

Q4.1

0.5 Points

Let $\{X_1, X_2, \dots\}$ be i.i.d. from $N(0, 1)$. What's the limit of $\frac{1}{n} \sum_{i=1}^n X_i^4$ as $n \rightarrow +\infty$?
 What's the approximate distribution of $\frac{1}{n} \sum_{i=1}^n X_i^4$ when n is large (don't forget to give the parameters of the distribution)? Show details.

$$\text{let } Y_i = X_i^4$$

$$\lim_{n \rightarrow \infty} \frac{1}{n} \sum_{i=1}^n Y_i = \lim_{n \rightarrow \infty} \bar{Y} = \mu_Y = \mu_{X^4} \quad (\text{LLN})$$

Since LLN, when n is large, given distribution will attain normality with μ_X and σ_X^2 .