

$$\delta\mathcal{L}_{\text{fermion}} = -\epsilon\sigma^\nu\partial_\nu\phi^*\bar{\sigma}^\mu\partial_\mu\psi + \psi^\dagger\bar{\sigma}^\mu\sigma^\nu\epsilon^\dagger\partial_\mu\partial_\nu\phi + i\epsilon^\dagger\bar{\sigma}^\mu\partial_\mu\psi\mathcal{F}^* + i\psi^\dagger\bar{\sigma}^\mu\partial_\mu(\epsilon\mathcal{F})$$

$$= \delta^{\text{old}}\mathcal{L}_{\text{fermion}} + i\epsilon^\dagger\bar{\sigma}^\mu\partial_\mu\psi\mathcal{F}^* - i(\partial_\mu\psi^\dagger)\bar{\sigma}^\mu\epsilon\mathcal{F} + \partial_\mu(i\psi^\dagger\bar{\sigma}^\mu\epsilon\mathcal{F})$$