$$\chi = c_{+}\chi_{+} + c_{-}\chi_{-} = \begin{pmatrix} c_{+} \\ c_{-} \end{pmatrix}$$