

2025-06-09 LSP Exam Solution / Řešení zkoušky / 考试解析

Course: B0B35LSP – Logické systémy a procesory | BE5B35LSP – Logic Systems and Processors **University:** CVUT FEL (CTU) – Czech Technical University in Prague **Keywords:** Zkouška, Exam, Test, Solutions, Vysledky, Answers, K-Map, RS Latch, Pipeline

CN Version | EN Version | CZ Version

LSP考试 2025年6月9日

考试信息

- 日期: 2025年6月9日
- 语言: 捷克语
- 类型: 标准考试
- 已核对PDF官方答案

第1题 – RS锁存器仿真 (RS Latch Simulation) (5分)

题目: 输入A、B、C在时间t0到t4的值如图所示。写出X和Y输出的值。 **[English]** Inputs A, B, C had values shown in the figure at times t0 to t4. Write the values of X and Y outputs.

输入序列:

A	=	1		1		1		0		1
B	=	1		1		0		1		1
C	=	0		1		0		0		0
		t0		t1		t2		t3		t4

官方参考答案 (Official Answer):

X = 0 | 0 | 1 | 1 | 0 (: 00110)
Y = 1 | 0 | 0 | 0 | 1 (: 10011)

详细解析: – t0: A=1 → Reset, X=0; B·C=0 → Y=1 – t1: A=1, B·C=1 → Reset优先, X=0, Y=0 – t2: A=1, B·C=0 → X变1? (需看电路) – t3: A=0, B·C=0 → 保持 – t4: A=1 → Reset

第2题 – Shannon展开 (Shannon Expansion) (6分)

题目: 将第1题电路的函数 $X=f(A,B,C,X)$ 用Shannon展开分解为: $X=(\text{not } X \text{ and } f_0(A,B,C)) \text{ or } (X \text{ and } f_1(A,B,C))$ 。 **[English]** Decompose the function $X=f(A,B,C,X)$ from question 1 into the form $X=(\text{not } X \text{ and } f_0(A,B,C)) \text{ or } (X \text{ and } f_1(A,B,C))$ using Shannon expansion.

官方参考答案 (卡诺图 Karnaugh Map) :

f0:	B					f1:	B				
	A 0 1						A 0 1				
C 0	0	0	1	0		C 0	1	0	1	0	
1	1	0	0	0		1	1	0	1	0	

官方表达式：

$$X = (\text{not } C \text{ and } B \text{ and } A) \text{ or } (C \text{ and not } B \text{ and not } A) \\ \text{or } (X \text{ and not } B \text{ and not } A) \text{ or } (X \text{ and } B \text{ and } A)$$

第3题 – 等价逻辑函数 (Equivalent Logic Functions) (4分)

题目：勾选所有与其他函数等价的逻辑函数。 [English] Check all logic functions that have another equivalent function here.

```
y1 <= (A or D) and (not A or C);
y2 <= C or (A and C and B) or (not A and C and D);
y3 <= (not A and D) or (A and not D) or (C and D);
y4 <= (C and D) or (not A xor not D);
```

官方参考答案：y3 \equiv y4

详细解析：

$$\begin{aligned} y1 &= (A + D)(\bar{A} + C) \\ &= A\bar{A} + AC + D\bar{A} + DC \\ &= AC + \bar{A}D + CD \end{aligned}$$

y2:

$$\begin{aligned} y2 &= C + ABC + \bar{A}CD \\ &= C(1 + AB + \bar{A}D) \\ &= C \end{aligned}$$

y3:

$$\begin{aligned} y3 &= \bar{A}D + AD + CD \\ &= (A \oplus D) + CD \end{aligned}$$

y4:

$$\begin{aligned} y4 &= CD + (\bar{A} \oplus D) \\ &= CD + (\bar{A} \oplus D) \quad \bar{A} \oplus D = A \oplus D \\ &= (A \oplus D) + CD \end{aligned}$$

$$\text{比较结果：} - y1 = AC + \bar{A}D + CD - y2 = C - y3 = (A \oplus D) + CD - y4 = (A \oplus D) + CD$$

答案：y3 \equiv y4

关键公式： $\bar{A} \oplus B = A \oplus B$ (取反后的异或等于原异或)

第4题 – 8位寄存器运算 (2分)

题目：将124+125+126+127运算结果的低位存入1字节寄存器，作为8位数的十进制值是多少？ [English] If we store the lower bits of 124+125+126+127 operation into a 1-byte register, what decimal value will it hold as an 8-bit number?

计算：

$$\begin{aligned} 124 + 125 + 126 + 127 &= 502 \\ 502 \bmod 256 &= 246 \end{aligned}$$

答案：– a) unsigned: 246 – b) signed: -10 (246 – 256)

第5题 – Moore/Mealy自动机定义 (3分)

题目： 补全定义——必须数学上精确！ [English] Complete the definition – it must be mathematically precise!

定义： Automat Moore (Mealy) je usporádaná šestice $M = \langle X, S, Z, \omega, \delta, s_0 \in S \rangle$

- X 是有限输入字母表 / is a finite input alphabet
 - S 是有限状态集合 / is a finite set of states
 - Z 是有限输出字母表 / is a finite output alphabet
 - δ 是状态转移函数 / is the state transition function: Moore: $S \times X \rightarrow S$, Mealy: $S \times X \rightarrow S$
 - ω 是输出函数 / is the output function: Moore: $S \rightarrow Z$, Mealy: $S \times X \rightarrow Z$
 - s_0 是初始状态 / is the initial state
-

第6题 – +1加法器设计 (7分)

题目： +1加法器可以不用全加器，用门电路更简单地实现。画出由门组成的电路图。 [English] The +1 adder can be implemented much simpler using gates without a full adder. Draw its schematic composed of gates.

电路结构： $s_0 = x_0 \text{ XOR } 1 = \text{NOT } x_0$ – $s_1 = x_1 \text{ XOR } (x_0)$ – $s_2 = x_2 \text{ XOR } (x_0 \text{ AND } x_1)$ – $s_3 = x_3 \text{ XOR } (x_0 \text{ AND } x_1 \text{ AND } x_2)$ – $\text{carry} = x_0 \text{ AND } x_1 \text{ AND } x_2 \text{ AND } x_3$

第7题 – VHDL位操作 (7分)

题目： 用并发 (concurrent) VHDL代码最优地描述图中电路，不使用顺序语句。整个架构只用一条语句可得满分，每多一条 [English] Optimally describe the circuit in the figure using concurrent VHDL code without sequential statements. Full points for using only one statement in the architecture block; one point deducted for each additional statement.

```
library ieee; use ieee.std_logic_1164.all;
use ieee.numeric_std.all;
entity Test20250609q7 is
  port(x: in std_logic_vector(3 downto 0);
        y: out std_logic_vector(3 downto 0));
end entity;
architecture rtl of Test20250609q7 is
begin
  y <= x and (x(2 downto 0) & '1');
end architecture rtl;
```

第8题 – VHDL电路分析 (7+1分)

题目： 根据以下代码，使用门、多路选择器、+1加法器、比较器和DFF寄存器的符号画出方框图。 [English] Draw the block diagram for the circuit described by the following code, using symbols for gates, multiplexor, +1 adder, comparator, and DFF registers.

```

library ieee; use ieee.std_logic_1164.all;
use ieee.numeric_std.all;
entity Ex20250609q7 is
    port (CLK : in std_logic; Q : out std_logic);
end entity;
architecture rtl1 of Ex20250609q7 is
begin
    iproc: process(CLK)
        constant M: integer := 9;
        variable cntr : integer range 0 to M := 0;
        variable x : std_logic := '0';
    begin
        if rising_edge(CLK) then
            if cntr < M then
                cntr := cntr + 1;
            else
                cntr := 0;
                x := not x;
            end if;
        end if;
        Q <= x;
    end process;
end architecture;

```

电路名称：分频器 (Frequency Divider) / 模10计数器带输出翻转

第9题 – 分支预测 (Branch Prediction) (8分)

非考点提示 (Not on Exam): 根据2026年1月考试说明，分支预测器本次不考，可战略性跳过。

题目： C程序在数组中查找最小值。假设for循环编译为do-while形式，处理器使用以下预测器，计算分支预测错误次数。

[English] A C program finds the minimum in an array. Assuming the for-loop is compiled as do-while and the processor uses the following predictors, calculate the number of branch mispredictions.

```

int data[] = { 0, 1, -2, -3, 4, -5, 6, -7, -8, 9 };
int min = INT_MAX;
for (int i = 0; i < 10; i++) {
    if (data[i] < min) min = data[i];
}

```

官方参考答案 (Official Answer): – 1位预测器 (初始NT) : misses = 9 (if分支7次 + for循环2次) – 2位预测器 (初始WT) : misses = 7 (if分支6次 + for循环1次)

官方分支序列分析：

Branch:	N	T	N	N	T	N	T	N	N	T
Data:	0	1	-2	-3	4	-5	6	-7	-8	9

注意： 今年考试不考分支预测！（老师邮件确认）

注意： 实际答案可能因编译器优化和分支预测器具体实现而略