exact binomial test

data: 140 and 200

number of successes = 140, number of trials = 200, p-value = 0.103

alternative hypothesis: true probability of success is not equal to 0.75

99 percent confidence interval:

0.6099163 0.7803014

sample estimates:

probability of success
0.7

$\alpha = 0.2$

Exact binomial test

data: 140 and 200

number of successes = 140, number of trials = 200, p-value = 0.103

alternative hypothesis: true probability of success is not equal to 0.75

80 percent confidence interval:

0.6545921 0.7423676

sample estimates:

probability of success

0.7

p remains the same for different confidence intervals. why?

Q3

a.