

# Day-1

### 1) Finding Majority Element in an Array

$$> \frac{n}{2} + 1$$

element

freq

$$n=9$$

3

2



5

✓ Input : {3, 3, 4, 2, 4, 4, 2, 4, 4}



Output : 4

Explanation: The frequency of 4 is 5 which is greater than the half of the size of the array size.

2

2

Input : {3, 3, 4, 2, 4, 4, 2, 4}

Output : No Majority Element

Explanation: There is no element whose frequency is greater than the half of the size of the array size.

$$\underline{n=9} \rightarrow \frac{9}{2}=4$$

Brute-Force

0	1	2	3	4	5	6	7	8
3	3	4	2	4	4	2	4	4

↳ 5

max\_Count = 5

index = 0 2

Count = 0

(max\_Count) >  $\frac{n}{2}$  → arr[Index]

not > → maj not found

```

function findMajority(arr[], n)
{
    ✓maxCount = 0;
    ✓index = -1;
    ↳ for (i = 0; i < n; i++) {
        count = 0;
        ↳ for (j = 0; j < n; j++) {
            if (arr[i] == arr[j])
                count++;
        }

        // update maxCount if count of
        // current element is greater
        if (count > maxCount) {
            maxCount = count; ✓
            index = i; ↳
        }
    }

    ↳
    // if maxCount is greater than n/2
    // return the corresponding element
    if (maxCount > n / 2)
        print(arr[index]);
    else
        print("No Majority Element");
}

```



TC :  $O(n^2)$

SC :  $O(1)$

$\rightarrow O(n \log n)$  T.C

$\rightarrow O(n) / O(1)$  S.C

Sorting Approach

0	1	2	3	4	5	6	7	8
3	3	4	2	4	4	2	4	4

more than  
1 may ele  $\rightarrow ?$

0	1	2	3	4	5	6	7	8
?	?	3	3	4	4	4	4	4

$x$      $x$      $x$      $x$      $i$      $\underbrace{~~~~~}_{\ast}$

(sorted)

$$n = 9 \rightarrow \frac{n}{2} = 4$$

let

Merge-Sort  $\Rightarrow$   $n \log n$

```

for i=0; i <= n/2; i++)
{
    if arr[i] == arr[i+n/2]
        return arr[i]
}
return -1

```

$\rightarrow O(n)$  T.C  
 $\rightarrow O(n)$  S.C

HashMap

$\hookrightarrow$  Key + value pair

arr

i	i	i	i	i	i	i	i	i
0	1	2	3	4	5	6	7	8
3	3	4	2	4	4	2	4	4

hm

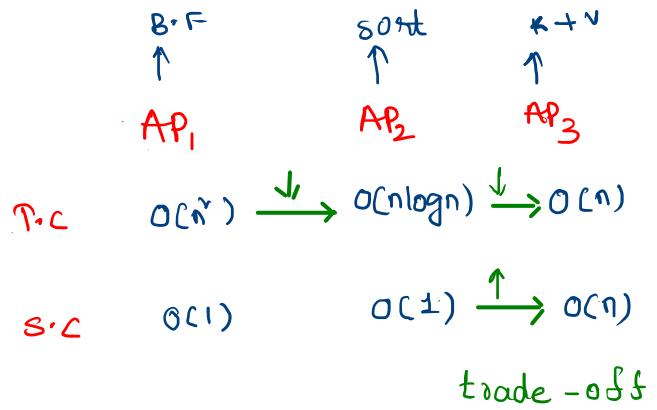
key	value
3	42
4	42
2	42

s.c  $\rightarrow$  worst case

$\hookrightarrow$  All elements can be distinct

$$\text{temp} = 5 \rightarrow > \frac{n}{2}$$

$$\text{key} = 4$$



Best  
 AP<sub>4</sub>  
 $O(1)$   
 $O(n)$   
 $O(\log n)$   
 ↳ some Algo

$n \rightarrow n$   
 ↳ May  
 $\downarrow$   
 $O(n)$   
 $\downarrow$   
 $O(\log n)$

Technique/Ideal  
 strategy

- ① Brute force ✓
- ② sorting ✓
- ③ Key + Value ✓

Moore-Voting Algo

0	1	2	3	4	5	6	7	8
3	3	4	2	4	4	2	4	4

start

Key = 2, Count = 0

1  
2  
↓

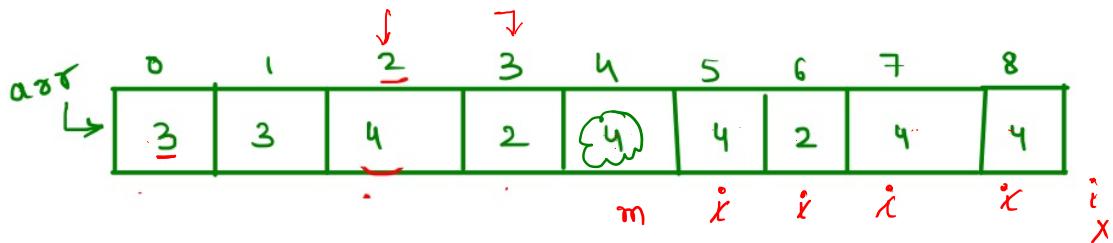
Contains 2 steps

\* ① : return some element as maj element.

✓ ② : It is our respo. to check, that element as Maj or not.

## Moore's Voting Algorithm

```
int findCandidate(int a[], int size)
{
    int maj_index = 0, count = 1;
    int i;
    for (i = 1; i < size; i++)
    {
        if (a[maj_index] == a[i])
            count++;
        else
            count--;
        if (count == 0)
        {
            maj_index = i;
            count = 1;
        }
    }
    return a[maj_index];
}
```



$$\text{maj\_index} = \underline{\underline{84}}$$

$$\text{count} = 1 \otimes 1 \otimes 1 \otimes 1 \otimes 1$$

$O(n)$  T.C

$O(1)$  S.C

$$\text{temp} = 4, \text{Count} = 0$$

for ( $i=0; i < n; i++$ )

{  
    if ( $a[m][i] == \text{temp}$ )  
        Count++

}

$\rightarrow \text{Count} > \lceil \frac{n}{2} \rceil \rightarrow \text{temp}$

$\rightarrow -1$

$\hookrightarrow \text{arr}[\cdot] = \{ 4, 4, 4, 4, 3, 3, 3, 2, 2, 1, 1 \}$



2) Two elements whose sum is close to zero

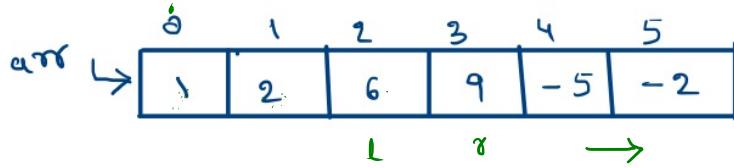
arr[] = { 1, 2, 6, 9, -5, -2 }

$O(n^2)$   $\theta \cdot c$

$O(1)$   $s \cdot c$

## Brute-Force

$$(a+b) \leq 0$$



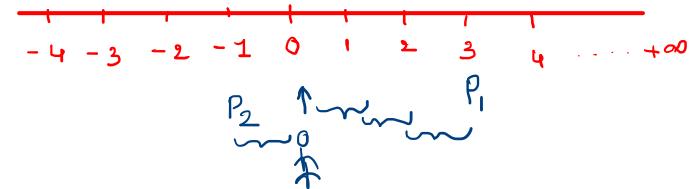
$$\min\_l = 0 \oplus 1$$

$$\min\_r = 1 \oplus 5$$

$$\min\_sum = 1 - 10$$

$$\begin{aligned} \text{sum} &= \text{arr}[l] + \text{arr}[r] \\ &= 1 + (-5) \\ &= -4 \end{aligned}$$

$$\text{arr}[] = \{ 1, 2, 6, 9, -5, -2 \}$$



$$P_1 : (1, 2) \div 3 -$$

$$P_2 : (-2, 1) = -1$$

Abs  $\rightarrow$  sum

```
function minAbsSumPair(int arr[], int arr_size)
{
    int l, r, min_sum, sum, min_l, min_r;
    if(arr_size < 2)
    {
        System.out.println("Invalid Input");
        return;
    }
    min_l = 0;
    min_r = 1;
    min_sum = arr[0] + arr[1];
    for(l = 0; l < arr_size - 1; l++)
    {
        for(r = l+1; r < arr_size; r++)
        {
            sum = arr[l] + arr[r];
            if(Math.abs(min_sum) > Math.abs(sum))
            {
                min_sum = sum;
                min_l = l;
                min_r = r;
            }
        }
    }
    print(arr[min_l] to arr[min_r]
,
```

$O(n \log n)$  T.C

$O(1)$  S.C

## sorting + 2 pointer

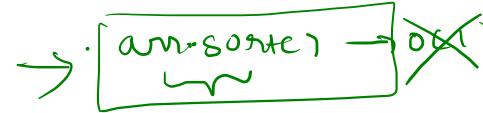
$\Leftarrow n \log n + n$

$\text{Sum} = 0$

$\min\_sum = \cancel{9999999999}$  ~~4~~  $\cancel{x} \checkmark$   
 $+ \infty$

$\min\_l = \emptyset 1$

$\min\_r = \emptyset 3$



0	1	2	3	4	5
1	2	6	9	-5	-2

0	1	2	3	4	5
-5	-2	1	2	6	9

$k \quad l \quad l \rightarrow r \quad x \quad \leftarrow$

$$\text{sum} = \text{arr}[l] + \text{arr}[r] = 4 + -3 = 0$$

if ( $\text{sum} > 0$ )

$r --$

else  $l + +$

## sorting + 2-pointer

```
static void minAbsSumPair(int arr[], int n)
{
    int sum, min_sum = 999999;
    int l = 0, r = n-1;
    int min_l = l, min_r = n-1;
    if(n < 2)
    {
        System.out.println("Invalid Input");
        return;
    }
    while(l < r)
    {
        sum = arr[l] + arr[r];
        if(Math.abs(sum) < Math.abs(min_sum))
        {
            min_sum = sum;
            min_l = l;
            min_r = r;
        }
        if(sum < 0)
            l++;
        else
            r--;
    }
    print(arr[min_l] to arr[min_r])
}
```

$$a+b+c = 20 - (-2) = 22$$



$\underbrace{(n-1) \text{ odd}} + 1 \text{ even}$   $\rightarrow O(n)$  T.C  
 3) separate odd and even  $\rightarrow O(n)$  S.C

i/p  $\text{arr}[\Sigma] = \{12, 34, 45, \dots, 3\}$

$\rightarrow \text{even}[\Sigma] \rightarrow 12, 34, 8, 20$

$\rightarrow \text{odd}[\Sigma] \rightarrow 45, 9, 3$

Given an array A[], write a function that segregates even and odd numbers. The functions should put all even numbers first, and then odd numbers.

**Example:**

Input =   
 \* Output = {12, 34, 8, 90, 45, 9, 3}

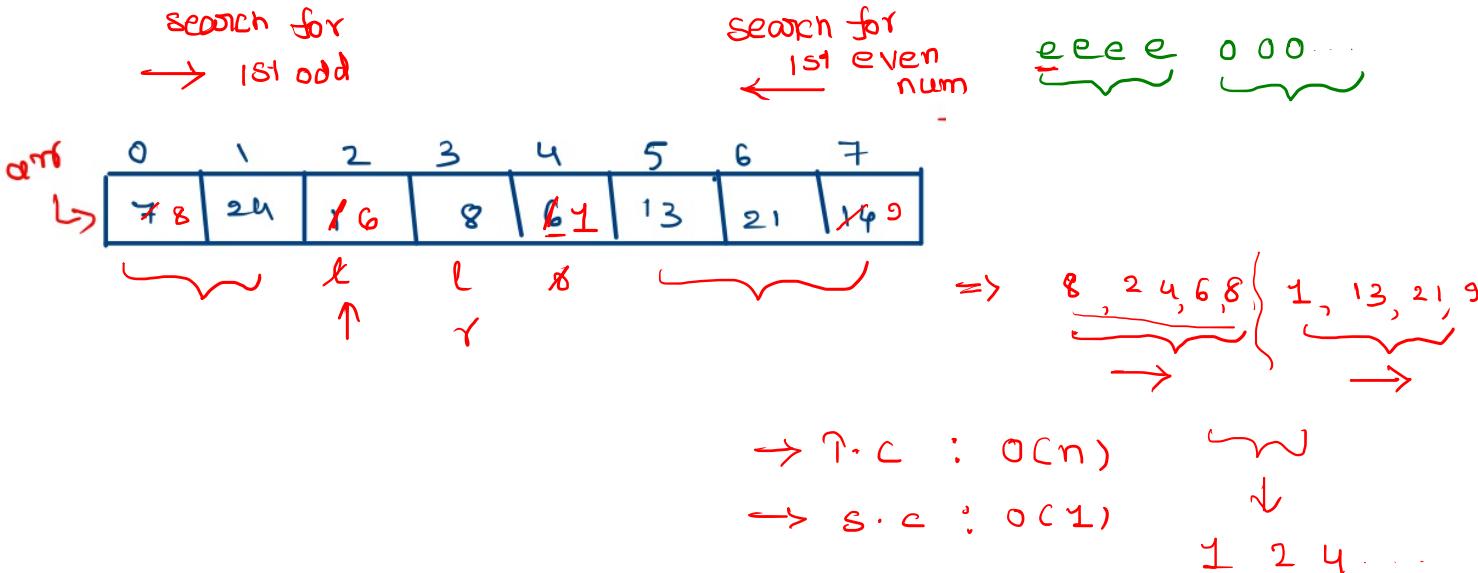
$\rightarrow \text{Loop}_1 : n \text{ times}$

In the output, the order of numbers can be changed, i.e., in the above example, 34 can come before 12 and 3 can come before 9.

$n \% 2 == 0 \rightarrow \text{even} \rightarrow \text{push/add to even array}$



2-pointer



```

segregateEvenOdd(int arr[])
{
    /* Initialize left and right indexes */
    int left = 0, right = arr.length - 1;
    → while (left < right) 1, 2, ... n
    {
        /* Increment left index while we see 0 at left */
        → while (arr[left] % 2 == 0 && left < right)
            left++;

        /* Decrement right index while we see 1 at right */
        ✓ while (arr[right] % 2 == 1 && left < right)
            right--;
    }

    if (left < right)
    {
        /* Swap arr[left] and arr[right]*/
        int temp = arr[left];
        arr[left] = arr[right];
        arr[right] = temp;
        left++;
        right--;
    }
}

```

L → ←  $\sigma$

Loop<sub>1</sub>

loop<sub>2</sub>  $\Rightarrow O(n^2)$  X

always need  
not to be true

Day-2

AP<sub>1</sub>: - BF  
T.C :  $O(n^3)$   
S.C :  $O(1)$

## \* 1) Triplet whose sum is x

**Input:** array = {12, 3, 4, 1, 6, 9}, sum = 24;

**Output:** 12, 3, 9

**Explanation:** There is a triplet (12, 3 and 9) present in the array whose sum is 24.

**Input:** array = {1, 2, 3, 4, 5}, sum = 9

**Output:** 5, 3, 1

**Explanation:** There is a triplet (5, 3 and 1) present in the array whose sum is 9.

$$a + b + c = \text{sum}$$

↳ given

$\eta \rightarrow \text{for}(i=0; i < n; i++)$   
  {  
  
 $\eta \rightarrow \text{for}(j=i+1; j < n; j++)$   
  {  
  
 $\eta \rightarrow \text{for}(k=j+1; k < n; k++)$   
  {  
    if (arr[i] + arr[j] +  
        arr[k] == sum)  
    {  
      return true  
    }  
  }  
}  
}

3  
4

## Brute-Force

arr	↳	0	1	2	3	4	5
		12	3	4	6	1	9

triplet  $\rightarrow \underline{a+b+c}$

target = 24

$$n\log n + n^2 - 2n \Rightarrow T.C: O(n^2)$$

S.C: O(1)

Sorting + 2-pointer

$$n\log n + \underline{(n-2)*n}$$

sum:  $1 + 3 + 12 = \underline{16}$

$1 + 4 + 12 = 17$

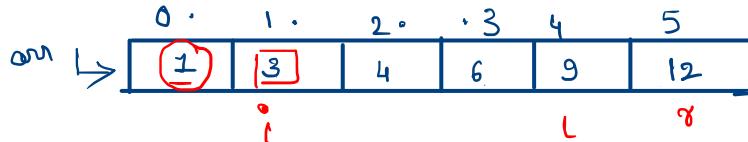
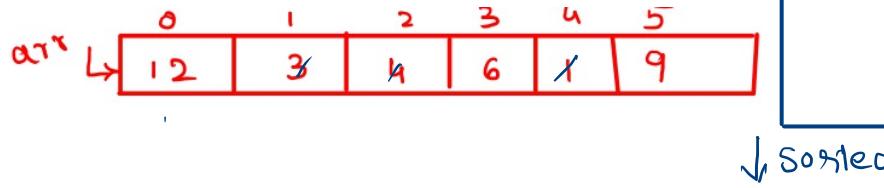
$1 + 6 + 12 = 19$

$1 + 9 + 12 = 22$

$3 + 4 + 12 = 19$

$3 + 6 + 12 = 21$

$3 + 9 + 12 = \underline{24}$



$$\text{sum} = \text{arr}[i] + \text{arr}[l] + \text{arr}[r]$$

$$\text{sum} = 16, \text{target} = 24$$

C<sub>1</sub>: sum = target  
Print triplet

C<sub>2</sub>: sum < target  
l++

C<sub>3</sub>: sum > target  
r--

3, 9, 12

Ex:- 24

```
boolean find3Numbers(int A[], int arr_size, int sum)
{
    int l, r;
    ✓for(int i = 0; i < arr_size - 2; i++) {
        ✓ l = i + 1;
        ✓ r = arr_size - 1;
        while (l < r) {
            if (A[i] + A[l] + A[r] == sum) { C1
                print("Triplet is " + A[i] + ", " + A[l] + ", " + A[r]);
                return true;
            }
            else if (A[i] + A[l] + A[r] < sum) C2
                l++; ✓
            else
                r--; C3
        }
    }
    return false;
}
```

▷ given target

✓ 3) separate zero's and ones

arr[] = { 1, 1, 0, 1, 0, 0, 0, 1 }

o/p :- { 0, 0, 0, 0, 1, 1, 1, 1 }

AP<sub>1</sub> :-    zero[] ✓    }    loop<sub>1</sub> : n times  
                  one[] ✓    }  
                                  +  
                                  { T.C : O(n)  
                                  S.C : O(n)

AP<sub>2</sub> :-    count approach.

Step<sub>1</sub> : → count # of zeros : zc

Step<sub>2</sub> : → # of ones = n - zeros : oc

Step<sub>3</sub> →    zc times → print all zeros  
                  oc times → n - n ones

T.C : O(n)  
S.C : O(1)

Count Approach ✓

→ arr[] = { 1,1,0,1,0,0,0,1}

→ o/p :- { 0,0,0,0,1,1,1,1}

2-pointer Approach

→ arr[] = { 1,1,0,1,0,0,0,1}

→ o/p :- { 0,0,0,0,1,1,1,1}

2-phr:

```
void segregate0and1(int arr[], int size)
{
    int left = 0, right = size - 1;

    while (left < right)
    {
        while (arr[left] == 0 && left < right)
            left++;

        while (arr[right] == 1 && left < right)
            right--;

        if (left < right)
        {
            arr[left] = 0;
            arr[right] = 1;
            left++;
            right--;
        }
    }
}
```

even: arr[i] % 2 == 0

\* Separate +ve and -ve numbers

① even & odd

② zero's & ones

T.C: O(n)  
S.C: O(1)

\* \* \*  
separate 0's , 1's and 2's

AP<sub>1</sub> :-  
any[] ✓  
0an[] ✓  
tan[] ✓ }  
 $O(n)$  : T.C  
 $O(n)$  : S.C

AP<sub>2</sub> :- Count app

✓ ZC }  
✓ O C }  
✓ T C      extra loops  
 $O(n)$  T.C  
 $O(1)$  S.C

## ✓ make a count

0	1	2	3	4	5	6	7	8
0	0	2	1	1	0	2	1	0

Input: {0, 1, 1, 0, 1, 2, 1, 2, 0, 0, 0, 1}

Output: {0, 0, 0, 0, 1, 1, 1, 1, 2, 2}

# \* EA Dutch National Flag Algorithm

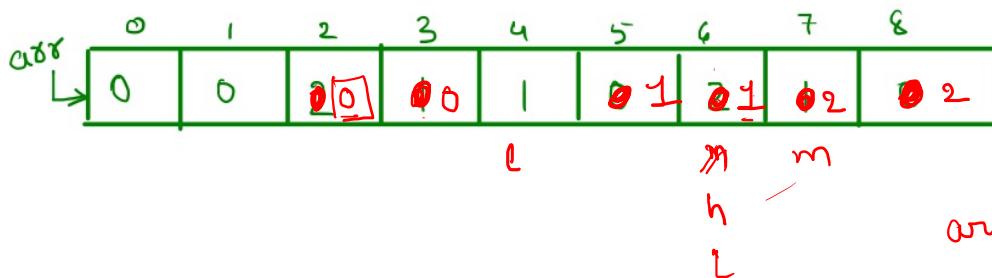
L < h x

m < n

0's    1's → 2 pos

0's    1's and 2's → 3 pos

< L, 8, mid >  
\* ↓



0 0 0 0 1 1 1 2 2

0 → swap(arr[low], arr[mid])

l++, mid++ ✓

1 → mid++ ✓

2 → swap(arr[mid], arr[high])

high--

?

```
static void sort012(int a[], int arr_size)
{
    int lo = 0, hi = arr_size - 1, mid = 0;
    → while (mid <= hi) {

        switch (a[mid]) {
            case 0: {
                swap(arr[low], arr[mid])
                lo++; mid++
                break;
            }

            case 1:
                mid++; break;

            case 2: {
                swap(arr[mid], arr[high]
                → hi--; mid++
                break;
            }
        }
    }
}
```



```
if(arr[i]===0)  
{zero.push(arr[i])}  
else if(arr[i]===1)  
{one.push(arr[i])}  
else{two.push(arr[i])}
```

```
var res = zero + " " + one + " " + two  
console.log(res)
```

$O(n)$   
 $O(n)$

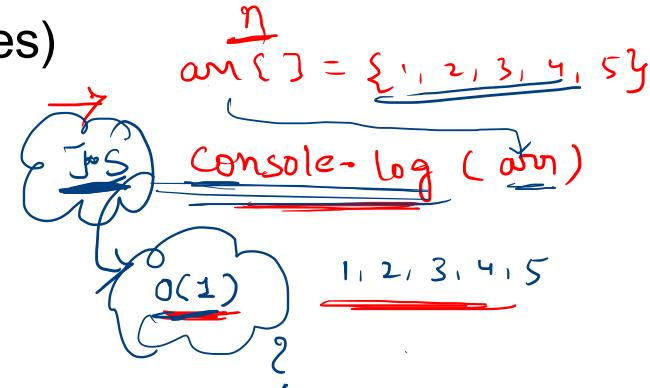


$$a = 10$$
$$c \cdot \log(n)$$

$\text{arr}[] = \{1, 7, 8, 4, 2\}$

$O(1)$  ?  
arr.push()  
Console.log(arr)

1, 2, 4, 7, 8



X { for(i=0; i<n; i++)  
min[ans[i]] }  
arr  
loop  
hashmap

~~DSA~~ → prog lang



am

10	view	10.5	
----	------	------	--

3)All twice except one

Input: ar[] = {7, 3, 5, 4, 5, 3, 4}

Output: 7

Check given integer is even or odd [ without using / , % ]