

## EXAMPLE – dsolve

```
[x, y] = dsolve('Dx+y=0,D2y-Dy=0')
```

```
[x, y] = dsolve('Dx+y=0,D2y-Dy=0','x(0)=2,y(0)=1,Dy(0)=1')
```

```
[x, y] = dsolve('Dx+y=0,D2y-Dy=0','x(0)=2,y(0)=1,Dy(0)=1,D2y(0)=4')
```

What will happen if input **contains third-order differential** equation?

```
[x, y] = dsolve('Dx+y=0,D3y-Dy=0','x(0)=2,y(0)=1,Dy(0)=1,D2y(0)=4')
```

If the input like this,

```
[x, y] = dsolve('Dx+y=0,D6y-D4y=0','x(0)=2,y(0)=1,Dy(0)=1,D2y(0)=4')
```

If you do not like 't' as variant

```
[x, y] = dsolve('Dx+y=0,D6y-D4y=0','x(0)=2,y(0)=1,Dy(0)=1,D2y(0)=4','p')
```

## EXAMPLE – ode

```
tspan = [0 5];  
y0 = 0;  
[t,y] = ode45(@(t,y) 2*t^2 + t, tspan, y0);  
plot(t,y);
```

What if a more complex equation?

$$y_1'' - \mu (1 - y_1^2) y_1' + y_1 = 0,$$

$$\begin{cases} dx(1) = x(2) \\ dx(2) = x(3) \\ \dots \\ dx(n-1) = x(n) = f(t, x(n-1), \dots, x(2), x(1)) \end{cases}$$

$$y_1' = y_2$$

$$y_2' = \mu(1 - y_1^2)y_2 - y_1.$$

## EXAMPLE – ode

```
function dx=myequ(t,x)
    dx = zeros(2,1);
    dx(1) = x(2);
    dx(2) = (1-x(1)^2)*x(2)-x(1);
end
```

```
function dx=myequ(t,y)
    dx = [x(2); (1 - x(1) ^ 2) * x(2) - x(1)]
```

Coefficient input:

```
function dx=myequ(t,x, alpha, beta)
    dx = zeros(2,1);
    dx(1) = x(2);
    dx(2) = (1-alpha*x(1)^2)*x(2)-beta*x(1);
End
```

```
function dx=myequ(t,y,alpha,beta)
    dx = [x(2); (1 - alpha*x(1) ^ 2) * x(2) - beta*x(1)]
```

```
[t,y] = ode45(@(t,y) odefcn(t,y,A,B), tspan, y0)
```

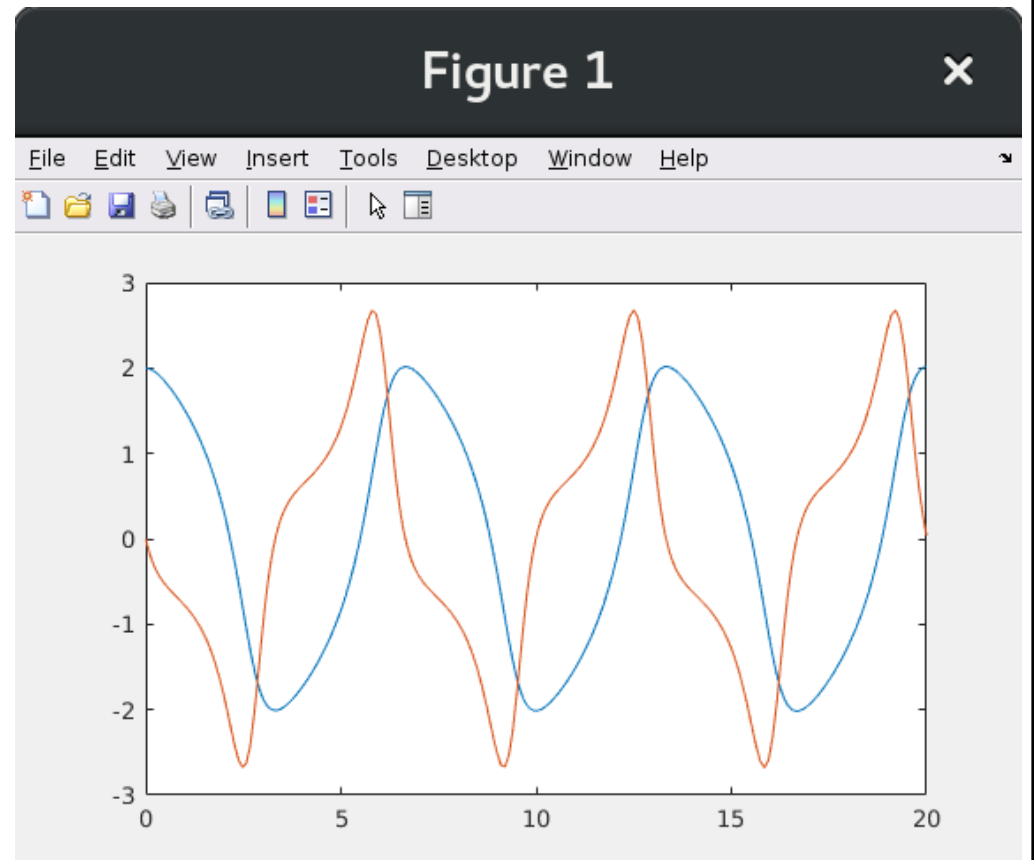
# EXAMPLE – ode

$\text{SpanT} = [0 \ 20]$

$\text{X0} = [2 \ 0]$

`[t, x] = ode45(@myequ,SpanT,X0);`

`plot(t, x)`



# EXAMPLE – ode

If we only want some solutions for certain t:

...

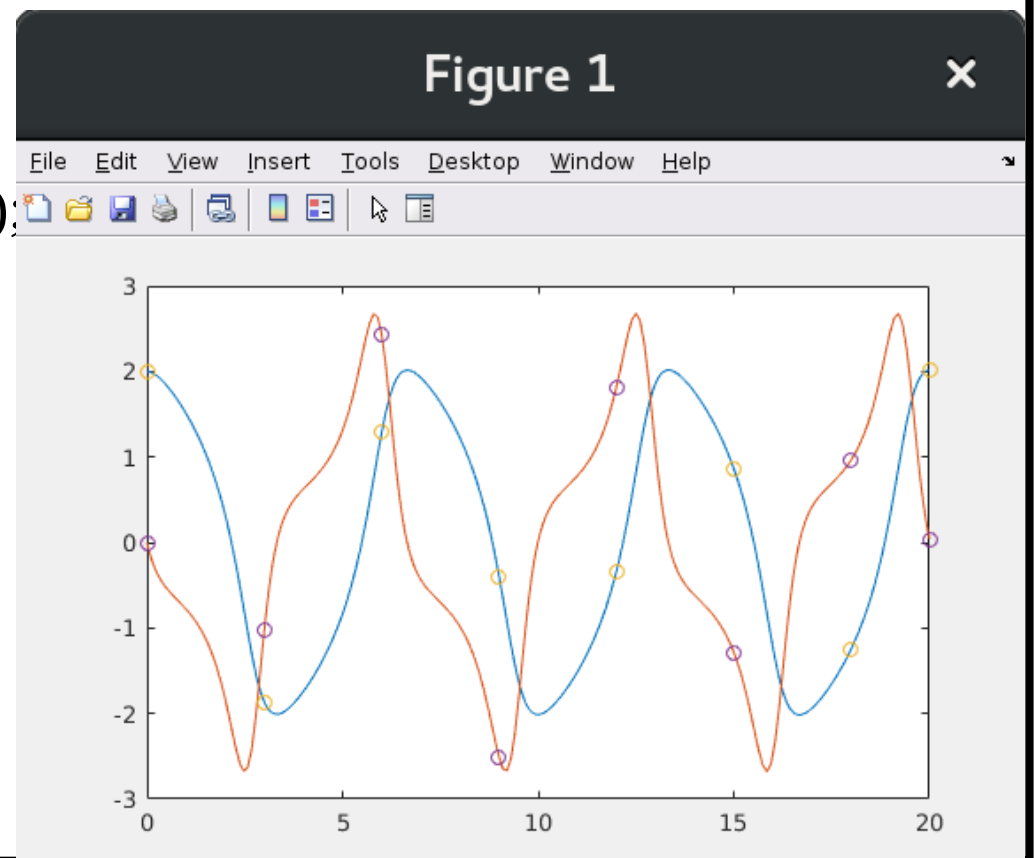
Hold on

SpanT = [0 3 6 9 12 15 18 20]

X0 = [2 0]

[t, x] = ode45(@myequ,SpanT,X0);

plot(t, x, 'o')



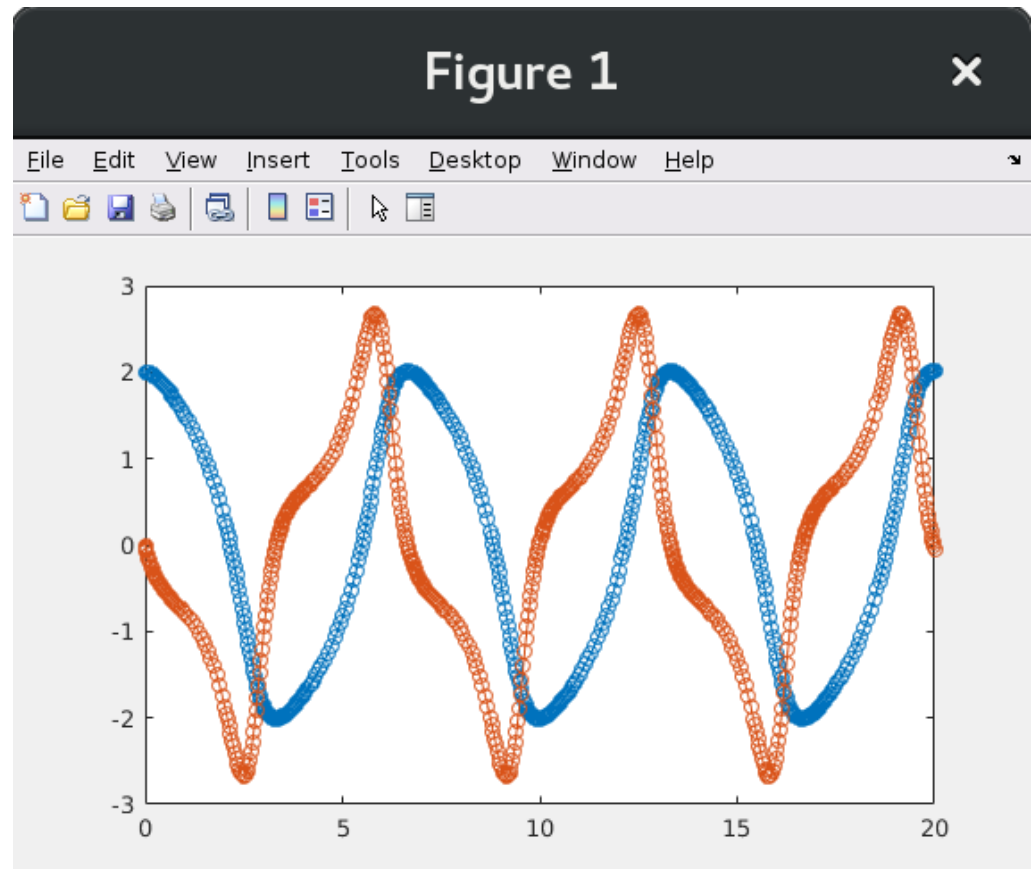
# EXAMPLE – ode

SpanT = [0 20]

X0 = [2 0]

options = odeset('RelTol',1e-5,'Stats','on','OutputFcn',@odeplot)

[t, x] = ode45(@myequ,SpanT,X0, options);



## EXAMPLE – Compare different ode methods

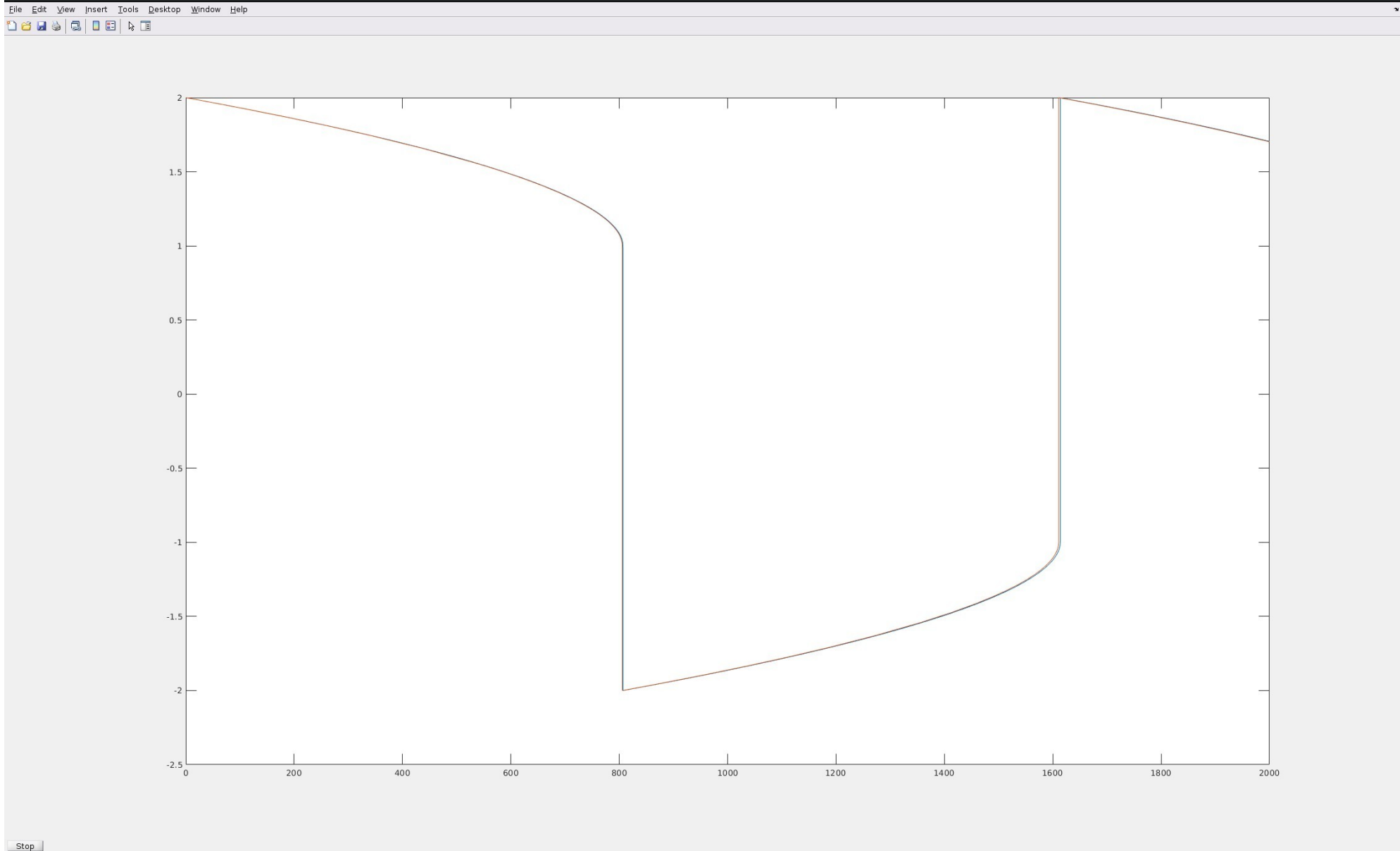
```
function dx=myequ3(t,x)
dx = [x(2); 1000*( 1 - x(1) ^ 2) * x(2) - x(1)];
End
```

```
[t, y] = ode45(@myequ3,[0 2000],[2 0]);
[t2, y2] = ode15s(@myequ3,[0 2000],[2 0]);
plot(t, y(:,1))
hold on
plot(t2, y2(:,1))
```

```
[t 3 , y 3 ] = ode113(@myequ3,[0 2000],[2 0]);
hold on
plot(t 3 , y 3 (:,1))
```

# EXAMPLE – Compare different ode methods

Figure 1

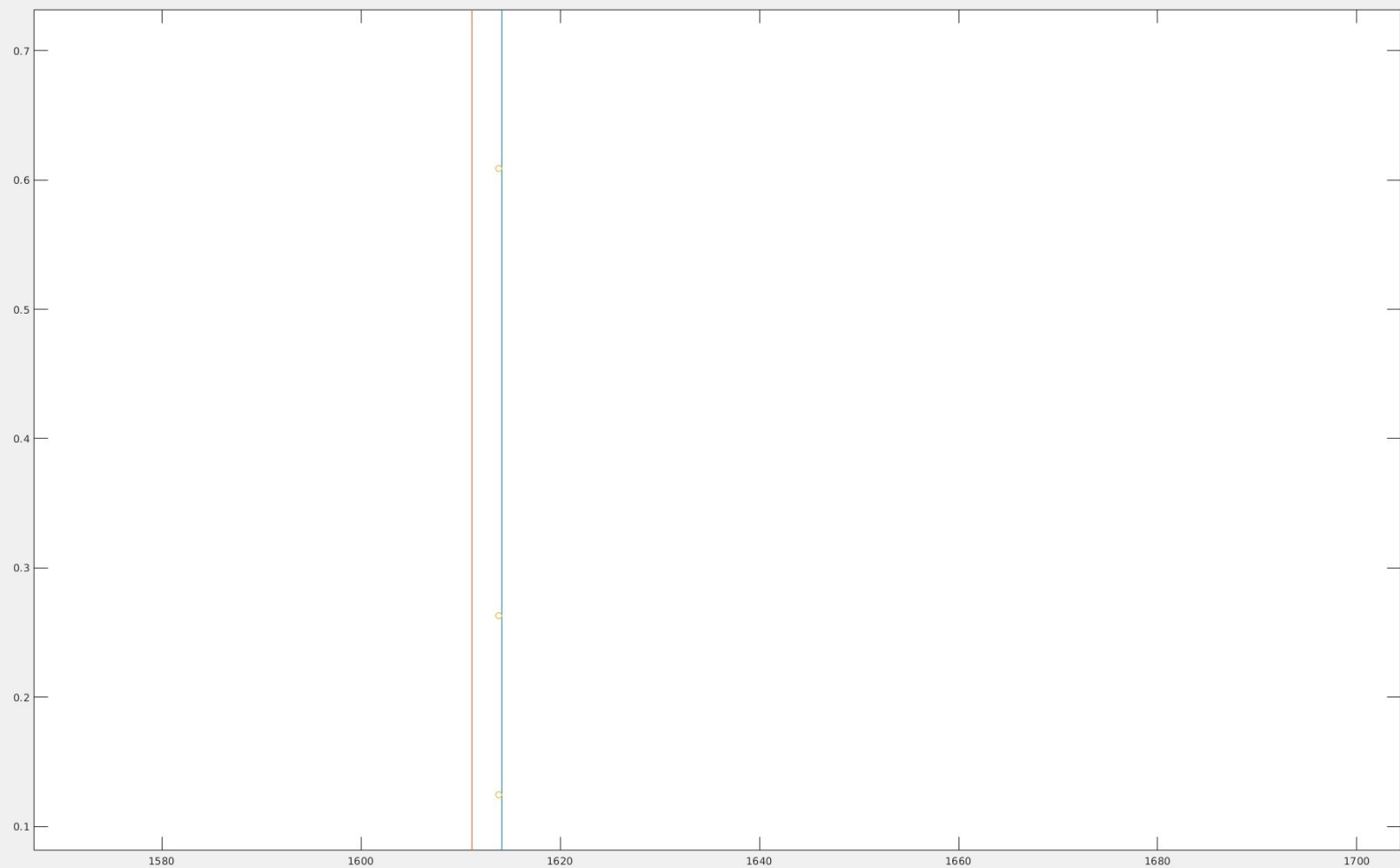




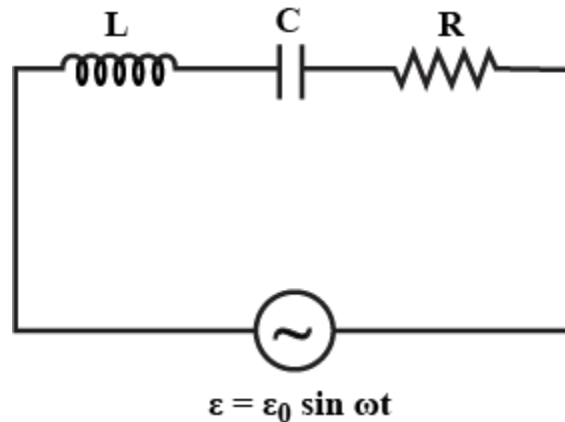
# EXAMPLE – Compare different ode methods

Figure 1

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## EXAMPLE – LCR circuit



**A series LCR circuit consists of an inductor L a capacitor C and a resistor R connected across a source of emf  $\varepsilon = \varepsilon_0 \sin \omega t$ .**

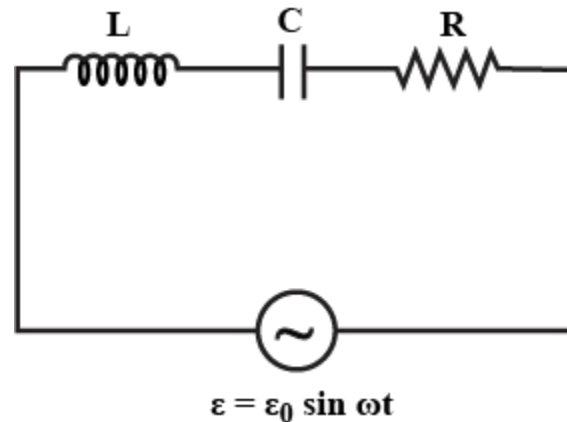
$$\frac{d^2 I}{dt^2} + \frac{R}{L} \frac{dI}{dt} + \frac{I}{LC} = \frac{1}{L} \frac{de(t)}{dt}$$

We set  $L = 10$ ,  $R = 200$ ,  $C = 5$ ,  $w = 100$

The equation can be changed as

$$D^2 I / Dt^2 = 10 * \cos(100t) - 20 * DI / Dt - I / 50$$

## EXAMPLE – LCR circuit

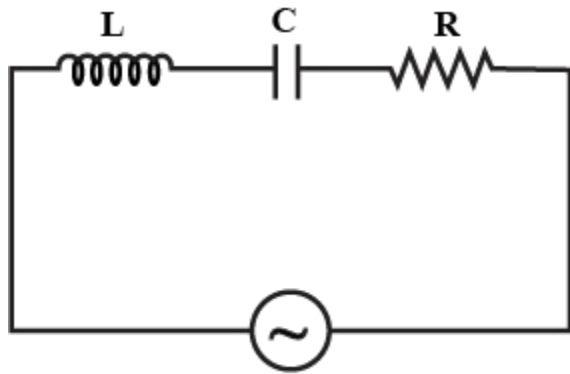


**A series LCR circuit consists of an inductor  $L$  a capacitor  $C$  and a resistor  $R$  connected across a source of emf  $\varepsilon = \varepsilon_0 \sin \omega t$ .**

```
function dx=LCREqu(t,x)
dx = [x(2); 10*cos(100*t)-20*x(2)-x(1)/50];
End
```

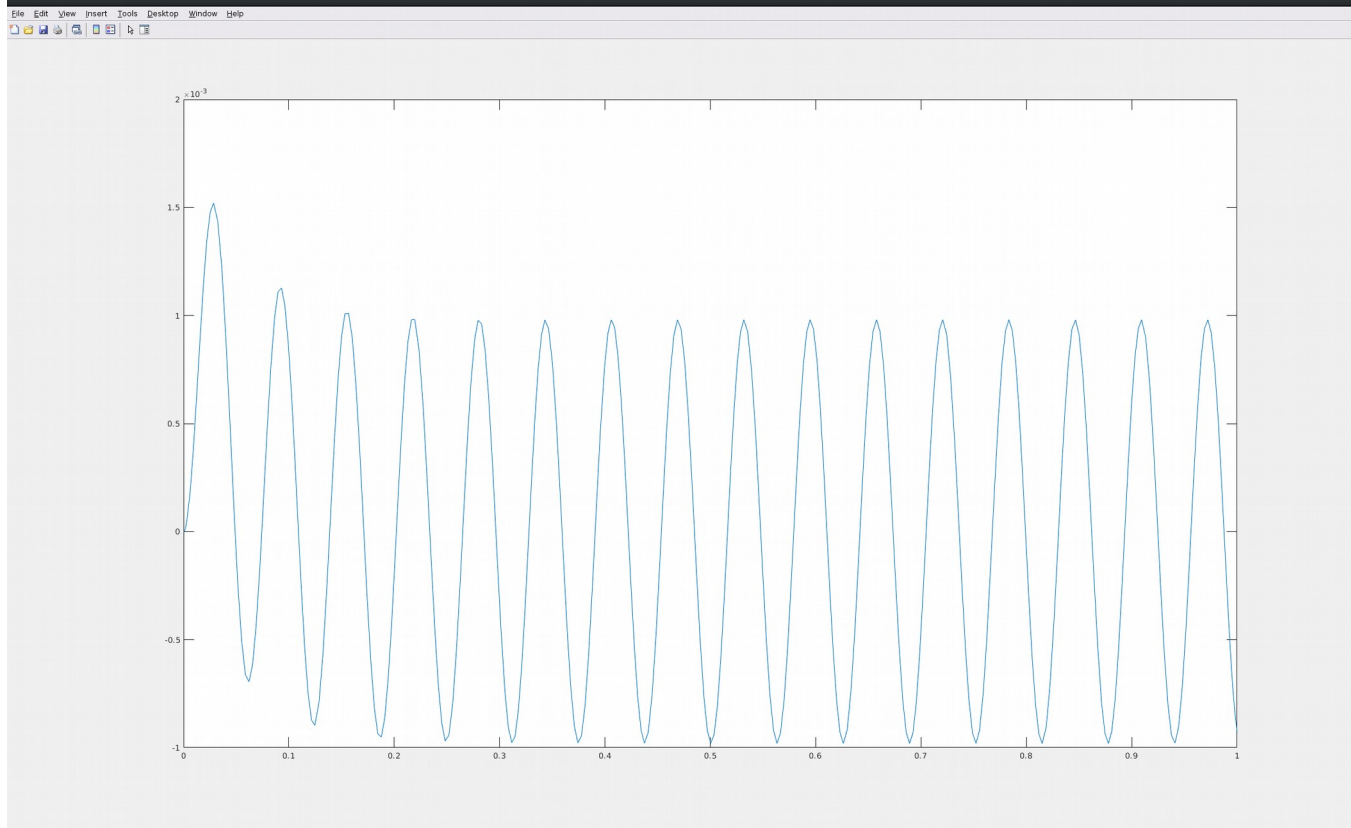
```
SpanT = [0 1]
X0 = [0 0]
[t x] = ode45('LCREqu',SpanT,X0)
```

# EXAMPLE – LCR circuit

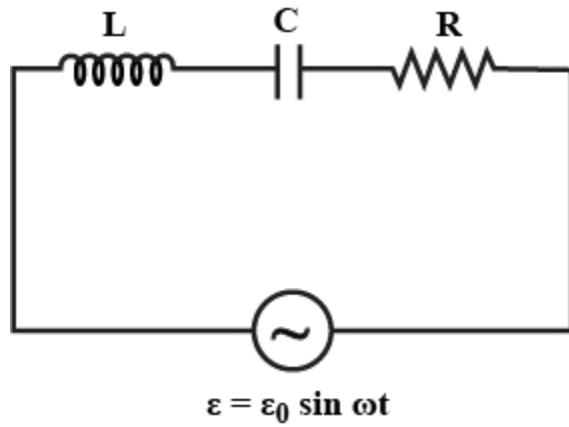


`plot(t, x(:,1))`

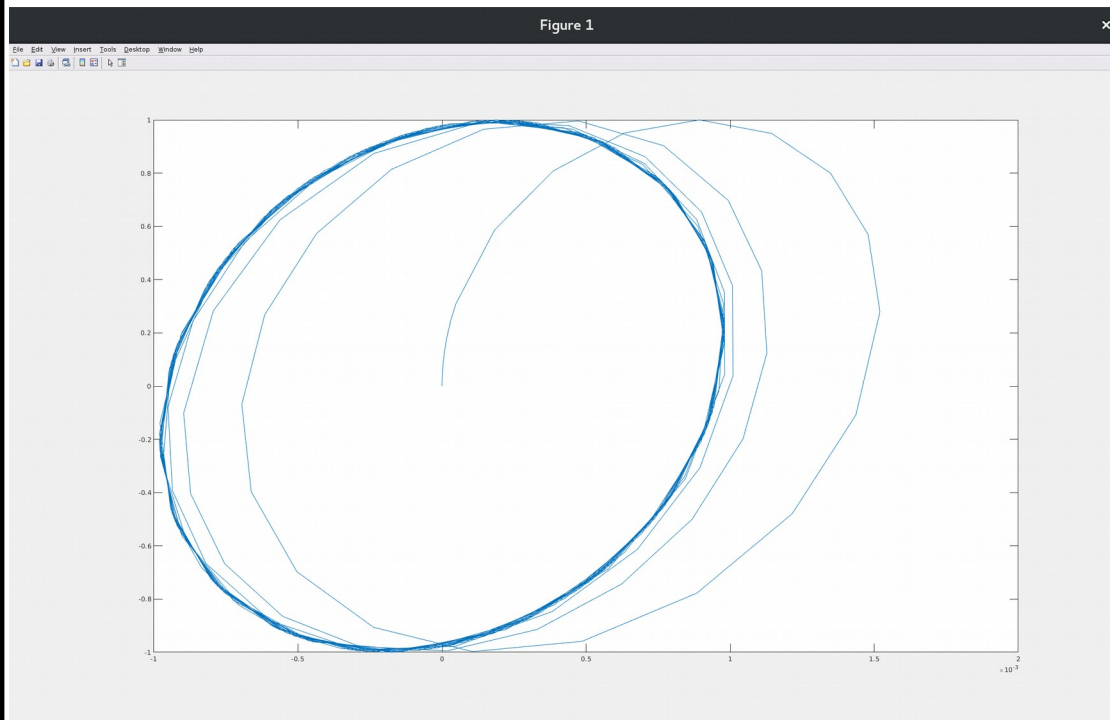
Figure 1



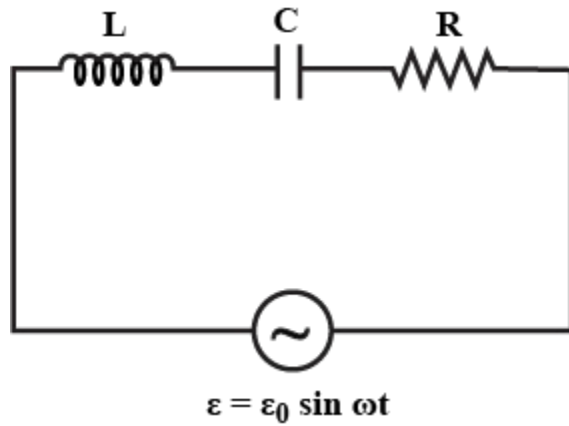
# EXAMPLE – LCR circuit



`plot(x(:,1), sin(100t))`



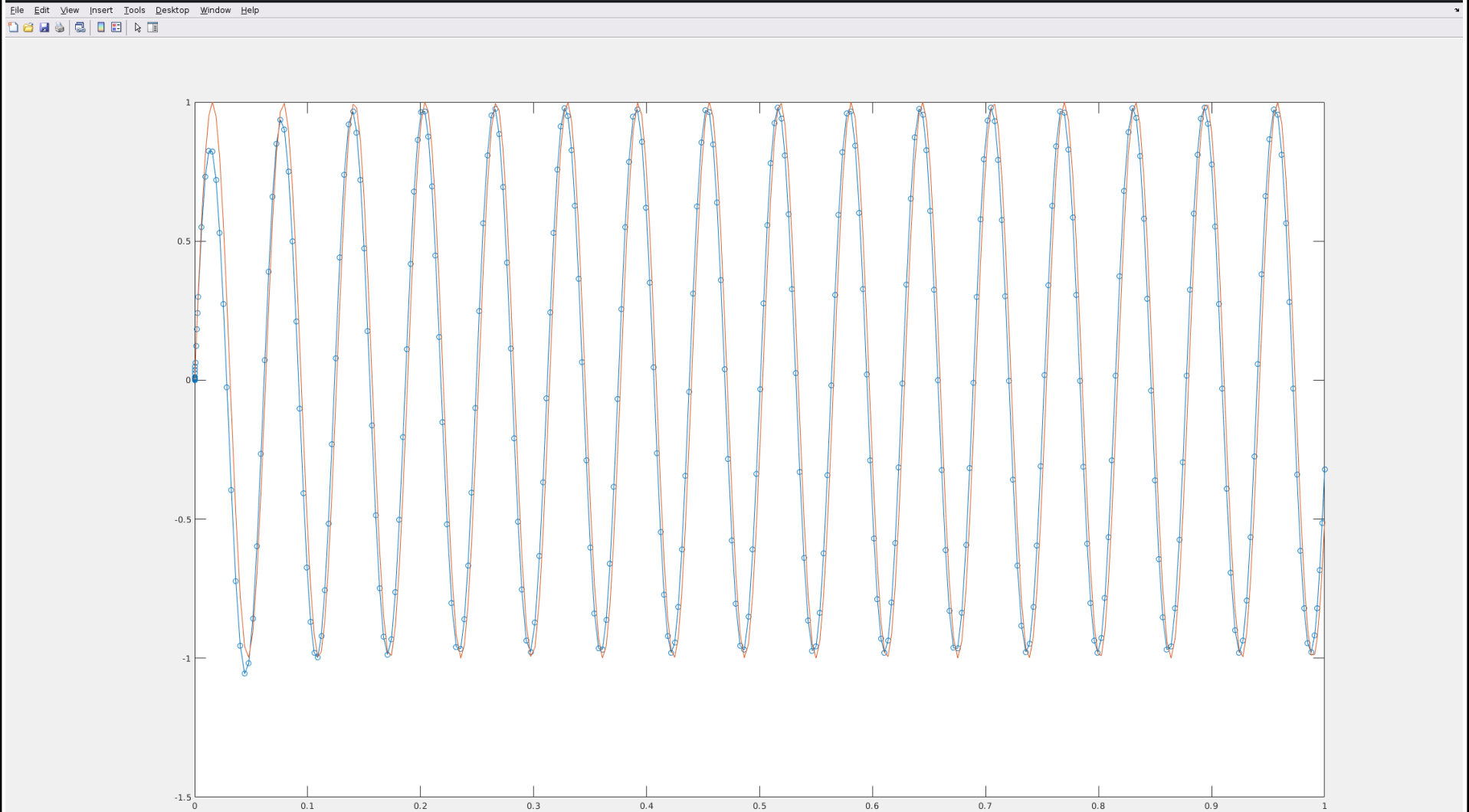
## EXAMPLE – LCR circuit



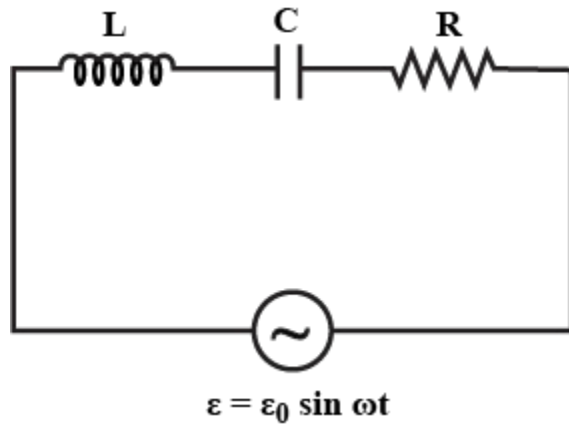
```
plot(t,10*x(:,2), '-o',t, sin(100*t), '-')
```

# EXAMPLE – LCR circuit

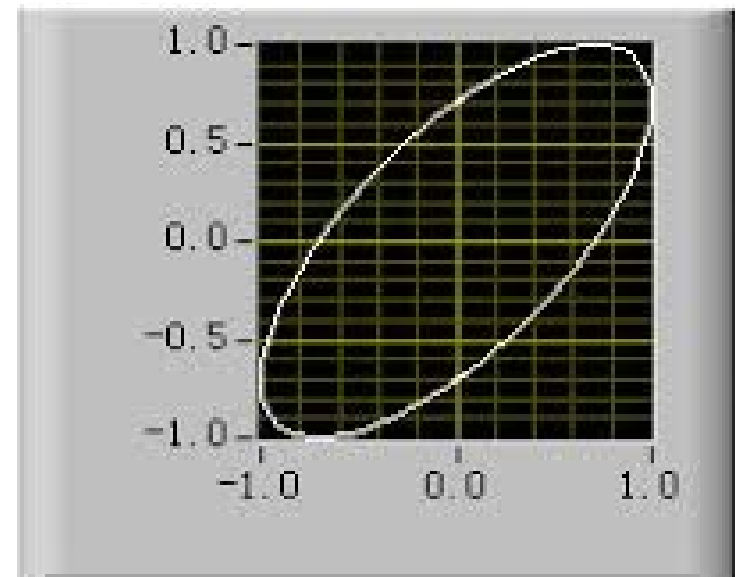
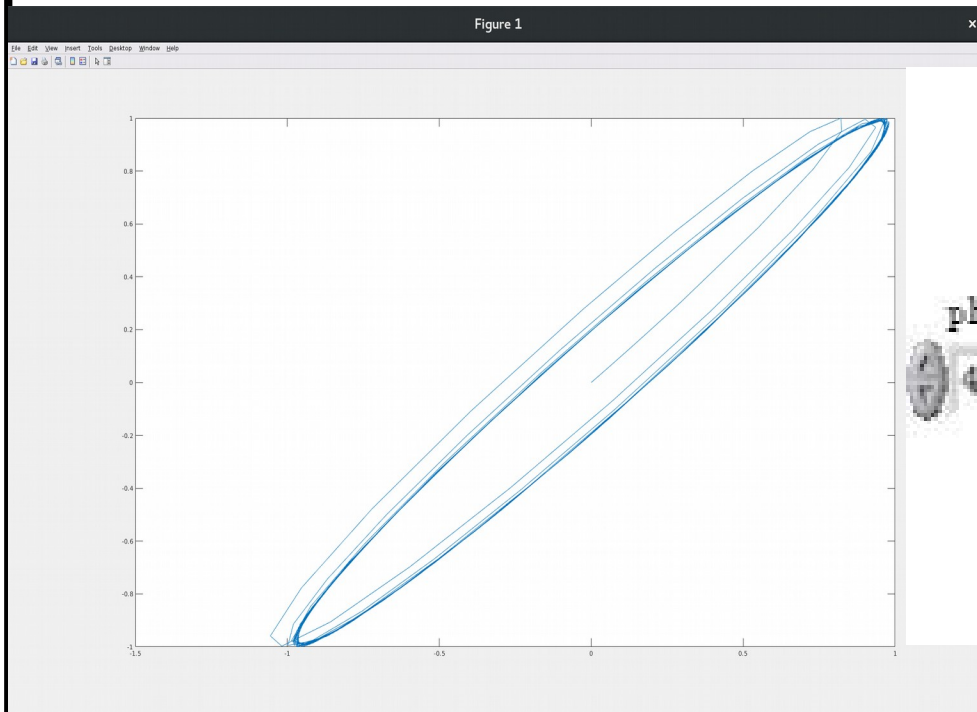
Figure 1



# EXAMPLE – LCR circuit

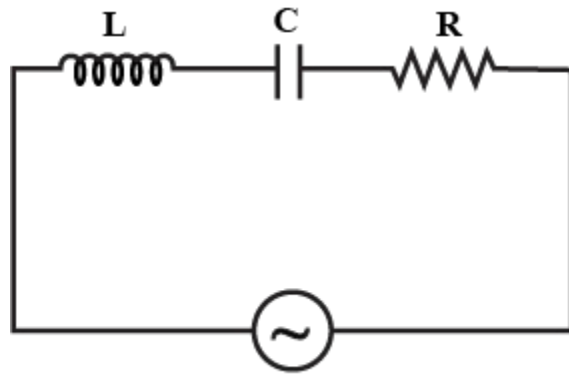


`Plot(10 * x(:,2), sin(100t))`





# EXAMPLE – LCR circuit



$$\varepsilon = \varepsilon_0 \sin \omega t$$

