Ito Integration

15. Define

$$M_t \stackrel{\text{def}}{=} \int_{s=0}^t e^{-s} dW_s.$$

For each t > 0, compute

- (a) $\mathbb{E}[M_t]$.
- (b) $\mathbb{E}[M_t^2]$
- 16. Define

$$A_t \stackrel{\text{def}}{=} \int_{s=0}^t W_s^3 dW_s$$

Compute

- (a) $\mathbb{E}[A_t]$
- (b) $\langle A \rangle_t$.
- (c) $\mathbb{E}[A_t^2]$.