

LSP Exam – 2018年1月15日

CVUT FEL (ČVUT) – České vysoké učení technické v Praze | Czech Technical University in Prague

中文版 | English | Cěstina

AI推演版本 – 以下为解析参考

题目4: 有符号/无符号数位值 常考

题目: 10位二进制数 10 0000 1111 的十进制值是多少? [English] What is the decimal value of the 10-bit binary number 10 0000 1111?

a) 无符号数(unsigned): _____

b) 有符号数(two's-complement): _____

详细解答

: 10 0000 1111
: 9 8765 4321 0

a) 无符号数计算:

$$\begin{aligned} &= 1 \times 2^9 + 0 \times 2^8 + 0 \times 2^7 + 0 \times 2^6 + 0 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 \\ &= 512 + 0 + 0 + 0 + 0 + 0 + 8 + 4 + 2 + 1 \\ &= 527 \end{aligned}$$

b) 有符号数(补码)计算:

方法1 – 直接计算:

$$\begin{aligned} &: -2^9 + () \\ &= -512 + (0 \times 2^8 + \dots + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0) \\ &= -512 + 15 \\ &= -497 \end{aligned}$$

方法2 – 取反加1:

$$\begin{aligned} &: 10 0000 1111 \\ &: 01 1111 0000 \\ 1: & 01 1111 0001 = 497 \\ &= -497 \end{aligned}$$

题目5: 等价逻辑函数 常考

题目: 标记所有与其他函数等价的逻辑函数: [English] Mark all logic functions that are equivalent to other functions:

```
f1 <= (A xor C) or (A and not C);  
f2 <= (B or C) and (not A or B or C);  
f3 <= ((C and not B) or (B and A));  
f4 <= (A or C) and (not A or not C);
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f5 <= (A and not B) xor (A and C);
f6 <= (A and not C) or (C and not A);
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用卡诺图求解每个函数

$f1 = (A \oplus C) \text{ or } (A \text{ and not } C)$

$f1$	$C=0$	$C=1$
A=0	0	1
A=1	1	1

$$f1 = A + C$$

$f2 = (B \text{ or } C) \text{ and } (\text{not } A \text{ or } B \text{ or } C)$

$f2$	$BC=00$	$BC=01$	$BC=11$	$BC=10$
A=0	0	1	1	1
A=1	0	1	1	0

$f3 = (C \text{ and not } B) \text{ or } (B \text{ and } A)$

$f3$	$BC=00$	$BC=01$	$BC=11$	$BC=10$
A=0	0	1	0	0
A=1	0	1	1	0

$f4 = (A \text{ or } C) \text{ and } (\text{not } A \text{ or not } C)$

$f4$	$C=0$	$C=1$
A=0	0	1
A=1	1	0

$f4 = A \oplus C$ (异或)

$f5 = (A \text{ and not } B) \text{ xor } (A \text{ and } C)$ 需要详细展开...

$f6 = (A \text{ and not } C) \text{ or } (C \text{ and not } A)$

$f6$	$C=0$	$C=1$
A=0	0	1
A=1	1	0

$f6 = A \oplus C$ (异或)

结论

$f4 \equiv f6$ (都等于 A XOR C)

题目: RS锁存器电路仿真 常考

题目: 根据给定电路, 输入A, B, C在时刻t0, t1, t2, t3的值如下, 写出Q输出值。[English] Given the circuit, write the Q output value for inputs A, B, C at times t0, t1, t2, t3 as shown.

A = ...0...|...1...|...1...|...1...

B = ...0...|...0...|...0...|...1...

C = ..1..|..1..|...0...|...0...|

t0 t1 t2 t3

答案

Q = ...1...|...0...|...0...|...1...|

题目: 香农展开 常考

将函数分解为:

Q = (not Q and f0(A,B,C)) or (Q and f1(A,B,C))

解题过程

f0 := f(A,B,C,'0') := (A B) + (B C)

f1 := f(A,B,C,'1') := (A B)

f0 的卡诺图

f0	C=0	C=1
AB=00	0	1
AB=01	0	0
AB=11	1	0
AB=10	0	0

f1 的卡诺图

f1	C=0	C=1
AB=00	1	1
AB=01	0	0
AB=11	1	1
AB=10	0	0

知识点速查

有符号数计算公式

- n 位补码范围: $[-2^{n-1}, 2^{n-1} - 1]$
- 负数计算: $-2^{n-1} + ()$

等价函数判断方法

1. 画出每个函数的卡诺图
2. 比较卡诺图是否完全相同
3. 相同的函数即为等价函数

香农展开公式

$$f(x_1, x_2, \dots, x_n, Q) = \bar{Q} \cdot f_0 + Q \cdot f_1$$

其中: $-f_0 = f(x_1, x_2, \dots, x_n, 0)$ $-f_1 = f(x_1, x_2, \dots, x_n, 1)$