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# LSP Exam 2019 - Questions and Answers [Official Answers Included]

> **CVUT FEL (ČVUT) - České vysoké učení technické v Praze | Czech Technical University in Prague**
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> **This file contains official answers (Official Answers Included)**

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## Question 2: RS Latch Circuit Simulation Frequently Tested

**Question**: Given inputs A, B, C values at times t0, t1, t2, t3 as shown, write the Q output value.

...
A = ..0../..1../..1../..1../
B = ..0../..0../..0../..1../
C = ..1../..1../..0../..0../

t0   t1   t2   t3
...

### Answer
...
Q = ...1.../...0.../...0.../...1.../
...

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## Question 3: Shannon Expansion Frequently Tested

**Question**: Decompose the function  $Q=f(A,B,C,Q)$  into:
...

$$Q = (\text{not } Q \text{ and } f_0(A,B,C)) \text{ or } (Q \text{ and } f_1(A,B,C))$$

...

### Solution Method

**Step 1**: Let  $Q=0$ , find  $f_0$ 
...

$$f_0 := f(A,B,C, '0')$$


$$:= (A \quad B) \cdot ('0' + (B \quad C))$$


$$:= (A \quad B) \cdot (B \quad C)$$

...

**Step 2**: Let  $Q=1$ , find  $f_1$ 
...

$$f_1 := f(A,B,C, '1')$$


$$:= (A \quad B) \cdot ('1' + (B \quad C))$$


$$:= (A \quad B) \cdot '1'$$


$$:= (A \quad B)$$

...

### Karnaugh Map for  $f_0: (A \quad B) \cdot (B \quad C)$ 

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...

	C=0	C=1
AB=00	0	1
AB=01	0	0
AB=11	1	0
AB=10	0	0

...

Circle: $(ABC) + (ABC) = (A \oplus B)(B \oplus C)$

Karnaugh Map for f1: $(A \oplus B)$

...

	C=0	C=1
AB=00	1	1
AB=01	0	0
AB=11	1	1
AB=10	0	0

...

Circle: $(AB) + (AB) = (A \oplus B) = A \text{ XNOR } B$

Question 5: Equivalent Logic Functions Frequently Tested

Question: Mark all logic functions that are equivalent to other functions:

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f1 <= (A xor C) or (A and not C);
f2 <= (B or C) and (not A or B or C);
f3 <= ((C and not B) or (B and A));
f4 <= (A or C) and (not A or not C);
f5 <= (A and not B) xor (A and C);
f6 <= (A and not C) or (C and not A);
```

...

### Answer

Analyze each function using Karnaugh maps:

\*\*Karnaugh Map for f4:\*\*

...

```
(A or C) and (not A or not C)
= (A + C) · (A + C)
= A·A + A·C + C·A + C·C
= A·C + A·C
= A ⊕ C
```

...

\*\*Karnaugh Map for f6:\*\*

...

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(A and not C) or (C and not A)
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= A·C + C·A
= A C
...

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Conclusion: **f4 f6** (both are A XOR C)

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Truth Table Quick Reference

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A C (XOR) Truth Table

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| A | C | A C |
|---|---|-----|
| 0 | 0 | 0   |
| 0 | 1 | 1   |
| 1 | 0 | 1   |
| 1 | 1 | 0   |

```

A B (XNOR) Truth Table

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| A | B | A B |
|---|---|-----|
| 0 | 0 | 1   |
| 0 | 1 | 0   |
| 1 | 0 | 0   |
| 1 | 1 | 1   |

```

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Knowledge Summary

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Shannon Expansion Solution Steps

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1. **Identify feedback variable**: Find the variable that is both input and output (e.g., Q)
2. **Substitute Q=0**: Get f0(other variables)
3. **Substitute Q=1**: Get f1(other variables)
4. **Draw Karnaugh maps**: Draw maps for f0 and f1 separately
5. **Verify**:  $Q = Q \cdot f0 + Q \cdot f1$

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Equivalent Function Identification Tips

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1. First simplify each expression
2. Compare using Karnaugh maps
3. Note XOR and XNOR equivalent forms:
  - $A \oplus C = A \cdot C + A \cdot C$
  - $A \oplus C = A \cdot C + A \cdot C = (A \oplus C)$