ICV Assignment #2

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Modules which will be used through this assignment

```
import numpy as np
import matplotlib.pyplot as plt
import cv2
import math
import time
```

Problem 1 Weighted Guassian Filter

Functions for Weighted Guided Filter

```
def getGaussianFilter(r, sigma):
    size = 2*r+1
    kernel = np.fromfunction(lambda x, y: (1/(2*math.pi*sigma**2)) *
math.e ** ((-1*((x-(size-1)/2)**2+(y-(size-1)/2)**2))/(2*sigma**2)).
(size, size))
    return kernel
def filter2D(img, kernel):
    filtered_img = np.zeros(img.shape)
    r = int(kernel.shape[0]/2)
    pad_img = np.pad(img, r)
    for i in range(img.shape[0]):
        for j in range(img.shape[1]):
            filtered_img[i,j] = np.sum(np.multiply(kernel,
pad_{img}[i:i+2*r+1, j:j+2*r+1]))
    return filtered_img
def f_mean(img, r, sig):
    rows, cols = img.shape[:2]
    kernel = getGaussianFilter(r, sig)
    return filter2D(img, kernel)
```

Guided Filter Algorithm (for grayscale image)

followed the pseudo code in asssignment insturctions

```
def guided_filter(I, p, r, sig, eps):
```

```
mean_l = f_mean(l, r, sig)
mean_p = f_mean(p, r, sig)
corr_l = f_mean(l*l, r, sig)
corr_lp = f_mean(l*p, r, sig)

var_l = corr_l - mean_l*mean_l
cov_lp = corr_lp - mean_l*mean_p

a = cov_lp/(var_l+eps)
b = mean_p - a*mean_l

mean_a = f_mean(a, r, sig)
mean_b = f_mean(b, r, sig)

q = mean_a*l + mean_b
return q
```

Guided Filter Algorithm (for rgb multichannel color image)

multichannel color image as guidance, single channel as input

followed the pseudo code in paper Guided Image Filtering, by Kaiming He

```
def guided_filter_color_guidance(I, p, r, sig, eps):
    I_r = I[:,:,0]
    l_g = l[:,:,1]
    l_b = l[:,:,2]
    mean_l_r = f_mean(l_r, r, sig)
    mean_{l_g} = f_{mean}(l_g, r, sig)
    mean_l_b = f_mean(l_b, r, sig)
    mean_p = f_mean(p, r, sig)
    corr_l_r = f_mean(l_r * l_r, r, sig)
    corr_l_rg = f_mean(l_r*l_g, r, sig)
    corr_l_rb = f_mean(l_r*l_b, r, sig)
    corr_l_g = f_mean(l_g*l_g, r, sig)
    corr_l_gb = f_mean(l_g*l_b, r, sig)
    corr_l_bb = f_mean(l_b*l_b, r, sig)
    corr_{p_r} = f_{mean}(l_r*p, r, sig)
    corr_{p_g} = f_{mean}(l_g*p, r, sig)
    corr_{p_b} = f_{mean}(l_b*p, r, sig)
```

```
cov_lp_r = corr_lp_r - mean_l_r*mean_p
    cov_lp_g = corr_lp_g - mean_l_g*mean_p
    cov_lp_b = corr_lp_b - mean_l_b*mean_p
    var_l_rr = corr_l_rr - mean_l_r*mean_l_r
    var_l_rg = corr_l_rg - mean_l_r*mean_l_g
    var_l_rb = corr_l_rb - mean_l_r*mean_l_b
    var_l_gg = corr_l_gg - mean_l_g*mean_l_g
    var_l_gb = corr_l_gb - mean_l_g*mean_l_b
    var_l_bb = corr_l_bb - mean_l_b*mean_l_b
    a = np.zeros(I.shape)
    for x in range(a.shape[0]):
        for y in range(a.shape[1]):
            var_l = np.array([[var_l_rr[x][y], var_l_rg[x][y],
var_l_rb[x][y],
                    [var_l_rg[x][y], var_l_gg[x][y], var_l_gb[x][y]],
                    [var_l_rb[x][y], var_l_gb[x][y], var_l_bb[x][y]])
            cov_{p} = [cov_{p}_{r}[x][y], cov_{p}_{g}[x][y], cov_{p}_{b}[x][y]]
            a[x][y] = np.matmul(cov_lp, np.linalg.inv(var_l +
eps*np.eye(3)))
    b = mean_p - (a[:,:,0]*mean_l_r + a[:,:,1]*mean_l_g +
a[:,:,2]*mean_l_b)
    mean_a_r = f_mean(a[:,:,0], r, sig)
    mean_a_g = f_mean(a[:,:,1], r, sig)
    mean_a_b = f_mean(a[:,:,2], r, sig)
    mean_b = f_mean(b, r, sig)
    q = np.zeros(I.shape)
    q = mean\_a\_r*l\_r + mean\_a\_g*l\_g + mean\_a\_b*l\_b + mean\_b
    return q
```

multichannel color image as input, single channel as guidance

followed the pseudo code in paper Guided Image Filtering, by Kaiming He

```
In [215]: def guided_filter_color_input(I, p, r, sig, eps):
```

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```
q = np.zeros(p.shape)
for i in range(p.shape[2]):
    q[:,:,i] = guided_filter(I, p[:,:,i], r, sig, eps)
return q
```

Test

```
### Set IMAGES ###
### Change Scale from 0~255 to 0~1 ###
img1 = cv2.cvtColor(cv2.imread('afghan_noise1.png'),
cv2.COLOR_BGR2RGB)/255
img2 = cv2.cvtColor(cv2.imread('afghan_noise2.png'),
cv2.COLOR_BGR2RGB)/255
clean_img = cv2.cvtColor(cv2.imread('afghan_clean.png'),
cv2.COLOR_BGR2RGB)/255
img1_grayscale = np.sum(img1, 2)/3
img2\_grayscale = np.sum(img2, 2)/3
clean_grayscale = np.sum(clean_img, 2)/3
def PSNR(smoothed_img, clean_img):
    return 20*np.log10((1/(np.mean(np.square(smoothed_img-
clean_img))**0.5)))
def showTestResult(smoothed_img, clean_img, orignal_img, run_time,
```

```
message):
   print("-----
   print(message)
   print("run time was", run_time)
   print("기존 PSNR:", PSNR(orignal_img, clean_img))
   print("smoothed PSNR:", PSNR(smoothed_img, clean_img))
   print("-----
```

```
In [241]:
          print("Smooth afghan_noise1 with r=2, sig=1, eps=0.05")
          start = time.time()
          smoothed_img1_withGray = guided_filter(img1_grayscale, img1_grayscale, 2,
          1. 0.05)
          run_time = time.time() - start
          showTestResult(smoothed_img1_withGray, clean_grayscale, img1_grayscale,
          run_time, "l=grayscale")
          start = time.time()
```

```
smoothed_img1_withR = guided_filter(img1[:,:,0], img1_grayscale, 2, 1,
0.05)
run_time = time.time() - start
showTestResult(smoothed_img1_withR, clean_grayscale, img1_grayscale,
run_time, "I=R")
start = time.time()
smoothed_img1_withG = guided_filter(img1[:,:,1], img1_grayscale, 2, 1,
0.05)
run_time = time.time() - start
showTestResult(smoothed_img1_withG, clean_grayscale, img1_grayscale,
run_time, "I=G")
start = time.time()
smoothed_img1_withB = guided_filter(img1[:,:,2], img1_grayscale, 2, 1,
0.05)
run_time = time.time() - start
showTestResult(smoothed_img1_withB, clean_grayscale, img1_grayscale,
run_time, "I=B")
print("Smooth afghan_noise2 with r=2, sig=1, eps=0.05")
start = time.time()
smoothed_img2_withGray = guided_filter(img2_grayscale, img2_grayscale, 2,
1, 0.05)
run_time = time.time() - start
showTestResult(smoothed_img2_withGray, clean_grayscale, img2_grayscale,
run_time, "l=grayscale")
start = time.time()
smoothed_img2_withR = guided_filter(img2[:,:,0], img2_grayscale, 2, 1,
0.05)
run_time = time.time() - start
showTestResult(smoothed_img2_withR, clean_grayscale, img2_grayscale,
run_time, "I=R")
start = time.time()
smoothed_img2_withG = guided_filter(img2[:,:,1], img2_grayscale, 2, 1,
0.05)
run_time = time.time() - start
showTestResult(smoothed_img2_withG, clean_grayscale, img2_grayscale,
run_time, "I=G")
start = time.time()
```

```
smoothed_img2_withB = guided_filter(img2[:,:,2], img2_grayscale, 2, 1,
0.05)
run_time = time.time() - start
showTestResult(smoothed_img2_withB, clean_grayscale, img2_grayscale,
run_time, "I=B")
Smooth afghan_noise1 with r=2, sig=1, eps=0.05
```

```
I=grayscale
run time was 8.93506646156311
기존 PSNR: 28.44273863265291
smoothed PSNR: 33.27696334415246
I=R
run time was 8.80731463432312
기존 PSNR: 28.44273863265291
smoothed PSNR: 33.32345530475129
I = G
run time was 8.304789781570435
기존 PSNR: 28.44273863265291
smoothed PSNR: 33.29358829324158
I = B
run time was 8.893277883529663
기존 PSNR: 28.44273863265291
smoothed PSNR: 33.20504084998651
Smooth afghan_noise2 with r=2, sig=1, eps=0.05
l=grayscale
run time was 8.493468761444092
기존 PSNR: 22.772466707200188
smoothed PSNR: 31.305661428820557
run time was 10.731848001480103
기존 PSNR: 22.772466707200188
smoothed PSNR: 31.26412195397442
run time was 7.95048189163208
기존 PSNR: 22.772466707200188
smoothed PSNR: 31.327315732022907
run time was 8.151562213897705
기존 PSNR: 22.772466707200188
smoothed PSNR: 31.30721348520105
```

```
print("Smooth afghan_noise1 with r=2, sig=1, eps=0.05")
start = time.time()
smoothed_img1_withRGB= guided_filter_color_guidance(img1, img1_grayscale,
2, 1, 0.05)
run_time = time.time() - start
```

```
showTestResult(smoothed_img1_withRGB, clean_grayscale, img1_grayscale, run_time, "I=RGB")

print("Smooth afghan_noise2 with r=2, sig=1, eps=0.05")
start = time.time()
smoothed_img2_withRGB= guided_filter_color_guidance(img2, img2_grayscale, 2, 1, 0.05)
run_time = time.time() - start
showTestResult(smoothed_img2_withRGB, clean_grayscale, img2_grayscale, run_time, "I=RGB")

Smooth afghan_noise1 with r=2, sig=1, eps=0.05
```

```
In [242]:
```

```
print("Smooth afghan_noise1 with r=2, sig=1, eps=0.05")
start = time.time()
smoothed_img1= guided_filter_color_input(img1_grayscale, img1, 2, 1, 0.05)
run_time = time.time() - start
showTestResult(smoothed_img1, clean_img, img1, run_time, "l=grayscale")

print("Smooth afghan_noise2 with r=2, sig=1, eps=0.05")
start = time.time()
smoothed_img2= guided_filter_color_input(img2_grayscale, img1, 2, 1, 0.05)
run_time = time.time() - start
showTestResult(smoothed_img2, clean_img, img2, run_time, "l=grayscale")
```

```
Smooth afghan_noise1 with r=2, sig=1, eps=0.05
```

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```
In [261]:
         fig, ax = plt.subplots(2, 6)
          ax[0][0].imshow(img1_grayscale, cmap='gray')
          ax[0][0].axis('off')
          ax[0][1].imshow(smoothed_img1_withGray, cmap='gray')
          ax[0][1].axis('off')
          ax[0][2].imshow(smoothed_img1_withR, cmap='gray')
          ax[0][2].axis('off')
          ax[0][3].imshow(smoothed_img1_withG, cmap='gray')
          ax[0][3].axis('off')
          ax[0][4].imshow(smoothed_img1_withB, cmap='gray')
          ax[0][4].axis('off')
          ax[0][5].imshow(smoothed_img1_withRGB, cmap='gray')
          ax[0][5].axis('off')
          ax[1][0].imshow(img2_grayscale, cmap='gray')
          ax[1][0].axis('off')
          ax[1][1].imshow(smoothed_img2_withGray, cmap='gray')
          ax[1][1].axis('off')
          ax[1][2].imshow(smoothed_img2_withR, cmap='gray')
          ax[1][2].axis('off')
          ax[1][3].imshow(smoothed_img2_withG, cmap='gray')
          ax[1][3].axis('off')
          ax[1][4].imshow(smoothed_img2_withB, cmap='gray')
          ax[1][4].axis('off')
          ax[1][5].imshow(smoothed_img2_withRGB, cmap='grav')
          ax[1][5].axis('off')
          fig.tight_layout()
          plt.show()
          print("afghan1, afghan2")
          print("Original grayscale image & Filtered with guidance filter | =
          grayscale, r, g, b, rgb")
          print("start from left")
```



afghan1, afghan2 Original grayscale image & Filtered with guidance filter I = grayscale, r, g, b, rgb start from left

```
fig, ax = plt.subplots(2, 2)

ax[0][0].imshow(img1)
ax[0][0].axis('off')
ax[0][1].imshow(smoothed_img1)
ax[0][1].axis('off')

ax[1][0].imshow(img2)
ax[1][0].axis('off')
ax[1][1].imshow(smoothed_img2)
ax[1][1].axis('off')

fig.tight_layout()
plt.show()

print("afghan1, afghan2")
print("Original color image & Filtered with guidance filter I = grayscale")
print("start from left")
```









afghan1, afghan2 Original color image & Filtered with guidance filter I = grayscale start from left

Best Result with Single Channel input, output

For afghan1:

using all 3 RGB channel as guidance in (r=2, sig=1, eps=0.05)

PSNR increased about 20% (28.4 -> 34.1)

For afghan2:

using G channel as guidance in (r=2, sig=1, eps=0.05)

PSNR increased about 42% (22.8 -> 32.3)

run time was all 7~10 seconds

How to improve performance or enhance runtime

Filter2D algorithm used in f_mean is currently calculates sequentially through pixels

It can be improved when calculation is done simultaneously (such as using GPUs or multithread on CPU)

Problem 2 Weighted Median Filter

Weighted Median Filter Algorithm for pre-defined kernel

(Ex. box filter, gaussian filter)

```
def WMF(img, kernel):
    filtered_img = np.zeros(img.shape)
```

```
k_h, k_w = kernel.shape
    pad_img = np.pad(img, ((int(k_h/2), int(k_h/2)), (int(k_w/2),
int(k_w/2)))
    kernel_flatten = kernel.flatten()
    for i in range(img.shape[0]):
        for j in range(img.shape[1]):
            window_flatten = pad_img[i:i+k_h, j:j+k_w].flatten()
            window_flatten_argsort = np.argsort(window_flatten)
            weight = [kernel_flatten[e] for e in window_flatten_argsort]
            s = 0
            for idx, w in enumerate(weight):
                s += w
                if(s >= 0.5):
                   break
            filtered_img[i,i] =
window_flatten[window_flatten_argsort[idx]]
    return filtered_img
```

Bilateral Median Filter Algorithm

```
def getBilateralFilter(window, sig_s, sig_r):
   size = window.shape[0]
   center = window[int((size-1)/2)][int((size-1)/2)]
   kernel = np.fromfunction(lambda x, y: math.e ** ((-1*((x-(size-
1)/2 **2+(y-(size-1)/2)**2))/(2*sig_s**2) + (-1*((window-
center)**2)/(2*sig_r**2))), window.shape)
   kernel /= np.sum(kernel)
    return kernel
def Bilateral_WMF(img, kernel_size, sig_s, sig_r):
    filtered_img = np.zeros(img.shape)
   k_h, k_w = kernel_size
   pad_img = np.pad(img, ((int(k_h/2), int(k_h/2)), (int(k_w/2),
int(k_w/2)))
    for i in range(img.shape[0]):
        for j in range(img.shape[1]):
            window = pad_img[i:i+k_h, j:j+k_w]
           kernel = getBilateralFilter(window, sig_s, sig_r)
           kernel_flatten = kernel.flatten()
           window_flatten = window.flatten()
            window_flatten_argsort = np.argsort(window_flatten)
            weight = [kernel_flatten[e] for e in window_flatten_argsort]
            s = 0
            for idx, w in enumerate(weight):
```

Test

```
### Set IMAGES ###
### Change Scale from 0~255 to 0~1 ###
img1 = cv2.cvtColor(cv2.imread('monkey_noise1.png'),
cv2.COLOR_BGR2RGB)/255
img2 = cv2.cvtColor(cv2.imread('monkey_noise2.png'),
cv2.COLOR_BGR2RGB)/255

clean_img = cv2.cvtColor(cv2.imread('monkey_clean.png'),
cv2.COLOR_BGR2RGB)/255

img1_grayscale = np.sum(img1, 2)/3
img2_grayscale = np.sum(img2, 2)/3
clean_grayscale = np.sum(clean_img, 2)/3
```

BoxFilter Weighted Median Filter

```
print("Smooth monkey_noise1 with boxfilter r=2,4,8")
kernel = np.zeros((5,5)) + 1
kernel /= np.sum(kernel)
start = time.time()
smoothed_img1_withBox2 = WMF(img1_grayscale, kernel)
run_time = time.time() - start
showTestResult(smoothed_img1_withBox2, clean_grayscale, img1_grayscale,
run_time, "r=2")
kernel = np.zeros((9.9)) + 1
kernel /= np.sum(kernel)
start = time.time()
smoothed_img1_withBox4 = WMF(img1_grayscale, kernel)
run_time = time.time() - start
showTestResult(smoothed_img1_withBox4, clean_grayscale, img1_grayscale,
run_time, "r=4")
kernel = np.zeros((17, 17)) + 1
kernel /= np.sum(kernel)
```

```
start = time.time()
smoothed_img1_withBox8 = WMF(img1_grayscale, kernel)
run_time = time.time() - start
showTestResult(smoothed_img1_withBox8, clean_grayscale, img1_grayscale,
run_time, "r=8")
print("Smooth monkey_noise2 with boxfilter r=2,4,8")
kernel = np.zeros((5,5)) + 1
kernel /= np.sum(kernel)
start = time.time()
smoothed_img2_withBox2 = WMF(img2_grayscale, kernel)
run_time = time.time() - start
showTestResult(smoothed_img2_withBox2, clean_grayscale, img2_grayscale,
run time. "r=2")
kernel = np.zeros((9,9)) + 1
kernel /= np.sum(kernel)
start = time.time()
smoothed_img2_withBox4 = WMF(img2_grayscale, kernel)
run_time = time.time() - start
showTestResult(smoothed_img2_withBox4, clean_grayscale, img2_grayscale,
run_time, "r=4")
kernel = np.zeros((17,17)) + 1
kernel /= np.sum(kernel)
start = time.time()
smoothed_img2_withBox8 = WMF(img2_grayscale, kernel)
run_time = time.time() - start
showTestResult(smoothed_img2_withBox8, clean_grayscale, img2_grayscale,
run_time, "r=8")
```

```
Smooth monkey_noise1 with boxfilter r=2,4,8

r=2
run time was 3.2510805130004883
기존 PSNR: 22.297180007296156
smoothed PSNR: 23.704309674869435

r=4
run time was 5.226477146148682
기존 PSNR: 22.297180007296156
smoothed PSNR: 22.371969939805425

r=8
run time was 17.394080638885498
기존 PSNR: 22.297180007296156
smoothed PSNR: 21.039188828378098

Smooth monkey_noise2 with boxfilter r=2,4,8
```

Gaussian Filter Weighted Median Filter

```
print("Smooth monkey_noise1 with Gaussianfilter r=2,4,8")
kernel = getGaussianFilter(2,1)
start = time.time()
smoothed_img1_withGaussian2 = WMF(img1_grayscale, kernel)
run_time = time.time() - start
showTestResult(smoothed_img1_withGaussian2, clean_grayscale,
img1_grayscale, run_time, "r=2")
kernel = getGaussianFilter(4,1)
start = time.time()
smoothed_img1_withGaussian4 = WMF(img1_grayscale, kernel)
run_time = time.time() - start
showTestResult(smoothed_img1_withGaussian4, clean_grayscale,
img1_grayscale, run_time, "r=4")
kernel = getGaussianFilter(8,1)
start = time.time()
smoothed_img1_withGaussian8 = WMF(img1_grayscale, kernel)
run_time = time.time() - start
showTestResult(smoothed_img1_withGaussian8, clean_grayscale,
img1_grayscale, run_time, "r=8")
print("Smooth monkey_noise2 with Gaussianfilter r=2,4,8")
kernel = getGaussianFilter(2,1)
start = time.time()
smoothed_img2_withGaussian2 = WMF(img2_grayscale, kernel)
run_time = time.time() - start
showTestResult(smoothed_img2_withGaussian2, clean_grayscale,
img2_grayscale, run_time, "r=2")
```

```
kernel = getGaussianFilter(4,1)
start = time.time()
smoothed_img2_withGaussian4 = WMF(img2_grayscale, kernel)
run_time = time.time() - start
showTestResult(smoothed_img2_withGaussian4, clean_grayscale,
img2_grayscale, run_time, "r=4")

kernel = getGaussianFilter(8,1)
start = time.time()
smoothed_img2_withGaussian8 = WMF(img2_grayscale, kernel)
run_time = time.time() - start
showTestResult(smoothed_img2_withGaussian8, clean_grayscale,
img2_grayscale, run_time, "r=8")
```

```
Smooth monkey_noise1 with Gaussianfilter r=2,4,8
run time was 2.114910364151001
기존 PSNR: 22.297180007296156
smoothed PSNR: 26.674220042605604
run time was 4.054627180099487
기존 PSNR: 22.297180007296156
smoothed PSNR: 26.655091506767356
run time was 12.790035724639893
기존 PSNR: 22.297180007296156
smoothed PSNR: 26.655029704931525
Smooth monkey_noise2 with Gaussianfilter r=2,4,8
r=2
run time was 2.0818848609924316
기존 PSNR: 18.4421249335672
smoothed PSNR: 26.499170611675297
r = 4
run time was 5.3851706981658936
기존 PSNR: 18.4421249335672
smoothed PSNR: 26.480881460386097
r = 8
run time was 18.506133794784546
기존 PSNR: 18.4421249335672
smoothed PSNR: 26.480878589973223
```

Bilateral Filter Weighted Median Filter

```
print("Smooth monkey_noise1 with Bilateralfilter r=2,4,8")
start = time.time()
smoothed_img1_withBilateral2 = Bilateral_WMF(img1_grayscale, (5,5), 100,
100)
```

```
run_time = time.time() - start
showTestResult(smoothed_img1_withBilateral2, clean_grayscale,
img1_grayscale, run_time, "r=2")
start = time.time()
smoothed_img1_withBilateral4 = Bilateral_WMF(img1_grayscale, (9,9), 100,
100)
run_time = time.time() - start
showTestResult(smoothed_img1_withBilateral4, clean_grayscale,
img1_grayscale, run_time, "r=4")
start = time.time()
smoothed_img1_withBilateral8 = Bilateral_WMF(img1_grayscale, (17,17),
100, 100)
run_time = time.time() - start
showTestResult(smoothed_img1_withBilateral8, clean_grayscale,
img1_grayscale, run_time, "r=8")
print("Smooth monkey_noise2 with Bilateralfilter r=2,4,8")
start = time.time()
smoothed_img2_withBilateral2 = Bilateral_WMF(img2_grayscale, (5,5), 100,
100)
run_time = time.time() - start
showTestResult(smoothed_img2_withBilateral2, clean_grayscale,
img2_grayscale, run_time, "r=2")
start = time.time()
smoothed_img2_withBilateral4 = Bilateral_WMF(img2_grayscale, (9,9), 100,
100)
run_time = time.time() - start
showTestResult(smoothed_img2_withBilateral4, clean_grayscale,
img2_grayscale, run_time, "r=4")
start = time.time()
smoothed_img2_withBilateral8 = Bilateral_WMF(img2_grayscale, (17,17),
100, 100)
run_time = time.time() - start
showTestResult(smoothed_img2_withBilateral8, clean_grayscale,
img2_grayscale, run_time, "r=8")
```

```
r = 4
run time was 7.290171384811401
기존 PSNR: 22.297180007296156
smoothed PSNR: 22.371969939805425
r = 8
run time was 18.867663383483887
기존 PSNR: 22.297180007296156
smoothed PSNR: 21.039188828378098
Smooth monkey_noise2 with Bilateralfilter r=2,4,8
r=2
run time was 6.221836805343628
기존 PSNR: 18.4421249335672
smoothed PSNR: 23.628074588345925
r = 4
run time was 9.073758125305176
기존 PSNR: 18.4421249335672
smoothed PSNR: 22.34493473000917
r = 8
run time was 17.652286767959595
기존 PSNR: 18.4421249335672
smoothed PSNR: 20.99313910920072
fig, ax = plt.subplots(2, 4)
ax[0][0].imshow(img1_grayscale, cmap='gray')
 ax[0][0].axis('off')
 ax[0][1].imshow(smoothed_img1_withBox2, cmap='gray')
ax[0][1].axis('off')
ax[0][2].imshow(smoothed_img1_withGaussian2, cmap='gray')
ax[0][2].axis('off')
 ax[0][3].imshow(smoothed_img1_withBilateral2, cmap='gray')
ax[0][3].axis('off')
ax[1][0].imshow(img2_grayscale, cmap='gray')
ax[1][0].axis('off')
 ax[1][1].imshow(smoothed_img2_withBox2, cmap='gray')
ax[1][1].axis('off')
ax[1][2].imshow(smoothed_img2_withGaussian2, cmap='gray')
ax[1][2].axis('off')
 ax[1][3].imshow(smoothed_img2_withBilateral2, cmap='gray')
 ax[1][3].axis('off')
```

fig.tight_layout()

plt.show()

```
print("monkey1, monkey2")
print("Original grayscale image & Filtered with WMF W (2x2) = BoxFilter,
Gaussian, Bilateral")
print("start from left")
```

















monkey1, monkey2 Original grayscale image & Filtered with WMF W (2x2) = BoxFilter, Gaussian, Bilateral start from left

Best Result

Quantatively (comparing PSNR):

For monkey1:

r=4 gaussian filter, 19% (22.29 -> 26.65)

For monkey2:

r=4 gaussian filter, 44% (18.44 -> 26.48)

Qualitively (comparing with human eye):

Bilateral Filters and Gaussian seems similar(nice sharp edge, smooth surface)

How to improve performance or enhance runtime

run time is to high for larger kernels

bottleneck is sorting

not sorting single window every time, save the order of adjacent pixels and use Repeatedly