

Q4

1 Point

Suppose Y has a χ_k^2 distribution. What's the limiting distribution of $(Y - k)/\sqrt{2k}$ as $k \rightarrow +\infty$? Show details.

$$Y \sim \chi_k^2(k, 2k)$$

$$\chi_k^2 = \sum_{i=1}^k z_i^2, \quad z_i \sim \mathcal{N}(0, 1)$$



$$E(z_i^2) = \mu, \quad \text{Var}(z_i^2) = \sigma^2 \quad (\text{both finite})$$

$$\frac{Y - k}{\sqrt{2k}} = \frac{Y - \mu}{\sigma} \longrightarrow \underbrace{\mathcal{N}(0, 1)} \text{ when } k \rightarrow \infty$$