

# **Electric Circuits I**

## **Laboratory 1: Vectors and Matrices MATLAB**

### **Objective:**

- In this laboratory you will learn how to represent and use vectors and matrices in MATLAB.

### **Background notes:**

In MATLAB an MxN matrix is a rectangular array of numbers with M rows and N columns. It can be defined by typing the matrix elements between square brackets. Elements along a row are separated by commas, and rows are separated by semi colons.

In Lab 0 you used row vectors for values of the angle and time variable. A row vector is a matrix with M=1.

In MATLAB Help, go to the Mathematics chapter. The second section is “Matrices in MATLAB.” Read the first four sections about creating, adding, and multiplying matrices.

### **Matrix Multiplication:**

Create 2 x 2 matrices A and B are as follows:

$$A = [ 2,1; 3,2] \text{ and } B=[ 3,1; 2,2]$$

Print A' and B', the transposes of these two matrices.

Compute the following 4 matrix products and print them. Are any the same? Which ones?

$$A1 = A * B, \quad A2 = B * A, \quad A3 = (A' * B')', \quad A4 = (B' * A')'$$

### **Matrix Inverses:**

Use “inv” to compute the following matrix inverses.

$$A1 = \text{inv}(A * B), \quad A2 = \text{inv}(A) * \text{inv}(B), \quad A3 = \text{inv}(B * A), \quad A4 = \text{inv}(B) * \text{inv}(A).$$

Check the inverse values. Multiply A1\*(A\*B) and also multiply (A\*B)\*A1. What are the two products?

## Solving Circuits with MATLAB:

The result of a KVL/KCL analysis of a circuit is the set of simultaneous equations:

$$V_1 + V_3 = 10$$

$$3V_1 + 3V_2 + 4V_3 = 12$$

$$2V_1 + 2V_2 + 3V_3 = 5$$

which can be written using matrices as follows:

$$\begin{bmatrix} 1 & 0 & 1 \\ 3 & 3 & 4 \\ 2 & 2 & 3 \end{bmatrix} \cdot \begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix} = \begin{bmatrix} 10 \\ 12 \\ 5 \end{bmatrix} = C \cdot V = S$$
$$C = \begin{bmatrix} 1 & 0 & 1 \\ 3 & 3 & 4 \\ 2 & 2 & 3 \end{bmatrix} \quad V = \begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix} \quad S = \begin{bmatrix} 10 \\ 12 \\ 5 \end{bmatrix}$$

To solve this 3x3 system of equations we invert the coefficients matrix C and multiply it by the source matrix S.

Invert the matrix C and solve the system for the voltage matrix V. Then verify that the result is correct by multiplying C\*V and compare the result with S.

## More About Matrix Inverses:

Find the inverse of the matrix D shown below:

$$D = [2,4; 1,2]$$

- Is there an inverse of D ?
- If the answer is 'NO' then why not?

## Products of Time Functions:

Given the following functions,

$p(t) = 5\cos(2\pi \cdot 3 \cdot t)$  and  $v(t) = 5 \cdot \exp(-0.5 \cdot t)$   
plot p(t) and v(t) from  $t = 0$  to  $t=10$  using time steps of 0.01.

Create the point by point product function  $b(t) = p(t)v(t)$  using  $b=p.*v$  and plot it. Note that the  $.*$  operation multiplies the two vectors point by point rather than computing a matrix product.

Note: Please show all your work.