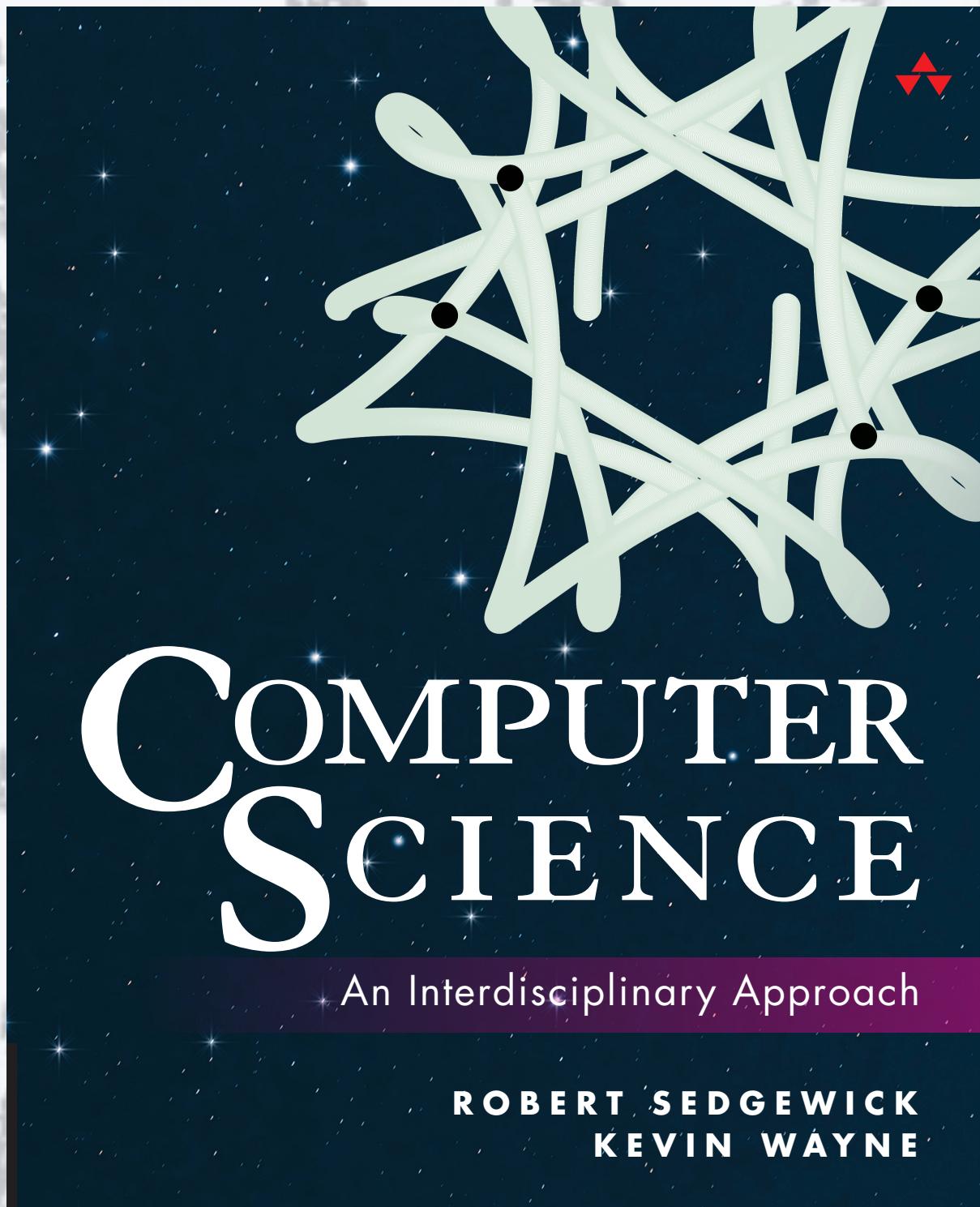




香港中文大學(深圳)
The Chinese University of Hong Kong, Shenzhen

数据科学学院
School of Data Science

COMPUTER SCIENCE
SEDGEWICK / WAYNE

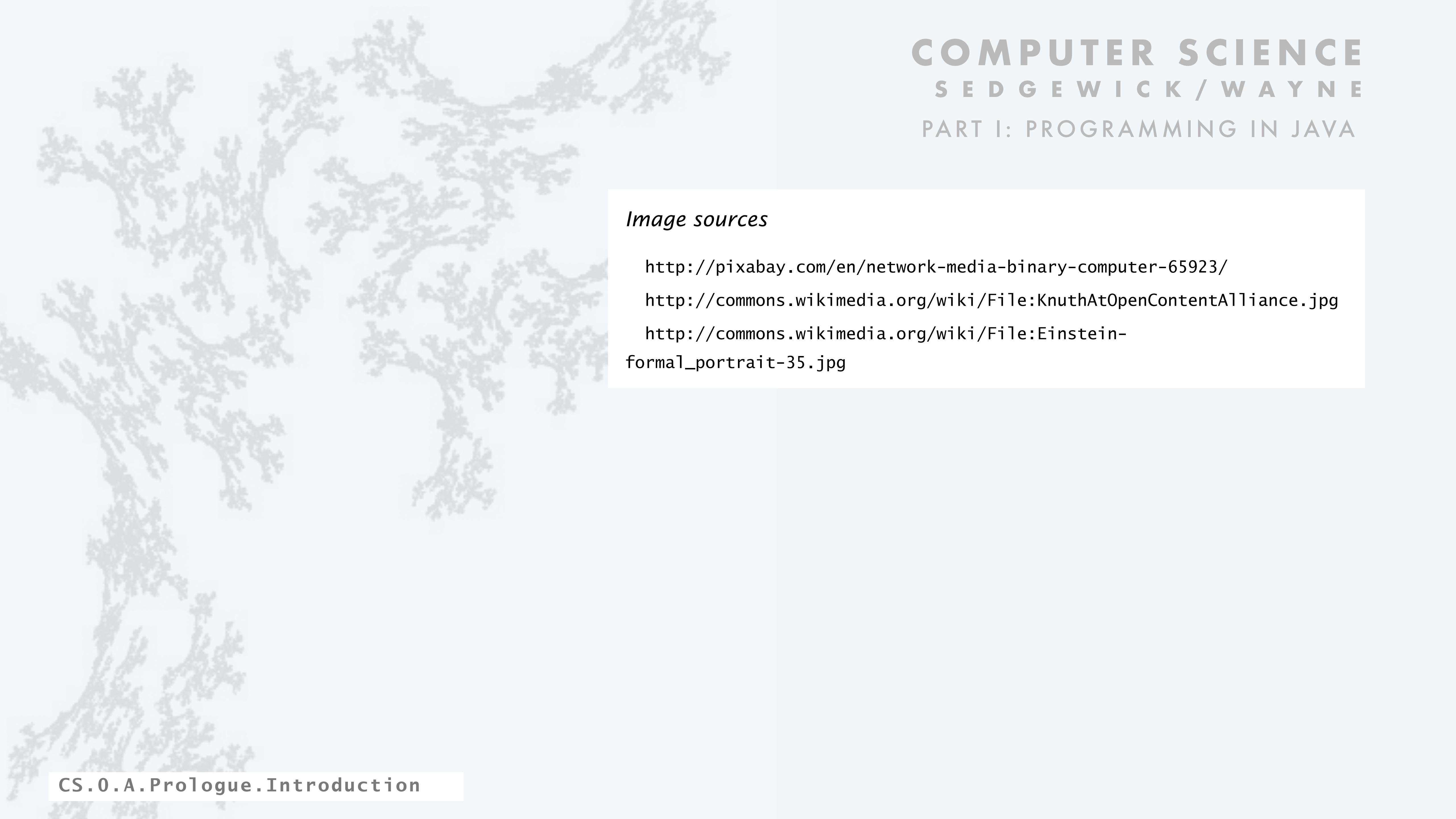


<http://introcs.cs.princeton.edu>

Prologue: A Simple Machine

Prologue: A Simple Machine

- Brief introduction
 - Secure communication with a one-time pad
 - Linear feedback shift registers
 - Implications



COMPUTER SCIENCE

SEGEWICK / WAYNE

PART I: PROGRAMMING IN JAVA

Image sources

<http://pixabay.com/en/network-media-binary-computer-65923/>

<http://commons.wikimedia.org/wiki/File:KnuthAtOpenContentAlliance.jpg>

http://commons.wikimedia.org/wiki/File:Einstein-formal_portrait-35.jpg

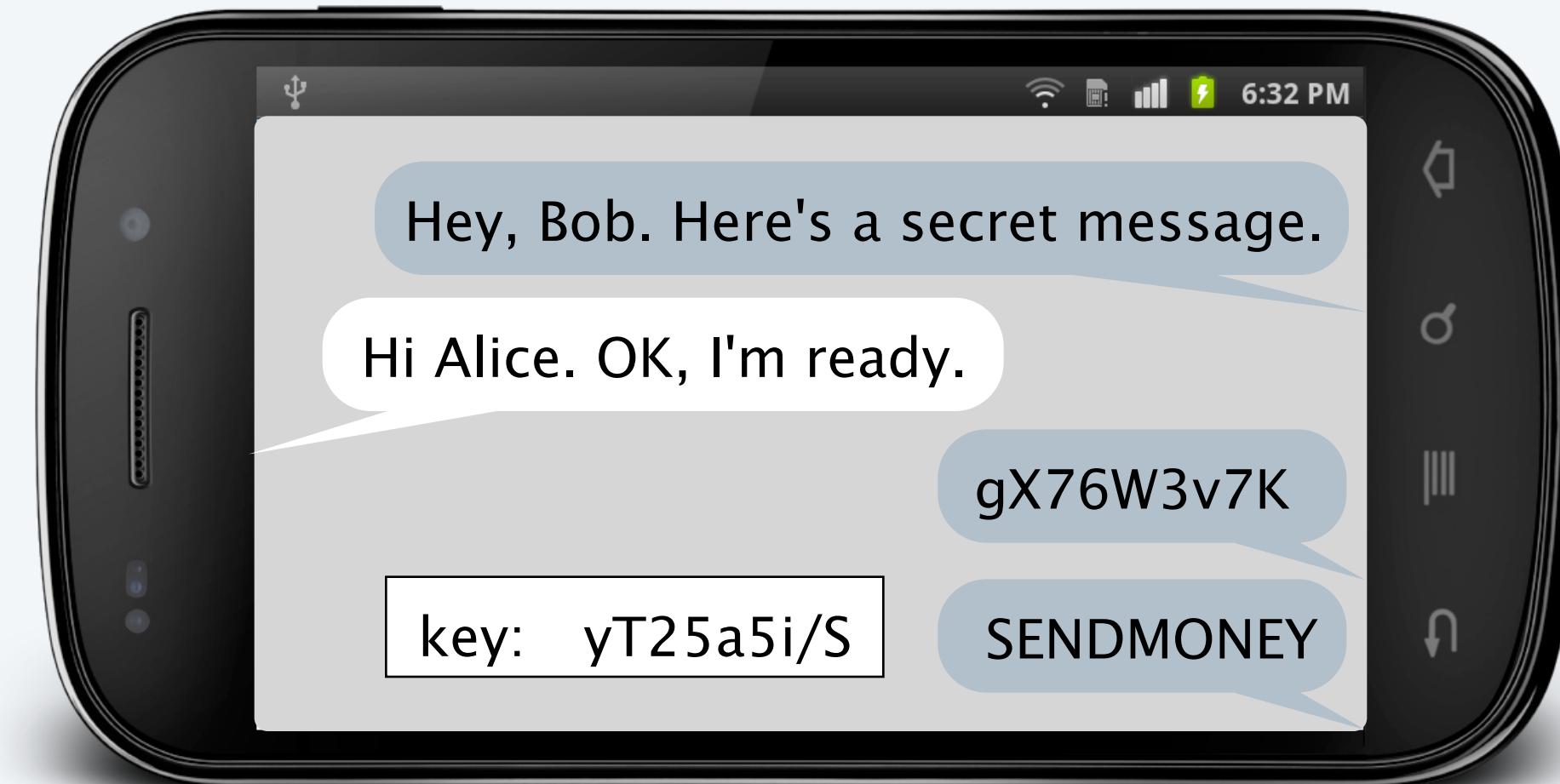
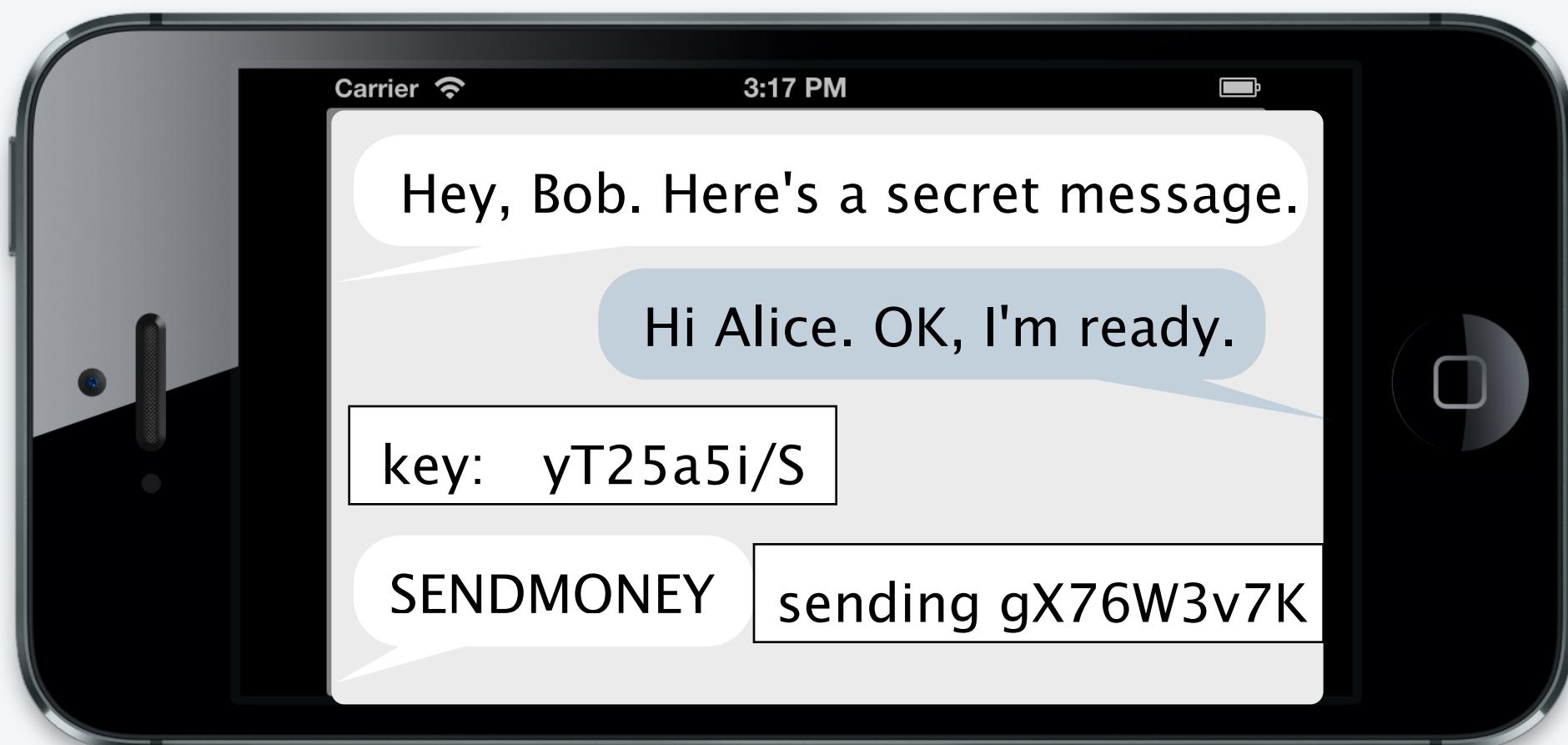
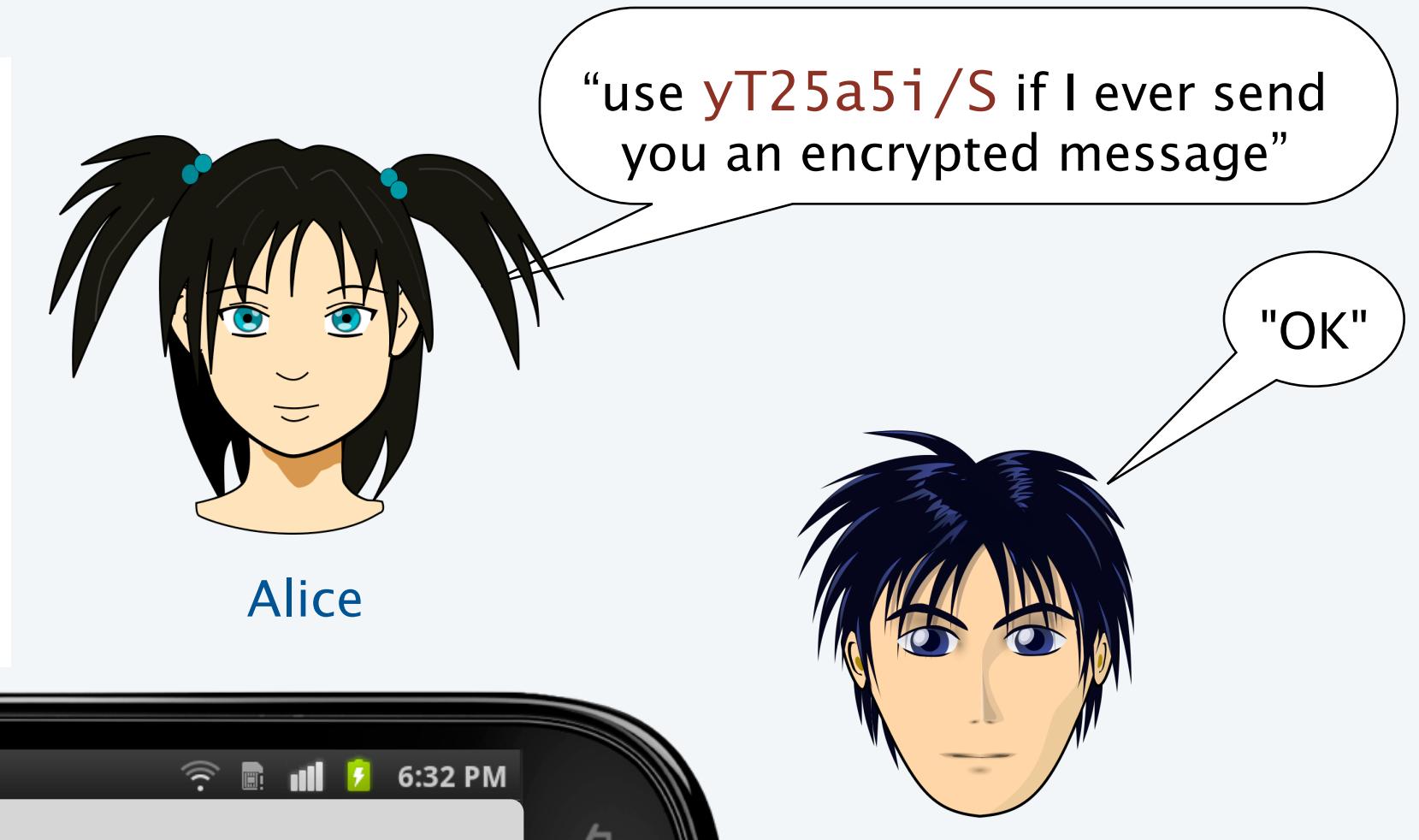
Prologue: A Simple Machine

- Brief introduction
- **Secure communication with a one-time pad**
- Linear feedback shift registers
- Implications

Sending a secret message with a cryptographic key

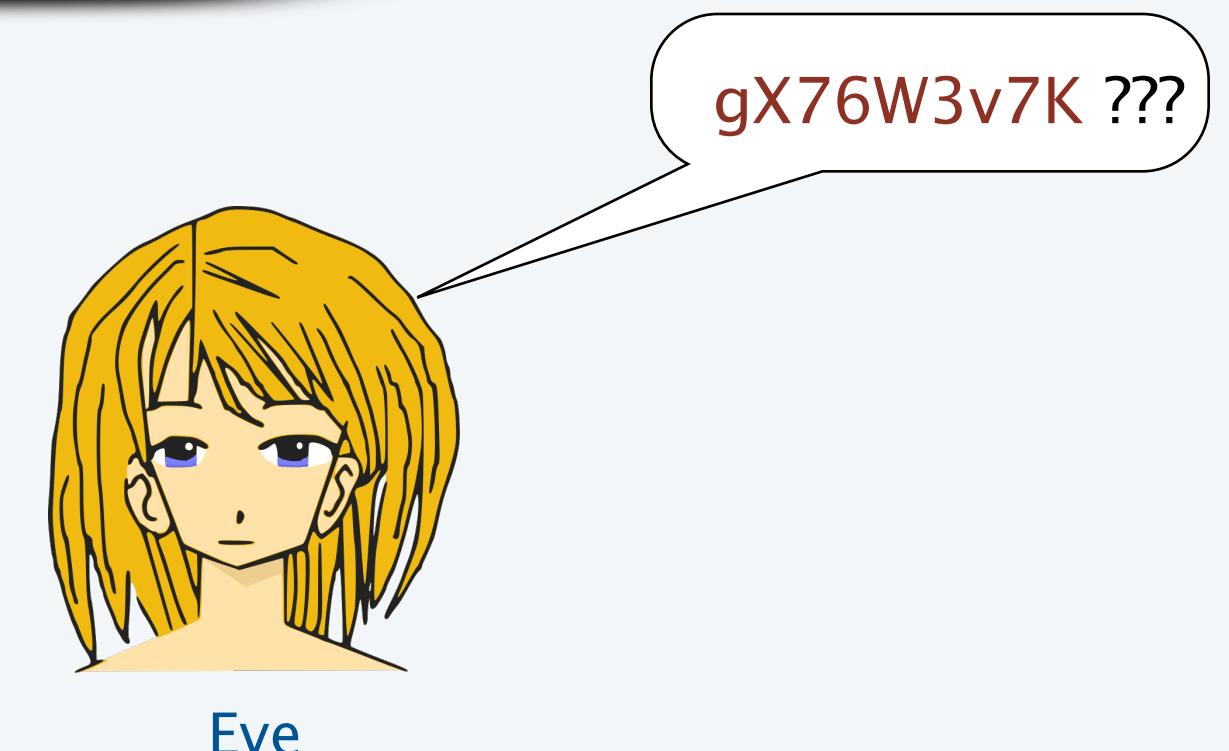
Alice wants to send a secret message to Bob.

- Sometime in the past, they exchange a **cryptographic key**.
- Alice uses the key to encrypt the message.
- Bob uses the *same* key to decrypt the message.



encrypted message gX76W3v7K is "in the clear" (anyone can read it)

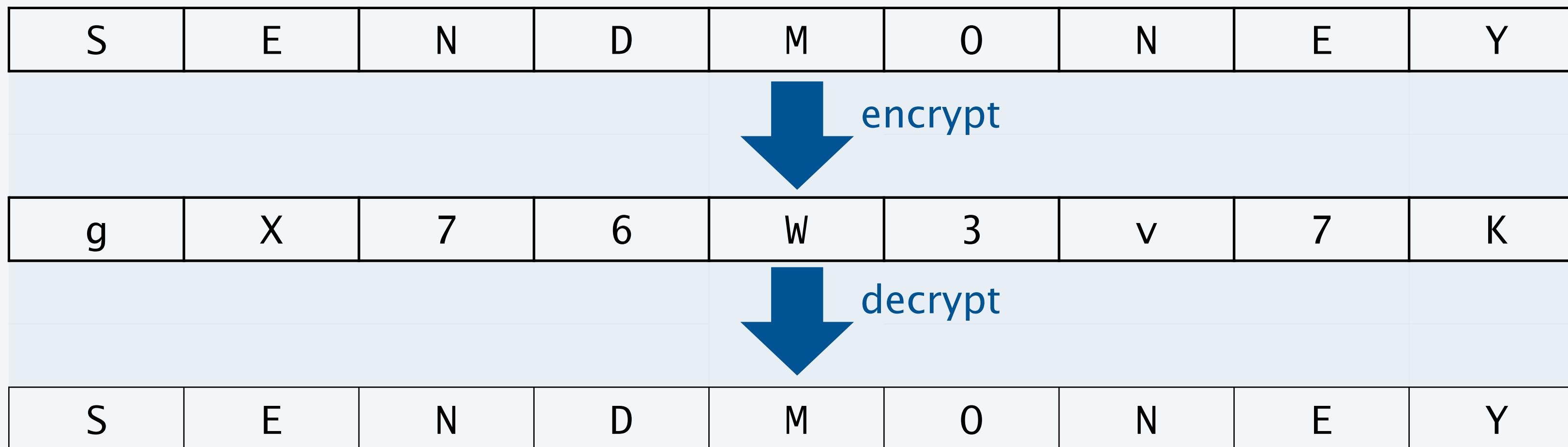
Critical point: Without the key, Eve cannot understand the message.



Q. How does the system work?

Encrypt/decrypt methods

Goal. Design a method to encrypt and decrypt data.



Example 1. Enigma encryption machine [German code, WWII]

- Broken by Turing bombe (one of the first uses of a computer).
- Broken code helped win Battle of Atlantic by providing U-boat locations.



Example 2. One-time pad [details to follow]

Example 3. Linear feedback shift register [later this lecture]

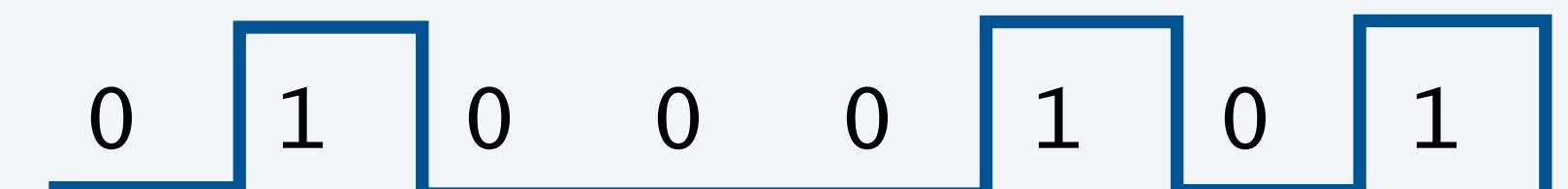
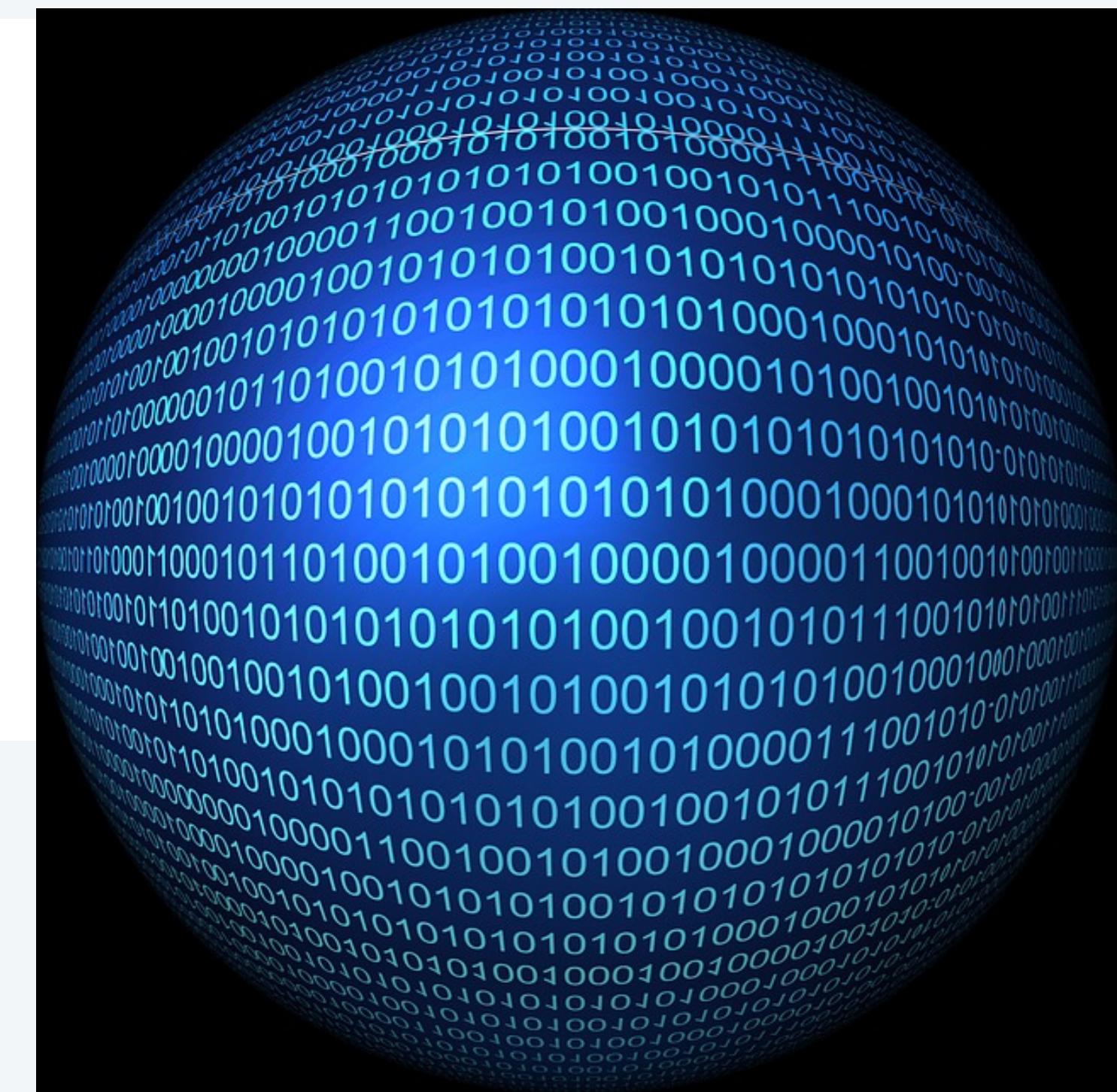
A digital world

A *bit* is a basic unit of information.

- Two possible values (0 or 1).
- Easy to represent in the physical world (*on* or *off*).

In modern computing and communications systems,
we represent *everything* as a sequence of bits.

- Text [details to follow in this lecture]
- Numbers
- Sound [details to follow in this course]
- Pictures [details to follow in this course]
- ...



$$01000101_2 = 69_{10}$$

Bottom line. If we can send and receive bits, we can send and receive *anything*.

well, not cars or cats (yet)

Encoding text as a sequence of bits

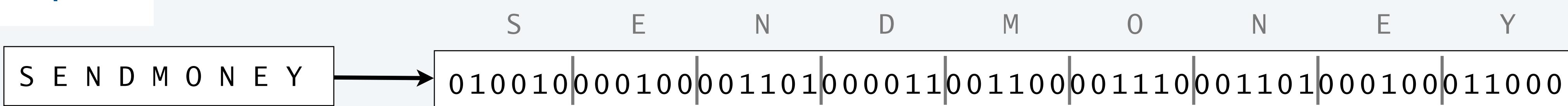
Base64 encoding of character strings

- A simple method for representing text.
- 64 different symbols allowed: A-Z, a-z, 0-9, +, /.
- 6 bits to represent each symbol.
- ASCII and Unicode methods used on your computer are similar.

	bits	symbols
Base64	6	64
ASCII	8	256
Unicode	16	65,536+

000000 A	001000 I	010000 Q	011000 Y	100000 g	101000 o	110000 w	111000 4
000001 B	001001 J	010001 R	011001 Z	100001 h	101001 p	110001 x	111001 5
000010 C	001010 K	010010 S	011010 a	100010 i	101010 q	110010 y	111010 6
000011 D	001011 L	010011 T	011011 b	100011 j	101011 r	110011 z	111011 7
000100 E	001100 M	010100 U	011100 c	100100 k	101100 s	110100 0	111100 8
000101 F	001101 N	010101 V	011101 d	100101 l	101101 t	110101 1	111101 9
000110 G	001110 O	010110 W	011110 e	100110 m	101110 u	110110 2	111110 +
000111 H	001111 P	010111 X	011111 f	100111 n	101111 v	110111 3	111111 /

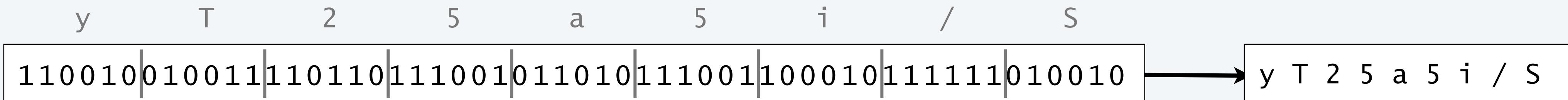
Example:



One-Time Pads

What is a one-time pad?

- A *cryptographic key* known only to the sender and receiver.
- Good choice: A *random* sequence of bits (stay tuned).
- Security depends on each sequence being used only once.



000000 A	001000 I	010000 Q	011000 Y	100000 g	101000 o	110000 w	111000 4
000001 B	001001 J	010001 R	011001 Z	100001 h	101001 p	110001 x	111001 5
000010 C	001010 K	010010 S	011010 a	100010 i	101010 q	110010 y	111010 6
000011 D	001011 L	010011 T	011011 b	100011 j	101011 r	110011 z	111011 7
000100 E	001100 M	010100 U	011100 c	100100 k	101100 s	110100 0	111100 8
000101 F	001101 N	010101 V	011101 d	100101 l	101101 t	110101 1	111101 9
000110 G	001110 O	010110 W	011110 e	100110 m	101110 u	110110 2	111110 +
000111 H	001111 P	010111 X	011111 f	100111 n	101111 v	110111 3	111111 /

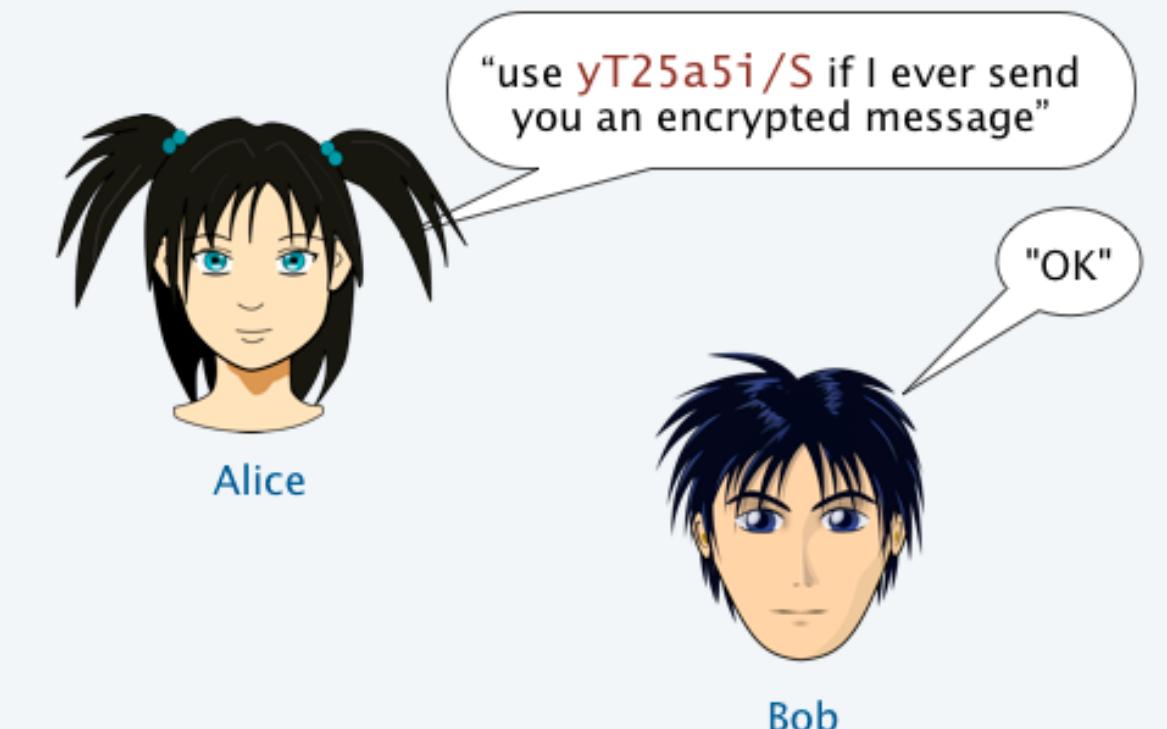
more convenient than bits
for initial exchange

Note: Any sequence of bits can be decoded into a sequence of characters.

Encryption with a one-time pad

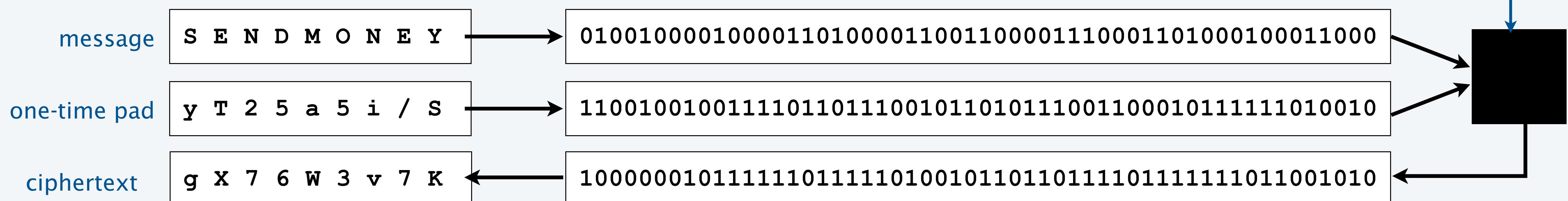
Preparation

- Create a "random" sequence of bits (a one-time pad).
- Send one-time pad to intended recipient through a secure channel.



Encryption

- Encode text as a sequence of N bits.
- Use the first N bits of the pad. ← important point: need to have as many bits in the pad as there are in the message.
- Compute a new sequence of N bits from the message and the pad.
- Decode result to get a sequence of characters.

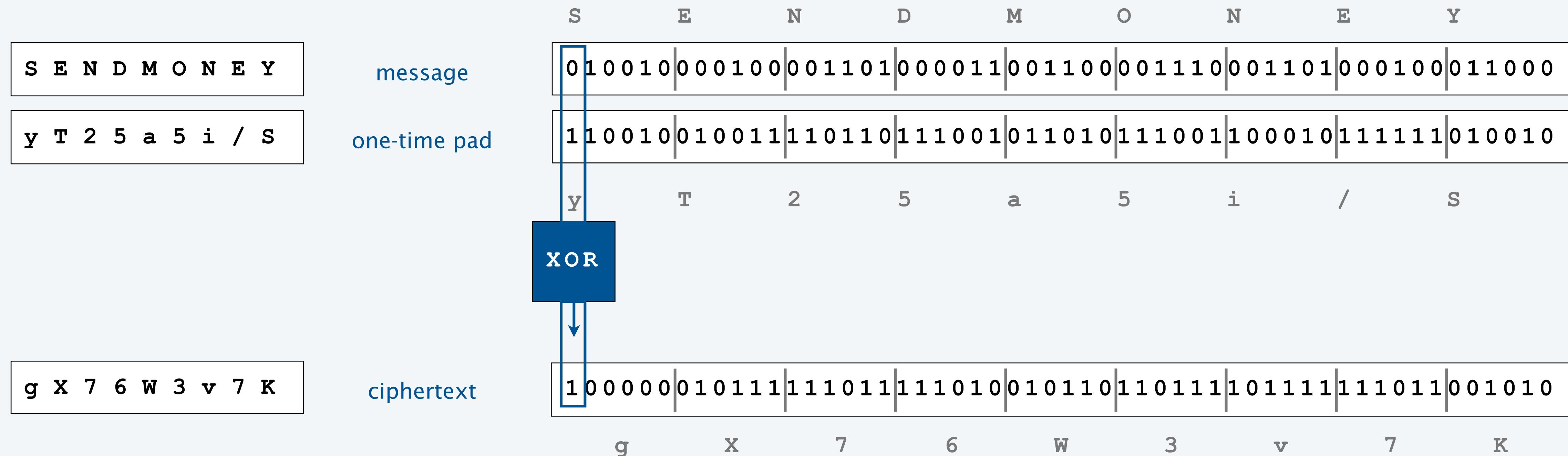


A (very) simple machine for encryption

To compute a ciphertext from a message and a one-time pad

- Encode message and pad in binary.
- Each ciphertext bit is the *bitwise exclusive or* of corresponding bits in message and pad.

Def. The *bitwise exclusive or* of two bits is 1 if they differ, 0 if they are the same.



Pop quiz on bitwise XOR encryption

Q. Encrypt the message E A S Y with the pad 0 1 2 3.

Pop quiz on bitwise XOR encryption

Q. Encrypt the message E A S Y with the pad 0 1 2 3.

000000 A	001000 I	010000 Q	011000 Y	100000 g	101000 o	110000 w	111000 4
000001 B	001001 J	010001 R	011001 Z	100001 h	101001 p	110001 x	111001 5
000010 C	001010 K	010010 S	011010 a	100010 i	101010 q	110010 y	111010 6
000011 D	001011 L	010011 T	011011 b	100011 j	101011 r	110011 z	111011 7
000100 E	001100 M	010100 U	011100 c	100100 k	101100 s	110100 0	111100 8
000101 F	001101 N	010101 V	011101 d	100101 l	101101 t	110101 1	111101 9
000110 G	001110 O	010110 W	011110 e	100110 m	101110 u	110110 2	111110 +
000111 H	001111 P	010111 X	011111 f	100111 n	101111 v	110111 3	111111 /

get coding table

E A S Y
000100 000000 010010 011000 encode message

0 1 2 3
110100 110101 110110 110111 encode pad

110000 110101 100100 101111 XOR to encrypt

w 1 k v decode

Decryption with a one-time pad

Sending a secret message with a cryptographic key

Alice wants to send a secret message to Bob.

- Sometime in the past, they exchange a **cryptographic key**.
- Alice uses the key to encrypt the message.
- Bob uses the *same* key to decrypt the message.

The diagram shows two mobile devices, Alice's and Bob's, displaying a messaging conversation. Alice sends a message to Bob: "Hey, Bob. Here's a secret message." Bob replies: "Hi Alice. OK, I'm ready." Alice then sends an encrypted message: "key: yT25a5i/S" followed by "SENDMONEY" and "sending gX76W3v7K". Bob replies with the same key and message: "key: yT25a5i/S" followed by "SENDMONEY" and "gX76W3v7K". A speech bubble from Eve says "gX76W3v7K ???", indicating she cannot understand the message without the key. At the top, Alice says "use yT25a5i/S if I ever send you an encrypted message" and Bob replies "OK".

encrypted message is "in the clear" (anyone can read it)

Critical point: Without the key, Eve cannot understand the message.

Q. How does the system work?

A. Alice's device uses a "bitwise exclusive or" machine to encrypt the message.

Q. What kind of machine does Bob's device use to *decrypt* the message?

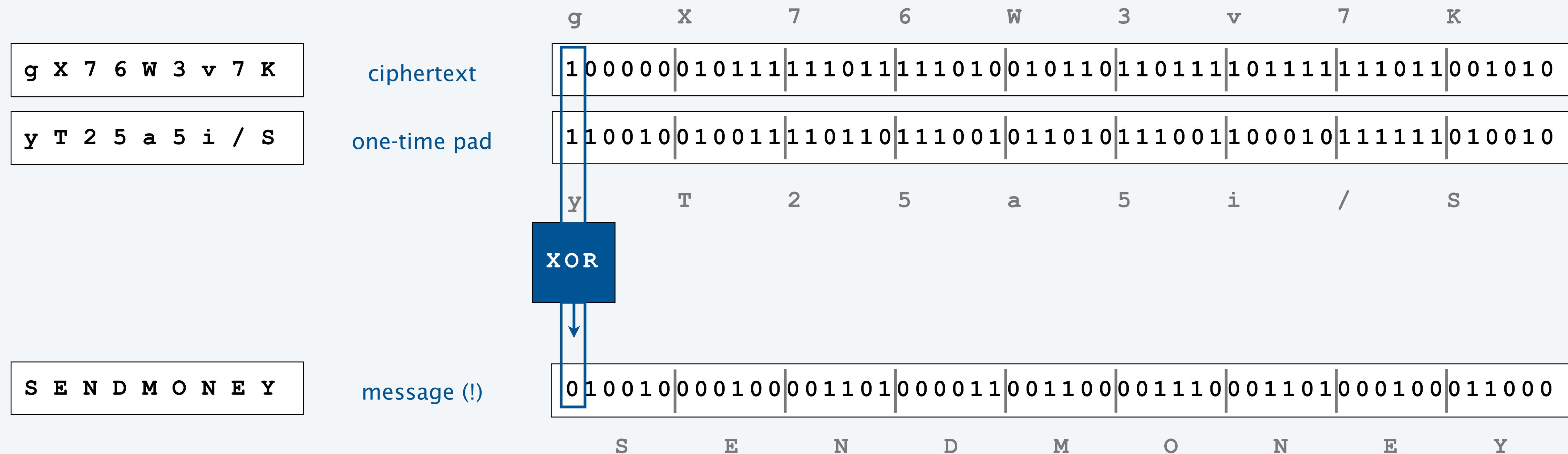
A. The same one (!!)

A (very) simple machine for encryption and decryption

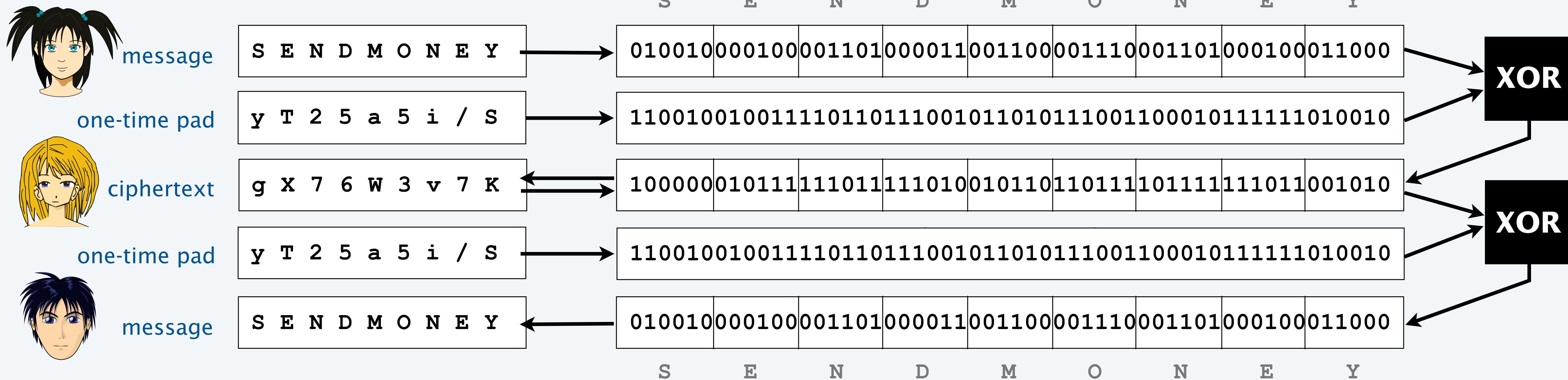
To compute a *message* from a *ciphertext* and a one-time pad

- Use binary encoding of ciphertext and pad.
- Each message bit is the *bitwise exclusive or* of corresponding bits in ciphertext and pad.

1 if they differ; 0 if they are the same



Why does it work?



Crucial property: Decrypted message is the same as the original message.

Let m be a bit of the message and k be the corresponding bit of the one-time pad.

To prove: $(m \wedge k) \wedge k = m$ ← Notation: $m \wedge k$ is equivalent to $\text{XOR}(m, k)$

Approach 1: Truth tables

m	k	$m \wedge k$	$(m \wedge k) \wedge k$
0	0	0	0
0	1	1	0
1	0	1	1
1	1	0	1

Approach 2: Boolean algebra

$$\begin{aligned}
 (k \wedge k) &= 0 \\
 m \wedge 0 &= m \\
 (m \wedge k) \wedge k &= m \wedge (k \wedge k) \\
 &= m \wedge 0 \\
 &= m
 \end{aligned}$$



Will other arithmetical operation support encryption/decryption?

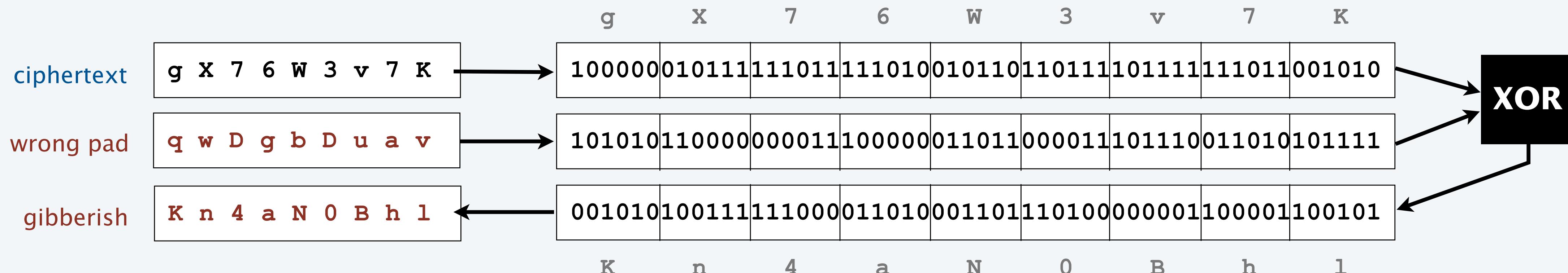
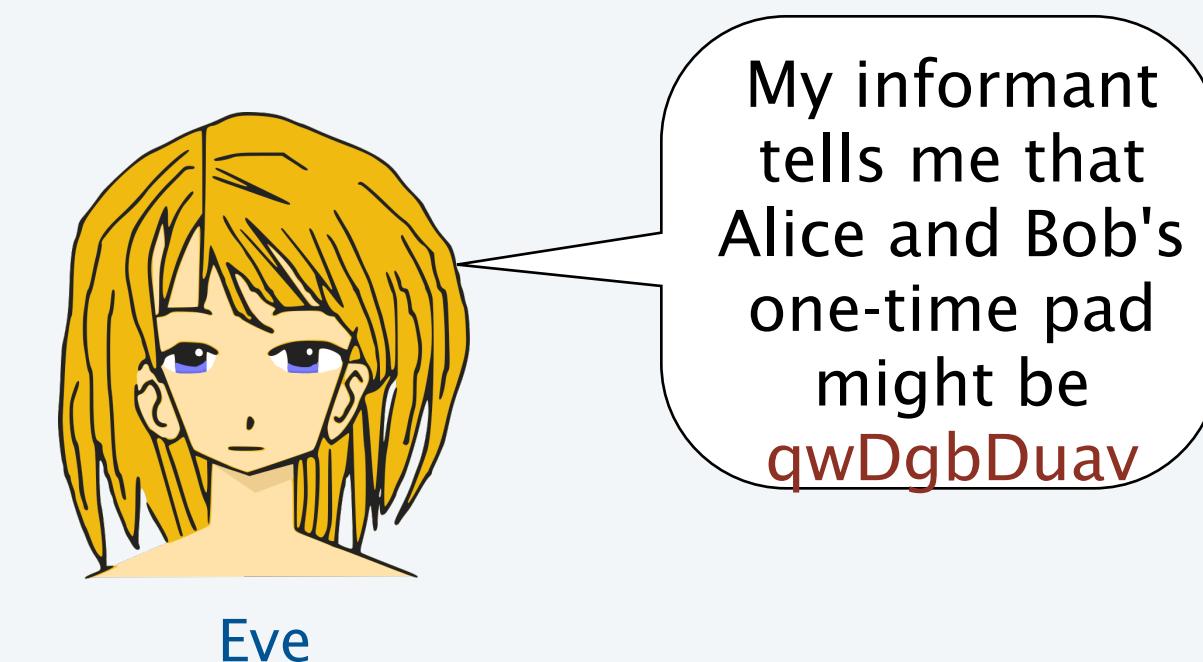
*

/

+

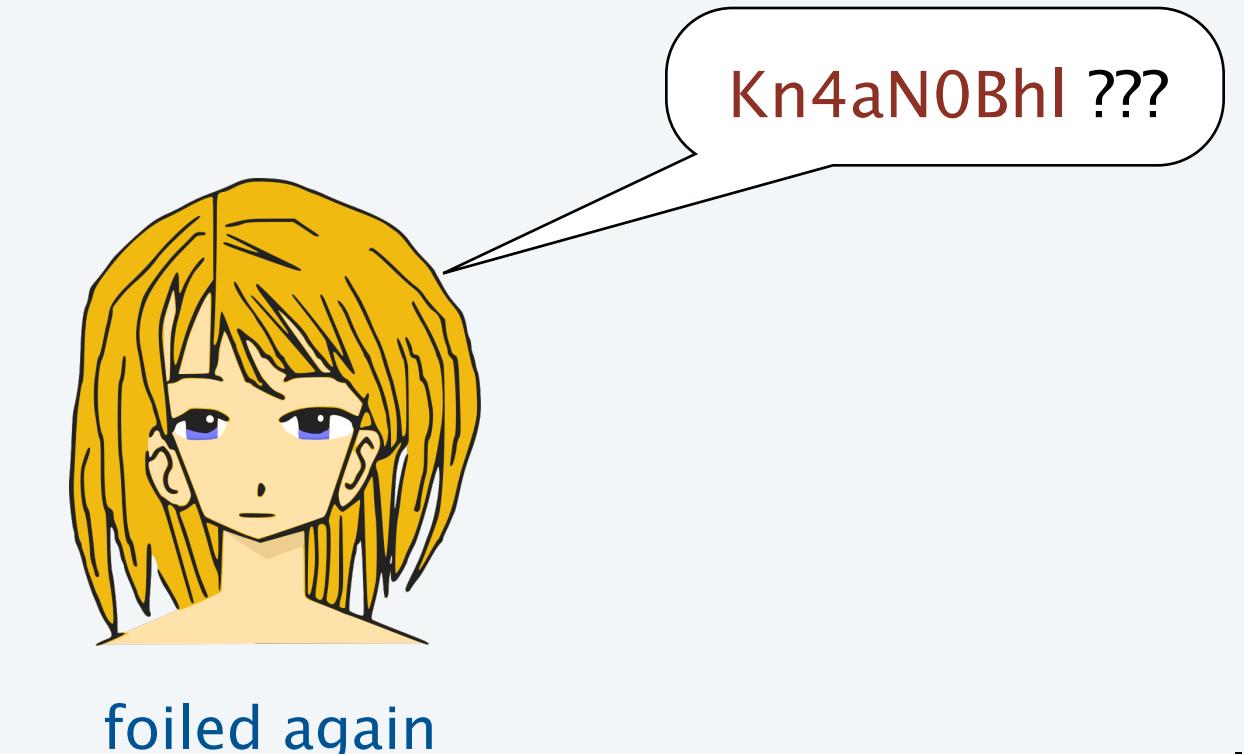
Decryption with the wrong pad

Eve *cannot* read a message without knowing the pad.



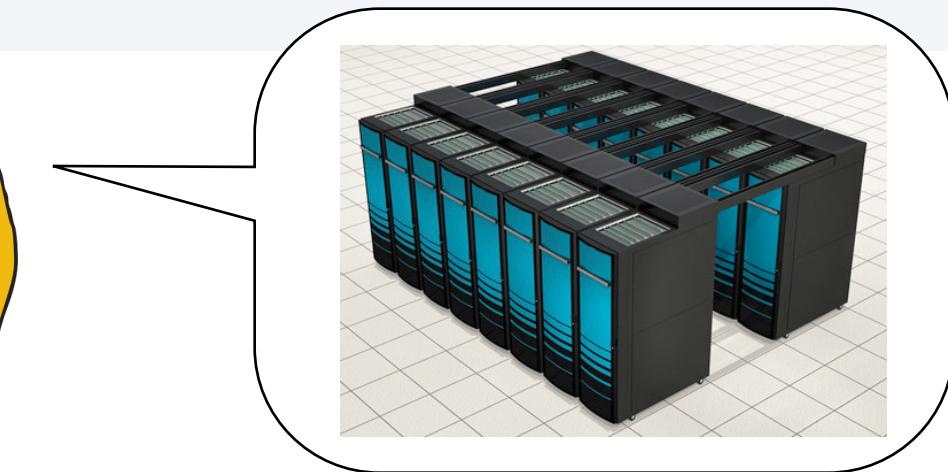
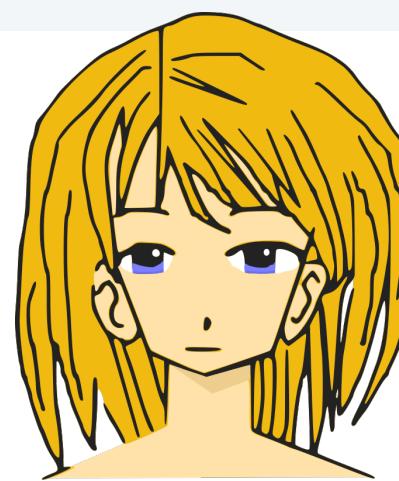
One-time pad is **provably secure** [Shannon, 1940s]

- IF each pad is used only once,
- AND the pad bits are random,
- THEN Eve cannot distinguish ciphertext from random bits.



Eve's problem with one-time pads

Eve has a computer. Why not try all possibilities?



Eve

Problem

- 54 bits, so there are 2^{54} possible pad values.
- Suppose Eve could check a million values per second.
- It would still take 570+ years to check all possibilities.

Much worse problem

- There are also 2^{54} possible messages.
- If Eve were to check all the pads, she'd see all the *messages*.
- No way to distinguish the real one from any other.

One-time pad is **provably secure**.

pad value	message?
AAAAAAAAAA	gX76W3v7K
AAAAAAAAAB	gX76W3v7L
AAAAAAAAAC	gX76W3v7I
...	
qwDgbDuav	Kn4aN0Bh1
...	
tTtpWk+1E	NEWTATTOO
...	
yT25a5i/S	SENDMONEY
...	
/////////+	fo7FpIQE0
/////////	fo7FpIQE1

Goods and bads of one-time pads

Goods.

- Very simple encryption method.
- Decrypt with the same method.
- Provably unbreakable if bits are truly random.
- Widely used in practice.

ZDXWWW EJKAWO FECIFE WSNZIP PXPKIY URMZHI JZTLBC YLGDYJ
HTSVTV RRYYEG EXNCGA GGQVRF FHZCIB EWLGGR BZXQDQ DGGIAK
YHJYEQ TDLCQT HZBSIZ IRZDYS RBYJFZ AIRCWI UCVXTW YKPQMK
CKHVEX VXYVCS WOGAAZ OUVVON GCNEVR LMBLYB SBDCDC PCGVJX
QXAUIP PXZQIJ JIUWYH COVWMJ UZOJHL DWHPER UBSRUJ HGAAPR
CRWVHI FRNTQW AJVWRT ACAKRD OZKIB VIQGBK IJCWHF GTTSSE
EXFIPJ KICASQ IOUQTP ZSGXGH YTYCTI BAZSTN JKMFXI RERYWE

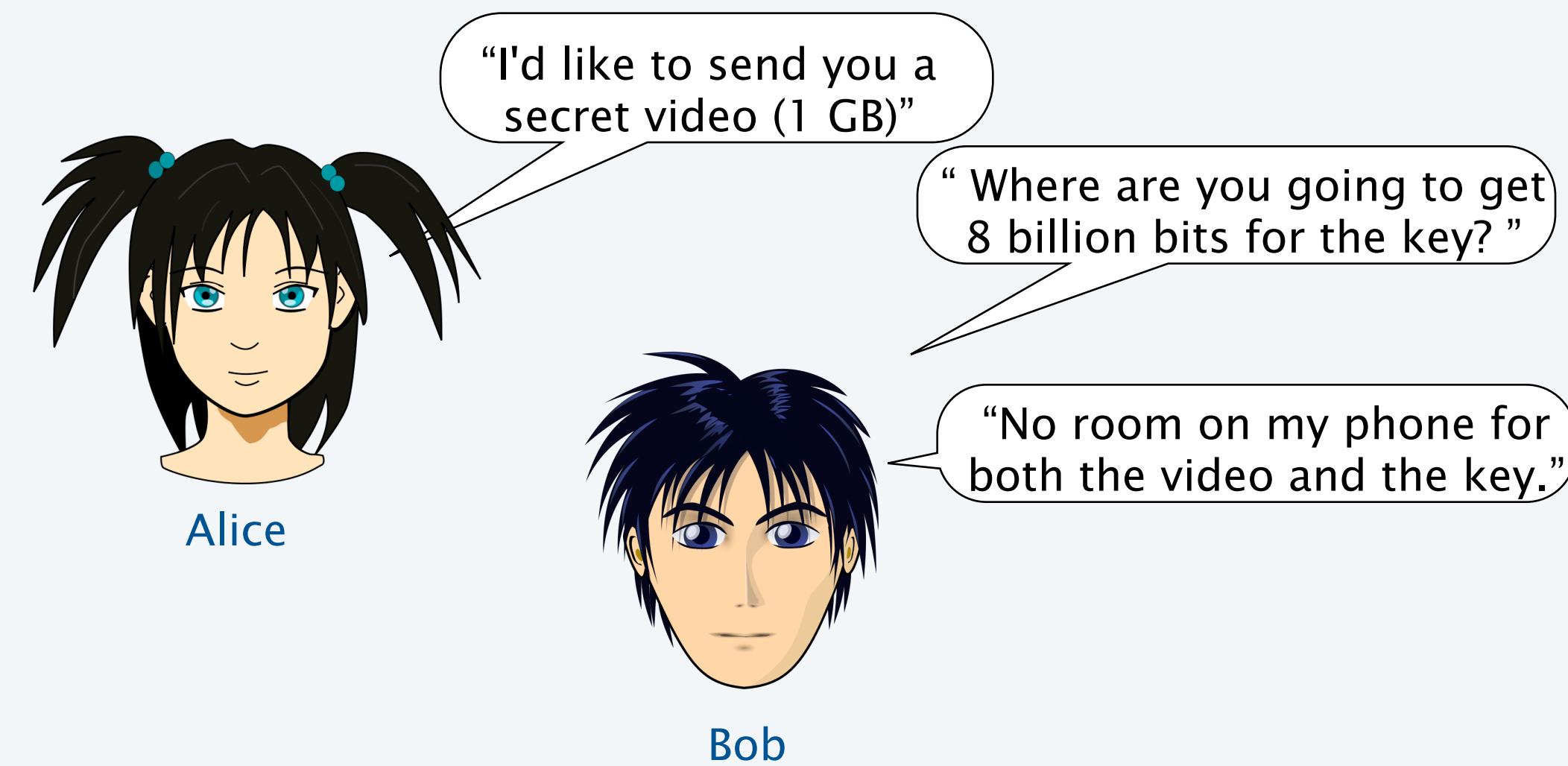
a one-time pad



cold war hotline

Bads.

- Easily breakable if seed is re-used.
- Truly random bits are very hard to come by.
- Need separate secure channel to distribute key.
- Pad must be as long as the message.



Random bits are not so easy to find

You might look on the internet.

RANDOM.ORG – Integer Generator

Home Games Numbers Lists & More Drawings Web Tools Statistics Testimonials Learn More Login

RANDOM.ORG

True Random Number Service

Do you own an iPhone, iPad or iPod Touch? Check out our new app! Android version coming soon.

Random Integer Generator

This form allows you to generate random integers. The randomness comes from atmospheric noise, which for many purposes is better than the pseudo-random number algorithms typically used in computer programs.

Part 1: The Integers

Generate random integers (maximum 10,000).

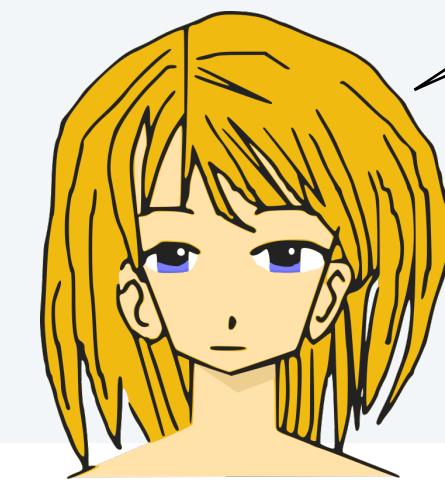
Each integer should have a value between and (both inclusive; limits $\pm 1,000,000,000$).

Format in column(s).

Part 2: Go!

Be patient! It may take a little while to generate your numbers...

The randomness comes from atmospheric noise



... if you trust the internet.

Next: Creating a (long) sequence of "pseudo-random" bits from a (short) key.

COMPUTER SCIENCE

SEGEWICK / WAYNE

PART I: PROGRAMMING IN JAVA

Image sources

<https://openclipart.org/detail/25617/astrid-graeber-adult-by-anonymous-25617>
<https://openclipart.org/detail/169320/girl-head-by-jza>
<https://openclipart.org/detail/191873/manga-girl---true-svg--by-j4p4n-191873>
<http://commons.wikimedia.org/wiki/File:Enigma-Machine.jpg>
<http://pixabay.com/en/binary-one-null-ball-administrator-63530/>
http://commons.wikimedia.org/wiki/File:Jimmy_Carter_Library_and_Museum_99.JPG

Prologue: A Simple Machine

- Brief introduction
- Secure communication with a one-time pad
- **Linear feedback shift registers**
- Implications

A pseudo-random number generator

is a *deterministic* machine that produces a long sequence of *pseudo random* bits.

Examples

Enigma.

Linear feedback shift register (next).

Blum-Blum-Shub generator.

...

[an early application of computing]

[research still ongoing]



“Anyone who considers arithmetical methods of producing random digits is, of course, in a state of sin.”

— John von Neumann



A pseudo-random number generator

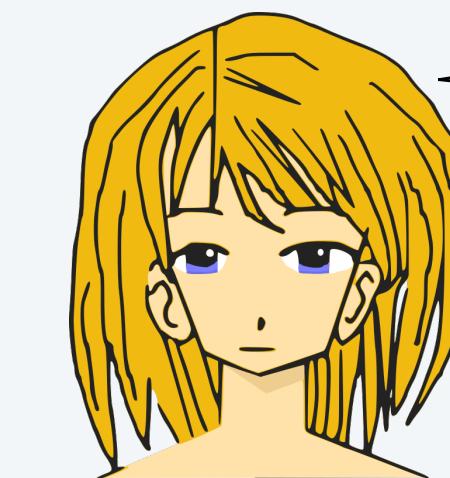
is a *deterministic* machine that produces a long sequence of *pseudo random* bits.

Deterministic: Given the current state of the machine, we know the next bit.



An absolute requirement: Alice and Bob need the same sequence.

Random: We never know the next bit.



10000001011111011
111010010110110111 ??
10111111011001010

Pseudo-random: The sequence of bits *appears to be* random.

Appears to be random??

- A profound and elusive concept.
- For this lecture: "Has enough properties of a random sequence that Eve can't tell the difference".

Ex. 1: No long repeats

Ex. 2: About the same number of 0s and 1s

Ex. 3: About the same number of 00s, 01s, 10s, and 11s.

...

Which of these sequences appear to be random?

0 0

X

0 1 0 1

X

but # of 0s and 1s
are about equal

0 0 1 1 0 1 1 0 0 0 1 1 0 1 1 0 0 0 1 1 0 1 1 0 0 1 1 0 1 1 0 0 1 1 0 1 1 0 0 1 1 0 1 1 0 0 1 1 0 1 1 0 0 1 1 0 1 1 0 0 1 1 0 0 0

X

but # of 00s 01s 10s
and 11s are about equal

0 1 0 0 1 0 0 0 0 1 0 0 0 0 1 1 0 1 0 0 0 0 1 1 0 0 1 1 0 0 0 0 1 1 1 0 0 0 1 1 0 1 0 0 0 1 0 0 0 1 0 0 0 1 1 0 0 0

X

SENDMONEY

1 1 0 0 1 0 0 1 0 0 1 1 1 0 1 1 0 1 1 1 0 0 1 0 1 1 0 1 0 1 1 1 0 1 1 0 0 1 0 1 1 1 1 1 0 1 0 0 1 0

✓

key for Alice and Bob

1 0 0 0 0 0 0 1 0 1 1 1 1 1 0 1 1 1 1 1 0 1 0 0 1 0 1 1 0 1 0 1 1 1 1 0 1 1 1 1 0 1 1 0 0 1 0 1 0 1 0

✓

ciphertext for SENDMONEY

1 0 0 0 0 0 0 1 1 1 0 0 0 1 0 1 1 0 0 0 1 0 0 0 1 1 0 0 0 1 0 0 0 1 0 1 0 0 1 1 0 0 1 0 1 1 0 0 1 1 0

✓

generated by coin flips

1 0 0 0 1 0 0 1 0 1 1 0 1 1 1 0 1 1 1 1 0 1 0 0 1 0 1 1 0 1 0 1 1 1 1 0 1 1 0 0 1 1 0 1 1 0 0 1 0 1 0 1 0

X

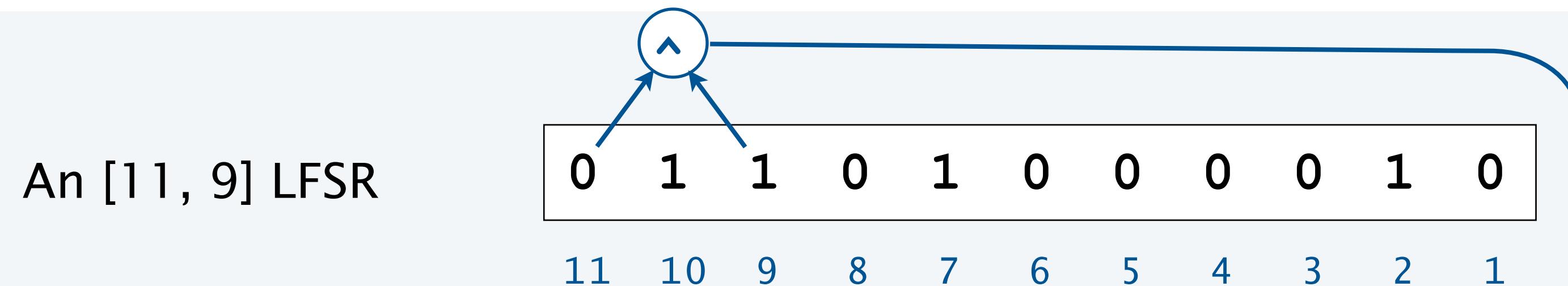
typed arbitrarily
(no long seqs of 0s or 1s)

Note: Any one of them *could* be random!

Linear feedback shift register

Terminology

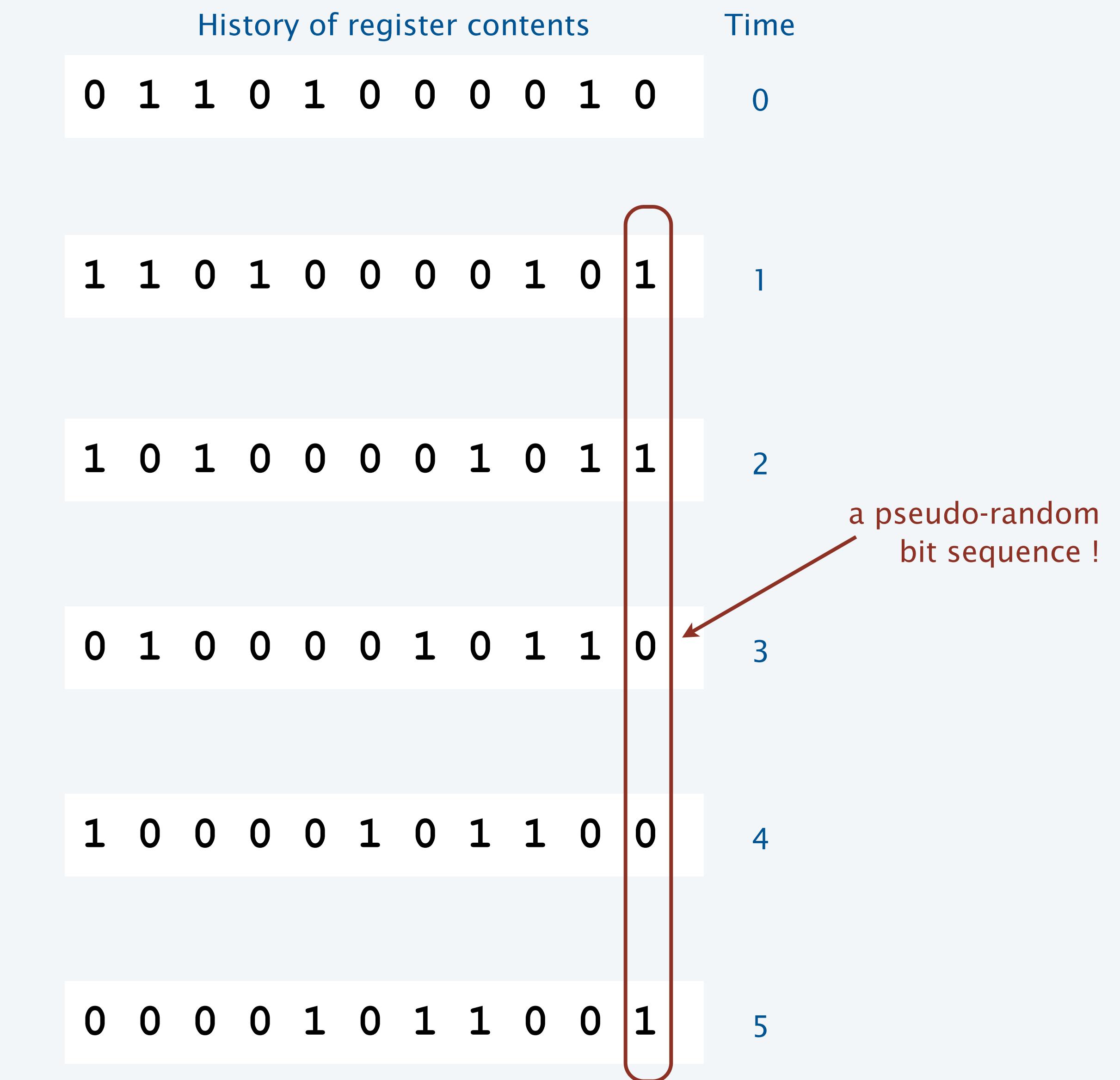
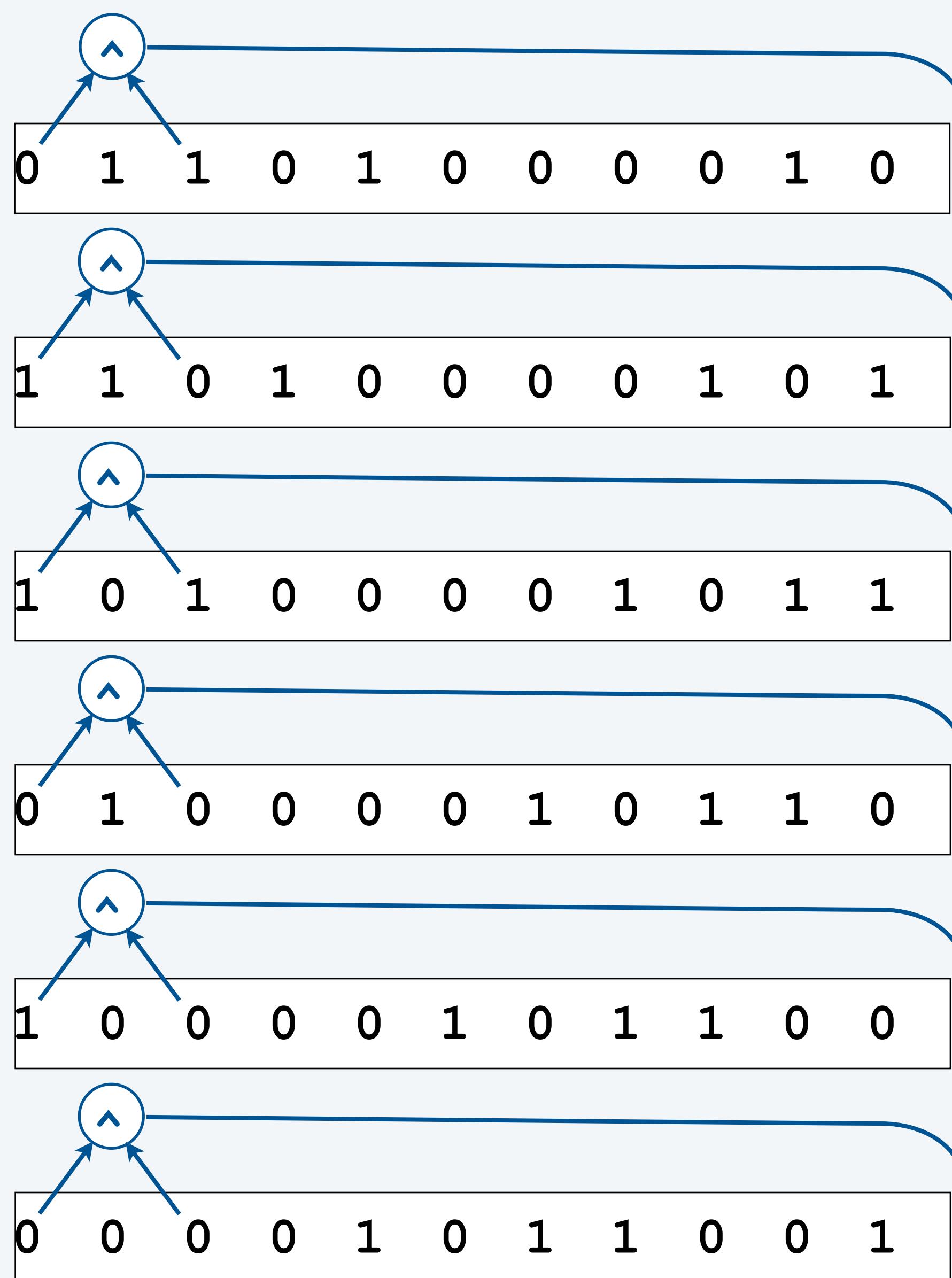
- Bit: 0 or 1.
- Cell: storage element that holds one bit.
- Register: sequence of cells.
- Seed: initial sequence of bits.
- Feedback: Compute XOR of two bits and put result at right.
- Shift register: when clock ticks, bits propagate one position to left.



More terminology

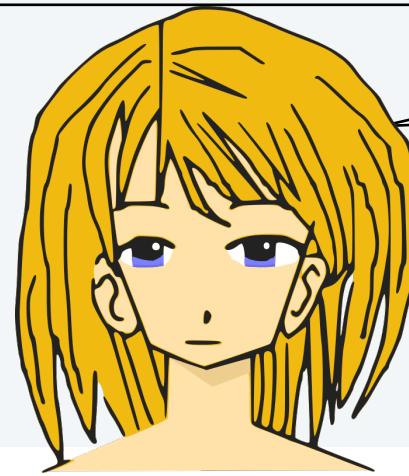
- Tap: Bit positions used for XOR (one must be leftmost). Numbered from right, starting at 1.
- $[N, k]$ LFSR: N -bit register with taps at N and k . Not all values of k give desired effect (stay tuned).

Linear feedback shift register simulation



A random bit sequence?

Q. Is this a random sequence?



Looks random to me.

No long repeats.

997 0s, 1003 1s.

256 00s, 254 01s, 256 10s, 257 11s.

...

one-time pad in our example

```
11001001001111011011100101101011100110001011111101001000010011010010111110011001001111111011100000101  
011000100001110101001101000011110010011001110111111101010000100001000100101010011000001011110001  
00100110101101111000110100110111001111010111100100010011101011101000001010010001000110101010111000  
000010110000010011100010111011010011011100100010011101011101000001010010001101111001100001101111000110  
1001110010011101110101010100000000010000000010100000010001000010101001000000011010000011100  
1000110111010111010001010001001000100100010101101010001100001001111001011100111001011110111001001  
010111011000010101110010000101110100100101011000111101110101010111000001001100001011111001  
00100011101011011000110001110111011010010110001100111101110001100111001111100010101100100011111101  
0110000100011100101011011100001101011001111001111011001011011101001100110100111100001110011001101  
111111110100000010010000010110100010011001010111110000100001100100111110001110001101101101110110  
1101011011000001101110001110101101100011011100101110111001010101100000111011000110101110111000  
101010110100000011001000011110100110001001111101011100010001011010101010110000011111000011000110011  
1101111100100000111000100110110101111011001001011101011001000111100010110011010011111100111000  
111101100101111110010000001110100001101001001110011011101010100100000101010000100000010  
01010001011000100111010010110100110011001111111100000000110000000111100000110011000111111101  
111101100000010111000010010110010110011110011110001111001101100111110001010001101001000100010  
11100101001011100011010111100110001111001011000111001110111101011010010001100110010001100111111  
00010000011010001110000101101100100111101111010010010011000110111110111010010101001010000011  
0001000111101011001000011110100011001001111101100100010111101010010010000110110100111011101  
011111010001000100101010110000001110000001101100001110110001110101011111000001000110001010111101
```

A. No. It is the output of an [11, 9] LFSR with seed 01101000010!

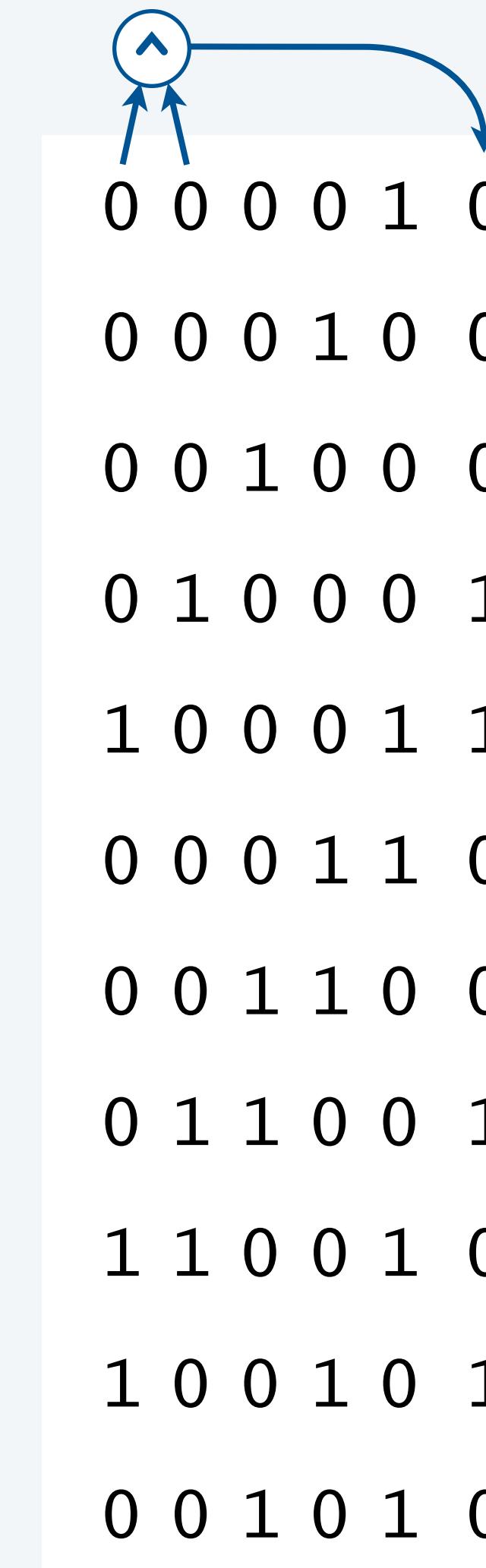
It is *pseudo-random*
(at least to some observers).

Pop quiz on LFSRs

Q. Give first 10 steps of [5, 4] LFSR with initial fill **00001**.

Pop quiz on LFSRs

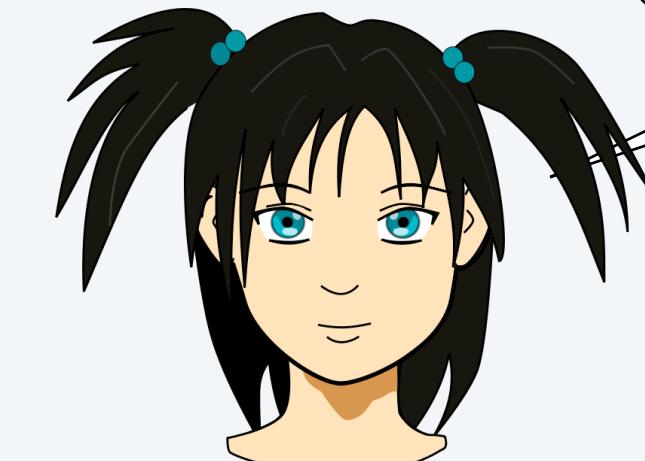
Q. Give first 10 steps of [5, 4] LFSR with initial fill **00001**.



Encryption/decryption with an LFSR

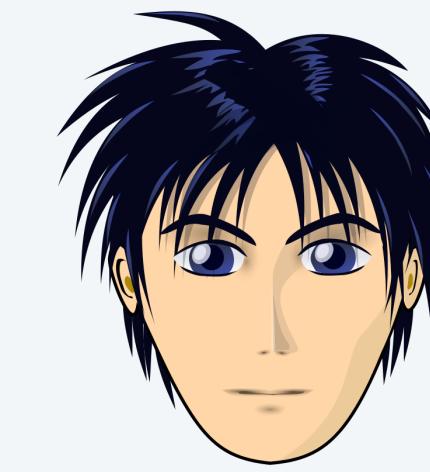
Preparation

- Alice creates a book of "random" (short) seeds.
- Alice sends the book to Bob through a secure channel.



Alice

"Use the next seed in the book to decode this secret video (1 GB)"

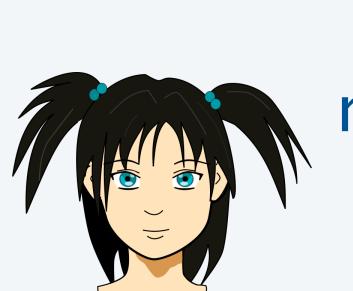


Bob

"OK (consults book)
01101000010"

Encryption/decryption

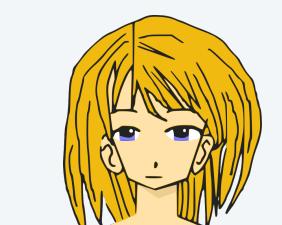
- Alice sends Bob a description of which seed to use.
- They use the specified seed to initialize an LFSR and produce N bits.
[and proceed in the same way as for one-time pads]



message

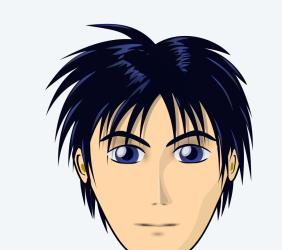
S E N D M O N E Y → 010010000100001101000011001100001110001101000100011000

XOR



seed

01101000010 → LFSR → 110010010011101101100101101011100110001011111010010



seed

01101000010 → LFSR → 110010010011101101100101101011100110001011111010010

XOR

message

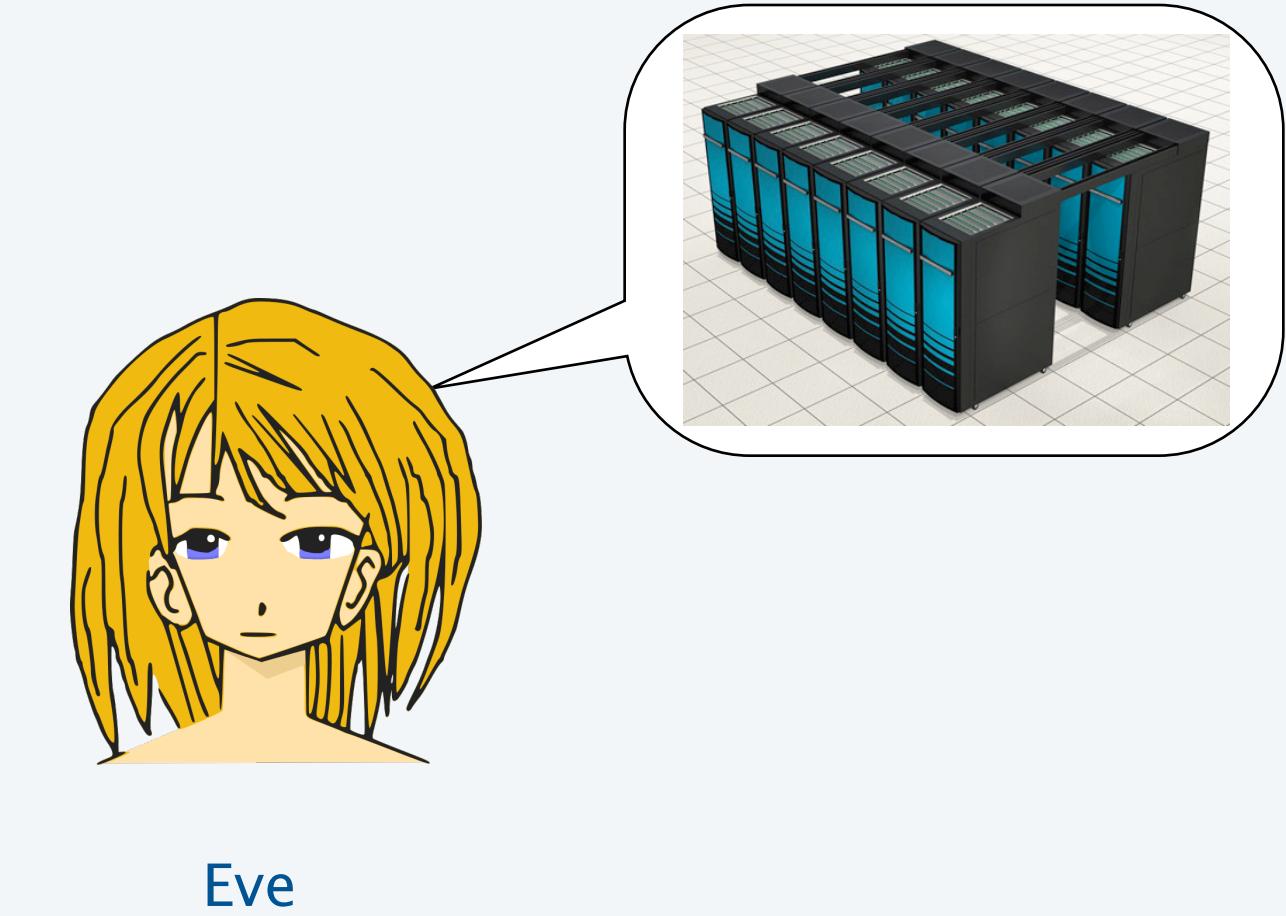
010010000100001101000011001100001110001101000100011000

Eve's opportunity with LFSR encryption

Without the seed, Eve cannot read the message.

Eve has computers. Why not try all possible seeds?

- Seeds are short, messages are long.
- All seeds give a tiny fraction of all messages.
- Extremely likely that all but real seed will produce gibberish.



Good news (for Eve): This approach can work.

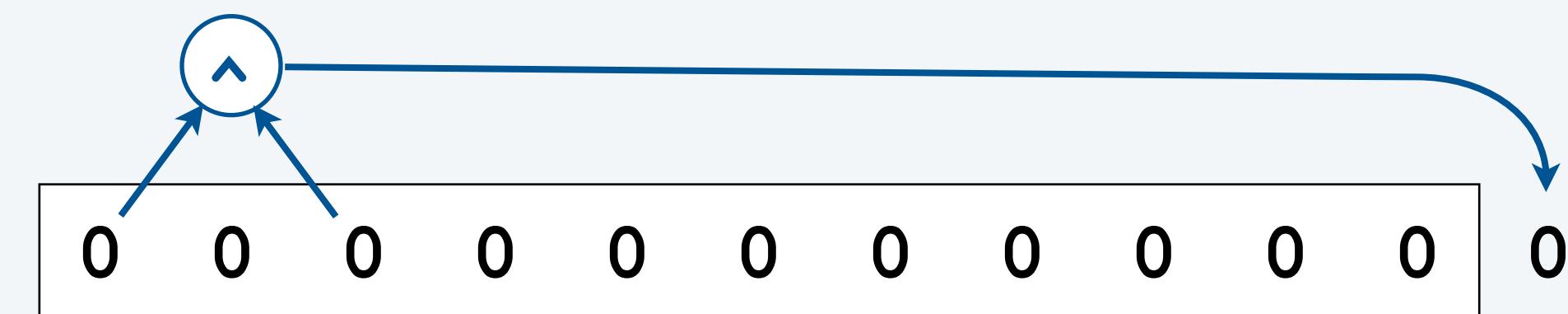
- Ex: 11-bit register implies 2047 possibilities.
- Extremely likely that only *one* of those is not gibberish.
- After this course, *you* could write a program to check whether any of the 2047 messages have words in the dictionary.

Bad news (for Eve): It is easy for Alice and Bob to use a much longer LFSR.

Key properties of LFSRs

Property 1.

- Don't use all 0s as a seed!
- Fill of all 0s will not otherwise occur.

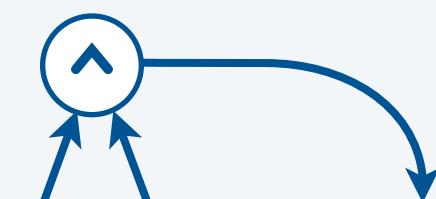


Key properties of LFSRs

Property 1.

- Don't use all 0s as a seed!
- Fill of all 0s will not otherwise occur.

Ex. [4,3] LFSR

	0 0 1 0 0	0
	0 1 0 0 1	1
	1 0 0 1 1	2
	0 0 1 1 0	3
	0 1 1 0 1	4
	1 1 0 1 0	5
	1 0 1 0 1	6
	0 1 0 1 1	7
	1 0 1 1 1	8
	0 1 1 1 1	9
	1 1 1 1 0	10
	1 1 1 0 0	11
	1 1 0 0 0	12
	1 0 0 0 1	13
	0 0 0 1 0	14
	0 0 1 0	15

Property 2. Bitstream must eventually cycle.

- $2^N - 1$ nonzero fills in an N -bit register.
- Future output completely determined by current fill.

Key properties of LFSRs

Property 1.

- Don't use all 0s as a seed!
- Fill of all 0s will not otherwise occur.

Ex. [4,2] LFSR

	0	0	1	0	1	0
	0	1	0	1	1	1
	1	0	1	1	1	2
	0	1	1	1	1	3
	1	1	1	1	0	4
	1	1	1	0	0	5
	1	1	0	0	0	6
	1	0	0	0	1	7
	0	0	0	1	0	8
	0	0	1	0		

Property 2. Bitstream must eventually cycle.

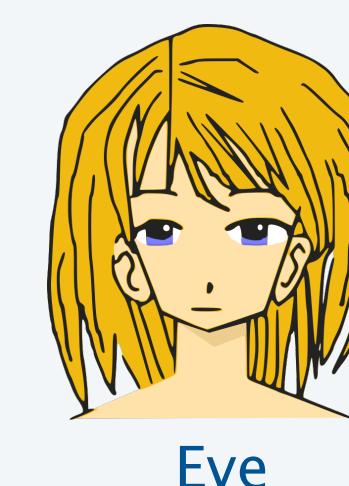
- $2^N - 1$ nonzero fills in an N -bit register.
- Future output completely determined by current fill.

Property 3. Cycle length in an N -bit register is *at most* $2^N - 1$.

- Could be smaller; cycle length depends on tap positions.
- Need theory of finite groups to know good tap positions.

Eve's problem with LFSR encryption

Without the seed, Eve cannot read the message.



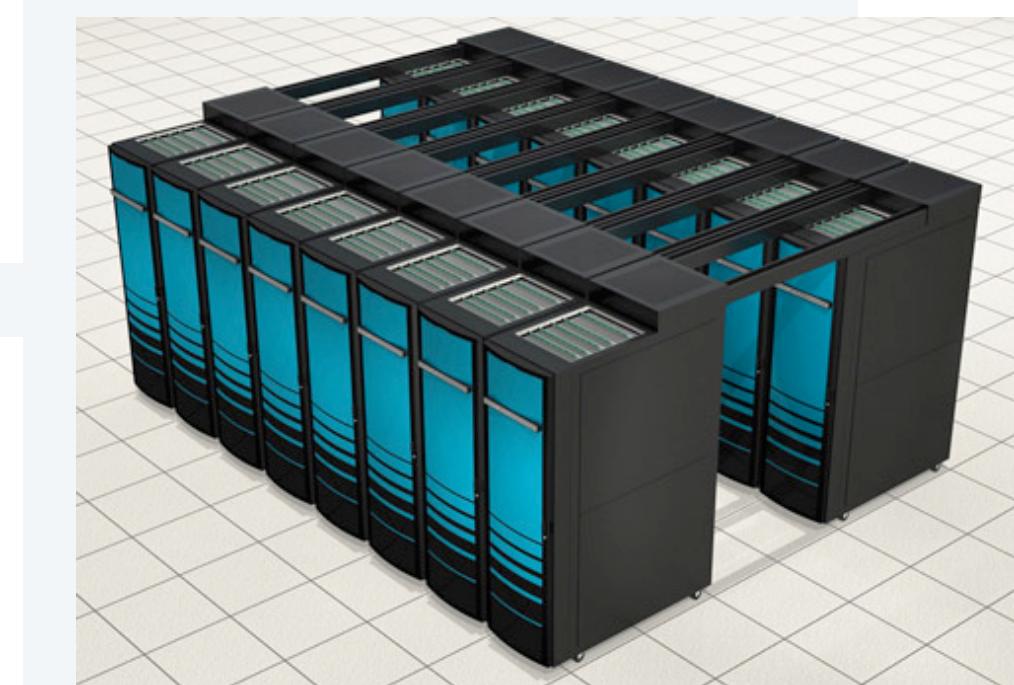
gX76W3v7K ???

Eve has computers. Why not try all possible seeds?

- Seeds are short, messages are long.
- All seeds give a tiny fraction of all messages.

Bad news (for Eve): There are still way too many possibilities.

- Ex: 63-bit register implies $2^{63} - 1$ possibilities.
- If Eve could check 1 million seeds per second, it would take her **2923 centuries** to try them all!



Bad news (for Alice and Bob): LFSR output is *not* random.

experts have cracked LFSRs

Exponential growth dwarfs technological improvements [stay tuned]

(30, 2^{30})

(20, 2^{20})

Goods and bads of LFSRs

Goods.

- Very simple encryption method.
- Decrypt with the same method.
- Scalable: 20 cells for 1 million bits; 30 cells for 1 billion bits.
- Widely used in practice. [Example: military cryptosystems.]



a commercially available LFSR

Bads.

- Easily breakable if seed is re-used.
- Still need secure key distribution.
- Experts can crack LFSR encryption.

Example.

- CSS encryption widely used for DVDs.
- Widely available DeCSS breaks it!

```
/*      efddt.c      Author: Charles M. Hannum <root@ihack.net>
/*      Usage is: cat title-key scrambled.vob | efddt >clear.vob
*/
#define m(i) (x[i]^s[i+84])<<

        unsigned char x[5]      ,y,s[2048];main(
        n){for( read(0,x,5) ;read(0,s ,n=2048
        ); write(1   ,s,n) )if(s
[y=s      [13]&8+20] /16%4 ==1 ){int
i=m(      1)17 ^256 +m(0) 8,k     =m(2)
0,j=      m(4) 17^ m(3) 9^k*    2-k%8
^8,a      =0,c     =26;for   (s[y]     -=16;
--c;j  *=2)a=      a*2^i&    1,i=i /2^j&1
<<24;for(j=      127;      ++j<n;c=c>
y)
c

+=y=i^i/8^i>>4^i>>12,
i=i>>8^y<<17,a^=a>>14,y=a^a*8^a<<6,a=a
>>8^y<<9,k=s[j],k      ="7Wo~'G_\216"[k
&7]+2^"cr3sfw6v,*k+>/n. "[k>>4]*2^k*257/
8,s[j]=k^(k&k*2&34)*6^c+~y
;}}
```

DeCSS DVD decryption code



In the context of this lecture...

Very simple computation procedure

- Can do an important and interesting job
- Can be extremely complicated to understand

Once the understanding is developed

- Build a more complicated machine
- Try to understand it



COMPUTER SCIENCE

SEGEWICK / WAYNE

PART I: PROGRAMMING IN JAVA

Image sources

<http://pixabay.com/en/ball-http-www-crash-administrator-216837/>

<http://commons.wikimedia.org/wiki/File:KnuthAtOpenContentAlliance.jpg>

http://commons.wikimedia.org/wiki/File:Einstein-formal_portrait-35.jpg

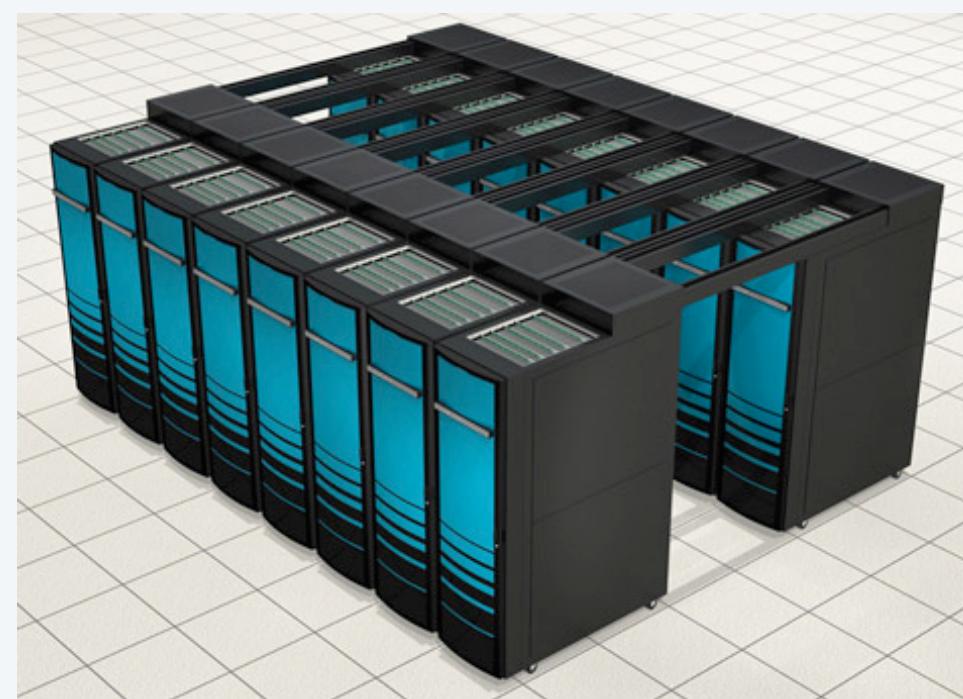
Prologue: A Simple Machine

- Brief introduction
- Secure communication with a one-time pad
- Linear feedback shift registers
- **Implications**

LFSRs and general-purpose computers



LFSR



computer

Important similarities.

- Both are built from simple components.
- Both scale to handle huge problems.
- Both require careful study to use effectively.

component	LFSR	computer
control	start, stop, load	same
clock		same
memory	12 bits	billions of bits
input	12 bits	bit sequence
computation	shift, XOR	+ - * / ...
output	pseudo-random bit sequence	any computable bit sequence

Critical differences: Operations, input. ← but the simplest computers differ only slightly from LFSRs!

- General purpose computer can simulate *any* abstract machine.
- All general purpose computers have equivalent power (!) [stay tuned].

A Profound Idea

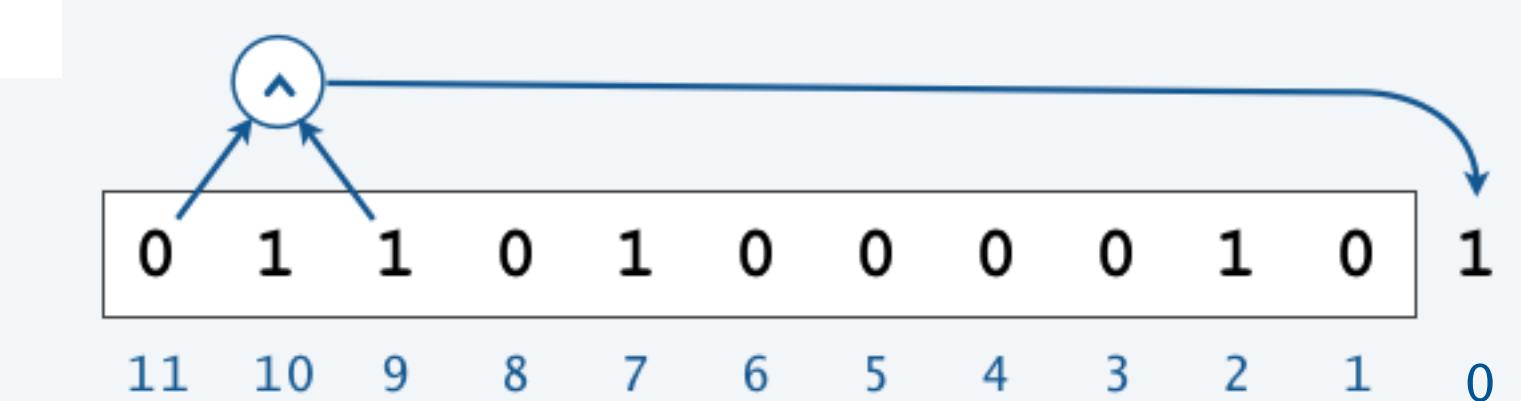
Programming. We can write a Java program to simulate the operation of **any** abstract machine.

- Basis for theoretical understanding of computation.
- Basis for bootstrapping real machines into existence.

Stay tuned (we cover these sorts of issues in this course).

```
public class LFSR
{
    public static void main(String[] args)
    {
        int[] a = { 0, 0, 1, 0, 0, 0, 0, 1, 0, 1, 1, 0 };
        for (int t = 0; t < 2000; t++)
        {
            a[0] = (a[11] ^ a[9]);
            System.out.print(a[0]);
            for (int i = 11; i > 0; i--)
                a[i] = a[i-1];
        }
        System.out.println();
    }
}
```

YOU will be writing
code like this within
a few weeks. →



```
% java LFSR
1100100100111011011100101101011100110001
011111010010001001101001011110011001001
111110111000010101100010000111010100110
1000011110010011001110111111010100000100
0010001010010101000110000010111000100100
11010110111100011010011011100111101...
```

Profound questions

Q. What is a random number?

LFSRs *do not* produce random numbers.

- They are *deterministic*. ← von Neumann's "state of sin": we *know* that "deterministic" is incompatible with "random"
- It is not obvious how to distinguish the bits LFSRs produce from random,
- BUT experts have figured out how to do so.

Q. Are random processes found in nature?

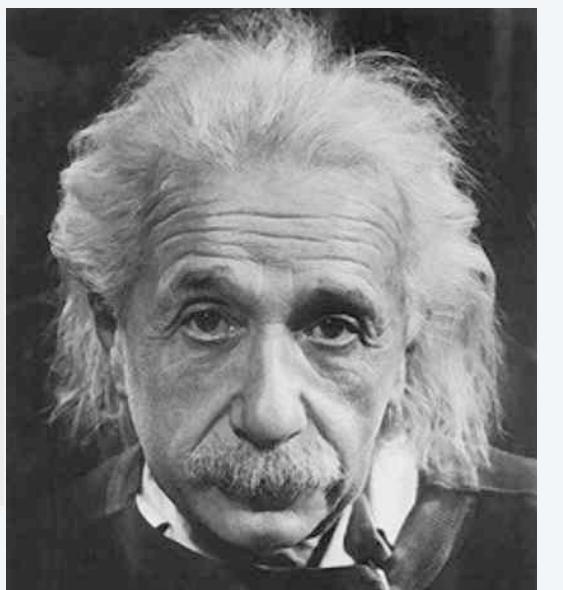
- Motion of cosmic rays or subatomic particles?
- Mutations in DNA?



Q. Is the natural world a (not-so-simple) deterministic machine??

"God does not play dice."

— Albert Einstein





COMPUTER SCIENCE

SEGEWICK / WAYNE

PART I: PROGRAMMING IN JAVA

Image sources

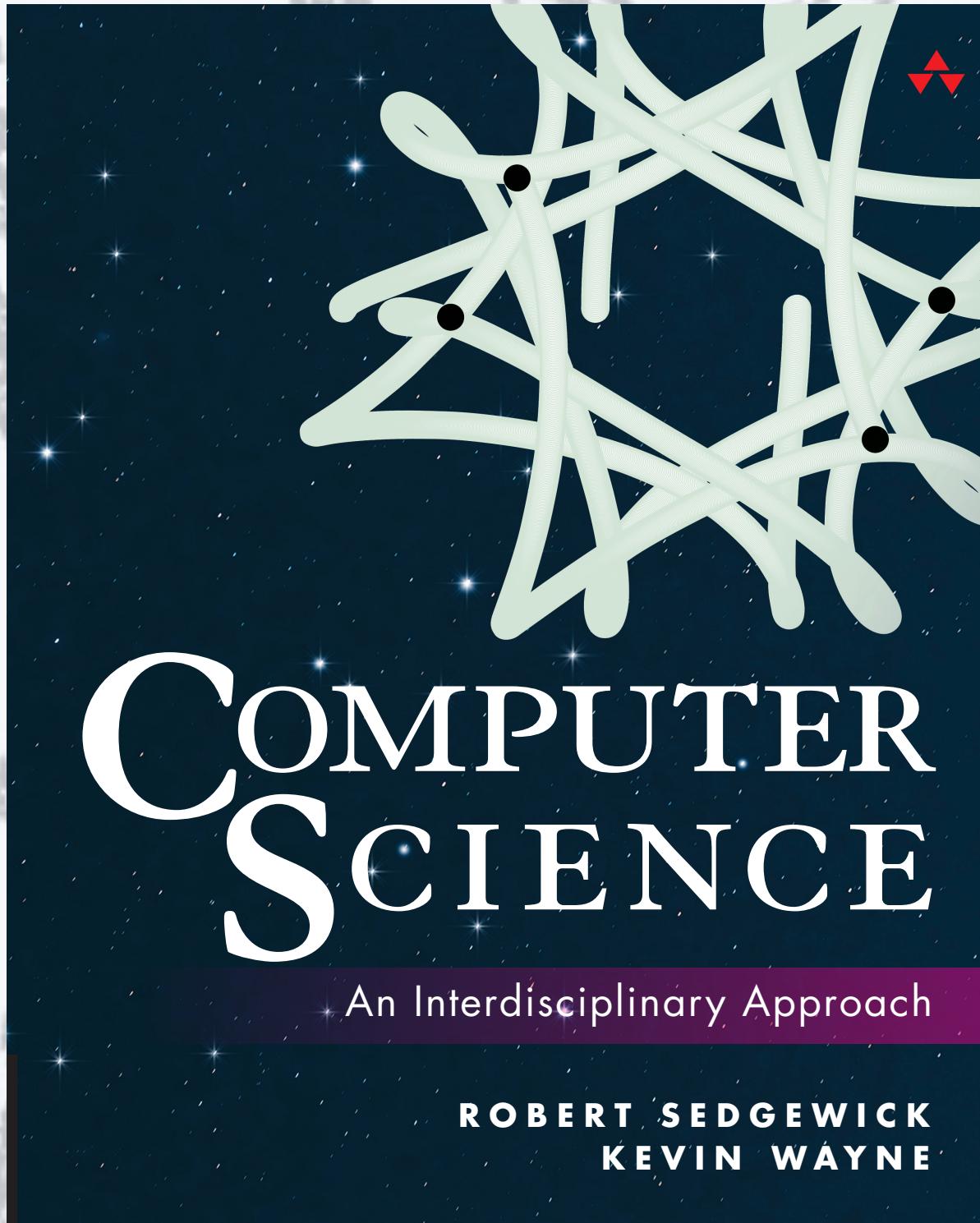
<http://pixabay.com/en/ball-http-www-crash-administrator-216837/>

<http://commons.wikimedia.org/wiki/File:KnuthAtOpenContentAlliance.jpg>

<http://pixabay.com/en/galaxy-space-universe-all-11098/>

http://commons.wikimedia.org/wiki/File:Einstein-formal_portrait-35.jpg

COMPUTER SCIENCE
SEDGEWICK / WAYNE



<http://introcs.cs.princeton.edu>

Prologue: A Simple Machine