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# The Security Evaluated Standardized Password Authenticated Key Exchange (SESPAKE) Protocol

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#### **Abstract**

This document specifies the Security Evaluated Standardized Password Authenticated Key Exchange (SESPAKE) protocol. The SESPAKE protocol provides password authenticated key exchange for usage in the systems for protection of sensitive information. The security proofs of the protocol were made for the case of an active adversary in the channel, including MitM attacks and attacks based on the impersonation of one of the subjects.

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#### 1. Introduction

The current document contains the description of the password authenticated key exchange protocol SESPAKE (security evaluated standardized password authenticated key exchange) for usage in the systems for protection of sensitive information. The protocol is intended to use for establishment of keys that are then used for organization of secure channel for protection of sensitive information. The security proofs of the protocol were made for the case of an active adversary in the channel, including MitM attacks and attacks based on the impersonation of one of the subjects.

## 2. Conventions Used in This Document

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in [RFC2119].

#### 3. Notations

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This document uses the following parameters of elliptic curves in accordance with [RFC6090]:

E an elliptic curve defined over a finite prime field GF(p), where p > 3;

the characteristic of the underlying prime field;

a, b
 the coefficients of the equation of the elliptic curve in the canonical form;

the elliptic curve group order;

q the elliptic curve subgroup order;

a generator of the subgroup of order q;

```
X, Ythe coordinates of the elliptic curve point in the canonical form;Ozero point (point of infinity) of the elliptic curve.
```

This memo uses the following functions:

```
HASH
```

the underlying hash function;

#### **HMAC**

the function for calculating a message authentication code, based on a HASH function in accordance with [RFC2104];

```
F(PW, salt, n)
```

the value of the function PBKDF2(PW,salt,n,len), where PBKDF2(PW,salt,n,len) is calculated according to [RFC2898] The parameter len is considered equal to minimal integer that is a multiple of 8 and satisfies the following condition:

```
len >= floor(log_2(q)).
```

This document uses the following terms and definitions for the sets and operations on the elements of these sets

```
B_n the set of byte strings of size n, n >= 0, for n = 0 the B_n set consists of a single empty string of size 0; if b is an element of B_n, then b = (b_1,...,b_n), where b_1,...,b_n are elements of \{0,...,255\};  
|| concatenation of byte strings A and C, i.e., if A in B_n1, C in B_n2, A = (a_1,a_2,...,a_n1) and C = (c_1,c_2,...,c_n2), then A||C = (a_1,a_2,...,a_n1,c_1,c_2,...,c_n2) is an element of B_(n1+n2);  
int(A) for the byte string A = (a_1,...,a_n) in B_n an integer int(A) = 256^{\circ}(n-1)a_n + ... + 256^{\circ}(0)a_1;  
bytes_n(X) the byte string A in B_n such that int(A) = X, where X is integer, 0 <= X < 256^{\circ}n;  
BYTES(Q) for Q in E, the byte string bytes_n(X) || bytes_n(Y), where X, Y are standard Weierstrass coordinates
```

# 4. Protocol Description

of point Q and  $n = ceil(log \{256\}(p))$ .

The main point of the SESPAKE protocol is that parties sharing a weak key (a password) generate a strong common key. The active adversary who has an access to a channel is not able to obtain any information that can be used to find a key in offline mode, i.e. without interaction with legitimate participants.

The protocol is used by the subjects A (client) and B (server) that share some secret parameter that was established in an out-of-band mechanism: a client is a participant who stores a password as a secret parameter and a server is a participant who stores a password-based computed point of the elliptic curve.

The SESPAKE protocol consists of two steps: the key agreement step and the key confirmation step. During the first step (the key agreement step) the parties exchange keys using Diffie-Hellman with public components masked by an element that depends on the password - one of the predefined elliptic curve points multiplied by the password-based coefficient. This approach provides an implicit key authentication, which means that after this step one party is assured that no other party aside from a specifically identified second party may gain access to the generated secret key. During the second step (the key confirmation step) the parties exchange strings that strongly depend on the generated key. After this step the parties are assured that a legitimate party and no one else actually has possession of the secret key.

To protect against online guessing attacks the failed connections counters were introduced in the SESPAKE protocol. There is also a special way of a small order point processing and a mechanism that provides a reflection attack protection by using different operations for different sides.

#### 4.1. Protocol Parameters

Various elliptic curves can be used in the protocol. For each elliptic curve supported by clients the following values MUST be defined:

- the protocol parameters identifier ID\_ALG (which can also define a HASH function, PRF used in PBKDF2 function, etc.), that is a byte string of an arbitrary length;
- the point P, that is a generator point of the subgroup of order q of the curve;
- the set of distinct curve points {Q\_1,Q\_2,...,Q\_N} of order q, where the total number of points N is defined for protocol instance.

The method of generation of the points {P,Q\_1,Q\_2,...,Q\_N} is described in Section 5.

The protocol parameters that are used by subject A are the following:

- 1. The secret password value PW, which is a byte string that is uniformly randomly chosen from a subset of cardinality 10^10 or greater of the set B k, where k? 6 is password length.
- 2. The list of curve identifiers supported by A.
- 3. Sets of points {Q\_1,Q\_2,...,Q\_N}, corresponding to curves supported by A.
- 4. The C\_1^A counter, that tracks the total number of unsuccessful authentication trials in a row, and a value of CLim\_1 that stores the maximum possible number of such events.
- 5. The C\_2^A counter, that tracks the total number of unsuccessful authentication events during the period of usage of the specific PW, and a value of CLim\_2 that stores the maximum possible number of such events.
- 6. The C\_3^A counter, that tracks the total number of authentication events (successful and unsuccessful) during the period of usage of the specific PW, and a value of CLim\_3 that stores the maximum possible number of such events.
- 7. The unique identifier ID\_A of the subject A (OPTIONAL), which is a byte string of an arbitrary length.

The protocol parameters that are used by subject B are the following:

- 1. The values ind and salt, where ind is in  $\{1,...,N\}$ , salt is in  $\{1,...,2^128-1\}$ .
- 2. The point Q PW, satisfying the following equation:

It is possible that the point Q\_PW is not stored and is calculated using PW in the beginning of the protocol. In that case B has to store PW and points Q\_1,Q\_2,...,Q\_N.

- 3. The ID\_ALG identifier.
- 4. The C\_1^B counter, that tracks the total number of unsuccessful authentication trials in a row, and a value of CLim\_1 that stores the maximum possible number of such events.
- 5. The C\_2^B counter, that tracks the total number of unsuccessful authentication events during the period of usage of the specific PW, and a value of CLim\_2 that stores the maximum possible number of such events.
- 6. The C\_3^B counter, that tracks the total number of authentication events (successful and unsuccessful) during the period of usage of the specific PW, and a value of CLim\_3 that stores the maximum possible number of such events.
- 7. The unique identifier ID\_B of the subject B (OPTIONAL), which is a byte string of an arbitrary length.

## 4.2. Initial Values of the Protocol Counters

After the setup of a new password value PW the values of the counters MUST be assigned as follows:

- $C_1^A = C_1^B = CLim_1$ , where  $CLim_1$  is in  $\{3,...,5\}$ ;
- C\_2^A = C\_2^B = CLim\_2, where CLim\_2 is in {7,...,20};
- $C_3^A = C_3^B = CLim_3$ , where  $CLim_3$  is in  $\{10^3, 10^3 + 1, ..., 10^5\}$ .

# 4.3. Protocol Steps

The basic SESPAKE steps are shown in the scheme below:

A [A_ID, PW]		B [B_ID, Q_PW , ind, salt]
if C_1^A or C_2^A or C_3^A = 0 ==> QUIT		
decrement C_1^A, C_2^A, C_3^A by 1	A_ID>	if C_1^B or C_2^B or C_3^B = 0 ==> QUIT
z_A = 0	< ID_ALG, B_ID (OPTIONAL), ind, salt	decrement C_1^B, C_2^B, C_3^B by 1
Q_PW^A = int(F(PW, salt, 2000)) * Q_ind		
choose alpha randomly from {1,,q-1}		
u_1 = alpha*P - Q_PW^A	u_1>	if u_1 not in E ==> QUIT
		z_B = 0
		Q_B = u_1 + Q_PW
		choose betta randomly from {1,,q-1}
		if $m/q^*Q_B = O ==> Q_B = betta^*P$ , $z_B = 1$
		K_B = HASH(BYTES((m/q*betta*(mod q))*Q_B))
if u_2 not in E ==> QUIT	< u_2	u_2 = betta*P + Q_PW
Q_A = u_2 - Q_PW^A		
if m/q*Q_A = O ==> Q_A = alpha*P, z_A = 1		
K_A = HASH(BYTES((m/q*alpha(mod q))*Q_A))		
U_1 = BYTES(u_1), U_2 = BYTES(u_2)		
MAC_A = HMAC(K_A, 0x01    ID_A    ind    salt    U_1    U_2    ID_ALG (OPTIONAL)    DATA_A)	DATA_A, MAC_A>	U_1 = BYTES(u_1), U_2 = BYTES(u_2)
		if MAC_A != HMAC(K_B, 0x01    ID_A    ind    salt    U_1    U_2    ID_ALG (OPTIONAL)    DATA_A) ==> QUIT
		if z_B = 1 ==> QUIT
		C_1^B = CLim_1, increment C_2^B by 1
if MAC_B != HMAC(K_A, 0x02    ID_B    ind    salt    U_1    U_2    ID_ALG (OPTIONAL)    DATA_A    DATA_B) ==> QUIT	< DATA_B, MAC_B	MAC_B = HMAC(K_B, 0x02    ID_B    ind    salt    U_1    U_2    ID_ALG (OPTIONAL)    DATA_A    DATA_B)
if z_A = 1 ==> QUIT		

A [A_ID, PW]	B [B_ID, Q_PW , ind, salt]
C_1^A = CLim_1, increment C_2^A by 1	

#### SESPAKE protocol steps

The full description of the protocol consists of the following steps:

- 1. If any of the counters C\_1^A, C\_2^A, C\_3^A is equal to 0, A finishes the protocol with an error that informs of exceeding the number of trials that is controlled by the corresponding counter.
- 2. A decrements each of the counters C\_1^A, C\_2^A, C\_3^A by 1, requests open authentication information from B and sends the ID\_A identifier.
- 3. If any of the counters C\_1^B, C\_2^B, C\_3^B is equal to 0, B finishes the protocol with an error that informs of exceeding the number of trials that is controlled by the corresponding counter.
- 4. B decrements each of the counters C\_1^B, C\_2^B, C\_3^B by 1.
- B sends the values of ind, salt and the ID\_ALG identifier to A. B also can OPTIONALLY send the ID\_B identifier to A. All following calculations are done by B in the elliptic curve group defined by the ID\_ALG identifier.
- 6. A sets the curve defined by the received ID\_ALG identifier as the used elliptic curve. All following calculations are done by A in this elliptic curve group.
- 7. A calculates the point Q\_PW^A = int (F (PW, salt, 2000))\*Q\_ind.
- 8. A chooses randomly (according to the uniform distribution) the value alpha, alpha is in  $\{1, ..., q-1\}$ , and assigns  $z_A = 0$ .
- 9. A sends the value u\_1 = alpha\*P Q\_PW^A to B.
- 10. After receiving u\_1, B checks that u\_1 is in E. If it is not, B finishes with an error, considering the authentication process unsuccessful.
- 11. B calculates Q\_B = u\_1 + Q\_PW, assigns z\_B = 0 and chooses randomly (according to the uniform distribution) the value betta, betta is in {1,...,q-1}.
- 12. If  $m/q^*Q_B = O$ , B assigns  $Q_B = betta^*P$  and  $z_B = 1$ .
- 13. B calculates K B = HASH (BYTES(( m/g\*betta\*(mod g))\*Q B )).
- 14. B sends the value u\_2 = betta\*P + Q\_PW to A.
- 15. After receiving u\_2, A checks that u\_2 is in E. If it is not, A finishes with an error, considering the authentication process unsuccessful.
- 16. A calculates Q\_A = u\_2 Q\_PW^A.
- 17. If  $m/q^*Q_A = O$ , then A assigns  $Q_A = alpha^*P$  and  $z_A = 1$ .
- 18. A calculates K\_A = HASH (BYTES(( m/q\*alpha(mod q))\*Q\_A )).
- 19. A calculates U\_1 = BYTES(u\_1), U\_2 = BYTES(u\_2).
- 20. A calculates MAC\_A = HMAC (K\_A, 0x01 || ID\_A || ind || salt || U\_1 || U\_2 || ID\_ALG (OPTIONAL) || DATA\_A), where DATA\_A is an OPTIONAL string that is authenticated with MAC A (if it is not used, then DATA\_A is considered to be of zero length).
- 21. A sends DATA\_A, MAC\_A to B.
- 22. B calculates U 1 = BYTES(u\_1), U\_2 = BYTES(u\_2).
- 23. B checks that the values MAC\_A and HMAC (K\_B, 0x01 || ID\_A || ind || salt || U\_1 || U\_2 || ID\_ALG (OPTIONAL) || DATA\_A) are equal. If they are not, it finishes with an error, considering the authentication process unsuccessful.
- 24. If  $z_B = 1$ , B finishes, considering the authentication process unsuccessful.
- 25. B sets the value of  $C_1^B$  to  $CLim_1$  and increments  $C_2^B$  by 1.
- 26. B calculates MAC\_B = HMAC(K\_B, 0x02 || ID\_B || ind || salt || U\_1 || U\_2 || ID\_ALG (OPTIONAL) || DATA\_A || DATA\_B), where DATA\_B is an OPTIONAL string that is authenticated with MAC\_B (if it is not used, then DATA\_B is considered to be of zero length).
- 27. B sends DATA B, MAC B to A.
- 28. A checks that the values MAC\_B and HMAC (K\_A, 0x02 || ID\_B || ind || salt || U\_1 || U\_2 ||

- ID\_ALG (OPTIONAL) || DATA\_A || DATA\_B) are equal. If they are not, it finishes with an error, considering the authentication process unsuccessful.
- 29. If  $z_A = 1$ , A finishes, considering the authentication process unsuccessful.
- 30. A sets the value of C\_1^A to CLim\_1 and increments C\_2^A by 1.

After the successful finish of the procedure the subjects A and B are mutually authenticated and each subject has an explicitly authenticated value of K = K\_A = K\_B.

#### Notes:

- 1. In the case when the interaction process can be initiated by any subject (client or server) the ID\_A and ID\_B options MUST be used and the receiver MUST check that the identifier he had received is not equal to his own, otherwise, it finishes the protocol. If an OPTIONAL parameter ID\_A (or ID\_B) is not used in the protocol, it SHOULD be considered equal to a fixed byte string (zero-length string is allowed) defined by a specific implementation.
- 2. The ind, ID\_A, ID\_B and salt parameters can be agreed in advance. If some parameter is agreed in advance, it is possible not to send it during a corresponding step. Nevertheless, all parameters MUST be used as corresponding inputs to HMAC function during stages 20, 23, 26 and 28.
- 3. The ID ALG parameter can be fixed or agreed in advance.
- 4. The ID\_ALG parameter is RECOMMENDED to be used in HMAC during stages 20, 23, 26 and 28.
- 5. Continuation of protocol interaction in case of any of the counters C\_1^A, C\_1^B being equal to zero MAY be done without changing password. In this case these counters can be used for protection against denial-of-service attacks. For example, continuation of interaction can be allowed after a certain delay.
- 6. Continuation of protocol interaction in case of any of the counters C\_2^A, C\_3^A, C\_2^B, C\_3^B being equal to zero MUST be done only after changing password.
- 7. It is RECOMMENDED that during the stages 9 and 14 the points u\_1 and u\_2 are sent in a non-compressed format (BYTES(u\_1) and BYTES(u\_2)). However, the point compression MAY be used.
- 8. The use of several Q points can reinforce the independence of the data streams in case of working with several applications, when, for example, two high-level protocols can use two different points. However, the use of more than one point is OPTIONAL.

# 5. Construction of Points Q\_1,...,Q\_N

This section provides an example of possible algorithm for generation of each point  $Q_i$  in the set  $\{Q_1,...,Q_N\}$  that corresponds to the given elliptic curve E.

The algorithm is based on choosing points with coordinates with a known preimages of a cryptographic hash function H, which is the GOST R 34.11-2012 hash function (see [RFC6986]) with 256-bit output, if  $2^254 < q < 2^256$ , and the GOST R 34.11-2012 hash function (see [RFC6986]) with 512-bit output, if  $2^508 < q < 2^512$ .

The algorithm consists of the following steps:

- 1. Set i = 1, SEED = 0, s = 4 or more.
- 2. Calculate  $X = int(HASH(BYTES(P)||bytes s(SEED))) \mod p$ .
- 3. Check that the value of  $X^3 + aX + b$  is a quadratic residue in the field  $F_p$ . If it is not, set SEED = SEED + 1 and return to Step 2.
- 4. Choose the value of  $Y = min\{r1, r2\}$ , where r1, r2 from  $\{0,1,...,p-1\}$  such that r1 != r2 and r1^2 = r2^2 = R mod p for R = X^3 + aX + b.
- 5. Check that for point Q = (X,Y) the following relations hold: Q != O and  $q^*Q = O$ . If they do, go to Step 6, if not, set SEED = SEED + 1 and return to Step 2.

6. Set  $Q_i = Q$ . If  $i \in N$ , then set i = i+1 and go to Step 2, else FINISH.

With the defined algorithm for any elliptic curve E point sets {Q\_1,...,Q\_N} are constructed. Constructed points in one set MUST have distinct X-coordinates.

N o t e: The knowledge of a hash function preimage prevents knowledge of the multiplicity of any point related to generator point P. It is of primary importance, because such a knowledge could be used to implement an attack against protocol with exhaustive search of password.

## 6. Acknowledgments

We thank Lolita Sonina, Georgiy Borodin, Sergey Agafin and Ekaterina Smyshlyaeva for their careful readings and useful comments.

# 7. Security Considerations

Any cryptographic algorithms, particularly HASH function and HMAC function, that are used in the SESPAKE protocol MUST be carefully designed and MUST be able to withstand all known types of cryptanalytic attack.

It is RECOMMENDED that the HASH function satisfies the following condition: hashlen  $\leq \log_2(q) + 4$ , where hashlen is the lengths of the HASH function output.

The output length of hash functions that are used in the SESPAKE protocol is RECOMMENDED to be greater or equal to 256 bits.

The points Q\_1, Q\_2,...,Q\_N and P MUST be chosen in such a way that they are provable pseudorandom. As a practical matter, this means that the algorithm for generation of each point Q\_i in the set {Q\_1,...,Q\_N} (see Section 5) ensures that multiplicity of any point under any other point is unknown.

For a certain ID\_ALG using N = 1 is RECOMMENDED.

N o t e: The exact adversary models, which have been considered during the security evaluation, can be found in the paper [SESPAKE-SECURITY], containing the security proofs.

#### 8. References

#### 8.1. Normative References

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[GOST3411-2012]	Federal Agency on Technical Regulating and Metrology (In Russian), "Information technology. Cryptographic Data Security. Hashing function", GOST R 34.11-2012, 2012.
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10.17487/RFC6986, August 2013.

[RFC7091] Dolmatov, V. and A. Degtyarev, "GOST R 34.10-2012: Digital Signature Algorithm", RFC

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[RFC7836] Smyshlyaev, S., Alekseev, E., Oshkin, I., Popov, V., Leontiev, S., Podobaev, V. and D.

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Standards GOST R 34.10-2012 and GOST R 34.11-2012", RFC 7836, DOI

10.17487/RFC7836, March 2016.

#### 8.2. Informative References

[SESPAKE-SECURITY] Smyshlyaev, S., Oshkin, I., Alekseev, E. and L. Ahmetzyanova, "On the Security of One Password Authenticated Key Exchange Protocol", 2015.

## Appendix A. Test Examples for GOST-based Protocol Implementation

The following test examples are made for the protocol implementation that is based on the Russian national standards GOST R 34.10-2012 [GOST3410-2012] and GOST R 34.11-2012 [GOST3411-2012]. The English versions of these standards can be found in [RFC7091] and [RFC6986].

# A.1. Examples of Points

There is one point Q\_1 for each of the elliptic curves below. This points were constructed using the method described in Section 5, in case when N = 1, where the GOST R 34.11-2012 hash function (see [RFC6986]) with 256-bit output is used if  $2^254 < q < 2^256$ , the GOST R 34.11-2012 hash function (see [RFC6986]) with 512-bit output is used if  $2^508 < q < 2^512$ .

Each of the points complies with the GOST R 34.10-2012 [GOST3410-2012] standard and is represented by a pair of (X, Y) coordinates in the canonical form and by a pair of (U, V) coordinates in the twisted Edwards form in accordance with the document [RFC7836] for the curves that have the equivalent representation in this form. There is a SEED value for each point, by which it was generated.

A.1.1. Curve id-GostR3410-2001-CryptoPro-A-ParamSet

Point Q 1

X = 0xa69d51caf1a309fa9e9b66187759b0174c274e080356f23cfcbfe84d396ad7bb

Y = 0x5d26f29ecc2e9ac0404dcf7986fa55fe94986362170f54b9616426a659786dac

SEED = 0x0001

A.1.2. Curve id-GostR3410-2001-CryptoPro-B-ParamSet

Point Q 1

X = 0x3d715a874a4b17cb3b517893a9794a2b36c89d2ffc693f01ee4cc27e7f49e399

Y = 0x1c5a641fcf7ce7e87cdf8cea38f3db3096eace2fad158384b53953365f4fe7fe

SEED = 0x0000

A.1.3. Curve id-GostR3410-2001-CryptoPro-C-ParamSet

Point Q 1

X = 0x1e36383e43bb6cfa2917167d71b7b5dd3d6d462b43d7c64282ae67dfbec2559d

Y = 0x137478a9f721c73932ea06b45cf72e37eb78a63f29a542e563c614650c8b6399

SEED = 0x0006

A.1.4. Curve id-tc26-gost-3410-2012-512-paramSetA

Point Q 1

X = 0x2a17f8833a32795327478871b5c5e88aefb91126c64b4b8327289bea62559425 d18198f133f400874328b220c74497cd240586cb249e158532cb8090776cd61c

Y = 0x728f0c4a73b48da41ce928358fad26b47a6e094e9362bae82559f83cddc4ec3a 4676bd3707edeaf4cd85e99695c64c241edc622be87dc0cf87f51f4367f723c5

```
SEED = 0x0001
A.1.5. Curve id-tc26-gost-3410-2012-512-paramSetB
Point Q 1
X = 0x7e1fae8285e035bec244bef2d0e5ebf436633cf50e55231dea9c9cf21d4c8c33
   df85d4305de92971f0a4b4c07e00d87bdbc720eb66e49079285aaf12e0171149
Y = 0x2cc89998b875d4463805ba0d858a196592db20ab161558ff2f4ef7a85725d209
   53967ae621afdeae89bb77c83a2528ef6fce02f68bda4679d7f2704947dbc408
SEED = 0x0000
A.1.6. Curve id-tc26-gost-3410-2012-256-paramSetA
Point Q 1
X = 0xb51adf93a40ab15792164fad3352f95b66369eb2a4ef5efae32829320363350e
Y = 0x74a358cc08593612f5955d249c96afb7e8b0bb6d8bd2bbe491046650d822be18
U = 0xebe97afffe0d0f88b8b0114b8de430ac2b34564e4420af24728e7305bc48aeaa
V = 0x828f2dcf8f06612b4fea4da72ca509c0f76dd37df424ea22bfa6f4f65748c1e4
SEED = 0x0001
A.1.7. Curve id-tc26-gost-3410-2012-512-paramSetC
Point Q_1
X = 0x489c91784e02e98f19a803abca319917f37689e5a18965251ce2ff4e8d8b298f
   5ba7470f9e0e713487f96f4a8397b3d09a270c9d367eb5e0e6561adeeb51581d
Y = 0x684ea885aca64eaf1b3fee36c0852a3be3bd8011b0ef18e203ff87028d6eb5db
```

# A.2. Test Examples of SESPAKE

SEED = 0x0013

This protocol implementation uses the GOST R 34.11-2012 hash function (see [RFC6986]) with 256-bit output as the H function and the HMAC\_GOSTR3411\_2012\_512 function defined in [RFC7836] as a PRF function for the F function. The parameter len is considered equal to 256, if  $2^254 < q < 2^56$ , and equal to 512, if  $2^508 < q < 2^512$ .

The test examples for the point of each curve in Appendix A.1 are given below.

2c144a0dcc71276542bfd72ca2a43fa4f4939da66d9a60793c704a8c94e16f18
U = 0x3a3496f97e96b3849a4fa7db60fd93858bde89958e4beebd05a6b3214216b37c
9d9a560076e7ea59714828b18fbfef996ffc98bf3dc9f2d3cb0ed36a0d6ace88
V = 0x52d884c8bf0ad6c5f7b3973e32a668daa1f1ed092eff138dae6203b2ccdec561
47464d35fec4b727b2480eb143074712c76550c7a54ff3ea26f70059480dcb50

```
A.2.1 Curve id-GostR3410-2001-CryptoPro-A-ParamSet

The input protocol parameters in this example take the following values:

N = 1
ind = 1
ID_A:
00 00 00 00
ID_B:
00 00 00 00
PW:
31 32 33 34 35 36 ('123456')
salt:
29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB

Q_ind:
X = 0xA69D51CAF1A309FA9E9B66187759B0174C274E080356F23CFCBFE84D396AD7BB
Y = 0x5D26F29ECC2E9AC0404DCF7986FA55FE94986362170F54B9616426A659786DAC
```

```
The function F (PW, salt, 2000) takes the following values:
F(PW,salt,2000):
 BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71
 D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67
The coordinates of the point Q PW are:
 X = 0x59495655D1E7C7424C622485F575CCF121F3122D274101E8AB734CC9C9A9B45E
 Y = 0x48D1C311D33C9B701F3B03618562A4A07A044E3AF31E3999E67B487778B53C62
During the calculation of the message u 1 on the subject A the parameter
alpha, the point alpha*P and the message u_1 take the following values:
alpha=0x1F2538097D5A031FA68BBB43C84D12B3DE47B7061C0D5E24993E0C873CDBA6B3
alpha*P:
 X = 0xBBC77CF42DC1E62D06227935379B4AA4D14FEA4F565DDF4CB4FA4D31579F9676
 Y = 0x8E16604A4AFDF28246684D4996274781F6CB80ABBBA1414C1513EC988509DABF
u 1:
 X = 0x204F564383B2A76081B907F3FCA8795E806BE2C2ED228730B5B9E37074229E8D
 Y = 0xE84F9E442C61DDE37B601A7F37E7CA11C56183FA071DFA9320EDE3E7521F9D41
During processing a message u 1, calculation the K B key and the message
u_2 on the subject B the parameters betta, src, K_B = HASH(src), betta*P
and u 2 take the following values:
betta=0xDC497D9EF6324912FD367840EE509A2032AEDB1C0A890D133B45F596FCCBD45D
 2E 01 A3 D8 4F DB 7E 94 7B B8 92 9B E9 36 3D F5
 F7 25 D6 40 1A A5 59 D4 1A 67 24 F8 D5 F1 8E 2C
 A0 DB A9 31 05 CD DA F4 BF AE A3 90 6F DD 71 9D
 BE B2 97 B6 A1 7F 4F BD 96 DC C7 23 EA 34 72 A9
 1A 62 65 54 92 1D C2 E9 2B 4D D8 D6 7D BE 5A 56
 62 E5 62 99 37 3F 06 79 95 35 AD 26 09 4E CA A3
betta*P:
 X = 0x6097341C1BE388E83E7CA2DF47FAB86E2271FD942E5B7B2EB2409E49F742BC29
 Y = 0xC81AA48BDB4CA6FA0EF18B9788AE25FE30857AA681B3942217F9FED151BAB7D0
u 2:
 X = 0 \times DC137A2F1D4A35AEBC0ECBF6D3486DEF8480BFDC752A86DD4F207D7D1910E22D
 Y = 0x7532F0CE99DCC772A4D77861DAE57C138F07AE304A727907FB0AAFDB624ED572
During processing a message u 2 and calculation the key on the subject A
the K A key takes the following value:
K_A:
 1A 62 65 54 92 1D C2 E9 2B 4D D8 D6 7D BE 5A 56
 62 E5 62 99 37 3F 06 79 95 35 AD 26 09 4E CA A3
The message MAC_A=HMAC (K_A, 0x01 || ID_A || ind || salt || u_1 || u_2)
from the subject A takes the following value:
MAC A:
 23 7A 03 C3 5F 49 17 CE 86 B3 58 94 45 F1 1E 1A
 6F 10 8B 2F DD 0A A9 E8 10 66 4B 25 59 60 B5 79
The message MAC B=HMAC (K B, 0x02 || ID B || ind || salt || u 1 || u 2)
from the subject B takes the following value:
MAC B:
 9E E0 E8 73 3B 06 98 50 80 4D 97 98 73 1D CD 1C
 FF E8 7A 3B 15 1F 0A E8 3E A9 6A FB 4F FC 31 E4
A.2.2 Curve id-GostR3410-2001-CryptoPro-B-ParamSet
```

The input protocol parameters in this example take the following values:

```
ind = 1
ID A:
 00 00 00 00
ID B:
 00 00 00 00
PW:
 31 32 33 34 35 36 ('123456')
salt:
 29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB
Q ind:
 X = 0x3D715A874A4B17CB3B517893A9794A2B36C89D2FFC693F01EE4CC27E7F49E399
 Y = 0x1C5A641FCF7CE7E87CDF8CEA38F3DB3096EACE2FAD158384B53953365F4FE7FE
The function F (PW, salt, 2000) takes the following values:
F(PW,salt,2000):
 BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71
 D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67
The coordinates of the point Q PW are:
 X = 0x6DC2AE26BC691FCA5A73D9C452790D15E34BA5404D92955B914C8D2662ABB985
 Y = 0x3B02AAA9DD65AE30C335CED12F3154BBAC059F66B088306747453EDF6E5DB077
During the calculation of the message u 1 on the subject A the parameter
alpha, the point alpha*P and the message u 1 take the following values:
alpha=0x499D72B90299CAB0DA1F8BE19D9122F622A13B32B730C46BD0664044F2144FAD
alpha*P:
 X = 0x61D6F916DB717222D74877F179F7EBEF7CD4D24D8C1F523C048E34A1DF30F8DD
 Y = 0x3EC48863049CFCFE662904082E78503F4973A4E105E2F1B18C69A5E7FB209000
u 1:
 X = 0x21F5437AF33D2A1171A070226B4AE82D3765CD0EEBFF1ECEFE158EBC50C63AB1
 Y = 0x5C9553B5D11AAAECE738AD9A9F8CB4C100AD4FA5E089D3CBCCEA8C0172EB7ECC
During processing a message u 1, calculation the K B key and the message
u 2 on the subject B the parameters betta, src, K B = HASH(src), betta*P
and u 2 take the following values:
betta=0x0F69FF614957EF83668EDC2D7ED614BE76F7B253DB23C5CC9C52BF7DF8F4669D
src:
 50 14 0A 5D ED 33 43 EF C8 25 7B 79 E6 46 D9 F0
 DF 43 82 8C 04 91 9B D4 60 C9 7A D1 4B A3 A8 6B
 00 C4 06 B5 74 4D 8E B1 49 DC 8E 7F C8 40 64 D8
 53 20 25 3E 57 A9 B6 B1 3D 0D 38 FE A8 EE 5E 0A
KB:
 A6 26 DE 01 B1 68 0F F7 51 30 09 12 2B CE E1 89
 68 83 39 4F 96 03 01 72 45 5C 9A E0 60 CC E4 4A
betta*P:
 X = 0x33BC6F7E9C0BA10CFB2B72546C327171295508EA97F8C8BA9F890F2478AB4D6C
 Y = 0x75D57B396C396F492F057E9222CCC686437A2AAD464E452EF426FC8EEED1A4A6
u 2:
 X = 0x089DDEE718EE8A224A7F37E22CFFD731C25FCBF58860364EE322412CDCEF99AC
 Y = 0x0ECE03D4E395A6354C571871BEF425A532D5D463B0F8FD427F91A43E20CDA55C
During processing a message u 2 and calculation the key on the subject A
the K_A key takes the following value:
K A:
 A6 26 DE 01 B1 68 0F F7 51 30 09 12 2B CE E1 89
 68 83 39 4F 96 03 01 72 45 5C 9A E0 60 CC E4 4A
The message MAC_A=HMAC (K_A, 0x01 || ID_A || ind || salt || u_1 || u_2)
from the subject A takes the following value:
```

```
MAC A:
 B9 1F 43 90 2A FA 90 D3 E5 C6 91 CB DC 43 8A 1E
 BF 54 7F 4C 2C B4 14 43 CC 38 79 7B E2 47 A7 D0
The message MAC_B=HMAC (K_B, 0x02 || ID_B || ind || salt || u_1 || u_2)
from the subject B takes the following value:
MAC B:
 79 D5 54 83 FD 99 B1 2B CC A5 ED C6 BB E1 D7 B9
 15 CE 04 51 B0 89 1E 77 5D 4A 61 CB 16 E3 3F CC
A.2.3 Curve id-GostR3410-2001-CryptoPro-C-ParamSet
The input protocol parameters in this example take the following values:
N = 1
ind = 1
ID A:
 00 00 00 00
ID B:
 00 00 00 00
PW:
 31 32 33 34 35 36 ('123456')
salt:
 29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB
Q ind:
 X = 0x1E36383E43BB6CFA2917167D71B7B5DD3D6D462B43D7C64282AE67DFBEC2559D
 Y = 0x137478A9F721C73932EA06B45CF72E37EB78A63F29A542E563C614650C8B6399
The function F (PW, salt, 2000) takes the following values:
F(PW,salt,2000):
 BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71
 D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67
The coordinates of the point Q PW are:
 X = 0x945821DAF91E158B839939630655A3B21FF3E146D27041E86C05650EB3B46B59
 Y = 0x3A0C2816AC97421FA0E879605F17F0C9C3EB734CFF196937F6284438D70BDC48
During the calculation of the message u 1 on the subject A the parameter
alpha, the point alpha*P and the message u_1 take the following values:
alpha=0x3A54AC3F19AD9D0B1EAC8ACDCEA70E581F1DAC33D13FEAFD81E762378639C1A8
alpha*P:
 X = 0x96B7F09C94D297C257A7DA48364C0076E59E48D221CBA604AE111CA3933B446A
 Y = 0x54E4953D86B77ECCEB578500931E822300F7E091F79592CA202A020D762C34A6
u 1:
 X = 0x81BBD6FCA464D2E2404A66D786CE4A777E739A89AEB68C2DAC99D53273B75387
 Y = 0x6B6DBD922EA7E060998F8B230AB6EF07AD2EC86B2BF66391D82A30612EADD411
During processing a message u 1, calculation the K B key and the message
u_2 on the subject B the parameters betta, src, K_B = HASH(src), betta*P
and u_2 take the following values:
betta=0x448781782BF7C0E52A1DD9E6758FD3482D90D3CFCCF42232CF357E59A4D49FD4
src:
 16 A1 2D 88 54 7E 1C 90 06 BA A0 08 E8 CB EC C9
 D1 68 91 ED C8 36 CF B7 5F 8E B9 56 FA 76 11 94
 D2 8E 25 DA D3 81 8D 16 3C 49 4B 05 9A 8C 70 A5
 A1 B8 8A 7F 80 A2 EE 35 49 30 18 46 54 2C 47 0B
KB:
 BE 7E 7E 47 B4 11 16 F2 C7 7E 3B 8F CE 40 30 72
 CA 82 45 0D 65 DE FC 71 A9 56 49 E4 DE EA EC EE
betta*P:
```

```
X = 0x4B9C0AB55A938121F282F48A2CC4396EB16E7E0068B495B0C1DD4667786A3EB7
 Y = 0x223460AA8E09383E9DF9844C5A0F2766484738E5B30128A171B69A77D9509B96
u 2:
 X = 0x2ED9B903254003A672E89EBEBC9E31503726AD124BB5FC0A726EE0E6FCCE323E
 Y = 0x4CF5E1042190120391EC8DB62FE25E9E26EC60FB0B78B242199839C295FCD022
During processing a message u 2 and calculation the key on the subject A
the K_A key takes the following value:
K A:
 BE 7E 7E 47 B4 11 16 F2 C7 7E 3B 8F CE 40 30 72
 CA 82 45 0D 65 DE FC 71 A9 56 49 E4 DE EA EC EE
The message MAC A=HMAC (K A, 0x01 || ID A || ind || salt || u 1 || u 2)
from the subject A takes the following value:
MAC A:
 D3 B4 1A E2 C9 43 11 36 06 3E 6D 08 A6 1B E9 63
 BD 5E D6 A1 FF F9 37 FA 8B 09 0A 98 E1 62 BF ED
The message MAC_B=HMAC (K_B, 0x02 || ID_B || ind || salt || u_1 || u_2)
from the subject B takes the following value:
MAC B:
 D6 B3 9A 44 99 BE D3 E0 4F AC F9 55 50 2D 16 B2
 CB 67 4A 20 5F AC 3C D8 3D 54 EC 2F D5 FC E2 58
A.2.4 Curve id-tc26-gost-3410-2012-512-paramSetA
The input protocol parameters in this example take the following values:
N = 1
ind = 1
ID A:
 00 00 00 00
ID B:
 00 00 00 00
PW:
 31 32 33 34 35 36 ('123456')
salt:
 29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB
Q ind:
 X = 0x2A17F8833A32795327478871B5C5E88AEFB91126C64B4B8327289BEA62559425
    D18198F133F400874328B220C74497CD240586CB249E158532CB8090776CD61C
 Y = 0x728F0C4A73B48DA41CE928358FAD26B47A6E094E9362BAE82559F83CDDC4EC3A
    4676BD3707EDEAF4CD85E99695C64C241EDC622BE87DC0CF87F51F4367F723C5
The function F (PW, salt, 2000) takes the following values:
F(PW,salt,2000):
 BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71
 D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67
 1C 62 13 E3 93 0E FD DA 26 45 17 92 C6 20 81 22
 EE 60 D2 00 52 0D 69 5D FD 9F 5F 0F D5 AB A7 02
The coordinates of the point Q PW are:
 X = 0x0C0AB53D0E0A9C607CAD758F558915A0A7DC5DC87B45E9A58FDDF30EC3385960
    283E030CD322D9E46B070637785FD49D2CD711F46807A24C40AF9A42C8E2D740
 Y = 0xDF93A8012B86D3A3D4F8A4D487DA15FC739EB31B20B3B0E8C8C032AAF8072C63
    37CF7D5B404719E5B4407C41D9A3216A08CA69C271484E9ED72B8AAA52E28B8B
During the calculation of the message u 1 on the subject A the parameter
alpha, the point alpha*P and the message u 1 take the following values:
alpha=0x3CE54325DB52FE798824AEAD11BB16FA766857D04A4AF7D468672F16D90E7396
```

046A46F815693E85B1CE5464DA9270181F82333B0715057BBE8D61D400505F0E

#### alpha\*P:

- X = 0xB93093EB0FCC463239B7DF276E09E592FCFC9B635504EA4531655D76A0A3078E 2B4E51CFE2FA400CC5DE9FBE369DB204B3E8ED7EDD85EE5CCA654C1AED70E396
- Y = 0x809770B8D910EA30BD2FA89736E91DC31815D2D9B31128077EEDC371E9F69466 F497DC64DD5B1FADC587F860EE256109138C4A9CD96B628E65A8F590520FC882

u 1:

- X = 0xE7510A9EDD37B869566C81052E2515E1563FDFE79F1D782D6200F33C3CC2764D40D0070B73AD5A47BAE9A8F2289C1B07DAC26A1A2FF9D3ECB0A8A94A4F179F13
- Y = 0xBA333B912570777B626A5337BC7F727952460EEBA2775707FE4537372E902DF5 636080B25399751BF48FB154F3C2319A91857C23F39F89EF54A8F043853F82DE

During processing a message u\_1, calculation the K\_B key and the message u\_2 on the subject B the parameters betta, src, K\_B = HASH(src), betta\*P and u\_2 take the following values:

betta=0xB5C286A79AA8E97EC0E19BC1959A1D15F12F8C97870BA9D68CC12811A56A3BB1 1440610825796A49D468CDC9C2D02D76598A27973D5960C5F50BCE28D8D345F4

src:

84 59 C2 0C B5 C5 32 41 6D B9 28 EB 50 C0 52 0F B2 1B 9C D3 9A 4E 76 06 B2 21 BE 15 CA 1D 02 DA 08 15 DE C4 49 79 C0 8C 7D 23 07 AF 24 7D DA 1F 89 EC 81 20 69 F5 D9 CD E3 06 AF F0 BC 3F D2 6E D2 01 B9 53 52 A2 56 06 B6 43 E8 88 30 2E FC 8D 3E 95 1E 3E B4 68 4A DB 5C 05 7B 8F 8C 89 B6 CC 0D EE D1 00 06 5B 51 8A 1C 71 7F 76 82 FF 61 2B BC 79 8E C7 B2 49 0F B7 00 3F 94 33 87 37 1C 1D K B:

53 24 DE F8 48 B6 63 CC 26 42 2F 5E 45 EE C3 4C 51 D2 43 61 B1 65 60 CA 58 A3 D3 28 45 86 CB 7A betta\*P:

- X = 0x238B38644E440452A99FA6B93D9FD7DA0CB83C32D3C1E3CFE5DF5C3EB0F9DB91 E588DAEDC849EA2FB867AE855A21B4077353C0794716A6480995113D8C20C7AF

u 2:

- X = 0xC33844126216E81B372001E77C1FE9C7547F9223CF7BB865C4472EC18BE0C79A 678CC5AE4028E3F3620CCE355514F1E589F8A0C433CEAFCBD2EE87884D953411
- Y = 0x8B520D083AAF257E8A54EC90CBADBAF4FEED2C2D868C82FF04FCBB9EF6F38E56 F6BAF9472D477414DA7E36F538ED223D2E2EE02FAE1A20A98C5A9FCF03B6F30D

During processing a message u\_2 and calculation the key on the subject A the K\_A key takes the following value:

#### K A:

53 24 DE F8 48 B6 63 CC 26 42 2F 5E 45 EE C3 4C 51 D2 43 61 B1 65 60 CA 58 A3 D3 28 45 86 CB 7A

The message MAC\_A=HMAC (K\_A, 0x01 || ID\_A || ind || salt || u\_1 || u\_2)

from the subject A takes the following value:

#### MAC A:

E8 EF 9E A8 F1 E6 B1 26 68 E5 8C D2 2D D8 EE C6

4A 16 71 00 39 FA A6 B6 03 99 22 20 FA FE 56 14

The message MAC\_B=HMAC (K\_B, 0x02  $\parallel$  ID\_B  $\parallel$  ind  $\parallel$  salt  $\parallel$  u\_1  $\parallel$  u\_2)

from the subject B takes the following value:

#### MAC B:

61 14 34 60 83 6B 23 5C EC D0 B4 9B 58 7E A4 5D

51 3C 3A 38 78 3F 1C 9D 3B 05 97 0A 95 6A 55 BA

```
A.2.5 Curve id-tc26-gost-3410-2012-512-paramSetB
The input protocol parameters in this example take the following values:
N = 1
ind = 1
ID A:
 00 00 00 00
ID B:
 00 00 00 00
PW:
 31 32 33 34 35 36 ('123456')
salt:
 29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB
Q ind:
 X = 0x7E1FAE8285E035BEC244BEF2D0E5EBF436633CF50E55231DEA9C9CF21D4C8C33
    DF85D4305DE92971F0A4B4C07E00D87BDBC720EB66E49079285AAF12E0171149
 Y = 0x2CC89998B875D4463805BA0D858A196592DB20AB161558FF2F4EF7A85725D209
    53967AE621AFDEAE89BB77C83A2528EF6FCE02F68BDA4679D7F2704947DBC408
The function F (PW, salt, 2000) takes the following values:
F(PW,salt,2000):
 BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71
 D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67
 1C 62 13 E3 93 0E FD DA 26 45 17 92 C6 20 81 22
 EE 60 D2 00 52 0D 69 5D FD 9F 5F 0F D5 AB A7 02
The coordinates of the point Q PW are:
 X = 0x7D03E65B8050D1E12CBB601A17B9273B0E728F5021CD47C8A4DD822E4627BA5F
    9C696286A2CDDA9A065509866B4DEDEDC4A118409604AD549F87A60AFA621161
 Y = 0x16037DAD45421EC50B00D50BDC6AC3B85348BC1D3A2F85DB27C3373580FEF87C
    2C743B7ED30F22BE22958044E716F93A61CA3213A361A2797A16A3AE62957377
During the calculation of the message u 1 on the subject A the parameter
alpha, the point alpha*P and the message u 1 take the following values:
alpha=0x715E893FA639BF341296E0623E6D29DADF26B163C278767A7982A989462A3863
    FE12AEF8BD403D59C4DC4720570D4163DB0805C7C10C4E818F9CB785B04B9997
alpha*P:
 X = 0x10C479EA1C04D3C2C02B0576A9C42D96226FF033C1191436777F66916030D87D
    02FB93738ED7669D07619FFCE7C1F3C4DB5E5DF49E2186D6FA1E2EB5767602B9
 Y = 0x039F6044191404E707F26D59D979136A831CCE43E1C5F0600D1DDF8F39D0CA3D
    52FBD943BF04DDCED1AA2CE8F5EBD7487ACDEF239C07D015084D796784F35436
u 1:
 X = 0x45C05CCE8290762F2470B719B4306D62B2911CEB144F7F72EF11D10498C7E921
    FF163FE72044B4E7332AD8CBEC3C12117820F53A60762315BCEB5BC6DA5CF1E0
 Y = 0x5BE483E382D0F5F0748C4F6A5045D99E62755B5ACC9554EC4A5B2093E121A2DD
    5C6066BC9EDE39373BA19899208BB419E38B39BBDEDEB0B09A5CAAEAA984D02E
During processing a message u_1, calculation the K_B key and the message
u_2 on the subject B the parameters betta, src, K_B = HASH(src), betta*P
and u 2 take the following values:
betta=0x30FA8C2B4146C2DBBE82BED04D7378877E8C06753BD0A0FF71EBF2BEFE8DA8F3
    DC0836468E2CE7C5C961281B6505140F8407413F03C2CB1D201EA1286CE30E6D
src:
 3F 04 02 E4 0A 9D 59 63 20 5B CD F4 FD 89 77 91
 9B BA F4 80 F8 E4 FB D1 25 5A EC E6 ED 57 26 4B
 D0 A2 87 98 4F 59 D1 02 04 B5 F4 5E 4D 77 F3 CF
 8A 63 B3 1B EB 2D F5 9F 8A F7 3C 20 9C CA 8B 50
 B4 18 D8 01 E4 90 AE 13 3F 04 F4 F3 F4 D8 FE 8E
```

```
19 64 6A 1B AF 44 D2 36 FC C2 1B 7F 4D 8F C6 A1
 E2 9D 6B 69 AC CE ED 4E 62 AB B2 0D AD 78 AC F4
 FE B0 ED 83 8E D9 1E 92 12 AB A3 89 71 4E 56 0C
K B:
 D5 90 E0 5E F5 AE CE 8B 7C FB FC 71 BE 45 5F 29
 A5 CC 66 6F 85 CD B1 7E 7C C7 16 C5 9F F1 70 E9
betta*P:
 X = 0x34C0149E7BB91AE377B02573FCC48AF7BFB7B16DEB8F9CE870F384688E3241A3
    A868588CC0EF4364CCA67D17E3260CD82485C202ADC76F895D5DF673B1788E67
 Y = 0x608E944929BD643569ED5189DB871453F13333A1EAF82B2FE1BE8100E775F13D
    D9925BD317B63BFAF05024D4A738852332B64501195C1B2EF789E34F23DDAFC5
u 2:
 X = 0x0535F95463444C4594B5A2E14B35760491C670925060B4BEBC97DE3A3076D1A5
    81F89026E04282B040925D9250201024ACA4B2713569B6C3916A6F3344B840AD
 Y = 0x40E6C2E55AEC31E7BCB6EA0242857FC6DFB5409803EDF4CA20141F72CC3C7988
    706E076765F4F004340E5294A7F8E53BA59CB67502F0044558C854A7D63FE900
During processing a message u 2 and calculation the key on the subject A
the K_A key takes the following value:
K A:
 D5 90 E0 5E F5 AE CE 8B 7C FB FC 71 BE 45 5F 29
 A5 CC 66 6F 85 CD B1 7E 7C C7 16 C5 9F F1 70 E9
The message MAC_A=HMAC (K_A, 0x01 || ID_A || ind || salt || u_1 || u_2)
from the subject A takes the following value:
MAC A:
 DE 46 BB 4C 8C E0 8A 6E F3 B8 DF AC CC 1A 39 B0
 8D 8C 27 B6 CB 0F CF 59 23 86 A6 48 F4 E5 BD 8C
The message MAC_B=HMAC (K_B, 0x02 || ID_B || ind || salt || u_1 || u_2)
from the subject B takes the following value:
MAC B:
 EC B1 1D E2 06 1C 55 F1 D1 14 59 CB 51 CE 31 40
 99 99 99 2F CA A1 22 2F B1 4F CE AB 96 EE 7A AC
A.2.6 Curve id-tc26-gost-3410-2012-256-paramSetA
The input protocol parameters in this example take the following values:
N = 1
ind = 1
ID A:
 00 00 00 00
ID B:
 00 00 00 00
PW:
 31 32 33 34 35 36 ('123456')
salt:
 29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB
Q ind:
 X = 0xB51ADF93A40AB15792164FAD3352F95B66369EB2A4EF5EFAE32829320363350E
 Y = 0x74A358CC08593612F5955D249C96AFB7E8B0BB6D8BD2BBE491046650D822BE18
The function F (PW, salt, 2000) takes the following values:
F(PW,salt,2000):
 BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71
 D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67
The coordinates of the point Q PW are:
```

X = 0xDBF99827078956812FA48C6E695DF589DEF1D18A2D4D35A96D75BF6854237629

```
Y = 0x9FDDD48BFBC57BEE1DA0CFF282884F284D471B388893C48F5ECB02FC18D67589
During the calculation of the message u 1 on the subject A the parameter
alpha, the point alpha*P and the message u_1 take the following values:
alpha=0x147B72F6684FB8FD1B418A899F7DBECAF5FCE60B13685BAA95328654A7F0707F
alpha*P:
 X = 0x33FBAC14EAE538275A769417829C431BD9FA622B6F02427EF55BD60EE6BC2888
 Y = 0x22F2EBCF960A82E6CDB4042D3DDDA511B2FBA925383C2273D952EA2D406EAE46
u 1:
 X = 0xE569AB544E3A13C41077DE97D659A1B7A13F61DDD808B633A5621FE2583A2C43
 Y = 0xA21A743A08F4D715661297ECD6F86553A808925BF34802BF7EC34C548A40B2C0
During processing a message u 1, calculation the K B key and the message
u_2 on the subject B the parameters betta, src, K_B = HASH(src), betta*P
and u 2 take the following values:
betta=0x30D5CFADAA0E31B405E6734C03EC4C5DF0F02F4BA25C9A3B320EE6453567B4CB
 A3 39 A0 B8 9C EF 1A 6F FD 4C A1 28 04 9E 06 84
 DF 4A 97 75 B6 89 A3 37 84 1B F7 D7 91 20 7F 35
 11 86 28 F7 28 8E AA 0F 7E C8 1D A2 0A 24 FF 1E
 69 93 C6 3D 9D D2 6A 90 B7 4D D1 A2 66 28 06 63
KB:
 7D F7 1A C3 27 ED 51 7D 0D E4 03 E8 17 C6 20 4B
 C1 91 65 B9 D1 00 2B 9F 10 88 A6 CD A6 EA CF 27
betta*P:
 X = 0x2B2D89FAB735433970564F2F28CFA1B57D640CB902BC6334A538F44155022CB2
 Y = 0x10EF6A82EEF1E70F942AA81D6B4CE5DEC0DDB9447512962874870E6F2849A96F
u 2:
 X = 0x190D2F283F7E861065DB53227D7FBDF429CEBF93791262CB29569BDF63C86CA4
 Y = 0xB3F1715721E9221897CCDE046C9B843A8386DBF7818A112F15A02BC820AC8F6D
During processing a message u 2 and calculation the key on the subject A
the K A key takes the following value:
K A:
 7D F7 1A C3 27 ED 51 7D 0D E4 03 E8 17 C6 20 4B
 C1 91 65 B9 D1 00 2B 9F 10 88 A6 CD A6 EA CF 27
The message MAC_A=HMAC (K_A, 0x01 || ID_A || ind || salt || u_1 || u_2)
from the subject A takes the following value:
MAC A:
 F9 29 B6 1A 3C 83 39 85 B8 29 F2 68 55 7F A8 11
 00 9F 82 0A B1 A7 30 B5 AA 33 4C 3E 6B A3 17 7F
The message MAC B=HMAC (K B, 0x02 || ID B || ind || salt || u 1 || u 2)
from the subject B takes the following value:
MAC B:
 A2 92 8A 5C F6 20 BB C4 90 0D E4 03 F7 FC 59 A5
 E9 80 B6 8B E0 46 D0 B5 D9 B4 AE 6A BF A8 0B D6
A.2.7 Curve id-tc26-gost-3410-2012-512-paramSetC
The input protocol parameters in this example take the following values:
N = 1
ind = 1
ID A:
 00 00 00 00
ID B:
 00 00 00 00
```

PW:

31 32 33 34 35 36 ('123456')

salt:

29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB

Q ind:

- X = 0x489C91784E02E98F19A803ABCA319917F37689E5A18965251CE2FF4E8D8B298F5A7470F9E0E713487F96F4A8397B3D09A270C9D367EB5E0E6561ADEEB51581D
- Y = 0x684EA885ACA64EAF1B3FEE36C0852A3BE3BD8011B0EF18E203FF87028D6EB5DB 2C144A0DCC71276542BFD72CA2A43FA4F4939DA66D9A60793C704A8C94E16F18

The function F (PW, salt, 2000) takes the following values:

F(PW,salt,2000):

BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71

D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67

1C 62 13 E3 93 0E FD DA 26 45 17 92 C6 20 81 22

EE 60 D2 00 52 0D 69 5D FD 9F 5F 0F D5 AB A7 02

The coordinates of the point Q PW are:

- X = 0x0185AE6271A81BB7F236A955F7CAA26FB63849813C0287D96C83A15AE6B6A864 67AB13B6D88CE8CD7DC2E5B97FF5F28FAC2C108F2A3CF3DB5515C9E6D7D210E8
- Y = 0xED0220F92EF771A71C64ECC77986DB7C03D37B3E2AB3E83F32CE5E074A762EC0 8253C9E2102B87532661275C4B1D16D2789CDABC58ACFDF7318DE70AB64F09B8

During the calculation of the message u\_1 on the subject A the parameter alpha, the point alpha\*P and the message u\_1 take the following values:

alpha=0x332F930421D14CFE260042159F18E49FD5A54167E94108AD80B1DE60B13DE799 9A34D611E63F3F870E5110247DF8EC7466E648ACF385E52CCB889ABF491EDFF0 alpha\*P:

- X = 0x561655966D52952E805574F4281F1ED3A2D498932B00CBA9DECB42837F09835BFFBFE2D84D6B6B242FE7B57F92E1A6F2413E12DDD6383E4437E13D72693469AD
- $\label{eq:Y} Y = 0xF6B18328B2715BD7F4178615273A36135BC0BF62F7D8BB9F080164AD36470AD0\\ 3660F51806C64C6691BADEF30F793720F8E3FEAED631D6A54A4C372DCBF80E82$

u 1:

src:

- X = 0x40645B4B9A908D74DEF98886A336F98BAE6ADA4C1AC9B7594A33D5E4A16486C5533C7F3C5DD84797AB5B4340BFC70CAF1011B69A01A715E5B9B5432D5151CBD7
- Y = 0x267FBB18D0B79559D1875909F2A15F7B49ECD8ED166CF7F4FCD1F448915504835E80D52BE8D34ADA5B5E159CF52979B1BCFE8F5048DC443A0983AA19192B8407

During processing a message u\_1, calculation the K\_B key and the message u\_2 on the subject B the parameters betta, src, K\_B = HASH(src), betta\*P and u\_2 take the following values:

betta=0x38481771E7D054F96212686B613881880BD8A6C89DDBC656178F014D2C093432 A033EE10415F13A160D44C2AD61E6E2E05A7F7EC286BCEA3EA4D4D53F8634FA2

4F 4D 64 B5 D0 70 08 E9 E6 85 87 4F 88 2C 3E 1E 60 A6 67 5E ED 42 1F C2 34 16 3F DE B4 4C 69 18 B7 BC CE AB 88 A0 F3 FB 78 8D A8 DB 10 18 51 FF 1A 41 68 22 BA 37 C3 53 CE C4 C5 A5 23 95 B7 72 AC 93 C0 54 E3 F4 05 5C ED 6F F0 BE E4 A6 A2 4E D6 8B 86 FE FA 70 DE 4A 2B 16 08 51 42 A4 DF F0 5D 32 EC 7D DF E3 04 F5 C7 04 FD FA 06 0F 64 E9 E8 32 14 00 25 F3 92 E5 03 50 77 0E 3F B6 2C AC

K\_B:

A0 83 84 A6 2F 4B E1 AE 48 98 FC A3 6D AA 3F AA 45 1B 3E C5 B5 9C E3 75 F8 9E 92 9F 4B 13 25 8C betta\*P:

X = 0xB7C5818687083433BC1AFF61CB5CA79E38232025E0C1F123B8651E62173CE6873F3E6FFE7281C2E45F4F524F66B0C263616ED08FD210AC4355CA3292B51D71C3

```
Y = 0x497F14205DBDC89BDDAF50520ED3B1429AD30777310186BE5E68070F016A44E0
    C766DB08E8AC23FBDFDE6D675AA4DF591EB18BA0D348DF7AA40973A2F1DCFA55
u 2:
 X = 0xB772FD97D6FDEC1DA0771BC059B3E5ADF9858311031EAE5AEC6A6EC8104B4105
    C45A6C65689A8EE636C687DB62CC0AFC9A48CA66E381286CC73F374C1DD8F445
 Y = 0xC64F69425FFEB2995130E85A08EDC3A686EC28EE6E8469F7F09BD3BCBDD843AC
    573578DA6BA1CB3F5F069F205233853F06255C4B28586C9A1643537497B1018C
During processing a message u 2 and calculation the key on the subject A
the K_A key takes the following value:
K A:
A0 83 84 A6 2F 4B E1 AE 48 98 FC A3 6D AA 3F AA
45 1B 3E C5 B5 9C E3 75 F8 9E 92 9F 4B 13 25 8C
The message MAC_A=HMAC (K_A, 0x01 || ID_A || ind || salt || u_1 || u_2)
from the subject A takes the following value:
MAC A:
12 63 F2 89 0E 90 EE 42 6B 9B A0 8A B9 EA 7F 1F
FF 26 E1 60 5C C6 5D E2 96 96 91 15 E5 31 76 87
The message MAC_B=HMAC (K_B, 0x02 || ID_B || ind || salt || u_1 || u_2)
from the subject B takes the following value:
MAC B:
 6D FD 06 04 5D 6D 97 A0 E4 19 B0 0E 00 35 B9 D2
 E3 AB 09 8B 7C A4 AD 52 54 60 FA B6 21 85 AA 57
```

## Appendix B. Point Verification Script

The points from the Appendix A.1 were generated with the following point verification script that is written in Python:

```
curvesParams = [
"OID": "id-GostR3410-2001-CryptoPro-A-ParamSet",
"m":0xFFFFFFFFFFFFFFFFFFFFFFFFFFF6C611070995AD10045841B09B761B893.
"q":0xFFFFFFFFFFFFFFFFFFFFFFFFFF6C611070995AD10045841B09B761B893,
"y":0x8D91E471E0989CDA27DF505A453F2B7635294F2DDF23E3B122ACC99C9E9F1E14,
"n":32
},
"OID": "id-GostR3410-2001-CryptoPro-B-ParamSet",
"b":0x3E1AF419A269A5F866A7D3C25C3DF80AE979259373FF2B182F49D4CE7E1BBC8B,
"m":0x8000000000000000000000000000000005F71A624E5E497161BCC8A198F,
"y":0x3FA8124359F96680B83D1C3EB2C070E5C545C9858D03ECFB744BF8D717717EFC,
"n":32
},
{
```

```
"OID": "id-GostR3410-2001-CryptoPro-C-ParamSet",
"p":0x9B9F605F5A858107AB1EC85E6B41C8AACF846E86789051D37998F7B9022D759B,
"a":0x9B9F605F5A858107AB1EC85E6B41C8AACF846E86789051D37998F7B9022D7598,
"b":32858,
"m":0x9B9F605F5A858107AB1EC85E6B41C8AA582CA3511EDDFB74F02F3A6598980BB9,
"q":0x9B9F605F5A858107AB1EC85E6B41C8AA582CA3511EDDFB74F02F3A6598980BB9,
"x":0,
"y":0x41ECE55743711A8C3CBF3783CD08C0EE4D4DC440D4641A8F366E550DFDB3BB67,
"n":32
},
"OID": "id-tc26-gost-3410-2012-512-paramSetA",
0xFFFFFFFFFFFFFDC7L,
0xFFFFFFFFFFFFFDC4L,
"b":(0xE8C2505DEDFC86DDC1BD0B2B6667F1DA34B82574761CB0E879BD08L<<<296)+\
 (0x1CFD0B6265EE3CB090F30D27614CB4574010DA90DD862EF9D4EBEEL<<80)+\
 0x4761503190785A71C760L,
(0xFFFFFFFF727E69532F48D89116FF22B8D4E0560609B4B38ABFAD2L<<80)+\
 0xB85DCACDB1411F10B275L,
(0xFFFFFFFF72E69532F48D89116FF22B8D4E0560609B4B38ABFAD2L<<80)+\
 0xB85DCACDB1411F10B275L,
"x":3,
"y":(0x7503CFE87A836AE3A61B8816E25450E6CE5E1C93ACF1ABC1778064L<<296)+\
 (0xFDCBEFA921DF1626BE4FD036E93D75E6A50E3A41E98028FE5FC235L<<80)+\
 0xF5B889A589CB5215F2A4L,
"n":64
},
"OID": "id-tc26-gost-3410-2012-512-paramSetB",
0x0000000000000000006FL,
0x0000000000000000006CL,
"b":(0x687D1B459DC841457E3E06CF6F5E2517B97C7D614AF138BCBF85DCL<<296)+\
 (0x806C4B289F3E965D2DB1416D217F8B276FAD1AB69C50F78BEE1FA3L<<80)+\
 0x106EFB8CCBC7C5140116L,
(0x00000000149A1EC142565A545ACFDB77BD9D40CFA8B996712101BL<<80)+\
 0xEA0EC6346C54374F25BDL,
(0x00000000149A1EC142565A545ACFDB77BD9D40CFA8B996712101BL<<80)+\
 0xEA0EC6346C54374F25BDL,
"x":2,
"y":(0x1A8F7EDA389B094C2C071E3647A8940F3C123B697578C213BE6DD9L<<296)+\
 (0xE6C8EC7335DCB228FD1EDF4A39152CBCAAF8C0398828041055F94CL<<80)+\
```

```
0xEEEC7E21340780FE41BDL,
"n":64
},
"OID":"id-tc26-gost-3410-2012-256-paramSetA",
"a":0xC2173F1513981673AF4892C23035A27CE25E2013BF95AA33B22C656F277E7335,
"b":0x295F9BAE7428ED9CCC20E7C359A9D41A22FCCD9108E17BF7BA9337A6F8AE9513,
"m":0x10000000000000000000000000000003F63377F21ED98D70456BD55B0D8319C,
"q":0x40000000000000000000000000000000FD8CDDFC87B6635C115AF556C360C67,
"x":0x91E38443A5E82C0D880923425712B2BB658B9196932E02C78B2582FE742DAA28.
"y":0x32879423AB1A0375895786C4BB46E9565FDE0B5344766740AF268ADB32322E5C,
"n":32
},
'OID':"id-tc26-gost-3410-2012-512-paramSetC",
0xFFFFFFFFFFFFFDC7L,
"a":(0xDC9203E514A721875485A529D2C722FB187BC8980EB866644DE41CL<<296)+\
 (0x68E143064546E861C0E2C9EDD92ADE71F46FCF50FF2AD97F951FDAL<<80)+\
 0x9F2A2EB6546F39689BD3L.
"b":(0xB4C4EE28CEBC6C2C8AC12952CF37F16AC7EFB6A9F69F4B57FFDA2EL<<296)+\
 (0x4F0DE5ADE038CBC2FFF719D2C18DE0284B8BFEF3B52B8CC7A5F5BFL<<80)+\
 0x0A3C8D2319A5312557E1L,
(0xFFFFFFFF26336E91941AAC0130CEA7FD451D40B323B6A79E9DA6L<<80)+\
 0x849A5188F3BD1FC08FB4L,
(0xFFFFFFFFC98CDBA46506AB004C33A9FF5147502CC8EDA9E7A769L<<80)+\
 0xA12694623CEF47F023EDL,
"x":(0xE2E31EDFC23DE7BDEBE241CE593EF5DE2295B7A9CBAEF021D385F7L<<296)+\
 (0x074CEA043AA27272A7AE602BF2A7B9033DB9ED3610C6FB85487EAEL<<80)+\
 0x97AAC5BC7928C1950148L,
"y":(0xF5CE40D95B5EB899ABBCCFF5911CB8577939804D6527378B8C108CL<<296)+\
 (0x3D2090FF9BE18E2D33E3021ED2EF32D85822423B6304F726AA854BL<<80)+\
 0xAE07D0396E9A9ADDC40FL,
"n":64
}
def str2list(s):
res = []
for c in s:
 res += [ ord( c ) ]
return res
def list2str( I ):
 r = ""
for k in I:
 r += chr(k)
 return r
```

```
def hprint( data ):
 for i in range( len( data ) ):
  r += "%02X " % data[ i ]
  if i % 16 == 15:
   r += "\n"
 print(r)
class Stribog:
 A = [
  0x8e20faa72ba0b470, 0x47107ddd9b505a38, 0xad08b0e0c3282d1c,
  0xd8045870ef14980e, 0x6c022c38f90a4c07, 0x3601161cf205268d,
  0x1b8e0b0e798c13c8, 0x83478b07b2468764, 0xa011d380818e8f40,
  0x5086e740ce47c920, 0x2843fd2067adea10, 0x14aff010bdd87508,
  0x0ad97808d06cb404, 0x05e23c0468365a02, 0x8c711e02341b2d01,
  0x46b60f011a83988e, 0x90dab52a387ae76f, 0x486dd4151c3dfdb9,
  0x24b86a840e90f0d2, 0x125c354207487869, 0x092e94218d243cba,
  0x8a174a9ec8121e5d, 0x4585254f64090fa0, 0xaccc9ca9328a8950,
  0x9d4df05d5f661451, 0xc0a878a0a1330aa6, 0x60543c50de970553,
  0x302a1e286fc58ca7, 0x18150f14b9ec46dd, 0x0c84890ad27623e0,
  0x0642ca05693b9f70, 0x0321658cba93c138, 0x86275df09ce8aaa8,
  0x439da0784e745554, 0xafc0503c273aa42a, 0xd960281e9d1d5215,
  0xe230140fc0802984, 0x71180a8960409a42, 0xb60c05ca30204d21,
  0x5b068c651810a89e, 0x456c34887a3805b9, 0xac361a443d1c8cd2,
  0x561b0d22900e4669, 0x2b838811480723ba, 0x9bcf4486248d9f5d,
  0xc3e9224312c8c1a0, 0xeffa11af0964ee50, 0xf97d86d98a327728,
  0xe4fa2054a80b329c, 0x727d102a548b194e, 0x39b008152acb8227,
  0x9258048415eb419d, 0x492c024284fbaec0, 0xaa16012142f35760,
  0x550b8e9e21f7a530, 0xa48b474f9ef5dc18, 0x70a6a56e2440598e,
  0x3853dc371220a247, 0x1ca76e95091051ad, 0x0edd37c48a08a6d8,
  0x07e095624504536c, 0x8d70c431ac02a736, 0xc83862965601dd1b,
  0x641c314b2b8ee083
 ]
 Sbox = [
  0xFC, 0xEE, 0xDD, 0x11, 0xCF, 0x6E, 0x31, 0x16, 0xFB, 0xC4, 0xFA,
  0xDA, 0x23, 0xC5, 0x04, 0x4D, 0xE9, 0x77, 0xF0, 0xDB, 0x93, 0x2E,
  0x99, 0xBA, 0x17, 0x36, 0xF1, 0xBB, 0x14, 0xCD, 0x5F, 0xC1, 0xF9,
  0x18, 0x65, 0x5A, 0xE2, 0x5C, 0xEF, 0x21, 0x81, 0x1C, 0x3C, 0x42,
  0x8B, 0x01, 0x8E, 0x4F, 0x05, 0x84, 0x02, 0xAE, 0xE3, 0x6A, 0x8F,
  0xA0, 0x06, 0x0B, 0xED, 0x98, 0x7F, 0xD4, 0xD3, 0x1F, 0xEB, 0x34,
  0x2C, 0x51, 0xEA, 0xC8, 0x48, 0xAB, 0xF2, 0x2A, 0x68, 0xA2, 0xFD,
  0x3A, 0xCE, 0xCC, 0xB5, 0x70, 0x0E, 0x56, 0x08, 0x0C, 0x76, 0x12,
  0xBF, 0x72, 0x13, 0x47, 0x9C, 0xB7, 0x5D, 0x87, 0x15, 0xA1, 0x96,
  0x29, 0x10, 0x7B, 0x9A, 0xC7, 0xF3, 0x91, 0x78, 0x6F, 0x9D, 0x9E,
  0xB2, 0xB1, 0x32, 0x75, 0x19, 0x3D, 0xFF, 0x35, 0x8A, 0x7E, 0x6D,
  0x54, 0xC6, 0x80, 0xC3, 0xBD, 0x0D, 0x57, 0xDF, 0xF5, 0x24, 0xA9,
  0x3E, 0xA8, 0x43, 0xC9, 0xD7, 0x79, 0xD6, 0xF6, 0x7C, 0x22, 0xB9,
  0x03, 0xE0, 0x0F, 0xEC, 0xDE, 0x7A, 0x94, 0xB0, 0xBC, 0xDC, 0xE8,
  0x28, 0x50, 0x4E, 0x33, 0x0A, 0x4A, 0xA7, 0x97, 0x60, 0x73, 0x1E,
  0x00, 0x62, 0x44, 0x1A, 0xB8, 0x38, 0x82, 0x64, 0x9F, 0x26, 0x41,
  0xAD, 0x45, 0x46, 0x92, 0x27, 0x5E, 0x55, 0x2F, 0x8C, 0xA3, 0xA5,
```

```
0x7D, 0x69, 0xD5, 0x95, 0x3B, 0x07, 0x58, 0xB3, 0x40, 0x86, 0xAC,
 0x1D, 0xF7, 0x30, 0x37, 0x6B, 0xE4, 0x88, 0xD9, 0xE7, 0x89, 0xE1,
 0x1B, 0x83, 0x49, 0x4C, 0x3F, 0xF8, 0xFE, 0x8D, 0x53, 0xAA, 0x90,
 0xCA, 0xD8, 0x85, 0x61, 0x20, 0x71, 0x67, 0xA4, 0x2D, 0x2B, 0x09,
 0x5B, 0xCB, 0x9B, 0x25, 0xD0, 0xBE, 0xE5, 0x6C, 0x52, 0x59, 0xA6,
 0x74, 0xD2, 0xE6, 0xF4, 0xB4, 0xC0, 0xD1, 0x66, 0xAF, 0xC2, 0x39,
 0x4B, 0x63, 0xB6
1
Tau = [
 0, 8, 16, 24, 32, 40, 48, 56,
 1, 9, 17, 25, 33, 41, 49, 57,
 2, 10, 18, 26, 34, 42, 50, 58,
 3, 11, 19, 27, 35, 43, 51, 59,
 4, 12, 20, 28, 36, 44, 52, 60,
 5, 13, 21, 29, 37, 45, 53, 61,
 6, 14, 22, 30, 38, 46, 54, 62,
 7, 15, 23, 31, 39, 47, 55, 63
1
__C = [
  0xb1, 0x08, 0x5b, 0xda, 0x1e, 0xca, 0xda, 0xe9,
  0xeb, 0xcb, 0x2f, 0x81, 0xc0, 0x65, 0x7c, 0x1f,
  0x2f, 0x6a, 0x76, 0x43, 0x2e, 0x45, 0xd0, 0x16,
  0x71, 0x4e, 0xb8, 0x8d, 0x75, 0x85, 0xc4, 0xfc,
  0x4b, 0x7c, 0xe0, 0x91, 0x92, 0x67, 0x69, 0x01,
  0xa2, 0x42, 0x2a, 0x08, 0xa4, 0x60, 0xd3, 0x15,
  0x05, 0x76, 0x74, 0x36, 0xcc, 0x74, 0x4d, 0x23,
  0xdd, 0x80, 0x65, 0x59, 0xf2, 0xa6, 0x45, 0x07
 ],
  0x6f, 0xa3, 0xb5, 0x8a, 0xa9, 0x9d, 0x2f, 0x1a,
  0x4f, 0xe3, 0x9d, 0x46, 0x0f, 0x70, 0xb5, 0xd7,
  0xf3, 0xfe, 0xea, 0x72, 0x0a, 0x23, 0x2b, 0x98,
  0x61, 0xd5, 0x5e, 0x0f, 0x16, 0xb5, 0x01, 0x31,
  0x9a, 0xb5, 0x17, 0x6b, 0x12, 0xd6, 0x99, 0x58,
  0x5c, 0xb5, 0x61, 0xc2, 0xdb, 0x0a, 0xa7, 0xca,
  0x55, 0xdd, 0xa2, 0x1b, 0xd7, 0xcb, 0xcd, 0x56,
  0xe6, 0x79, 0x04, 0x70, 0x21, 0xb1, 0x9b, 0xb7
 ],
  0xf5, 0x74, 0xdc, 0xac, 0x2b, 0xce, 0x2f, 0xc7,
  0x0a, 0x39, 0xfc, 0x28, 0x6a, 0x3d, 0x84, 0x35,
  0x06, 0xf1, 0x5e, 0x5f, 0x52, 0x9c, 0x1f, 0x8b,
  0xf2, 0xea, 0x75, 0x14, 0xb1, 0x29, 0x7b, 0x7b,
  0xd3, 0xe2, 0x0f, 0xe4, 0x90, 0x35, 0x9e, 0xb1,
  0xc1, 0xc9, 0x3a, 0x37, 0x60, 0x62, 0xdb, 0x09,
  0xc2, 0xb6, 0xf4, 0x43, 0x86, 0x7a, 0xdb, 0x31,
  0x99, 0x1e, 0x96, 0xf5, 0x0a, 0xba, 0x0a, 0xb2
 ],
  0xef, 0x1f, 0xdf, 0xb3, 0xe8, 0x15, 0x66, 0xd2,
```

```
0xf9, 0x48, 0xe1, 0xa0, 0x5d, 0x71, 0xe4, 0xdd,
 0x48, 0x8e, 0x85, 0x7e, 0x33, 0x5c, 0x3c, 0x7d,
 0x9d, 0x72, 0x1c, 0xad, 0x68, 0x5e, 0x35, 0x3f,
 0xa9, 0xd7, 0x2c, 0x82, 0xed, 0x03, 0xd6, 0x75,
 0xd8, 0xb7, 0x13, 0x33, 0x93, 0x52, 0x03, 0xbe,
 0x34, 0x53, 0xea, 0xa1, 0x93, 0xe8, 0x37, 0xf1,
 0x22, 0x0c, 0xbe, 0xbc, 0x84, 0xe3, 0xd1, 0x2e
],
 0x4b, 0xea, 0x6b, 0xac, 0xad, 0x47, 0x47, 0x99,
 0x9a, 0x3f, 0x41, 0x0c, 0x6c, 0xa9, 0x23, 0x63,
 0x7f, 0x15, 0x1c, 0x1f, 0x16, 0x86, 0x10, 0x4a,
 0x35, 0x9e, 0x35, 0xd7, 0x80, 0x0f, 0xff, 0xbd,
 0xbf, 0xcd, 0x17, 0x47, 0x25, 0x3a, 0xf5, 0xa3,
 0xdf, 0xff, 0x00, 0xb7, 0x23, 0x27, 0x1a, 0x16,
 0x7a, 0x56, 0xa2, 0x7e, 0xa9, 0xea, 0x63, 0xf5,
 0x60, 0x17, 0x58, 0xfd, 0x7c, 0x6c, 0xfe, 0x57
 0xae, 0x4f, 0xae, 0xae, 0x1d, 0x3a, 0xd3, 0xd9,
 0x6f, 0xa4, 0xc3, 0x3b, 0x7a, 0x30, 0x39, 0xc0,
 0x2d, 0x66, 0xc4, 0xf9, 0x51, 0x42, 0xa4, 0x6c,
 0x18, 0x7f, 0x9a, 0xb4, 0x9a, 0xf0, 0x8e, 0xc6,
 0xcf, 0xfa, 0xa6, 0xb7, 0x1c, 0x9a, 0xb7, 0xb4,
 0x0a, 0xf2, 0x1f, 0x66, 0xc2, 0xbe, 0xc6, 0xb6,
 0xbf, 0x71, 0xc5, 0x72, 0x36, 0x90, 0x4f, 0x35,
 0xfa, 0x68, 0x40, 0x7a, 0x46, 0x64, 0x7d, 0x6e
],
 0xf4, 0xc7, 0x0e, 0x16, 0xee, 0xaa, 0xc5, 0xec,
 0x51, 0xac, 0x86, 0xfe, 0xbf, 0x24, 0x09, 0x54,
 0x39, 0x9e, 0xc6, 0xc7, 0xe6, 0xbf, 0x87, 0xc9,
 0xd3, 0x47, 0x3e, 0x33, 0x19, 0x7a, 0x93, 0xc9,
 0x09, 0x92, 0xab, 0xc5, 0x2d, 0x82, 0x2c, 0x37,
 0x06, 0x47, 0x69, 0x83, 0x28, 0x4a, 0x05, 0x04,
 0x35, 0x17, 0x45, 0x4c, 0xa2, 0x3c, 0x4a, 0xf3,
 0x88, 0x86, 0x56, 0x4d, 0x3a, 0x14, 0xd4, 0x93
],
 0x9b, 0x1f, 0x5b, 0x42, 0x4d, 0x93, 0xc9, 0xa7,
 0x03, 0xe7, 0xaa, 0x02, 0x0c, 0x6e, 0x41, 0x41,
 0x4e, 0xb7, 0xf8, 0x71, 0x9c, 0x36, 0xde, 0x1e,
 0x89, 0xb4, 0x44, 0x3b, 0x4d, 0xdb, 0xc4, 0x9a,
 0xf4, 0x89, 0x2b, 0xcb, 0x92, 0x9b, 0x06, 0x90,
 0x69, 0xd1, 0x8d, 0x2b, 0xd1, 0xa5, 0xc4, 0x2f,
 0x36, 0xac, 0xc2, 0x35, 0x59, 0x51, 0xa8, 0xd9,
 0xa4, 0x7f, 0x0d, 0xd4, 0xbf, 0x02, 0xe7, 0x1e
],
 0x37, 0x8f, 0x5a, 0x54, 0x16, 0x31, 0x22, 0x9b,
 0x94, 0x4c, 0x9a, 0xd8, 0xec, 0x16, 0x5f, 0xde,
 0x3a, 0x7d, 0x3a, 0x1b, 0x25, 0x89, 0x42, 0x24,
 0x3c, 0xd9, 0x55, 0xb7, 0xe0, 0x0d, 0x09, 0x84,
```

```
0x80, 0x0a, 0x44, 0x0b, 0xdb, 0xb2, 0xce, 0xb1,
   0x7b, 0x2b, 0x8a, 0x9a, 0xa6, 0x07, 0x9c, 0x54,
   0x0e, 0x38, 0xdc, 0x92, 0xcb, 0x1f, 0x2a, 0x60,
   0x72, 0x61, 0x44, 0x51, 0x83, 0x23, 0x5a, 0xdb
 ],
   0xab, 0xbe, 0xde, 0xa6, 0x80, 0x05, 0x6f, 0x52,
   0x38, 0x2a, 0xe5, 0x48, 0xb2, 0xe4, 0xf3, 0xf3,
   0x89, 0x41, 0xe7, 0x1c, 0xff, 0x8a, 0x78, 0xdb,
   0x1f, 0xff, 0xe1, 0x8a, 0x1b, 0x33, 0x61, 0x03,
   0x9f, 0xe7, 0x67, 0x02, 0xaf, 0x69, 0x33, 0x4b,
   0x7a, 0x1e, 0x6c, 0x30, 0x3b, 0x76, 0x52, 0xf4,
   0x36, 0x98, 0xfa, 0xd1, 0x15, 0x3b, 0xb6, 0xc3,
   0x74, 0xb4, 0xc7, 0xfb, 0x98, 0x45, 0x9c, 0xed
 ],
 [
   0x7b, 0xcd, 0x9e, 0xd0, 0xef, 0xc8, 0x89, 0xfb,
   0x30, 0x02, 0xc6, 0xcd, 0x63, 0x5a, 0xfe, 0x94,
   0xd8, 0xfa, 0x6b, 0xbb, 0xeb, 0xab, 0x07, 0x61,
   0x20, 0x01, 0x80, 0x21, 0x14, 0x84, 0x66, 0x79,
   0x8a, 0x1d, 0x71, 0xef, 0xea, 0x48, 0xb9, 0xca,
   0xef, 0xba, 0xcd, 0x1d, 0x7d, 0x47, 0x6e, 0x98,
   0xde, 0xa2, 0x59, 0x4a, 0xc0, 0x6f, 0xd8, 0x5d,
   0x6b, 0xca, 0xa4, 0xcd, 0x81, 0xf3, 0x2d, 0x1b
 ],
   0x37, 0x8e, 0xe7, 0x67, 0xf1, 0x16, 0x31, 0xba,
   0xd2, 0x13, 0x80, 0xb0, 0x04, 0x49, 0xb1, 0x7a,
   0xcd, 0xa4, 0x3c, 0x32, 0xbc, 0xdf, 0x1d, 0x77,
   0xf8, 0x20, 0x12, 0xd4, 0x30, 0x21, 0x9f, 0x9b,
   0x5d, 0x80, 0xef, 0x9d, 0x18, 0x91, 0xcc, 0x86,
   0xe7, 0x1d, 0xa4, 0xaa, 0x88, 0xe1, 0x28, 0x52,
   0xfa, 0xf4, 0x17, 0xd5, 0xd9, 0xb2, 0x1b, 0x99,
   0x48, 0xbc, 0x92, 0x4a, 0xf1, 0x1b, 0xd7, 0x20
 ]
]
def __AddModulo(self, A, B):
 result = [0] * 64
 t = 0
 for i in reversed(range(0, 64)):
  t = A[i] + B[i] + (t >> 8)
  result[i] = t & 0xFF
 return result
def __AddXor(self, A, B):
 result = [0] * 64
 for i in range(0, 64):
   result[i] = A[i] ^ B[i]
 return result
def __S(self, state):
 result = [0] * 64
```

```
for i in range(0, 64):
   result[i] = self.__Sbox[state[i]]
 return result
def __P(self, state):
 result = [0] * 64
 for i in range(0, 64):
  result[i] = state[self.__Tau[i]]
 return result
def __L(self, state):
 result = [0] * 64
 for i in range(0, 8):
  t = 0
  for k in range(0, 8):
    for j in range(0, 8):
     if ((state[i * 8 + k] & (1 << (7 - j)))! = 0):
       t \sim self._A[k * 8 + j]
  for k in range(0, 8):
    result[i * 8 + k] = (t & (0xFF << (7 - k) * 8)) >> (7 - k) * 8
 return result
def __KeySchedule(self, K, i):
 K = self.__AddXor(K, self.__C[i])
 K = self. S(K)
 K = self._P(K)
 K = self.\__L(K)
 return K
# E(K, m)
def __E(self, K, m):
 state = self.__AddXor(K, m)
 for i in range(0, 12):
  state = self.__S(state)
  state = self.__P(state)
  state = self.__L(state)
  K = self.__KeySchedule(K, i)
  state = self.__AddXor(state, K)
 return state
def __G_n(self, N, h, m):
 K = self.\_AddXor(h, N)
 K = self._S(K)
 K = self. P(K)
 K = self.\__L(K)
 t = self.\__E(K, m)
 t = self._AddXor(t, h)
 return self.__AddXor(t, m)
def __Padding(self, last, N, h, Sigma):
 if (len(last) < 64):
  padding = [0] * (64 - len(last))
```

```
padding[-1] = 1
  padded_message = padding + last
 h = self.__G_n(N, h, padded_message)
 N_{len} = [0] * 64
 N_{en}[63] = (len(last) * 8) & 0xff
 N len[62] = (len(last) * 8) >> 8
 N = self.\_AddModulo(N, N_len)
 Sigma = self.__AddModulo(Sigma, padded_message)
 return (h, N, Sigma)
def digest( self, message, out=512 ):
 return list2str( self.GetHash( str2list( message ), out ) )
def GetHash(self, message, out=512, no_pad=False):
 N = [0] * 64
 Sigma = [0] * 64
 if out == 512:
  h = [0] * 64
 elif out == 256:
  h = [0x01] * 64
  print("Wrong hash out length!")
 N_512 = [0] * 64
 N 512[62] = 0x02 # 512 = 0x200
 length_bits = len(message) * 8
 length = len(message)
 i = 0
 asd = message[::-1]
 while (length_bits >= 512):
  tmp = (message[i * 64: (i + 1) * 64])[::-1]
  h = self. \underline{G}_n(N, h, tmp)
  N = self.\_AddModulo(N, N_512)
  Sigma = self.__AddModulo(Sigma, tmp)
  length_bits -= 512
  i += 1
 last = (message[i * 64: length])[::-1]
 if (len(last) == 0 and no_pad):
  pass
  h, N, Sigma = self.__Padding(last, N, h, Sigma)
 N_0 = [0] * 64
 h = self. \underline{G}_n(N_0, h, N)
 h = self. \underline{G}_n(N_0, h, Sigma)
 if out == 512:
```

```
return h[::-1]
  elif out == 256:
    return (h[0:32])[::-1]
 def hash(self, str_message, out=512, no_pad=False):
  return list2str(self.GetHash(str2list(str_message), out, no_pad))
def H256(msg):
 S = Stribog()
 return S.hash(msg, out=256)
def H512(msg):
 S = Stribog()
 return S.hash(msg)
def num2le(s, n):
 res = ""
 for i in range(n):
  res += chr(s & 0xFF)
  s >> = 8
 return res
def le2num(s):
 res = 0
 for i in range(len(s) - 1, -1, -1):
  res = (res << 8) + ord(s[i])
 return res
def XGCD(a,b):
 """XGCD(a,b) returns a list of form [g,x,y], where g is GCD(a,b) and
 x,y satisfy the equation g = ax + by."""
 a1=1; b1=0; a2=0; b2=1; aneg=1; bneg=1; swap = False
 if (a < 0):
  a = -a; aneg=-1
 if(b < 0):
  b = -b; bneg=-1
 if(b > a):
  swap = True
  [a,b] = [b,a]
 while (1):
  quot = -(a / b)
  a = a \% b
  a1 = a1 + quot*a2; b1 = b1 + quot*b2
  if(a == 0):
   if(swap):
     return [b, b2*bneg, a2*aneg]
     return [b, a2*aneg, b2*bneg]
  quot = -(b / a)
  b = b \% a
  a2 = a2 + quot*a1; b2 = b2 + quot*b1
  if(b == 0):
   if(swap):
```

```
return [a, b1*bneg, a1*aneg]
    else:
     return [a, a1*aneg, b1*bneg]
def getMultByMask( elems, mask ):
 n = len( elems )
 r = 1
 for i in range( n ):
  if mask & 1:
    r *= elems[ n - 1 - i ]
  mask = mask >> 1
 return r
def subF(P, other, p):
 return (P - other) % p
def divF(P, other, p):
 return mulF(P, invF(other, p), p)
def addF(P, other, p):
 return (P + other) % p
def mulF(P, other, p):
 return (P * other) % p
def invF(R, p):
 assert (R != 0)
 return XGCD(R, p)[1] % p
def negF(R, p):
 return (-R) % p
def powF(R, m, p):
 assert R != None
 assert type(m) in (int, long)
 if m == 0:
  assert R != 0
  return 1
 elif m < 0:
  t = invF(R, p)
  return powF(t, (-m), p)
 else:
  i = m.bit_length() - 1
  r = 1
  while i > 0:
    if (m >> i) & 1:
     r = (r * R) % p
```

```
r = (r * r) % p
   i -= 1
  if m & 1:
    r = (r * R) % p
  return r
def add(Px, Py, Qx, Qy, p, a, b):
 if Qx == Qy == None:
  return [Px, Py]
 if Px == Py == None:
  return [Qx, Qy]
 if (Px == Qx) and (Py == negF(Qy, p)):
  return [None, None]
 if (Px == Qx) and (Py == Qy):
  assert Py != 0
  return duplicate(Px, Py, p, a)
 else:
  I = divF(subF(Qy, Py, p), subF(Qx, Px, p), p)
  resX = subF(subF(powF(1, 2, p), Px, p), Qx, p)
  resY = subF( mulF( I, subF( Px, resX, p ), p ), Py, p )
  return [resX, resY]
def duplicate(Px, Py, p, a):
 if (Px == None) and (Py == None):
  return [None, None]
 if Py == 0:
  return [None, None]
 I = divF(addF(mulF(powF(Px, 2, p), 3, p), a, p), mulF(Py, 2, p), p)
 resX = subF(powF(I, 2, p), mulF(Px, 2, p), p)
 resY = subF(mulF(I, subF(Px, resX, p), p), Py, p)
 return [resX, resY]
def mul(Px, Py, s, p, a, b):
 assert type(s) in (int, long)
 assert Px != None and Py != None
 X = Px
 Y = Py
 i = s.bit length() - 1
 resX = None
 resY = None
 while i > 0:
  if (s >> i) & 1:
   resX, resY = add(resX, resY, X, Y, p, a, b)
  resX, resY = duplicate(resX, resY, p, a)
  i -= 1
 if s & 1:
```

```
resX, resY = add(resX, resY, X, Y, p, a, b)
 return [resX, resY]
def Ord(Px, Py, m, q, p, a, b):
 assert Px != None and Py != None
 assert (m != None) and (q != None)
 assert mul(Px, Py, m, p, a, b) == [None, None]
 X = Px
 Y = Py
 r = m
 for mask in range(1 << len(q)):
  t = getMultByMask(q, mask)
  Rx, Ry = mul(X, Y, t, p, a, b)
  if (Rx == None) and (Ry == None):
    r = min(r, t)
 return r
def isQuadraticResidue(R, p):
 if R == 0:
  assert False
 temp = powF(R, ((p - 1) / 2), p)
 if temp == (p - 1):
  return False
 else:
  assert temp == 1
  return True
def getRandomQuadraticNonresidue(p):
 from random import randint
 r = (randint(2, p - 1)) \% p
 while isQuadraticResidue(r, p):
  r = (randint(2, p - 1)) \% p
 return r
def ModSqrt(R, p):
 assert R != None
 assert isQuadraticResidue(R, p)
 if p % 4 == 3:
  res = powF(R, (p + 1) / 4, p)
  if powF(res, 2, p) != R:
    res = None
  return [res, negF(res, p)]
 else:
  ainvF = invF(R, p)
  s = p - 1
  alpha = 0
  while (s % 2) == 0:
    alpha += 1
    s = s / 2
```

```
b = powF(getRandomQuadraticNonresidue(p), s, p)
  r = powF(R, (s + 1) / 2, p)
  bi = 1
  for k in range(0, alpha - 1): # alpha >= 2 because p % 4 = 1
   d = 2 ** (alpha - k - 2)
   x = powF(mulF(powF(mulF(bj, r, p), 2, p), ainvF, p), d, p)
   if x != 1:
     bj = mulF(bj, powF(b, (2 ** k), p), p)
  res = mulF(bj, r, p)
  return [res, negF(res, p)]
def generateQs(p, pByteSize, a, b, m, q, orderDivisors, Px, Py, N):
 assert pByteSize in (256 / 8, 512 / 8)
 PxBytes = num2le( Px, pByteSize )
 PyBytes = num2le( Py, pByteSize )
 Qs = []
 S = []
 Hash_src = []
 Hash res = []
 co_factor = m / q
 seed = 0
 while len( Qs ) != N:
  hashSrc = PxBytes + PyBytes + num2le( seed, 4 )
  if pByteSize == (256/8):
   QxBytes = H256( hashSrc )
  else:
   QxBytes = H512( hashSrc )
  Qx = le2num(QxBytes) % p
  R = addF(addF(powF(Qx, 3, p), mulF(Qx, a, p), p), b, p)
  if (R == 0) or (not isQuadraticResidue(R, p)):
   seed += 1
   continue
  Qy_sqrt = ModSqrt(R, p)
  Qy = min(Qy_sqrt)
  if co_factor * Ord(Qx, Qy, m, orderDivisors, p, a, b) != m:
   seed += 1
   continue
  Qs += [(Qx, Qy)]
  S += [seed]
  Hash_src += [hashSrc]
  Hash_res += [QxBytes]
  seed += 1
 return Qs, S, Hash_src, Hash_res
if __name__ == "__main__":
 for i, curve in enumerate(curvesParams):
```

```
print "A.1." + str(i+1) + ". Curve " + curve["OID"]
if "3410-2012-256-paramSetA" in curve["OID"] or \
     "3410-2012-512-paramSetC" in curve["OID"]:
 Q, S, Hash_src, Hash_res = generateQs(curve["p"],\
                  curve["n"],\
                  curve["a"],\
                  curve["b"],\
                  curve["m"],\
                  curve["q"],\
                  [ 2, 2, curve["q"]],\
                  curve["x"],\
                  curve["y"],\
                  1)
else:
 Q, S, Hash_src, Hash_res = generateQs(curve["p"],\
                  curve["n"],\
                  curve["a"],\
                  curve["b"],\
                  curve["m"],\
                  curve["q"],\
                  [curve["q"]],\
                  curve["x"],\
                  curve["y"],\
                  1)
for q, s, hash_src, hash_res in zip(Q, S, Hash_src, Hash_res):
 print "Point Q_" + str(j)
 j += 1
 print "X=", hex(q[0])[:-1]
 print "Y=", hex(q[1])[:-1]
 print "SEED=","{0:#0{1}x}".format(s,6)
 print
```

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