

Electric Circuits I

Laboratory 1: Vectors and Matrices MATLAB

Objective:

- In this laboratory you will learn how to represent and use vectors and matrices in MATLAB.

Background notes:

In MATLAB an $M \times N$ matrix is a rectangular array of numbers with M rows and N columns. It can be defined by typing the matrix elements between square brackets. Elements along a row are separated by commas, and rows are separated by semi colons.

In Lab 0 you used row vectors for values of the angle and time variable. A row vector is a matrix with $M=1$.

In MATLAB Help, go to the Mathematics chapter. The second section is “Matrices in MATLAB.” Read the first four sections about creating, adding, and multiplying matrices.

Matrix Multiplication:

Create 2 x 2 matrices A and B are as follows:

$A = \begin{bmatrix} 2,1; 3,2 \end{bmatrix}$ and $B = \begin{bmatrix} 3,1; 2,2 \end{bmatrix}$

Print A' and B' , the transposes of these two matrices.

Compute the following 4 matrix products and print them. Are any the same? Which ones?

$A1 = A * B$, $A2 = B * A$, $A3 = (A' * B')'$, $A4 = (B' * A')'$

Matrix Inverses:

Use “inv” to compute the following matrix inverses.

$A1 = \text{inv}(A * B)$, $A2 = \text{inv}(A) * \text{inv}(B)$, $A3 = \text{inv}(B * A)$, $A4 = \text{inv}(B) * \text{inv}(A)$.

Check the inverse values. Multiply $A1 * (A * B)$ and also multiply $(A * B) * A1$. What are the two products?

Solving Circuits with MATLAB:

The result of a KVL/KCL analysis of a circuit is the set of simultaneous equations:

$$V1 + V3 = 10$$

$$3V1 + 3V2 + 4V3 = 12$$

$$2V1 + 2V2 + 3V3 = 5$$

which can be written using matrices as follows:

$$\begin{bmatrix} 1 & 0 & 1 \\ 3 & 3 & 4 \\ 2 & 2 & 3 \end{bmatrix} \cdot \begin{bmatrix} V1 \\ V2 \\ V3 \end{bmatrix} = \begin{bmatrix} 10 \\ 12 \\ 5 \end{bmatrix} = C \cdot V = S$$

$$C = \begin{bmatrix} 1 & 0 & 1 \\ 3 & 3 & 4 \\ 2 & 2 & 3 \end{bmatrix} \quad V = \begin{bmatrix} V1 \\ V2 \\ V3 \end{bmatrix} \quad S = \begin{bmatrix} 10 \\ 12 \\ 5 \end{bmatrix}$$

To solve this 3x3 system of equations we invert the coefficients matrix C and multiply it by the source matrix S.

Invert the matrix C and solve the system for the voltage matrix V. Then verify that the result is correct by multiplying C*V and compare the result with S.

More About Matrix Inverses:

Find the inverse of the matrix D shown below:

$$D = [2,4; 1,2]$$

- Is there an inverse of D ?
- If the answer is 'NO' then why not?

Products of Time Functions:

Given the following functions,

$$p(t) = 5\cos(2\pi \cdot 3 \cdot t) \text{ and } v(t) = 5\exp(-0.5 \cdot t)$$

plot p(t) and v(t) from t = 0 to t=10 using time steps of 0.01.

Create the point by point product function b(t) = p(t)v(t) using b=p.*v and plot it. Note that the .* operation multiplies the two vectors point by point rather than computing a matrix product.

Note: Please show all your work.