

基

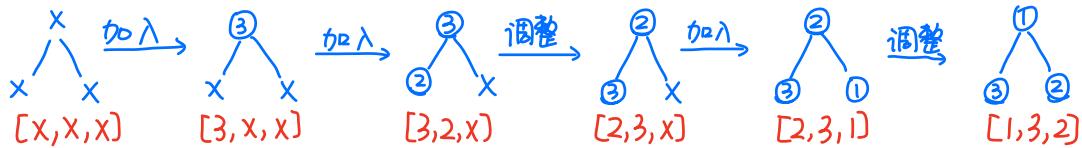
础

众

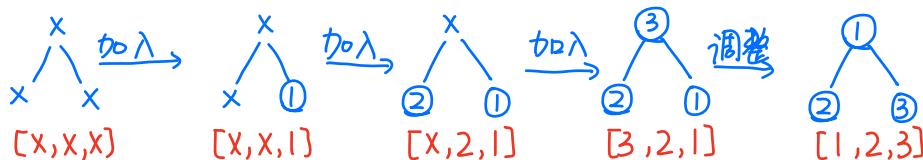
浪

nums = [3, 2, 1] # 原始数据

基于 sift up 的 heapify: $O(n \log n)$



基于 sift down 的 heapify: $O(n)$



```

>> from heapq import *
>> h = []
>> for x in [(1,'J'),(4,'N'),(3,'H'),(1,'A')]: heappush(h, item) # O(log k)
>> h=[(1,'J'),(4,'N'),(3,'H'),(1,'A')] #
>> heapify(h) # heapify data inplace O(k)
>> while h:
    print(heapop(h)) #O(logk)

```

```

from random import randint
x=randint(LB,UB)

```

```

from functools import cmp_to_key
cmp=lambda x,y:-1 if str(x)+str(y)<str(y)+str(x) else 1
nums.sort(key=cmp_to_key(cmp))

```

(1) find first position of a num that's \geq target ; return len(nums) if not found
 $idx = bisect_left(nums, target)$

(2) find first position of a num that's $>$ target ; return len(nums) if not found
 $idx = bisect_right(nums, target)$

(3) $\nexists \leq target$ à last position
 $idx = bisect_left(nums, target+1)-1$
 $idx = bisect_right(nums, target)-1$

(4) $\nexists \geq target$ à first position
 $idx = bisect_left(nums, target)$
 $idx = bisect_right(nums, target-1)$

<pre> def dec(func): def inner(): s=time.time() func() print(time.time()-s) return inner </pre>	\Rightarrow <pre> @dec def func(): print('func') </pre>	\Leftrightarrow <pre> def func(): print('func') func=dec(func) </pre>
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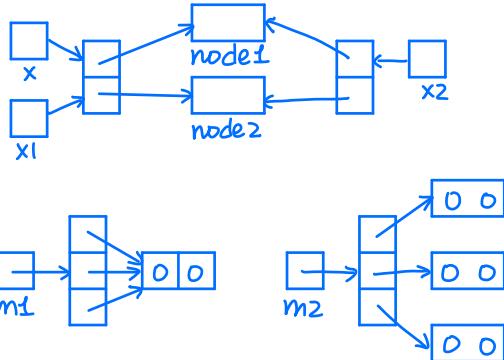
*decorator 模式

Python: $-3 \% 4 \rightarrow 1$ $-3 // 4 \rightarrow -1$ $-(3 // 4) \rightarrow 0$
Java: $-3 \% 4 \rightarrow -3$ $-3 // 4 \rightarrow 0$

$a \pm b \% \text{mod} = (a \% \text{mod} \pm b \% \text{mod}) \% \text{mod}$
 $a * b \% \text{mod} = a \% \text{mod} * b \% \text{mod}$

```
a=[1,2,3,1]
b=[1,3,1,2]
collections.Counter(a)==collections.Counter(b)
a+b # a[x]+b[x]
a-b # a[x]-b[x] (keeping only positive counts)
a&b # min(a[x],b[x])
a|b # max(a[x],b[x])
```

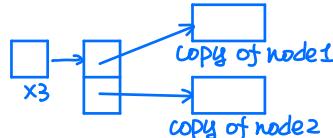
```
math.gcd      def gcd(a,b):
math.log
math.sqrt
math.factorial      if b==0:
                    return a
                    return gcd(b,a%b)
```



*singleton 模式

```
def singleton(aClass):
    instance = None
    def onClass(*args, **kwargs):
        nonlocal instance
        if instance == None:
            instance = aClass(*args, **kwargs)
        return instance
    return onCall
```

```
@singleton
class Spam:
    pass
```



m1=[[0]*2]*3 # shallow copy (wrong)
m2=[[0]*2 for _ in range(3)] # correct or m2=[[0 for _ in range(2)] for _ in range(3)]

```
L=[1,2]
L.append(L)
```

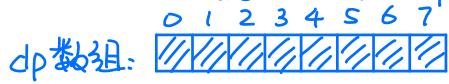
如果数组长度为n, 窗口大小为k
 \Rightarrow 总共有 $n-(k-1)$ 个这样的窗口, 最后一个窗口的坐标为 $n-k$



$[*num, i]$ is equivalent to $num+[i]$
sortedIdx = [x for (x,y) in sorted(enumerate(nums), key=lambda: x[1])]
sorted(res, key=lambda: x[0], reverse=True)
Node.__lt__ = lambda x,y: (x.val, x.index) < (y.val, y.index)

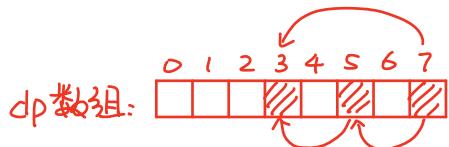
$-2^{31} \sim 2^{31}-1$
 $-2^{147483648} \sim 2^{147483647}$

Iterative DP (for loop)



为了计算 $dp[7]$, 我们必须先得到 $dp[0] \sim dp[6] \Rightarrow$ 不能剪枝

Recursive DP (DFS with memoization)



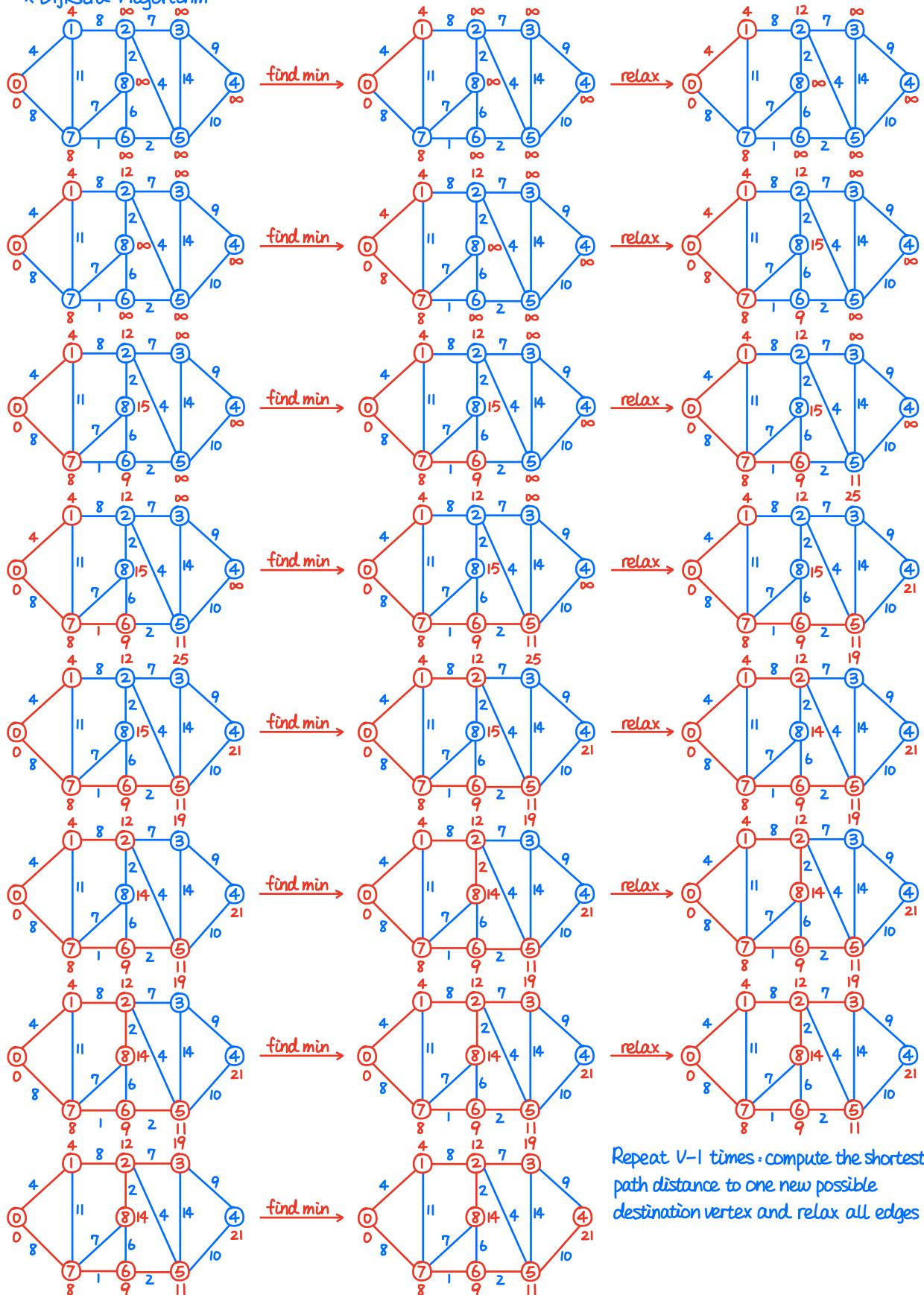
为了计算 $dp[7]$, 我们可以只动态计算出它所依赖的先前状态 \Rightarrow 可以剪枝

(图里没箭头表示依赖关系: $DP[7]$ 依赖于 $DP[3]$ 和 $DP[5]$; $DP[5]$ 依赖于 $DP[3]$)

底层数据结构	Python	Java	C++
Dynamic Array	list	ArrayList	vector
Deque (array-based)	N/A	ArrayDeque	deque (头部链接)
Deque (linked-list-based)	deque	LinkedList	list
Hash Table (key-value)	dict	HashMap	unordered_map
Hash Table (key-only)	set	HashSet	unordered_set
Balanced BST (key-value)	N/A	TreeMap	map
Balanced BST (key-only)	N/A	TreeSet	set
Heap	heapq	PriorityQueue	priority_queue
LinkedList + Hash table	OrderedDict	LinkedHashMap	N/A

Compute the shortest path distances from the source to "every" other vertex

* Dijkstra Algorithm



Repeat $V-1$ times: compute the shortest path distance to one new possible destination vertex and relax all edges

Relaxation: if $\text{dist}(s \rightarrow u) + \text{cost}(u \rightarrow v) < \text{dist}(s \rightarrow v)$, update $\text{dist}(s \rightarrow v) = \text{dist}(s \rightarrow u) + \text{cost}(u \rightarrow v)$

With binary heap

$$T(n) = O((E+V) \log V), S(n) = O(V)$$

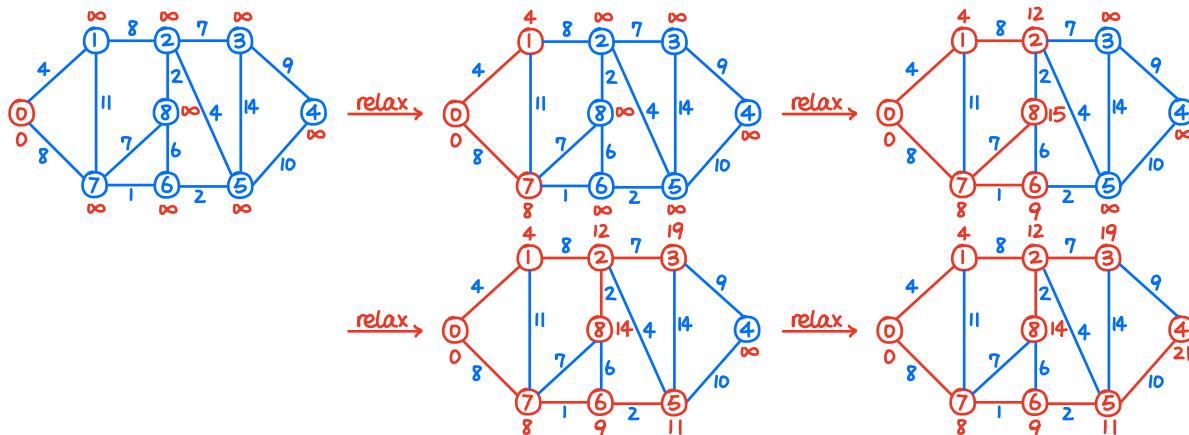
↓ for connected graph

$$T(n) = O(E \log V), S(n) = O(V)$$

* Bellman-Ford Algorithm: (restrict the number of vertexes to use ⇒ subproblems)

Either computes shortest paths from the source to all destinations, or, detects the negative cycle

Computing the shortest paths in the presence of a negative cycle is intractable (NP-hard)



- 1) for $k=1, \dots, V-1$ (or stop early)
compute the shortest distances with $\leq k$ edges
- 2) Run one extra iteration: v that's reachable from s
if we see any improvement ⇒ negative cycle detected
(To reconstruct the negative cycle, simply remember the predecessors and run dfs to catch any repetition)

$$T(n) = O(VE), S(n) = O(V^2)$$

↓ 滚动数组

$$S(n) = O(V)$$

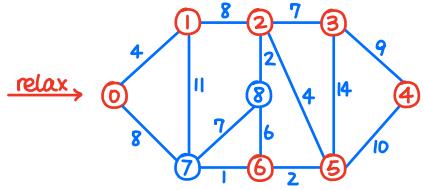
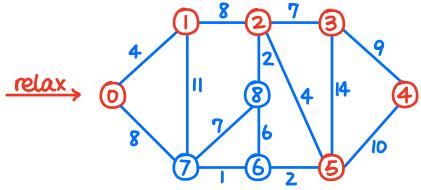
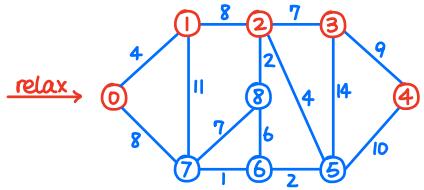
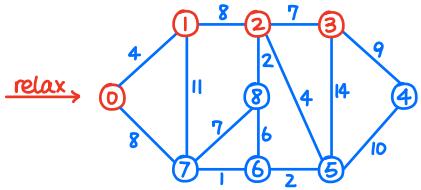
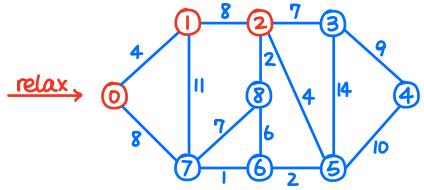
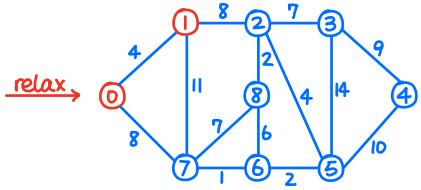
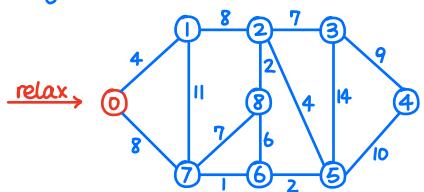
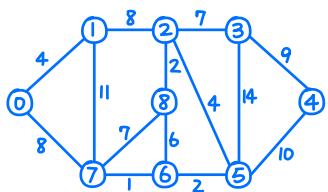
Note: the longest possible path without a cycle can have $V-1$ edges

Undirected graph: $\sum \text{degree}(v) = 2|V|$

Directed graph: $\sum \text{in-deg}(v) = |V|$

* All-Pairs Shortest Paths (APSP) Floyd-Warshall Algorithm (restrict which vertexes to use \Rightarrow subproblems)

→ some prefix of the vertexes



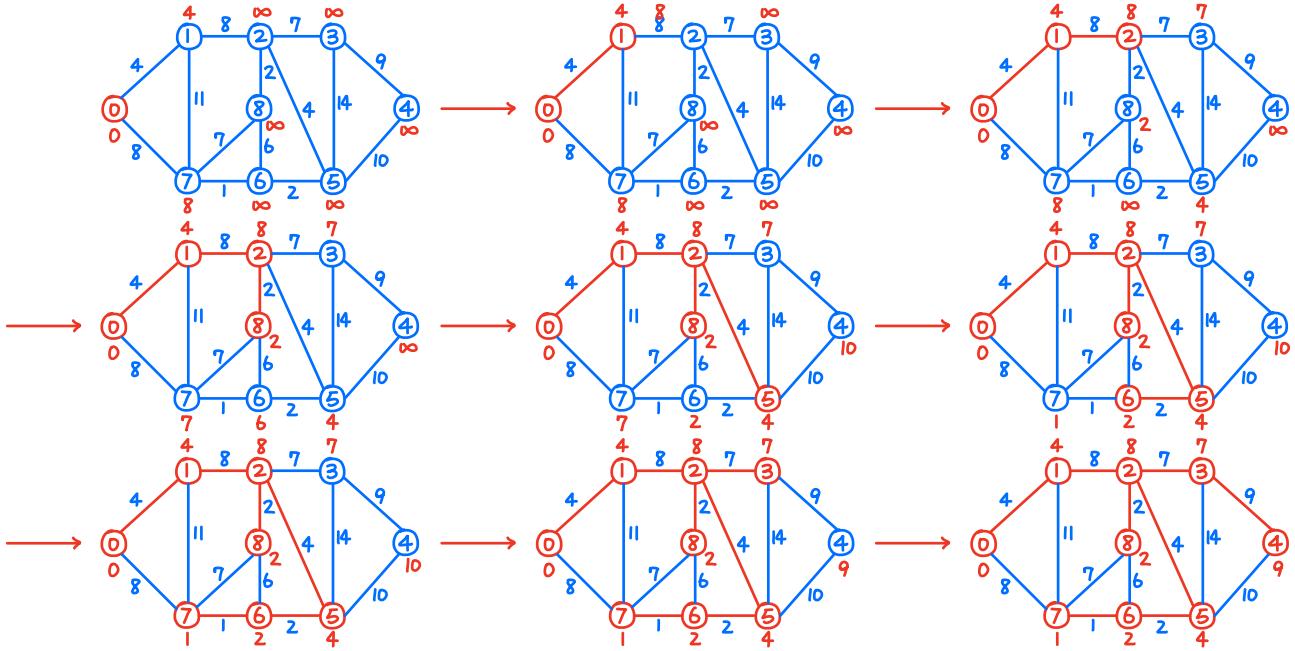
- 1) for $k = 1, \dots, V$:
compute the shortest path with vertexes $1, \dots, k$ as internal nodes for all source-destination pairs (i, j)
 - 2) if we see any negative diagonal element
 \Rightarrow negative cycle detected

$$T(n) = O(V^3), S(n) = O(V^3)$$

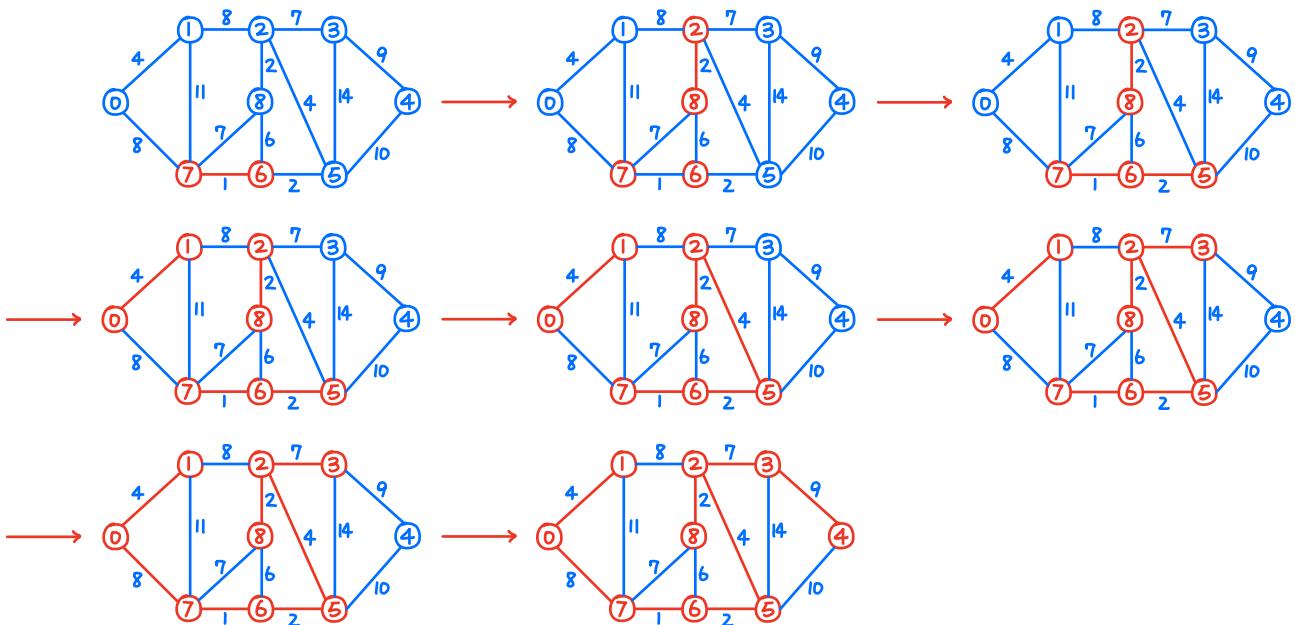
↓ 滚动数组

$$S(n) = O(V^2)$$

* Prim's Algorithm (MST): expand the tree by adding the minimum weight edge.
With binary heap: $T(n) = O(E \log V)$



* Kruskal's Algorithm (MST): include the minimum weight edge if it does not form a cycle
With union find: $T(n) = O(E \log V)$



模

板

```

# avg case: O(n log n) worst case: O(n^2)
def quickSort(A, start, end):
    if start >= end:
        return
    idx = partition(A, start, end)
    quickSort(A, start, idx - 1)
    quickSort(A, idx + 1, end)

def partition(A, start, end):
    mid = start + (end - start) // 2
    pivot = A[mid]
    A[start], A[mid] = A[mid], A[start]
    left, right = start + 1, end
    while left <= right:
        while left <= right and A[left] < pivot:
            left += 1
        while left <= right and A[right] > pivot:
            right -= 1
        if left <= right:
            A[left], A[right] = A[right], A[left]
            left += 1
            right -= 1
    A[start], A[right] = A[right], A[start]
    return right

def sortColors2(colors, k):
    return quickSort(colors, 1, k, 0, len(colors) - 1)

```

```

def quickSort(colors, colorStart, colorEnd, start, end):
    if colorStart >= colorEnd or start >= end:
        return
    colorPivot = (colorStart + colorEnd) // 2
    left, i, right = start, start, end
    while i <= right:
        if colors[i] <= colorPivot:
            colors[left], colors[i] = colors[i], colors[left]
            i += 1
            left += 1
        elif colors[i] == colorPivot:
            i += 1
        else:
            colors[right], colors[i] = colors[i], colors[right]
            j -= 1
    quickSort(colors, colorStart, colorPivot - 1, start, left - 1)
    quickSort(colors, colorPivot + 1, colorEnd, right + 1, end)

```

```

# avg case: O(n) worst case: O(n^2)
def quickSelect(A, start, end, k):
    if start == end:
        return A[k]
    left, right = start, end
    pivot = A[start + (end - start) // 2]
    while left <= right:
        while left <= right and A[left] < pivot:
            left += 1
        while left <= right and A[right] > pivot:
            right -= 1
        if left <= right:
            A[left], A[right] = A[right], A[left]
            left += 1
            right -= 1
    if k <= right:
        return quickSelect(A, start, right, k)
    if k >= left:
        return quickSelect(A, left, end, k)
    return None

```

Quick Sort 两种常见写法：

1. 互换左右指针，注意：

分成：

$\leq P$	$\geq P$
----------	----------

 ✓

而不是：

$< P$	$\geq P$
-------	----------

 ✗

如图) [1 1 1 1]

[] [1 1 1 1] ✗ 死循环！

2. 柳老师法：把 pivot 提出来，然后分别和左右指针互换，就没上面那个问题。

P	$\leq P$	$\geq P$
---	----------	----------

 [1 1 1 1]
[] [1 1 1 1]

✓ 问题规模变小！OK！

```

from collections import deque
def bfs(root):
    queue = deque([root])
    visited = set([root])
    while queue:
        for i in range(len(queue)): # 分层遍历
            node = queue.popleft()
            for neighbor in node.neighbors:
                if neighbor not in visited:
                    queue.append(neighbor)
                    visited.add(neighbor)

def topSort(graph):
    from collections import deque
    indegrees = {node: 0 for node in graph}
    for node in graph:
        for neighbor in node.neighbors:
            indegrees[neighbor] += 1
    res = []
    queue = deque(node for node in graph if indegrees[node] == 0)
    while queue:
        node = queue.popleft()
        res.append(node)
        for neighbor in node.neighbors:
            indegrees[neighbor] -= 1
            if indegrees[neighbor] == 0:
                queue.append(neighbor)
    if len(res) == len(graph):
        return res
    return -1

def combinationSum(nums, target):
    nums.sort()
    res = []
    dfs(nums, target, 0, [], res)
    return res

def dfs(nums, target, start, state, res):
    if target == 0:
        res.append(state[:]) # deep copy
        return
    if target < 0:
        return
    for i in range(start, len(nums)):
        if i > start and nums[i] == nums[i-1]:
            continue
        state.append(nums[i])
        self.dfs(nums, target - nums[i], i+1, state, res)
        state.pop() # back track

```

```

def binarySearch(A, target):
    start, end = 0, len(A) - 1
    while start + 1 < end: #
        mid = start + (end - start) // 2 #
        if A[mid] < target:
            start = mid #
        elif A[mid] == target:
            end = mid #
        else:
            end = mid #
    if A[start] == target:
        return start
    if A[end] == target:
        return end
    return -1

```

```

def kthLargest(nums, k):
    from heapq import *
    h = []
    for num in nums:
        heappush(h, num)
        if len(h) > k:
            heappop(h)
    return h[0]

```

```

def middleNode(head):
    slowPtr, fastPtr = head, head
    while (fastPtr is not None) and (fastPtr.next is not None):
        slowPtr = slowPtr.next
        fastPtr = fastPtr.next.next
    return slowPtr

def reverseList(head):
    cur = head
    prev = None
    while cur is not None:
        temp = cur.next
        cur.next = prev
        prev = cur
        cur = temp
    return prev

```

```

class Trie:
    def __init__(self):
        self.children = {}
        self.isWord = False

    def insert(self, word):
        p = self
        for c in word:
            if c not in p.children:
                p.children[c] = Trie()
            p = p.children[c]
        p.isWord = True

    def _startsWith(self, prefix):
        p = self
        for c in prefix:
            if c not in p.children:
                return None
            p = p.children[c]
        return p

    def startsWith(self, prefix):
        return self._startsWith(prefix) is not None

    def search(self, word):
        p = self._startsWith(word)
        return p is not None and p.isWord

```

```

class UnionFind:
    def __init__(self):
        self.parents = {}
        self.ranks = {}

    def add(self, x):
        if x in self.parents:
            return
        self.parents[x] = x
        self.ranks[x] = 1

    def find(self, x):
        if self.parents[x] != x:
            self.parents[x] = self.find(self.parents[x])
        return self.parents[x]

    def union(self, x, y):
        p = self.find(x)
        q = self.find(y)
        if p == q:
            return False
        if self.ranks[p] < self.ranks[q]:
            self.parents[p] = q
        elif self.ranks[p] > self.ranks[q]:
            self.parents[q] = p
        else:
            self.parents[q] = p
            self.ranks[p] += 1
        return True

```

↓ path compression

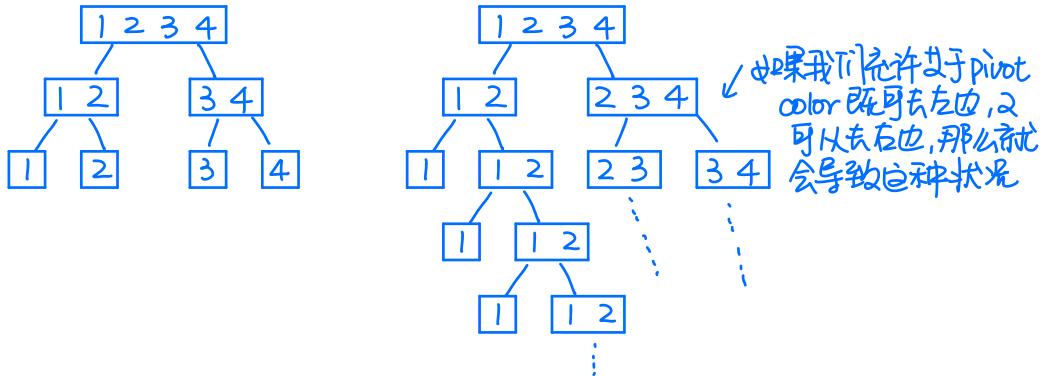
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Lintcode 143 Sort Colors II

1. 分颜色 (这一步很像 merge sort)

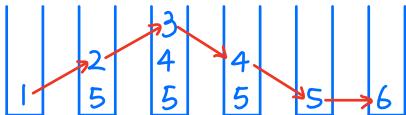
分治时候不能有重合, 比如左边这个OK, 右边这个不行, 会 stack overflow



2. Partition (这一步是类似Quick Sort)

$< P$ $\geq P$ or $\leq P$ $\geq P$ or $\leq P$ $> P$

Leetcode 114 Flatten Binary Tree to Linked List



Lintcode 92 01 背包 + 最多装多满

Lintcode 125 01 背包 + 最大价值

Lintcode 440 完全背包 + 最大价值

Lintcode 562 完全背包 + 刚好填满的方案数

Lintcode 563 01 背包 + 刚好填满的方案数

Lintcode 564 完全背包 + 刚好填满的方案数 (permutation)

Lintcode 798 多重背包 + 最大价值

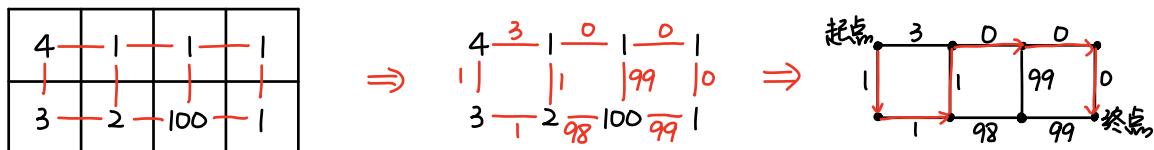
Lintcode 799 多重背包 + 可以选到的方案数

Lintcode 800 01 背包 + 最大概率

Lintcode 801 完全背包 + 最多装多满

		解法1 (recursive DP)	解法2 (iterative DP)
Lintcode 107	Word Break (Any sol)	✗ 栈溢出	✓
Lintcode 582	Word Break II (#sols)	✓	✗ MLE
Lintcode 683	Word Break III (All sols)	✓	✓

Lintcode 258 Map Jump



即转化为一个在 weighted graph 上求最小 cost 路径问题

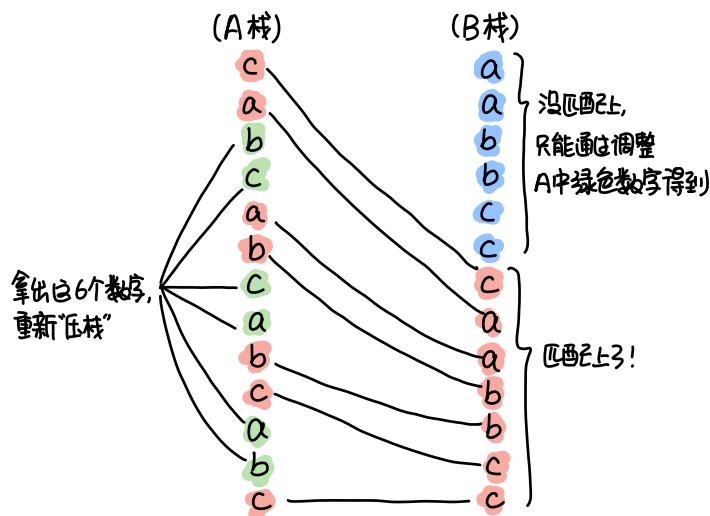
注意：这里为计算每条路径的 cost，我们只关注所有边的权值，取 max (而不是 sum)

换句话说，我们关注的是 bottleneck，而不是路径和。dijkstra 或 bellman ford (不会写) 本神即写

Lintcode 307 Transform String

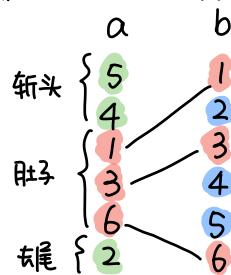
输入：“cabcabcabcbc” 正确答案：6
“aabbcccaabbcc”

1. 它个放入头部的動作有鳥像“压栈”
2. 那么不妨把A和B想象成两个栈
3. 问题即转换成如何把A栈调整成B栈
4. 统计那些没匹配上的数即可



Lintcode 313 Minimum insertion

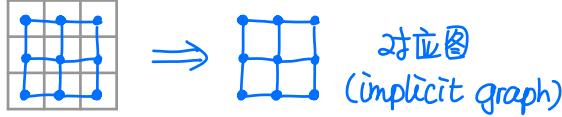
假设 b 是已经排好序的，我们要找到“肚子”最长有多长



Lintcode 611 knight Shortest Path

1. 考虑一个 3×3 的棋盘

2. 上下左右移动



3. 马步移动



Lintcode 1514 Robot Room Cleaner

```

1 DIR = ((-1, 0), (0, 1), (1, 0), (0, -1))
2 class Solution:
3     def cleanRoom(self, robot):
4         self.dfs(0, 0, robot, 0, set())
5
6     def goBack(self, robot):
7         robot.turnLeft()
8         robot.turnLeft()
9         robot.move()
10        robot.turnRight()
11        robot.turnRight()
12
13    def dfs(self, x, y, robot, d, visited):
14        visited.add((x, y)) ① 把当前点加进去
15        robot.clean()
16        for i in range(4):
17            nd = (d + i) % 4
18            dx, dy = DIR[nd]
19            nx, ny = x + dx, y + dy
20            if (nx, ny) not in visited and robot.move():
21                self.dfs(nx, ny, robot, nd, visited)
22                self.goBack(robot)
23            robot.turnRight()

```

```

1 DIR = ((-1, 0), (0, 1), (1, 0), (0, -1))
2 class Solution:
3     def cleanRoom(self, robot):
4         visited = set()
5         visited.add((0, 0))
6         self.dfs(0, 0, robot, 0, visited)
7
8     def goBack(self, robot):
9         robot.turnLeft()
10        robot.turnLeft()
11        robot.move()
12        robot.turnRight()
13        robot.turnRight()
14
15    def dfs(self, x, y, robot, d, visited):
16        robot.clean()
17        for i in range(4):
18            nd = (d + i) % 4
19            dx, dy = DIR[nd]
20            nx, ny = x + dx, y + dy
21            if (nx, ny) not in visited ② 把下一个点加进去:
22                visited.add((nx, ny))
23                self.dfs(nx, ny, robot, nd, visited)
24                self.goBack(robot)
25            robot.turnRight()

```

写法2

Lintcode 1834 Grouping Options

1. 本质上是求同盒同(不为空)的分组问题。

只不过这里用排序的方式来选代表。比如 [1,2] 和 [2,1] 是有价值的，我们选取前者为代表

$dp[i][j]$ 全 i 个球, j 个盒子的方案数

$$= \sum (dp[i-j][k] \text{ for } k \in \text{range}(1, j+1))$$

(先把 j 个工具人到盒子里去定位, 然后把剩下的分为 1 到 j 组)

$$(简化后) = \underbrace{dp[i-1][j-1]}_{\text{① 最小组为1的方案数}} + \underbrace{dp[i-j][j]}_{\text{② 最小组>1的方案数, 虽然每组都>1, 总数就减j, 但还是分成非空的j组 (不然会产生矛盾)}}$$

① 最小组为1的方案数 ② 最小组>1的方案数, 虽然每组都>1,

总数就减j, 但还是分成非空的j组 (不然会产生矛盾)

2. 求同盒同(为空)

$$dp[i][j] = \underbrace{dp[i][j-1]}_{\text{① 最小组为0的方案数}} + \underbrace{dp[i-j][j]}_{\text{② 最小组>0的方案数}}$$

① 最小组为0的方案数 ② 最小组>0的方案数

Leetcode 4 median of two sorted arrays

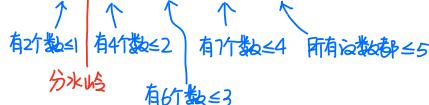
如果我们统计 \leq 每个候选答案(假设已排序)的数的个数 cnt , 这个 cnt 数组一定是(非严格)递增的。

而我们要找的是 the first position where $cnt \geq k$

举个例子: $A=[1,2,3,4]$, $B=[1,2,3,5]$, $k=3$ (肉眼可见答案应该是2)

答案范围: $[1, | 2, 3, 4, 5]$

对应 cnt : $[2, | 4, 6, 7, 8]$



我们要找啥? 最小的一个候选答案 such that 有3个数(或更多) \leq 该候选答案

\Leftrightarrow 第一个候选答案 such that 有3个数(或更多) \leq 该候选答案

回到我们妄图上, 那条分水岭就是我们要找!

1) 在分水岭之前, \leq 候选答案的数不足3个

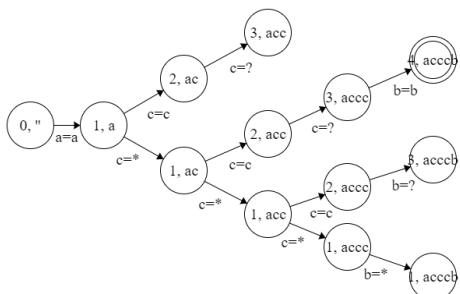
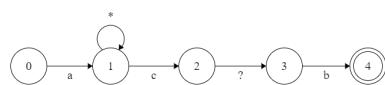
2) 在分水岭之后, \leq 候选答案的数到达3个以上

如果分水岭存在, 那么就是一个典型包围圈问题, 二分法一定可以找到我们答案。

现在的问题是, 有没有可能这个分水岭不存在? 或者说这个 $OOXX$ 的 pattern 不存在?

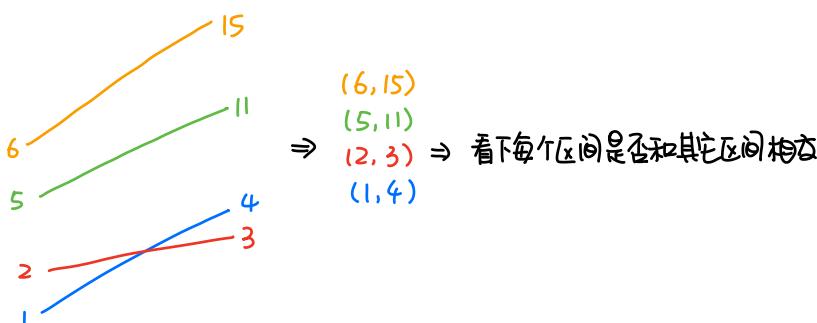
我认为是不可能的, 因为 cnt 数组一定是(非严格)递增的, 自然会有那么一条分水岭。

Leetcode 44 Wildcard matching

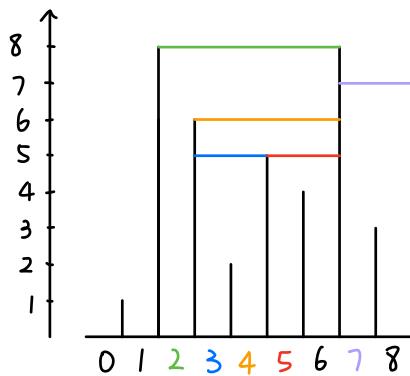


$(a * c ? b, acccb)$
 $\downarrow a=a$
 $(*c ? b, cccb)$
 $\downarrow c=?$
 $(c ? b, cccb)$
 $\downarrow c=c$
 $(?b, cccb)$
 $\downarrow c=?$
 $(b, cccb)$
 $\downarrow c=?$
 (b, cb)
 $\downarrow c=c$
 $(?b, cb)$
 $\downarrow c=?$
 (b, b)
 $\downarrow b=b$
 $(?b, b)$
 $\downarrow b=?$
 (b, b)
 $\downarrow b=?$
 $([], [])$
 $(b, [])$

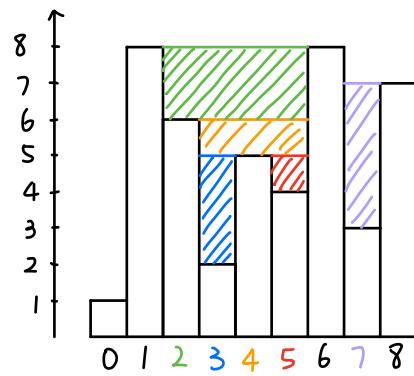
[困难题] 相交的直线, 给出 n 条不同的直线, 每条直线可以用两个参数 (k, b) 表示, 即 $y = kx + b$. 同时规定一个 x 轴上的区间范围 $[l_0, h_1]$, 问在这个范围内, 有多少条直线至少与其他一条直线相交.



Leetcode 11 Container with Most Water

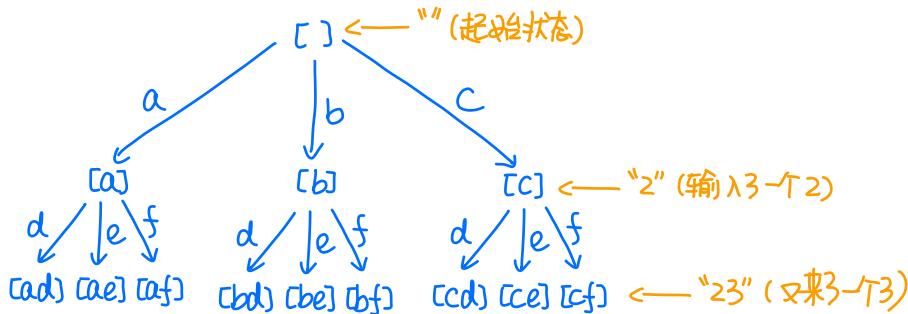


Leetcode 42 Trapping Rain Water

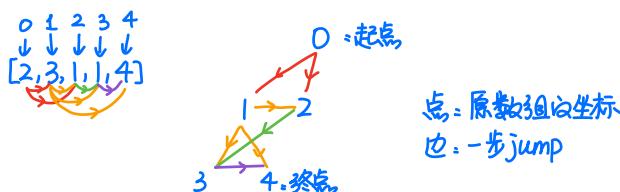


Leetcode 17 Letter Combinations of a Phone Number

这道题里面，图的构成是取决于输入的。假如输入为“23”：

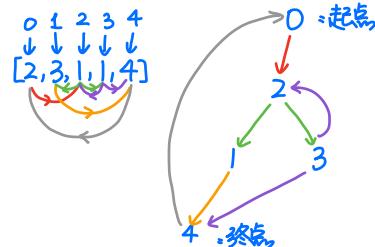


Leetcode 55 Jump Game & Leetcode 45 Jump Game II



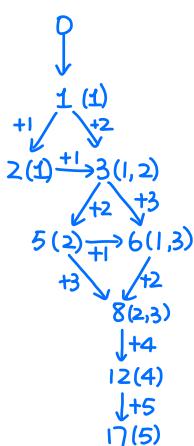
转换成了一个在简单图上求最短路径的问题 ⇒ 直接BFS或并队列

Leetcode 1306 Jump Game III



Leetcode 403 Frog Jump

- BFS
- 1) 扩展遍历
- 2) 不需要记录seen



Leetcode 287 Find the duplicate number

1. 两种标记方法

0 1 2 3 4
[2 1 4 2 3]

1) 用下标来标记

$0 \rightarrow \underline{2} \rightarrow 4 \rightarrow 3$

环的起点就是重复值

2) 用值来标记

$\underline{2}' \rightarrow 4 \rightarrow 3 \rightarrow \underline{2}''$

指向环的点就是重复值

2) 注意图中可能会存在多个环

0 1 2 3 4 5
[5 2 4 5 1 3]

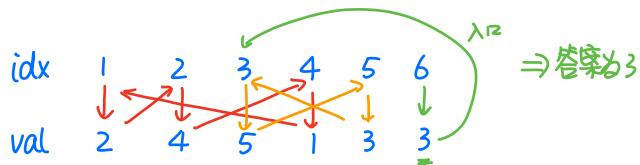
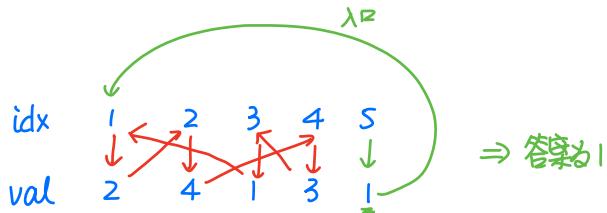
$0 \rightarrow 5 \rightarrow 3$

$1 \rightarrow 2 \rightarrow 4$

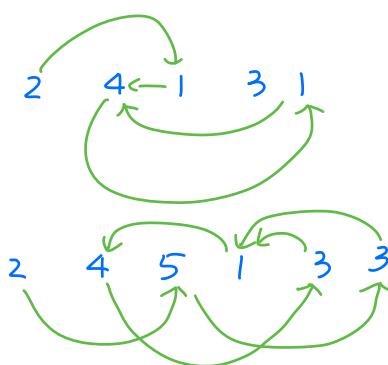
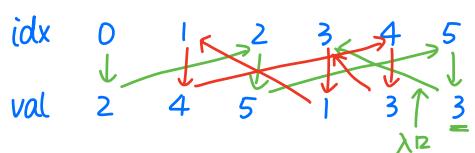
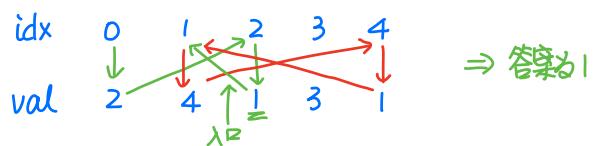
$5 \rightarrow 3 \rightarrow 5$

$2 \rightarrow 4 \rightarrow 1$

① 287 群主做法 (1-index)

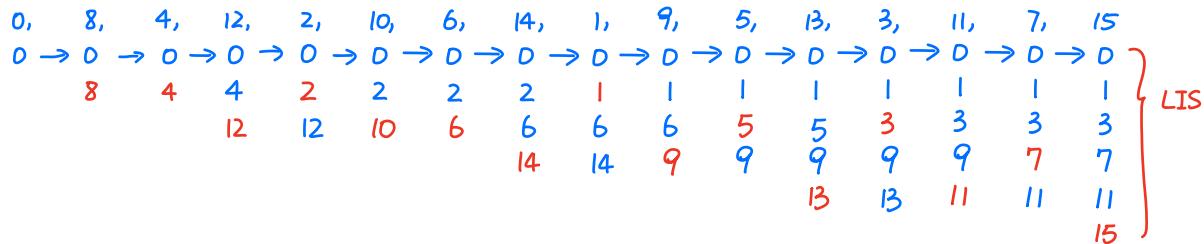


① 287 普通做法 (0-index)



Leetcode 300 LIS

$dp[i]$ 表示找长度为 i 的递增子列，长度是多少。假如当前处理的数为 x ，如果前面有 $i-1$ 个比 x 小的， x 又比 $dp[i]$ 小，那么 x 就是更小的符合条件的 $dp[i]$

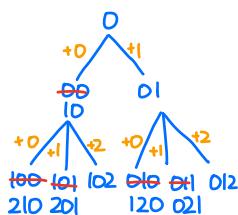


Leetcode 903 Valid Permutation for DI sequence

permutation 还可以这样生成：

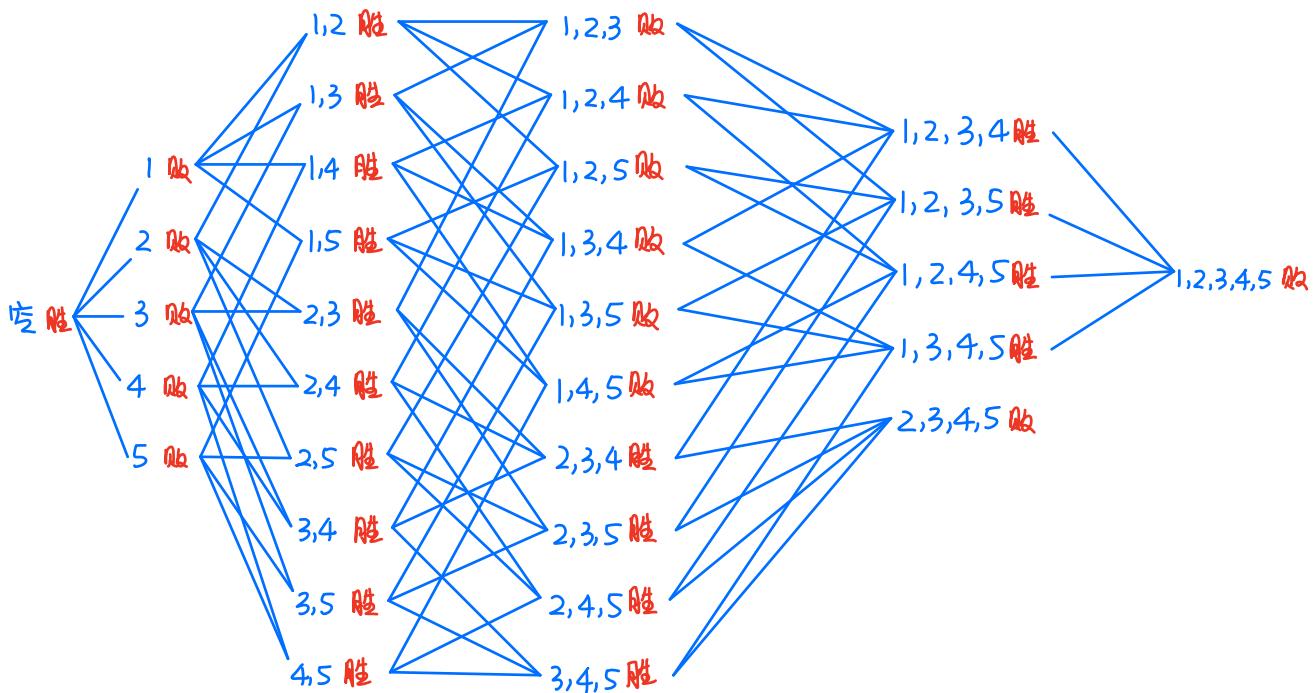
1) 生成 0~i 的全排列，比如 012, 021, 102, 120, 201, 210

2) 在每一个上一轮生成的全排列后面贴一个 0~i+1 的数，并把之前位上大于等于当前数的进行提升



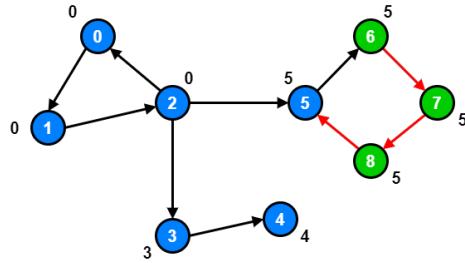
Leetcode 464 Can I win

$n=5$, target = 14

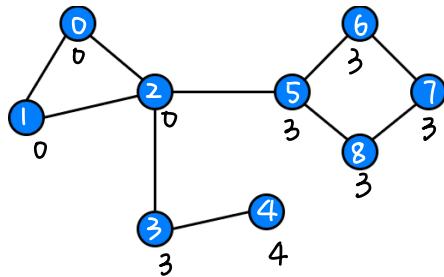


Leetcode 1192 Critical Connection in a Network

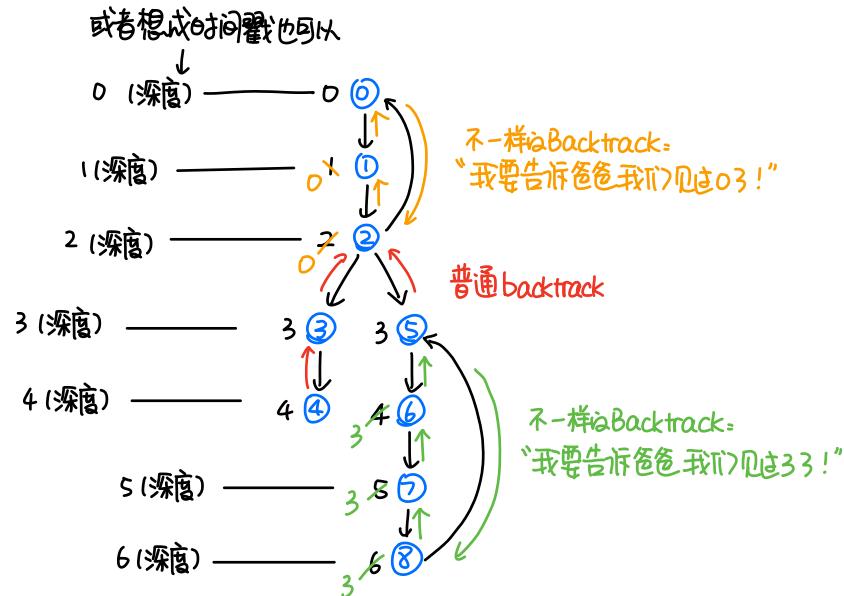
解法1: Tarjan Algorithm, 维护一个全局的时间戳, 称为 low link
 所有 $u \rightarrow v$ 的边中, 只要 u 的时间戳小于 v 的时间戳 $\Rightarrow u \rightarrow v$ 是关键连接, 称为 bridge
 $\Rightarrow 2 \rightarrow 5, 2 \rightarrow 3, 3 \rightarrow 4$



解法2: 伪 Tarjan(?), 利用 DFS 的递归深度来维护一个局部时间戳

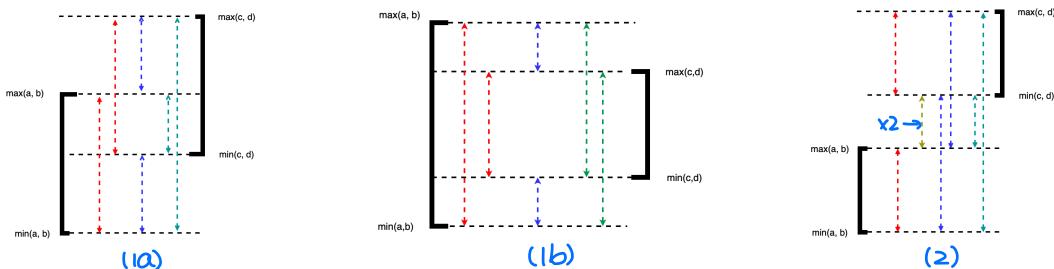


具体过程如下:



Leetcode 1330 Reverse Subarray to Maximum Array Value

$\cdots, a, [b, \dots, c], d, \cdots$
 \downarrow
 $\cdots, a, [c, \dots, b], d, \cdots$
 $\text{diff} = |a - c| + |b - d| - |a - b| - |c - d|$



分情况讨论：(1)如果 $[\min(a,b), \max(a,b)]$ 和 $[\min(c,d), \max(c,d)]$ 这两个区间有重合,那么结果不会变吗
 (2)如果 $[\min(a,b), \max(a,b)]$ 和 $[\min(c,d), \max(c,d)]$ 这两个区间无重合,则增值如图中黄线所示(x2)

Leetcode 1439 Find the kth smallest sum of a matrix with sorted rows

$\{a_1, a_2, a_3, a_4, a_5, a_6, a_7, \dots, a_n\}$
 $b_1, b_2, b_3, b_4, b_5, b_6, b_7, \dots, b_n$
 $c_1, c_2, c_3, c_4, c_5, c_6, c_7, \dots, c_n$

Claim: $a_5 + b_i + c_i$ 不可能為第4小段 sum, b_i, i

反证法：

假如 $a_5 + b_i + c_j$ 为第4小段 sum, $\exists i, j$

⇒ 有且仅有3个sum比0.5+bit[i]小①

23

$$\begin{aligned} a_5 + b_1 + c_j &\geq a_5 + b_1 + c_i \\ &> a_4 + b_1 + c_i \\ &> a_3 + b_1 + c_i \\ &> a_2 + b_1 + c_i \\ &> a_1 + b_1 + c_i \end{aligned}$$

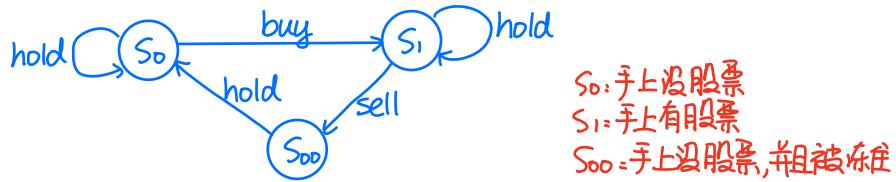
⇒ 我们找到了 4 个 sum 比 Q_{stbitb} 小②

①、②产矛盾，证毕

LeetCode 1954 Minimum Garden Perimeter to Collect Enough Apples

8	7	6	5	4	5	6	7	8	$i=1: d(1) = 8 \times 1 + 8 \times 2 - 4 \times 1 - 4 \times 2$
7	6	5	4	3	4	5	6	7	$i=2: d(2) = 8 \times 2 + 8 \times 3 + 8 \times 4 - 4 \times 2 - 4 \times 4$
6	5	4	3	2	3	4	5	6	$i=3: d(3) = 8 \times 3 + 8 \times 4 + 8 \times 5 + 8 \times 6 - 4 \times 3 - 4 \times 6$
5	4	3	2	1	2	3	4	5	$i=4: d(4) = 8 \times 4 + 8 \times 5 + 8 \times 6 + 8 \times 7 + 8 \times 8 - 4 \times 4 - 4 \times 8$
4	3	2	1	0	1	2	3	4	$\Rightarrow d(i) = 8 \times (i+2i)(i+1)/2 - 4i - 4 \times 2i$
5	4	3	2	1	2	3	4	3	$= 4 \times 3i(i+1) - 4i - 8i$
6	5	4	3	2	3	4	5	2	$= 12i^2 + 12i - 12i$
7	6	5	4	3	4	5	6	1	$= 12i^2$
8	7	6	5	4	5	6	7	8	$\Rightarrow \sum_{i=1}^n d(i) = 12 \times 1^2 + 12 \times 2^2 + 12 \times 3^2 + 12 \times 4^2 + \dots + 12 \times n^2$
									$= [2 \times n(n+1)(2n+1)]/6$
									$= 2n(n+1)(2n+1)$

Leetcode 309 Best time to buy and sell stock with cool down

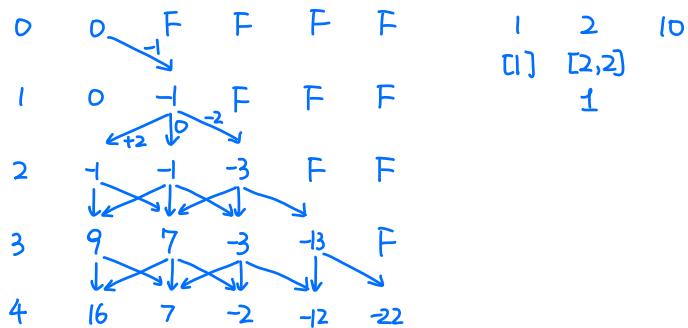


Lintcode 1691. Best time to buy & sell stock V

$dp[i][j]$ - profit of holding j stocks on day i

stock price $a = [1, 2, 10, 9]$

0 1 2 3 4 → day



[讨论题目] We are writing a tool to help users manage their calendars at a corporation. Given a list of meeting times and sizes and a list of the available meeting room sizes, find a way to fit all of the meetings in a big enough room

room = [3, 4, 5] # 会议室大小

meeting = [(7, 9, 2), (8, 12, 3), (9, 11, 5), (9, 11, 4)] # 起始时间, 结束时间, 需求

先预处理一下, 找到能满足需求的最小会议室大小

meeting = [(7, 9, 3), (8, 12, 3), (9, 11, 5), (9, 11, 4)]

先按会议室大小, 再按开始时间排序

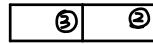
meeting = [(9, 11, 5), (9, 11, 4), (7, 9, 3), (8, 12, 3)]

然后, 贪心地进行会议安排即可, 如果安排不了, 就返回 Impossible

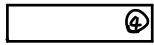
5



4



3



1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 → t