

Consider the following continuously-compounded yields for US Treasury STRIPs:

Maturity (Years)	STRIP Yield
0.5	0.0500
1.0	0.0520
1.5	0.0510
2.0	0.0530

What would be the no-arbitrage value on a Treasury note that has a face (principal) value of \$100, a time until maturity of exactly 2 years, and pays semi-annual coupons at an annual coupon rate of 6.00 percent?

State your answer in dollars to the nearest 1 cent, e.g., 103.45

$$C = cT = 0.03 \times 100 = 3$$

$$\frac{1 \times 3}{\left(1 + \frac{0.05}{2}\right)^{2 \times \frac{1}{2}}} + \frac{1 \times 3}{\left(1 + \frac{0.052}{2}\right)^{2 \times 1}} + \frac{1 \times 3}{\left(1 + \frac{0.051}{2}\right)^{2 \times \frac{3}{2}}}$$

$$+ \frac{1 \times 3}{\left(1 + \frac{0.053}{2}\right)^{2 \times 2}} + \frac{100}{\left(1 + \frac{0.053}{2}\right)^{2 \times 2}} = 101.3271214$$

Consider the following continuously-compounded spot yields for zero-coupon bonds.

Maturity (Years)	Spot Yield
0.5	0.0500
1.0	0.0520
1.5	0.0510
2.0	0.0530

What would be the no-arbitrage forward rate on a "12 by 18" forward rate agreement (FRA)? That is, what is the forward rate $f_0(1,1.5)$ assuming an $m=180$ -day investment maturity?

State your answer as a percentage rate to 2 decimal places using the standard money market rate convention used in FRA quotes, e.g., 5.12.

$$P(0,1) = e^{-0.052 \times 1} = 0.9493288668$$

$$P(0,1.5) = e^{-0.051 \times 1.5} = 0.9263529143$$

$$f_0(1,1.5) = \frac{1}{m} \left(\frac{P(0,1)}{P(0,1.5)} - 1 \right) = 4.96\%$$

On Friday, September 23, 2022 the following quotes were given for a Treasury Bond maturing on May 15, 2038. Note that these quotes are for a face value of \$100 and are in terms of dollars and cents, not in terms of 32nd of a dollar.

Maturity	Coupon	Bid	Ask	Change
Treasury Bond				
May 15, 2038	4.500	109.2640	109.2740	+0.1440

Find the invoice price for buying \$100,000 in face (principal) value of this bond.

State your answer to the nearest \$1, for example 97,243.

Ask price

$m=2$

$$B_0 = 109.2740 + \frac{4.5}{2} \times \frac{131}{184}$$

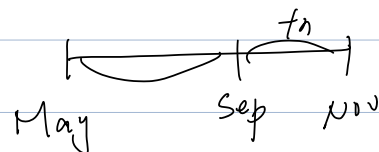
$$= 110.8759$$

$$110.8759 \times 1000 = 110876$$

$$t_b = 184$$

$$t_n = 53$$

$$\rightarrow t_d = 131$$



A U.S. Treasury STRIP matures in exactly 5 years and has a continuously-compounded yield to maturity of 4.40%. Suppose that the continuously-compounded forward rate for borrowing or lending over one-half of a year starting in 4.5 years and ending in 5.0 years equals 4.30%. What is the no-arbitrage, continuously-compounded yield to maturity on a U.S. Treasury STRIP maturing in exactly 4.5 years?

State your answer as a percentage rate to the third decimal point, for example, 4.132 .

$$f_0(t, t+m) = \frac{t+m}{m} y(0, t+m) - \frac{t}{m} y(0, t)$$

$$0.043 = \frac{5}{0.5} 0.044 - \frac{4.5}{0.5} y(0, 4.5)$$

$$0.043 = 0.44 - 9 y(0, 4.5)$$

$$y(0, 4.5) = \frac{0.44 - 0.043}{9} = 0.04411$$

An underwriter is setting the terms of a new 2-year corporate note (bond) that a corporation plans to issue soon. The note will pay semi-annual coupons and will have a 2-year maturity. The underwriter observes the following semi-annually compounded yields on U.S. Treasury STRIPs:

Maturity (Years)	Spot Yield
0.5 $y(0, \frac{1}{2})$	0.040
1.0 $y(0, 1)$	0.044
1.5 $y(0, \frac{3}{2})$	0.048
2.0 $y(0, 2)$	0.050

$m=2$

The underwriter wants to set the note's coupon rate so that the note sells at its par value. Given the corporation's credit risk, the underwriter expects that investors will require a coupon rate equal to 200 basis points (2.00%) greater than that of an equivalent maturity, default-free Treasury note that sells at par. What coupon rate should the underwriter set for this new corporate note?

Express your answer for the coupon rate as a percentage of face value to the second decimal point, for example, 5.23 .

$$p(0, \frac{1}{2}) = e^{-0.04 \times \frac{1}{2}} = 0.98019867$$

$$p(0, 1) = e^{-0.04} = 0.95695395$$

$$p(0, \frac{3}{2}) = e^{-0.048 \times 1.5} = 0.9305308958$$

$$p(0, 2) = e^{-0.05 \times 2} = 0.907837418$$

$$C = \frac{2(1 - p(0, 2))}{p(0, \frac{1}{2}) + p(0, 1) + p(0, \frac{3}{2}) + p(0, 2)} = 0.05045$$

$$\rightarrow 5.047 + 2 = 7.047 \neq$$