

- p. 10
vector supermultiplet 是否有 chirality?
Ans:
- p. 10
Define chirality
Ans: 見 backup p. 51
- p.12
為什麼 Higgs mass 的修正來自於 fermions 和 scalars?
Ans:
- p. 14
change slope $\sim 10^4$ GeV 的原因是什麼?
Ans: 使用不同的 model. Baer 回答: The RGEs change when one transitions from the SM to the MSSM. See Ch. 9.2 of Weak Scale Supersymmetry
- p. 19
 ϵ is a spinor and ϵ^\dagger is the hermitian conjugate of ϵ , 那麼為什麼 $\delta\phi^* = \epsilon^\dagger\psi^\dagger$ 而不是 $\psi^\dagger\epsilon^\dagger$?
Ans:

$$\underbrace{\Psi_{\dot{\alpha}}^\dagger}_R \equiv (\underbrace{\Psi_\alpha}_L)^\dagger = (\Psi^\dagger)_\alpha, \quad (\underbrace{\Psi^{\dagger\dot{\alpha}}}_R)^\dagger = \Psi^\alpha, \quad \bar{\Psi}_{\dot{\alpha}} = (\Psi_\alpha)^*$$

$$\xi^\dagger\chi^\dagger = \chi^\dagger\xi^\dagger = (\xi\chi)^*$$

$$\xi^\dagger\bar{\sigma}^\mu\chi = -\chi\sigma^\mu\xi^\dagger = (\chi^\dagger\bar{\sigma}^\mu\xi)^* = -(\xi\sigma^\mu\chi^\dagger)^*$$

只是使用 complex conjugate , 若是量子場時才使用 hermitian conjugate.

$$(\psi\chi)^\dagger = \bar{\chi}_{\dot{\alpha}}\bar{\psi}^{\dot{\alpha}} = (\chi\psi)^* = \bar{\chi}\bar{\psi} = \bar{\psi}\bar{\chi}$$

$$\delta\phi = \epsilon\psi \rightarrow (\delta\phi)^* = (\epsilon\psi)^* = \epsilon^\dagger\psi^\dagger$$

- p. 20
 $\delta\psi_\alpha = -i(\sigma^\mu\epsilon^\dagger)_\alpha\partial_\mu\phi + \epsilon_\alpha\mathcal{F}$
 $\delta\psi_{\dot{\alpha}}^\dagger = i(\epsilon\sigma^\mu)_{\dot{\alpha}}\partial_\mu\phi^* + \epsilon_{\dot{\alpha}}^\dagger\mathcal{F}^*$

其中的 $\sigma^\mu\epsilon^\dagger$ 和 $\epsilon\sigma^\mu$ 的順序為什麼不同?

Ans:

$$\begin{aligned} \delta\psi_\alpha &= -i(\sigma^\mu\epsilon^\dagger)_\alpha\partial_\mu\phi + \epsilon_\alpha\mathcal{F} \\ \Rightarrow (\delta\psi_\alpha)^\dagger &= [-i(\sigma^\mu\epsilon^\dagger)_\alpha\partial_\mu\phi + \epsilon_\alpha\mathcal{F}]^\dagger \\ &= +i[(\sigma^\mu\epsilon^\dagger)_\alpha\partial_\mu\phi]^\dagger + (\epsilon_\alpha\mathcal{F})^\dagger \end{aligned}$$

其中 $(\epsilon_\alpha \mathcal{F})^\dagger = \mathcal{F}^\dagger (\epsilon_\alpha)^\dagger = \mathcal{F}^\dagger \epsilon_\alpha^\dagger = \epsilon_\alpha^\dagger \mathcal{F}^\dagger = \epsilon_\alpha^\dagger \mathcal{F}^*$ (因為 \mathcal{F} 是 scalar field, 所以 $\mathcal{F}^\dagger = \mathcal{F}^*$)

$$\begin{aligned} [(\sigma^\mu \epsilon^\dagger)_\alpha \partial_\mu \phi]^\dagger &= (\partial_\mu \phi)^\dagger [(\sigma^\mu \epsilon^\dagger)_\alpha]^\dagger \\ &= \partial_\mu \phi^* (\sigma^\mu \epsilon^\dagger)^\dagger_\alpha \\ &= (\sigma^\mu \epsilon^\dagger)^\dagger_\alpha \partial_\mu \phi^* \\ &= [\epsilon (\sigma^\mu)^\dagger]_\alpha \partial_\mu \phi^* \\ &= (\epsilon \sigma^\mu)_{\dot{\alpha}} \partial_\mu \phi^* \end{aligned}$$

其中 $(\sigma^\mu)^\dagger = \sigma^\mu$, 列出 $\mu = 0, 1, 2, 3, 4$ 就知道了.

所以 $(\delta \psi_\alpha)^\dagger = \delta \psi_{\dot{\alpha}}^\dagger = i(\epsilon \sigma^\mu)_{\dot{\alpha}} \partial_\mu \phi^* + \epsilon_{\dot{\alpha}}^\dagger \mathcal{F}^*$

- p. 21
查 closure 的定義.

Ans:

- p. 26
 $\bar{\theta} \bar{\sigma}^\mu \theta v_\mu$ 項, 為什麼要有 $\bar{\sigma}^\mu$? v_μ 是什麼?
建議用 θ^2 取代 $\theta \theta$.

Ans:

$$\bar{\theta} \bar{\sigma}^\mu \theta = \bar{\theta}_{\dot{\alpha}} (\bar{\sigma}^\mu)^{\dot{\alpha}\alpha} \theta_\alpha$$

其中 $(\bar{\sigma}^\mu)^{\dot{\alpha}\alpha} = (1, +\sigma_i)^{\dot{\alpha}\alpha}$, 不能直接乘, 因為一個是 $\dot{\alpha}$ 另一個是 α .
 v_μ 是 A_μ (gauge boson field).

- p. 27
為什麼 Q 中會有 σ ?
Ans: 見 Theis P9 的推導.

- p. 32
 $\sqrt{2}$ 一直出現, 為什麼?
Ans: Bilal P.21: normalization of fields and the definition of $\delta \phi$
Martin P.20: Historical reason. Lykken P.20: conversion.

- p. 33
Define C, D, M, .
real scalars 用 real scalar fields 取代.
Ans: C 是 scalar field, D 是 real 的輔助場 D_a (gauge auxiliary field), λ 是 gaugino field. $\frac{i}{2}(M + iN)$ 是 \mathcal{F} , $-\frac{i}{2}(M - iN)$ 是 \mathcal{F}^* .

- p. 35
 V_{WZ} 是否仍然是 invariant?
Ans:

- p. 41
M, m 是什麼?

Ans: M is mass.

Fermion mass term:

$$-\frac{1}{2}\psi_i\langle\frac{\partial^2 W}{\partial\phi_i\partial\phi_j}\rangle\psi_j$$

e.g. $\langle\phi_1\rangle = 0 \Rightarrow M_{\psi_2} = M_{\psi_3} = M, \quad M_{\psi_1} = 0.$

scalar mass $V = W^i W_i^* \Rightarrow M_{\phi_1} = 0, M_{\phi_2} = M, \phi_3$ 是 complex field $\frac{1}{\sqrt{2}}(a + ib).$

$$m_a^2 = M^2 - 2g^2 m^2, m_b^2 = M^2 + 2g^2 m^2.$$

• **p. 44**

有兩個 Higgs doublet，那麼哪一個是 Standard Model 的 Higgs?

Ans: 是 h_0 .

8 個 Higgs state 在 symmetry breaking 後，其中 3 個形成 W^\pm, Z^0 , 5 個形成 A_0, h_0, H_0, H^\pm .

A_0 : pseudoscalar，由 $(\Im\frac{H_u^0}{\sqrt{2}}, \Im\frac{H_d^0}{\sqrt{2}})$ 形成，

h_0, H_0 : neutral scalar，由 $(\Re\frac{H_u^0}{\sqrt{2}}, \Re\frac{H_d^0}{\sqrt{2}})$ 形成，

h_0 是接近 SM Higgs 質量的。

• **p. 60**

查 W^0 和 B^0 如何 mix 成 Z^0 和 γ ? (Griffiths 的粒子物理課本可能有答案)

Ans:

$$\begin{aligned} A_\mu &= B_\mu \cos \theta_W + W_\mu^3 \sin \theta_W \\ Z_\mu &= -B_\mu \sin \theta_W + W_\mu^3 \cos \theta_W \end{aligned}$$

其中 $\theta_W = 28.75^\circ$ is weak mixing angle.

• **p. 61**

Hypercharge 的定義是什麼?

Ans: $Y = S + A$, S = strangeness, A = baryon number, 見 backup 66, $H_u : Y = \frac{1}{2}, H_d : Y = -\frac{1}{2}, T_3 = \frac{1}{2}$ or $-\frac{1}{2}$.

• **p. 63**

$\tilde{t}\tilde{t}H_u^0 - \tilde{t}_L\tilde{b}_L H_u^+$ 第二項代表什麼?

Ans: 是 stop 和 sbottom 的 coupling term. H_u^0 only neutral Higgs has VEV $\neq 0$.