## **AP Physics C: Electricity and Magnetism**From the 2015 Administration

Humble Academy 航铂教育

## **Humble**Academy **航铂教育**

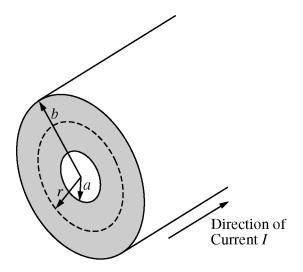
专业国际课程辅导 AP、IB、A Level、OSSD、国际学科竞赛、学术拓展训练

南京校区 秦淮区中山南路 1 号南京中心 47 楼

## I Multiple Choice Questions

Time: 45 minutes 35 Questions

**Directions:** Each of the questions or incomplete statements below is followed by five suggested answers or completions. Select the one that is best in each case and then fill in the corresponding circle on the answer sheet.

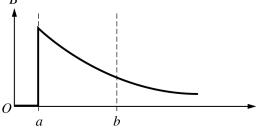


1. A long, cylindrical conductor with inner radius a and outer radius b carries a current I distributed uniformly over its cross section (the shaded region shown above). Which of the following graphs best shows the magnitude of the magnetic field B as a function of the distance r from the axis of the conductor?

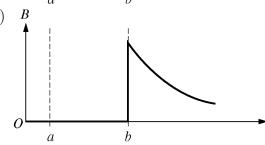
(A) *B* 



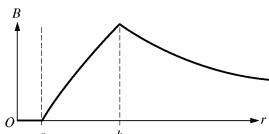
(B)



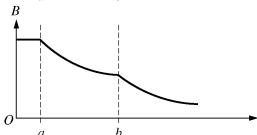
(C)



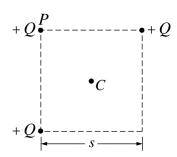
(D)



(E)



See the instruction for questions 2 to 3.



Three particles each with charge +Q are placed on three corners of a square, as shown above. The sides of the square have length s. Point C is at the center of the square.

2. What is the direction of the electric field at point C?







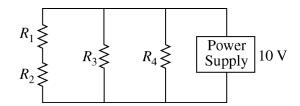




- 3. The particle at corner P is allowed to move while the other two particles are held in place. What is the work done by the electric field as the particle at corner P moves to infinity?
  - (A)  $\frac{2kQ^2}{s}$

- (B)  $\frac{2kQ}{s}$  (C)  $\frac{kQ}{s^2}$  (D)  $\frac{kQ^2}{s^2}$  (E)  $\frac{2kQ^2}{s^2}$

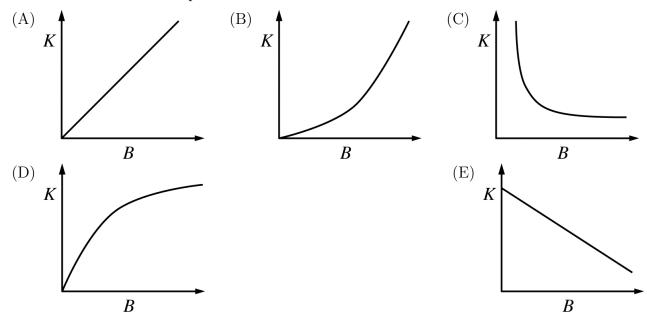
See the instruction for questions 4 to 5.



Four resistors, all with the same resistance R, are connected as shown above.

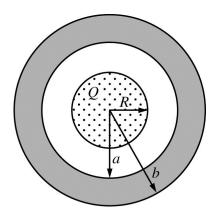
- 4. What is the equivalent resistance of the network?
  - (A) 4R
- (B) 3R
- (C) 5R/2
- (D) R
- (E) 2R/5
- 5. If the power supply produces 10 V and the resistance R is 5  $\Omega$ , what is the current in resistor  $R_4$  ?
  - (A) 15 A
- (B) 5 A
- (C) 2A
- (D) 1/2 A
- (E) 1/5 A

6. A positron (charge +e, mass  $m_e$ ) moves in a circular path of radius R due to a uniform magnetic field of strength B applied perpendicular to the plane of the circle. If B is varied, which of the following best represents a graph of the kinetic energy of the positron as a function of B so that the positron maintains the same radius R?



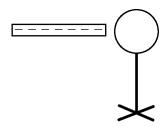
- 7. The current in a wire is 5 A. What is the value of the closed integral  $\oint \vec{B} \cdot d\vec{\ell}$  of the magnetic field along a closed path around the wire?
  - (A)  $\pi \times 10^{-7} \,\mathrm{T} \cdot \mathrm{m}$
  - (B)  $2\pi \times 10^{-7} \,\mathrm{T} \cdot \mathrm{m}$
  - (C)  $10\pi \times 10^{-7} \,\mathrm{T \cdot m}$
  - (D)  $20\pi \times 10^{-7} \,\mathrm{T \cdot m}$
  - (E)  $40\pi \times 10^{-7} \,\mathrm{T \cdot m}$

See the instruction for questions 8 to 9.



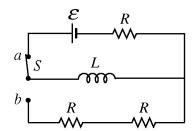
An insulated nonconducting sphere of radius R has a charge Q uniformly distributed throughout its volume. It is surrounded by a concentric spherical conducting shell of inner radius a and outer radius b, as shown in the figure above. There is no net charge on the conducting shell. Let a be the electric field magnitude at a distance a from the center of the spheres.

- 8. Which of the following represents a correct application of Gauss's law for r > b?
  - (A)  $0 = E(4\pi)r^2$
  - (B)  $\frac{Q}{\epsilon_0} = E(4\pi)r^2$
  - (C)  $\frac{Q}{\epsilon_0} = E(4\pi)R^2$
  - (D)  $\frac{Qr^3}{\epsilon_0 R^3} = E(4\pi)r^2$
  - (E)  $\frac{Qa^3}{\epsilon_0 R^3} = E(4\pi)r^2$
- 9. Which of the following represents a correct application of Gauss's law for r < R?
  - (A)  $0 = E(4\pi)r^2$
  - (B)  $\frac{Q}{\epsilon_0} = E(4\pi)r^2$
  - (C)  $\frac{Q}{\epsilon_0} = E(4\pi)R^2$
  - (D)  $\frac{Qr^3}{\epsilon_0 R^3} = E(4\pi)r^2$
  - (E)  $\frac{Qa^3}{\epsilon_0 R^3} = E(4\pi)r^2$



- 10. A spherical conductor is on an insulating stand, as shown in the figure above. A negatively charged rod is brought close to the sphere but does not touch the sphere. Which of the following describes the resulting charge on the sphere?
  - (A) Positive
  - (B) Negative
  - (C) No net charge, but the sphere is polarized with positive charge on the left side.
  - (D) No net charge, but the sphere is polarized with negative charge on the left side.
  - (E) No net charge and no polarization

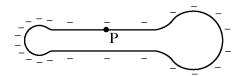
See the instruction for questions 11 to 13.



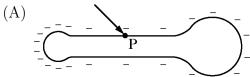
In the circuit above, all of the resistors have the same resistance R. Switch S has been in position a for a very long time.

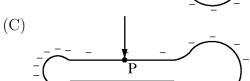
- 11. What is the energy stored by the inductor?
  - (A) Zero
- (B)  $\frac{\mathcal{E}^2}{R}$
- (C)  $\frac{1}{2}L\mathcal{E}^2$
- (D)  $\frac{1}{2}L\frac{\mathcal{E}}{R}$
- (E)  $\frac{1}{2}L\frac{\mathcal{E}^2}{R^2}$
- 12. The switch is now moved instantaneously to position b. The voltage across the inductor immediately after the move is
  - (A) zero
  - (B) greater than zero but less than  $\mathcal{E}$
  - (C)  $\mathcal{E}$
  - (D) greater than  $\mathcal{E}$  but not infinite
  - (E) infinite
- 13. The time constant when the switch is in position a is  $\tau_0$ . How does the time constant when the switch is in position b compare to  $\tau_0$ ?
  - (A) It is zero.
  - (B) It is less than  $\tau_0$  but greater than zero.
  - (C) It is equal to  $\tau_0$ .
  - (D) It is greater than  $\tau_0$  but not infinite.
  - (E) It is infinite.

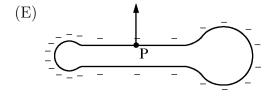
- 14. If a dielectric is inserted between the plates of a capacitor while the capacitor maintains its connection to a constant voltage source, which of the following is true?
  - (A) The capacitance of the capacitor is unchanged.
  - (B) The charge on the capacitor plates increases.
  - (C) The potential difference across the capacitor increases.
  - (D) The electric field between the capacitor plates increases.
  - (E) The electric field between the capacitor plates decreases.

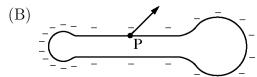


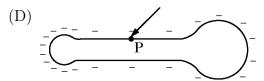
15. The conductor shown above is given a negative charge that spreads over its surface. Which of the following best represents the direction of the electric field at the point P on the cylindrical portion of the conductor?

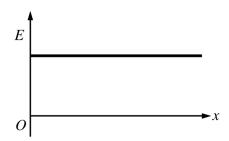










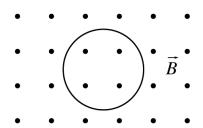


- 16. The graph above shows the electric field E as a function of x, where x is the distance from a given charge arrangement in an xyz-coordinate system. Which of the following could be the arrangement?
  - (A) A positive point charge at x = 0
  - (B) Positive charges uniformly distributed inside a sphere with x=0 on the sphere's surface
  - (C) Positive charges uniformly distributed on the surface of a sphere with x=0 on the sphere's surface
  - (D) Positive charges uniformly distributed along the y-axis
  - (E) Positive charges uniformly distributed over the yz-plane

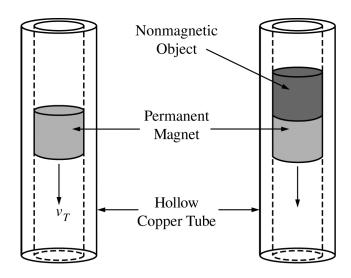
- 17. A negatively charged particle moves in the positive x-direction in a uniform magnetic field directed in the positive y-direction. The particle will experience a force directed in the
  - (A) positive z-direction
  - (B) negative z-direction
  - (C) positive x-direction
  - (D) negative x-direction
  - (E) positive y-direction



- 18. Two wires are 10 cm apart, as shown in the figure above. One wire has a current of 3 A to the right, and the other wire has a current of 5 A to the left. What is the magnitude of the magnetic field, in teslas, at the point midway between the wires?
  - (A)  $\frac{20 \times 4\pi \times 10^{-7}}{\pi}$
  - (B)  $\frac{40 \times 4\pi \times 10^{-7}}{\pi}$
  - (C)  $\frac{80 \times 4\pi \times 10^{-7}}{\pi}$
  - (D)  $\frac{100 \times 4\pi \times 10^{-7}}{\pi}$
  - (E)  $\frac{160 \times 4\pi \times 10^{-7}}{\pi}$

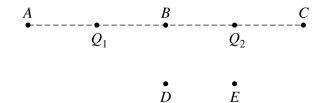


- 19. A uniform magnetic field  $\vec{B}$  is directed out of the page, as represented above. A loop of wire of area  $0.8\,\mathrm{m}^2$  is in the plane of the page. At a certain instant, the field has a magnitude of  $5.0\,\mathrm{T}$  and is decreasing at the rate of  $0.5\,\mathrm{T/s}$ . The magnitude of the induced emf in the wire loop at this instant is most nearly
  - (A) 0.4 V
- (B) 1.6 V
- (C) 2.0 V
- (D) 4.0 V
- (E) 8.0 V



- 20. A permanent magnet of mass M is dropped down the interior of a hollow cylindrical tube made of copper, as shown at left in the figure above. Friction between the inside of the tube and the magnet is negligible. As the magnet moves downward, an upward magnetic force  $F_B$  is induced, and the magnet's velocity quickly reaches a constant terminal value  $v_T$ . A nonmagnetic object of mass M is attached to the permanent magnet and the drop is repeated, as shown at right in the figure above. When terminal velocity is reached, how do the new values of  $F_B$  and  $v_T$  compare with their values without the object?
  - (A)  $F_B$  and  $v_T$  are the same.
  - (B)  $F_B$  is larger and  $v_T$  is smaller.
  - (C)  $F_B$  is smaller and  $v_T$  is larger.
  - (D)  $F_B$  and  $v_T$  are both larger.
  - (E)  $F_B$  and  $v_T$  are both smaller.

See the instruction for questions 21 to 22.



Two point charges,  $Q_1 = +3 \,\mu\text{C}$  and  $Q_2 = -3 \,\mu\text{C}$ , are situated as shown in the figure above.

- 21. At which labeled point is the magnitude of the electric field greatest?
  - (A) A
- (B) B
- (C) C
- (D) D
- (E) E

- 22. At which labeled point is the electric potential the lowest?
  - (A) A
- (B) B
- (C) C
- (D) D
- (E) E

23. A loop of wire with resistance  $2\Omega$  lies in a magnetic field. The magnetic flux  $\phi_m$  through the loop as a function of time t is given by  $\phi_m = (2t^2 + 2t)$ , where  $\phi_m$  is in tesla · meters squared and t is in seconds. What is the current in the loop at t = 3 s?

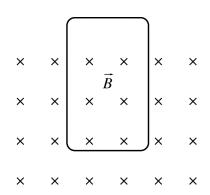
(A) 6 A

(B) 7A

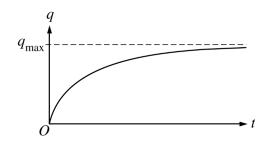
(C) 12 A

(D) 14 A

(E) 24 A



- 24. A conducting loop in the plane of the page is partially inside a uniform magnetic field  $\vec{B}$ , as shown in the figure above. What is the direction of the net force on the loop as the magnitude of the magnetic field decreases?
  - (A) Toward the left
  - (B) Toward the right
  - (C) Toward the top of the page
  - (D) Toward the bottom of the page
  - (E) Out of the page



- 25. A capacitor of capacitance C is connected in series with resistance R and a battery of emf  $\mathcal{E}$ . The graph above shows the charge q on the capacitor approaching a value  $q_{\max}$  with increasing time t. What is  $q_{\text{max}}$ ?
  - (A)  $\frac{R}{C\mathcal{E}}$
- (B)  $\frac{RC}{\mathcal{E}}$  (C)  $\frac{\mathcal{E}}{RC}$  (D)  $\frac{\mathcal{E}}{R}$
- (E)  $C\mathcal{E}$

26. A 9 V battery is connected to a  $450\,\Omega$  load. If the internal resistance of the battery is negligible, how long will it take for 2 C to pass through the load?

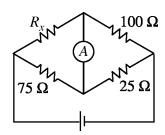
(A) 0.01 s

(B)  $0.02 \, \mathrm{s}$ 

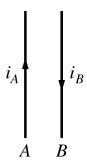
(C)  $25 \, s$ 

(D)  $50 \, s$ 

(E) 100 s

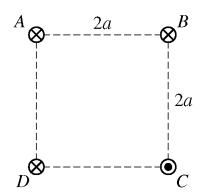


- 27. In the circuit shown above, the resistances have the values given and there is no current in the ammeter A. What is the value of  $R_x$ ?
  - (A)  $25\Omega$
- (B)  $33\Omega$
- (C)  $75\Omega$
- (D)  $100 \Omega$
- (E)  $300 \Omega$



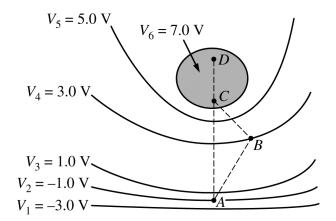
28. Two parallel wires, A and B, have currents in opposite directions, as shown in the figure above. Current  $i_B$  is twice as large as  $i_A$ . The force on wire A due to current  $i_B$  has magnitude F. Which of the following correctly describes the direction and magnitude of the force on wire B due to current  $i_A$ ?

	<u>Direction</u>	Magnitude
(A)	To the left	F
(B)	To the left	2F
(C)	To the left	4F
(D)	To the right	F
(E)	To the right	2F



- 29. Four long, straight wires are arranged at the vertices of a square with sides of length 2a, as shown in the figure above. Each wire carries a current I. The currents of three of the wires are directed into the page, while the current at point C is directed out of the page. What is the magnetic field at the center of the square?
  - (A)  $\frac{\mu_0 I}{\sqrt{2}\pi a}$  toward wire D
  - (B)  $\frac{\mu_0 I}{\sqrt{2}\pi a}$  toward wire B
  - (C)  $\frac{\mu_0 I}{\sqrt{2}\pi a}$  toward the bottom of the page
  - (D)  $\frac{\mu_0 I}{2\pi a}$  toward wire D
  - (E)  $\frac{\mu_0 I}{2\pi a}$  toward wire B

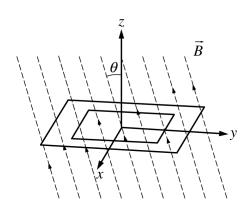
See the instruction for questions 30 to 31.

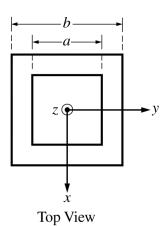


Equipotential lines due to an electric field in a certain region of space are illustrated in the figure above. Points A and B are located on lines  $V_2$  and  $V_4$ , respectively, and points C and D are located within the equipotential region  $V_6$ .

- 30. At which labeled point is the magnitude of the electric field the greatest?
  - (A) A
- (B) B
- (C) C
- (D) D
- (E) It is the same at all the points.
- 31. How much work is required by an external force to move a  $2.0\,\mu\text{C}$  charge from rest at point A to rest at point D via the path ABCD?
  - (A)  $2.0 \,\mu J$
- (B)  $3.0 \,\mu J$
- (C)  $4.0 \,\mu J$
- (D)  $12 \,\mu J$
- (E)  $16 \,\mu J$

- 32. A proton p (charge +e, mass  $m_p$ ) collides head-on with a deuteron d (charge +e, mass  $2m_p$ ). During the collision the particles interact through an electrostatic Coulomb force. Which of the following statements is true about the accelerations  $\vec{a}_p$  of the proton and  $\vec{a}_d$  of the deuteron during the collision?
- (A)  $\vec{a}_p = -2\vec{a}_d$  (B)  $\vec{a}_p = -\vec{a}_d$  (C)  $\vec{a}_p = -\vec{a}_d/2$  (D)  $\vec{a}_p = \vec{a}_d$  (E)  $\vec{a}_p = 2\vec{a}_d$

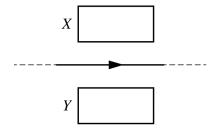




- 33. Two square loops of thin metal wire are positioned on the horizontal xy-plane in a magnetic field  $\vec{B}$  that is directed upward through the loops at an angle  $\theta$  with the vertical z-axis, as shown in the figure above. The small loop has side length a. The large loop has side length b. The magnetic flux in the space between the loops is
  - (A)  $B(b^2-a^2)\sin\theta$  (B)  $B(b^2-a^2)\cos\theta$  (C)  $B(b-a)^2\cos\theta$  (D)  $Ba^2\sin\theta$  (E)  $Bb^2\sin\theta$

## See the instruction for questions 34 to 35.

General instruction (if any) goes here.



Two identical rectangular conducting loops and a very long, straight wire lie in the plane of the page, as shown above. The loops are equal distances from the wire, and there is a current to the right in the wire.

34. If the current in the wire is decreasing, what is the direction of the induced current, if any, in each of the loops?

	$\underline{\text{Loop } X}$	$\underline{\text{Loop } Y}$
(A)	Counterclockwise	Clockwise
(B)	Counterclockwise	Counterclockwise
(C)	Clockwise	Counterclockwise
(D)	Clockwise	Clockwise
(E)	None	None

35. If the current in the wire is constant and the wire is moved toward loop X, what is the direction of the induced current, if any, in each of the loops?

$\underline{\text{Loop } X}$	$\underline{\text{Loop } Y}$
(A) Counterclockwise	Clockwise
(B) Counterclockwise	Counterclockwise
(C) Clockwise	Counterclockwise
(D) Clockwise	Clockwise
(E) None	None