APPENDIX

We provide the gradients used for ASGD in the proposed algorithms.

MVN2VEC-CON:

$$\frac{\partial O_{\text{CON}}}{\partial \mathbf{f}_{u}^{\upsilon}} = \left(1 - \sigma(\mathbf{f}_{u}^{\upsilon} \cdot \boldsymbol{\varphi}_{\theta}^{\upsilon}(\{\tilde{\mathbf{g}}_{n}^{\upsilon'}\}_{\upsilon' \in \mathcal{V}}))\right) \cdot \boldsymbol{\varphi}_{\theta}^{\upsilon}(\{\tilde{\mathbf{g}}_{n}^{\upsilon'}\}_{\upsilon' \in \mathcal{V}})$$

$$- \sum_{i=1}^{K} \sigma(\mathbf{f}_{u}^{\upsilon} \cdot \boldsymbol{\varphi}_{\theta}^{\upsilon}(\{\tilde{\mathbf{g}}_{n_{i}'}^{\upsilon'}\}_{\upsilon' \in \mathcal{V}})) \cdot \boldsymbol{\varphi}_{\theta}^{\upsilon}(\{\tilde{\mathbf{g}}_{n_{i}'}^{\upsilon'}\}_{\upsilon' \in \mathcal{V}}), \tag{9}$$

$$\frac{\partial O_{\text{CON}}}{\partial \tilde{\mathbf{g}}_{n}^{\hat{\boldsymbol{v}}}} = \left(1 - \sigma(\mathbf{f}_{u}^{\upsilon} \cdot \boldsymbol{\varphi}_{\theta}^{\upsilon}(\{\tilde{\mathbf{g}}_{n}^{\upsilon'}\}_{\upsilon' \in \mathcal{V}}))\right) \cdot \mathbf{f}_{u}^{\upsilon} \cdot \begin{cases} \theta + \frac{1 - \theta}{|\mathcal{V}|}, & \hat{\boldsymbol{v}} = \upsilon, \\ \theta, & \hat{\boldsymbol{v}} \neq \upsilon, \end{cases}$$
(10)

$$\frac{\partial \mathcal{O}_{\text{con}}}{\partial \tilde{\mathbf{g}}_{n_{i}^{\prime}}^{\upsilon}} = -\sigma(\mathbf{f}_{u}^{\upsilon} \cdot \varphi_{\theta}^{\upsilon}((\tilde{\mathbf{g}}_{n_{i}^{\prime}}^{\upsilon'})_{\upsilon' \in \mathcal{V}})) \cdot \mathbf{f}_{u}^{\upsilon} \cdot \begin{cases} \theta + \frac{1-\theta}{|\mathcal{V}|}, & \hat{\upsilon} = \upsilon, \\ \theta, & \hat{\upsilon} \neq \upsilon. \end{cases} \tag{11}$$

MVN2VEC-REG:

$$\frac{\partial O_{\text{REG}}}{\partial \mathbf{f}_{u}^{\upsilon}} = \left(1 - \sigma(\mathbf{f}_{u}^{\upsilon} \cdot \tilde{\mathbf{f}}_{n}^{\upsilon})\right) \cdot \tilde{\mathbf{f}}_{n}^{\upsilon} - \sum_{i=1}^{K} \sigma(\mathbf{f}_{u}^{\upsilon} \cdot \tilde{\mathbf{f}}_{n_{i}^{\prime}}^{\upsilon}) \cdot \tilde{\mathbf{f}}_{n_{i}^{\prime}}^{\upsilon} + 2\gamma \left(K + 1\right) \left(1 - \frac{1}{|\mathcal{V}|}\right) \cdot \left(\mathbf{f}_{u}^{\upsilon} - \frac{1}{|\mathcal{V}|} \sum_{z' \in \mathcal{V}} \mathbf{f}_{u}^{\upsilon'}\right), \tag{12}$$

$$\frac{\partial O_{\text{REG}}}{\partial \tilde{\mathbf{f}}_{n}^{\upsilon}} = \left(1 - \sigma(\mathbf{f}_{u}^{\upsilon} \cdot \tilde{\mathbf{f}}_{n}^{\upsilon})\right) \cdot \mathbf{f}_{u}^{\upsilon} + 2\gamma \left(1 - \frac{1}{|\mathcal{V}|}\right) \cdot \left(\tilde{\mathbf{f}}_{n}^{\upsilon} - \frac{1}{|\mathcal{V}|} \sum_{\upsilon' \in \mathcal{V}} \tilde{\mathbf{f}}_{n}^{\upsilon'}\right),\tag{13}$$

$$\frac{\partial O_{\text{REG}}}{\partial \tilde{\mathbf{f}}_{n_{i}^{\prime}}^{\upsilon}} = -\sigma(\mathbf{f}_{u}^{\upsilon} \cdot \tilde{\mathbf{f}}_{n_{i}^{\prime}}^{\upsilon}) \cdot \mathbf{f}_{u}^{\upsilon} + 2\gamma \left(1 - \frac{1}{|\mathcal{V}|}\right) \cdot \left(\tilde{\mathbf{f}}_{n_{i}^{\prime}}^{\upsilon} - \frac{1}{|\mathcal{V}|} \sum_{\upsilon^{\prime} \in \mathcal{V}} \tilde{\mathbf{f}}_{n_{i}^{\prime}}^{\upsilon^{\prime}}\right). \tag{14}$$

Note that in implementation, |V| should be the number of views in which u is associated with at least one edge.