$$\begin{split} \delta \mathcal{L}_{\text{fermion}} &= -\epsilon \sigma^{\nu} \partial_{\nu} \phi^{*} \overline{\sigma}^{\mu} \partial_{\mu} \psi + \psi^{\dagger} \overline{\sigma}^{\mu} \sigma^{\nu} \epsilon^{\dagger} \partial_{\mu} \partial_{\nu} \phi + i \epsilon^{\dagger} \overline{\sigma}^{\mu} \partial_{\mu} \psi \mathcal{F}^{*} + i \psi^{\dagger} \overline{\sigma}^{\mu} \partial_{\mu} (\epsilon \mathcal{F}) \\ &= \delta^{\text{old}} \mathcal{L}_{\text{fermion}} + i \epsilon^{\dagger} \overline{\sigma}^{\mu} \partial_{\mu} \psi \mathcal{F}^{*} - i (\partial_{\mu} \psi^{\dagger}) \overline{\sigma}^{\mu} \epsilon \mathcal{F} + \partial_{\mu} (i \psi^{\dagger} \overline{\sigma}^{\mu} \epsilon \mathcal{F}) \end{split}$$