$(\chi \sigma^{\mu} \overline{\sigma}^{\nu} \psi)^{\dagger} = \overline{\psi} \overline{\sigma}^{\nu} \sigma^{\mu} \overline{\chi}$