### **Problems & Exercises**

### **10.1 Angular Acceleration**

1. At its peak, a tornado is 60.0 m in diameter and carries 500 km/h winds. What is its angular velocity in revolutions per second?

#### 2. Integrated Concepts

An ultracentrifuge accelerates from rest to 100,000 rpm in 2.00 min. (a) What is its angular acceleration in  $\operatorname{rad/s^2}$ ? (b) What is the tangential acceleration of a point 9.50 cm from the axis of rotation? (c) What is the radial acceleration in  $\operatorname{m/s^2}$  and multiples of g of this point at full rpm?

### 3. Integrated Concepts

You have a grindstone (a disk) that is 90.0 kg, has a 0.340-m radius, and is turning at 90.0 rpm, and you press a steel axe against it with a radial force of 20.0 N. (a) Assuming the kinetic coefficient of friction between steel and stone is 0.20, calculate the angular acceleration of the grindstone. (b) How many turns will the stone make before coming to rest?

#### 4. Unreasonable Results

You are told that a basketball player spins the ball with an angular acceleration of  $100 \, \text{rad/s}^2$ . (a) What is the ball's final angular velocity if the ball starts from rest and the acceleration lasts 2.00 s? (b) What is unreasonable about the result? (c) Which premises are unreasonable or inconsistent?

### **10.2 Kinematics of Rotational Motion**

- **5.** With the aid of a string, a gyroscope is accelerated from rest to 32 rad/s in 0.40 s.
- (a) What is its angular acceleration in rad/s<sup>2</sup>?
- (b) How many revolutions does it go through in the process?
- **6.** Suppose a piece of dust finds itself on a CD. If the spin rate of the CD is 500 rpm, and the piece of dust is 4.3 cm from the center, what is the total distance traveled by the dust in 3 minutes? (Ignore accelerations due to getting the CD rotating.)
- **7.** A gyroscope slows from an initial rate of 32.0 rad/s at a rate of  $0.700 \text{ rad/s}^2$ .
- (a) How long does it take to come to rest?
- (b) How many revolutions does it make before stopping?

- **8.** During a very quick stop, a car decelerates at  $7.00 \text{ m/s}^2$ .
- (a) What is the angular acceleration of its 0.280-m-radius tires, assuming they do not slip on the pavement?
- (b) How many revolutions do the tires make before coming to rest, given their initial angular velocity is 95.0 rad/s?
- (c) How long does the car take to stop completely?
- (d) What distance does the car travel in this time?
- (e) What was the car's initial velocity?
- (f) Do the values obtained seem reasonable, considering that this stop happens very quickly?



Figure 10.37 Yo-yos are amusing toys that display significant physics and are engineered to enhance performance based on physical laws. (credit: Beyond Neon, Flickr)

- **9.** Everyday application: Suppose a yo-yo has a center shaft that has a 0.250 cm radius and that its string is being pulled.
- (a) If the string is stationary and the yo-yo accelerates away from it at a rate of  $1.50~\text{m/s}^2$ , what is the angular acceleration of the yo-yo?
- (c) The outside radius of the yo-yo is 3.50 cm. What is the tangential acceleration of a point on its edge?

### 10.3 Dynamics of Rotational Motion: Rotational Inertia

- 10. This problem considers additional aspects of example Calculating the Effect of Mass Distribution on a Merry-Go-Round. (a) How long does it take the father to give the merry-go-round an angular velocity of 1.50 rad/s? (b) How many revolutions must he go through to generate this velocity? (c) If he exerts a slowing force of 300 N at a radius of 1.35 m, how long would it take him to stop them?
- 11. Calculate the moment of inertia of a skater given the following information. (a) The 60.0-kg skater is approximated as a cylinder that has a 0.110-m radius. (b) The skater with arms extended is approximately a cylinder that is 52.5 kg, has a 0.110-m radius, and has two 0.900-m-long arms which are 3.75 kg each and extend straight out from the cylinder like rods rotated about their ends.
- 12. The triceps muscle in the back of the upper arm extends the forearm. This muscle in a professional boxer exerts a force of  $2.00\times10^3~N$  with an effective perpendicular lever arm of 3.00 cm, producing an angular acceleration of the forearm of  $120~rad/s^2$ . What is the moment of inertia of the boxer's forearm?

13. A soccer player extends her lower leg in a kicking motion by exerting a force with the muscle above the knee in the front of her leg. She produces an angular acceleration of  $30.00\ rad/s^2$  and her lower leg has a moment of inertia of  $0.750\ kg\cdot m^2$ . What is the force exerted by the muscle if its effective perpendicular lever arm is 1.90 cm?

**14.** Suppose you exert a force of 180 N tangential to a 0.280-m-radius 75.0-kg grindstone (a solid disk).

(a)What torque is exerted? (b) What is the angular acceleration assuming negligible opposing friction? (c) What is the angular acceleration if there is an opposing frictional force of 20.0 N exerted 1.50 cm from the axis?

**15.** Consider the 12.0 kg motorcycle wheel shown in Figure 10.38. Assume it to be approximately an annular ring with an inner radius of 0.280 m and an outer radius of 0.330 m. The motorcycle is on its center stand, so that the wheel can spin freely. (a) If the drive chain exerts a force of 2200 N at a radius of 5.00 cm, what is the angular acceleration of the wheel? (b) What is the tangential acceleration of a point on the outer edge of the tire? (c) How long, starting from rest, does it take to reach an angular velocity of 80.0 rad/s?

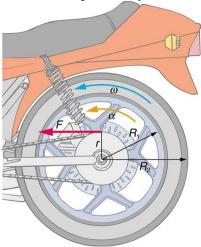


Figure 10.38 A motorcycle wheel has a moment of inertia approximately that of an annular ring.

**16.** Zorch, an archenemy of Superman, decides to slow Earth's rotation to once per 28.0 h by exerting an opposing force at and parallel to the equator. Superman is not immediately concerned, because he knows Zorch can only exert a force of  $4.00\times10^7~\rm N$  (a little greater than a Saturn V rocket's thrust). How long must Zorch push with this force to accomplish his goal? (This period gives Superman time to devote to other villains.) Explicitly show how you follow the steps found in **Problem-Solving Strategy for Rotational Dynamics**.

17. An automobile engine can produce 200 N  $\cdot$  m of torque. Calculate the angular acceleration produced if 95.0% of this torque is applied to the drive shaft, axle, and rear wheels of a car, given the following information. The car is suspended so that the wheels can turn freely. Each wheel acts like a 15.0 kg disk that has a 0.180 m radius. The walls of each tire act like a 2.00-kg annular ring that has inside radius of 0.180 m and outside radius of 0.320 m. The tread of each tire acts like a 10.0-kg hoop of radius 0.330 m. The 14.0-kg axle acts like a rod that has a 2.00-cm radius. The 30.0-kg drive shaft acts like a rod that has a 3.20-cm radius.

**18.** Starting with the formula for the moment of inertia of a rod rotated around an axis through one end perpendicular to its length  $\left(I=M\ell^{-2}/3\right)$ , prove that the moment of inertia of a rod rotated about an axis through its center perpendicular to its length is  $I=M\ell^{-2}/12$ . You will find the graphics in **Figure 10.12** useful in visualizing these rotations.

#### 19. Unreasonable Results

A gymnast doing a forward flip lands on the mat and exerts a 500-N  $\cdot$  m torque to slow and then reverse her angular velocity. Her initial angular velocity is 10.0 rad/s, and her moment of inertia is  $0.050~kg \cdot m^2$ . (a) What time is required for her to exactly reverse her spin? (b) What is unreasonable about the result? (c) Which premises are unreasonable or inconsistent?

### 20. Unreasonable Results

An advertisement claims that an 800-kg car is aided by its 20.0-kg flywheel, which can accelerate the car from rest to a speed of 30.0 m/s. The flywheel is a disk with a 0.150-m radius. (a) Calculate the angular velocity the flywheel must have if 95.0% of its rotational energy is used to get the car up to speed. (b) What is unreasonable about the result? (c) Which premise is unreasonable or which premises are inconsistent?

### 10.4 Rotational Kinetic Energy: Work and Energy Revisited

21. This problem considers energy and work aspects of Example 10.7—use data from that example as needed. (a) Calculate the rotational kinetic energy in the merry-go-round plus child when they have an angular velocity of 20.0 rpm. (b) Using energy considerations, find the number of revolutions the father will have to push to achieve this angular velocity starting from rest. (c) Again, using energy considerations, calculate the force the father must exert to stop the merry-go-round in two revolutions

- **22.** What is the final velocity of a hoop that rolls without slipping down a 5.00-m-high hill, starting from rest?
- **23.** (a) Calculate the rotational kinetic energy of Earth on its axis. (b) What is the rotational kinetic energy of Earth in its orbit around the Sun?
- **24.** Calculate the rotational kinetic energy in the motorcycle wheel (Figure 10.38) if its angular velocity is 120 rad/s. Assume M = 12.0 kg,  $R_1 = 0.280$  m, and  $R_2 = 0.330$  m.
- **25.** A baseball pitcher throws the ball in a motion where there is rotation of the forearm about the elbow joint as well as other movements. If the linear velocity of the ball relative to the elbow joint is 20.0 m/s at a distance of 0.480 m from the joint and the moment of inertia of the forearm is
- $0.500\; kg \cdot m^2$  , what is the rotational kinetic energy of the forearm?
- **26.** While punting a football, a kicker rotates his leg about the hip joint. The moment of inertia of the leg is  $3.75~{\rm kg\cdot m^2}$  and its rotational kinetic energy is 175 J. (a) What is the angular velocity of the leg? (b) What is the velocity of tip of the punter's shoe if it is 1.05 m from the hip joint? (c) Explain how the football can be given a velocity greater than the tip of the shoe (necessary for a decent kick distance).

- 27. A bus contains a 1500 kg flywheel (a disk that has a 0.600 m radius) and has a total mass of 10,000 kg. (a) Calculate the angular velocity the flywheel must have to contain enough energy to take the bus from rest to a speed of 20.0 m/s, assuming 90.0% of the rotational kinetic energy can be transformed into translational energy. (b) How high a hill can the bus climb with this stored energy and still have a speed of 3.00 m/s at the top of the hill? Explicitly show how you follow the steps in the Problem-Solving Strategy for Rotational Energy.
- **28.** A ball with an initial velocity of 8.00 m/s rolls up a hill without slipping. Treating the ball as a spherical shell, calculate the vertical height it reaches. (b) Repeat the calculation for the same ball if it slides up the hill without rolling.
- **29.** While exercising in a fitness center, a man lies face down on a bench and lifts a weight with one lower leg by contacting the muscles in the back of the upper leg. (a) Find the angular acceleration produced given the mass lifted is 10.0 kg at a distance of 28.0 cm from the knee joint, the moment of inertia of the lower leg is  $0.900~kg\cdot m^2$ , the muscle force is 1500 N, and its effective perpendicular lever arm is 3.00 cm. (b) How much work is done if the leg rotates through an angle of
- **30.** To develop muscle tone, a woman lifts a 2.00-kg weight held in her hand. She uses her biceps muscle to flex the lower arm through an angle of  $60.0^{\circ}$ . (a) What is the angular acceleration if the weight is 24.0 cm from the elbow joint, her forearm has a moment of inertia of  $0.250~{\rm kg\cdot m^2}$ , and the net force she exerts is 750 N at an effective perpendicular lever arm of 2.00 cm? (b) How much work does she do?

20.0° with a constant force exerted by the muscle?

- **31.** Consider two cylinders that start down identical inclines from rest except that one is frictionless. Thus one cylinder rolls without slipping, while the other slides frictionlessly without rolling. They both travel a short distance at the bottom and then start up another incline. (a) Show that they both reach the same height on the other incline, and that this height is equal to their original height. (b) Find the ratio of the time the rolling cylinder takes to reach the height on the second incline to the time the sliding cylinder takes to reach the height on the second incline. (c) Explain why the time for the rolling motion is greater than that for the sliding motion.
- **32.** What is the moment of inertia of an object that rolls without slipping down a 2.00-m-high incline starting from rest, and has a final velocity of 6.00 m/s? Express the moment of inertia as a multiple of  $MR^2$ , where M is the mass of the object and R is its radius.
- **33.** Suppose a 200-kg motorcycle has two wheels like, the one described in **Example 10.15** and is heading toward a hill at a speed of 30.0 m/s. (a) How high can it coast up the hill, if you neglect friction? (b) How much energy is lost to friction if the motorcycle only gains an altitude of 35.0 m before coming to rest?
- **34.** In softball, the pitcher throws with the arm fully extended (straight at the elbow). In a fast pitch the ball leaves the hand with a speed of 139 km/h. (a) Find the rotational kinetic energy of the pitcher's arm given its moment of inertia is  $0.720~kg\cdot m^2$  and the ball leaves the hand at a distance of

0.600 m from the pivot at the shoulder. (b) What force did the muscles exert to cause the arm to rotate if their effective perpendicular lever arm is 4.00 cm and the ball is 0.156 kg?

#### 35. Construct Your Own Problem

Consider the work done by a spinning skater pulling her arms in to increase her rate of spin. Construct a problem in which you calculate the work done with a "force multiplied by distance" calculation and compare it to the skater's increase in kinetic energy.

### **10.5 Angular Momentum and Its Conservation**

- **36.** (a) Calculate the angular momentum of the Earth in its orbit around the Sun.
- (b) Compare this angular momentum with the angular momentum of Earth on its axis.
- **37.** (a) What is the angular momentum of the Moon in its orbit around Earth?
- (b) How does this angular momentum compare with the angular momentum of the Moon on its axis? Remember that the Moon keeps one side toward Earth at all times.
- (c) Discuss whether the values found in parts (a) and (b) seem consistent with the fact that tidal effects with Earth have caused the Moon to rotate with one side always facing Earth.
- **38.** Suppose you start an antique car by exerting a force of 300 N on its crank for 0.250 s. What angular momentum is given to the engine if the handle of the crank is 0.300 m from the pivot and the force is exerted to create maximum torque the entire time?
- **39.** A playground merry-go-round has a mass of 120 kg and a radius of 1.80 m and it is rotating with an angular velocity of 0.500 rev/s. What is its angular velocity after a 22.0-kg child gets onto it by grabbing its outer edge? The child is initially at rest.
- **40.** Three children are riding on the edge of a merry-go-round that is 100 kg, has a 1.60-m radius, and is spinning at 20.0 rpm. The children have masses of 22.0, 28.0, and 33.0 kg. If the child who has a mass of 28.0 kg moves to the center of the merry-go-round, what is the new angular velocity in rpm?
- **41.** (a) Calculate the angular momentum of an ice skater spinning at 6.00 rev/s given his moment of inertia is
- $0.400~kg\cdot m^2$  . (b) He reduces his rate of spin (his angular velocity) by extending his arms and increasing his moment of inertia. Find the value of his moment of inertia if his angular velocity decreases to 1.25 rev/s. (c) Suppose instead he keeps his arms in and allows friction of the ice to slow him to 3.00 rev/s. What average torque was exerted if this takes 15.0 s?
- **42.** Consider the Earth-Moon system. Construct a problem in which you calculate the total angular momentum of the system including the spins of the Earth and the Moon on their axes and the orbital angular momentum of the Earth-Moon system in its nearly monthly rotation. Calculate what happens to the Moon's orbital radius if the Earth's rotation decreases due to tidal drag. Among the things to be considered are the amount by which the Earth's rotation slows and the fact that the Moon will continue to have one side always facing the Earth.

### **10.6 Collisions of Extended Bodies in Two Dimensions**

**43.** Repeat Example 10.15 in which the disk strikes and adheres to the stick 0.100 m from the nail.

- **44.** Repeat Example 10.15 in which the disk originally spins clockwise at 1000 rpm and has a radius of 1.50 cm.
- **45.** Twin skaters approach one another as shown in Figure **10.39** and lock hands. (a) Calculate their final angular velocity, given each had an initial speed of 2.50 m/s relative to the ice. Each has a mass of 70.0 kg, and each has a center of mass located 0.800 m from their locked hands. You may approximate their moments of inertia to be that of point masses at this radius. (b) Compare the initial kinetic energy and final kinetic energy.

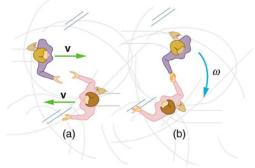


Figure 10.39 Twin skaters approach each other with identical speeds. Then, the skaters lock hands and spin.

- **46.** Suppose a 0.250-kg ball is thrown at 15.0 m/s to a motionless person standing on ice who catches it with an outstretched arm as shown in **Figure 10.40**.
- (a) Calculate the final linear velocity of the person, given his mass is 70.0 kg.
- (b) What is his angular velocity if each arm is 5.00 kg? You may treat the ball as a point mass and treat the person's arms as uniform rods (each has a length of 0.900 m) and the rest of his body as a uniform cylinder of radius 0.180 m. Neglect the effect of the ball on his center of mass so that his center of mass remains in his geometrical center.
- (c) Compare the initial and final total kinetic energies.

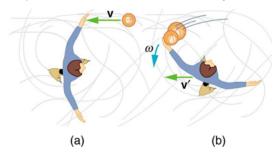


Figure 10.40 The figure shows the overhead view of a person standing motionless on ice about to catch a ball. Both arms are outstretched. After catching the ball, the skater recoils and rotates.

**47.** Repeat Example 10.15 in which the stick is free to have translational motion as well as rotational motion.

### **Test Prep for AP® Courses**

### 10.3 Dynamics of Rotational Motion: Rotational Inertia

1. A piece of wood can be carved by spinning it on a motorized lathe and holding a sharp chisel to the edge of the wood as it spins. How does the angular velocity of a piece of wood with a radius of 0.2 m spinning on a lathe change when

### **10.7 Gyroscopic Effects: Vector Aspects of Angular Momentum**

#### 48. Integrated Concepts

The axis of Earth makes a 23.5° angle with a direction perpendicular to the plane of Earth's orbit. As shown in Figure 10.41, this axis precesses, making one complete rotation in 25,780 y.

- (a) Calculate the change in angular momentum in half this time.
- (b) What is the average torque producing this change in angular momentum?
- (c) If this torque were created by a single force (it is not) acting at the most effective point on the equator, what would its magnitude be?

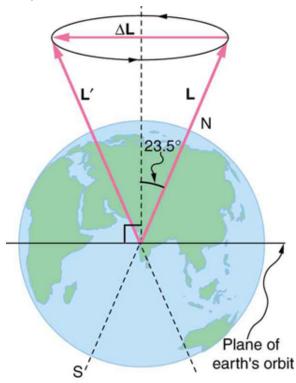


Figure 10.41 The Earth's axis slowly precesses, always making an angle of 23.5° with the direction perpendicular to the plane of Earth's orbit. The change in angular momentum for the two shown positions is quite large, although the magnitude  $\,L\,$  is unchanged.

a chisel is held to the wood's edge with a force of 50 N?

- a. It increases by 0.1 N•m multiplied by the moment of inertia of the wood.
- It decreases by 0.1 N•m divided by the moment of inertia of the wood-and-lathe system.
- It decreases by 0.1 N•m multiplied by the moment of inertia of the wood.
- d. It decreases by  $0.1 \text{ m/s}^2$ .

- **2.** A Ferris wheel is loaded with people in the chairs at the following positions: 4 o'clock, 1 o'clock, 9 o'clock, and 6 o'clock. As the wheel begins to turn, what forces are acting on the system? How will each force affect the angular velocity and angular momentum?
- **3.** A lever is placed on a fulcrum. A rock is placed on the left end of the lever and a downward (clockwise) force is applied to the right end of the lever. What measurements would be most effective to help you determine the angular momentum of the system? (Assume the lever itself has negligible mass.)
- a. the angular velocity and mass of the rock
- the angular velocity and mass of the rock, and the radius of the lever
- the velocity of the force, the radius of the lever, and the mass of the rock
- the mass of the rock, the length of the lever on both sides of the fulcrum, and the force applied on the right side of the lever
- **4.** You can use the following setup to determine angular acceleration and angular momentum: A lever is placed on a fulcrum. A rock is placed on the left end of the lever and a known downward (clockwise) force is applied to the right end of the lever. What calculations would you perform? How would you account for gravity in your calculations?
- **5.** Consider two sizes of disk, both of mass M. One size of disk has radius R; the other has radius 2R. System A consists of two of the larger disks rigidly connected to each other with a common axis of rotation. System B consists of one of the larger disks and a number of the smaller disks rigidly connected with a common axis of rotation. If the moment of inertia for system A equals the moment of inertia for system B, how many of the smaller disks are in system B?
- a. 1
- b. 2
- c. 3
- d. 4
- **6.** How do you arrange these objects so that the resulting system has the maximum possible moment of inertia? What is that moment of inertia?

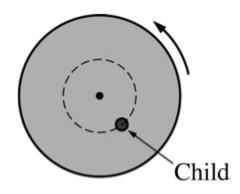
# 10.4 Rotational Kinetic Energy: Work and Energy Revisited

- 7. Gear A, which turns clockwise, meshes with gear B, which turns counterclockwise. When more force is applied through gear A, torque is created. How does the angular velocity of gear B change as a result?
- a. It increases in magnitude.
- b. It decreases in magnitude.
- c. It changes direction.
- d. It stays the same.
- **8.** Which will cause a greater increase in the angular velocity of a disk: doubling the torque applied or halving the radius at which the torque is applied? Explain.
- **9.** Which measure would not be useful to help you determine the change in angular velocity when the torque on a fishing reel is increased?
- a. the radius of the reel
- b. the amount of line that unspools
- c. the angular momentum of the fishing line
- d. the time it takes the line to unspool
- **10.** What data could you collect to study the change in angular velocity when two people push a merry-go-round instead of one, providing twice as much torque? How would you use the data you collect?

### 10.5 Angular Momentum and Its Conservation

- **11.** Which rotational system would be best to use as a model to measure how angular momentum changes when forces on the system are changed?
- a. a fishing reel
- b. a planet and its moon
- c. a figure skater spinning
- d. a person's lower leg
- **12.** You are collecting data to study changes in the angular momentum of a bicycle wheel when a force is applied to it. Which of the following measurements would be least helpful to you?
  - a. the time for which the force is applied
  - b. the radius at which the force is applied
  - the angular velocity of the wheel when the force is applied
  - d. the direction of the force
- **13.** Which torque applied to a disk with radius 7.0 cm for 3.5 s will produce an angular momentum of 25 N•m•s?
- a. 7.1 N•m
- b. 357.1 N·m
- c. 3.6 N·m
- d. 612.5 N•m
- **14.** Which of the following would be the best way to produce measurable amounts of torque on a system to test the relationship between the angular momentum of the system, the average torque applied to the system, and the time for which the torque is applied?
- having different numbers of people push on a merry-goround
- b. placing known masses on one end of a seesaw
- c. touching the outer edge of a bicycle wheel to a treadmill that is moving at different speeds
- d. hanging known masses from a string that is wound around a spool suspended horizontally on an axle

15.



### Top View

Figure 10.42 A curved arrow lies at the side of a gray disk. There is a point at the center of the disk, and around the point there is a dashed circle. There is a point labeled "Child" on the dashed circle. Below the disc is a label saying "Top View". The diagram above shows a top view of a child of mass M on a circular platform of mass 2M that is rotating counterclockwise. Assume the platform rotates without friction. Which of the following describes an action by the child that will increase the angular speed of the platform-child system and why?

- a. The child moves toward the center of the platform, increasing the total angular momentum of the system.
- b. The child moves toward the center of the platform, decreasing the rotational inertia of the system.
- The child moves away from the center of the platform, increasing the total angular momentum of the system.
- The child moves away from the center of the platform, decreasing the rotational inertia of the system.

16.

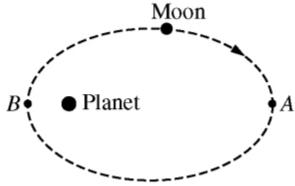


Figure 10.43 A point labeled "Moon" lies on a dashed ellipse. Two other points, labeled "A" and "B", lie at opposite ends of the ellipse. A point labeled "Planet" lies inside the ellipse. A moon is in an elliptical orbit about a planet as shown above. At point A the moon has speed uA and is at distance RA from the planet. At point B the moon has speed uB. Has the moon's angular momentum changed? Explain your answer.

- 17. A hamster sits 0.10 m from the center of a lazy Susan of negligible mass. The wheel has an angular velocity of 1.0 rev/s. How will the angular velocity of the lazy Susan change if the hamster walks to 0.30 m from the center of rotation? Assume zero friction and no external torque.
- a. It will speed up to 2.0 rev/s.
- b. It will speed up to 9.0 rev/s.
- c. It will slow to 0.01 rev/s.
- d. It will slow to 0.02 rev/s.
- **18.** Earth has a mass of  $6.0 \times 10^{24}$  kg, a radius of  $6.4 \times 10^6$  m, and an angular velocity of  $1.2 \times 10^{-5}$  rev/s. How would the planet's angular velocity change if a layer of Earth with mass  $1.0 \times 10^{23}$  kg broke off of the Earth, decreasing Earth's radius by  $0.2 \times 10^6$  m? Assume no friction.
- **19.** Consider system A, consisting of two disks of radius *R*, with both rotating clockwise. Now consider system B, consisting of one disk of radius *R* rotating counterclockwise and another disk of radius 2*R* rotating clockwise. All of the disks have the same mass, and all have the same magnitude of angular velocity.

Which system has the greatest angular momentum?

- a. A
- b. B
- c. They're equal.
- d. Not enough information
- **20.** Assume that a baseball bat being swung at  $3\pi$  rad/s by a batting machine is equivalent to a 1.1 m thin rod with a mass of 1.0 kg. How fast would a 0.15 kg baseball that squarely hits the very tip of the bat have to be going for the net angular momentum of the bat-ball system to be zero?

### 10.6 Collisions of Extended Bodies in Two

#### **Dimensions**

- **21.** A box with a mass of 2.0 kg rests on one end of a seesaw. The seesaw is 6.0 m long, and we can assume it has negligible mass. Approximately what angular momentum will the box have if someone with a mass of 65 kg sits on the other end of the seesaw quickly, with a velocity of 1.2 m/s?
- a. 702 kg•m<sup>2</sup>/s
- b. 39 kg•m<sup>2</sup>/s
- c. 18 kg•m<sup>2</sup>/s
- d. 1.2 kg•m<sup>2</sup>/s
- **22.** A spinner in a board game can be thought of as a thin rod that spins about an axis at its center. The spinner in a certain game is 12 cm long and has a mass of 10 g. How will its angular velocity change when it is flicked at one end with a force equivalent to 15 g travelling at 5.0 m/s if all the energy of the collision is transferred to the spinner? (You can use the table in **Figure 10.12** to estimate the rotational inertia of the spinner.)
- **23.** A cyclist pedals to exert a torque on the rear wheel of the bicycle. When the cyclist changes to a higher gear, the torque increases. Which of the following would be the most effective strategy to help you determine the change in angular momentum of the bicycle wheel?
  - a. multiplying the ratio between the two torques by the mass of the bicycle and rider
- b. adding the two torques together, and multiplying by the time for which both torques are applied
- multiplying the difference in the two torques by the time for which the new torque is applied
- d. multiplying both torques by the mass of the bicycle and rider
- **24.** An electric screwdriver has two speeds, each of which exerts a different torque on a screw. Describe what calculations you could use to help you compare the angular momentum of a screw at each speed. What measurements would you need to make in order to calculate this?
- **25.** Why is it important to consider the shape of an object when determining the object's angular momentum?
- a. The shape determines the location of the center of mass. The location of the center of mass in turn determines the angular velocity of the object.
- The shape helps you determine the location of the object's outer edge, where rotational velocity will be greatest.
- The shape helps you determine the location of the center of rotation.
- d. The shape determines the location of the center of mass. The location of the center of mass contributes to the object's rotational inertia, which contributes to its angular momentum.
- **26.** How could you collect and analyze data to test the difference between the torques provided by two speeds on a tabletop fan?
- **27.** Describe a rotational system you could use to demonstrate the effect on the system's angular momentum of applying different amounts of external torque.
- **28.** How could you use simple equipment such as balls and string to study the changes in angular momentum of a system when it interacts with another system?

## **10.7 Gyroscopic Effects: Vector Aspects of Angular Momentum**

**29.** A globe (model of the Earth) is a hollow sphere with a radius of 16 cm. By wrapping a cord around the equator of a globe and pulling on it, a person exerts a torque on the globe of 120 N  $\cdot$  m for 1.2 s. What angular momentum does the globe have after 1.2 s?

**30.** How could you use a fishing reel to test the relationship between the torque applied to a system, the time for which the torque was applied, and the resulting angular momentum of the system? How would you measure angular momentum?

### **Chapter 10**

### **Problems & Exercises**

1

 $\omega = 0.737 \text{ rev/s}$ 

3

- (a)  $-0.26 \text{ rad/s}^2$
- (b) 27 rev

5

- (a)  $80 \text{ rad/s}^2$
- (b) 1.0 rev

7

- (a) 45.7 s
- (b) 116 rev

9

- a)  $600 \text{ rad/s}^2$
- b) 450 rad/s
- c) 21.0 m/s

10

- (a) 0.338 s
- (b) 0.0403 rev
- (c) 0.313 s

12

 $0.50~\text{kg}\cdot\text{m}^2$ 

14

- (a)  $50.4 \text{ N} \cdot \text{m}$
- (b)  $17.1 \text{ rad/s}^2$
- (c)  $17.0 \text{ rad/s}^2$

16

 $3.96 \times 10^{18} \text{ s}$ 

or  $1.26 \times 10^{11}$  y

18

Answer Key 1605

$$I_{end}=I_{center}+m\Big(\frac{l}{2}\Big)^2$$
 Thus, 
$$I_{center}=I_{end}-\frac{1}{4}ml^2=\frac{1}{3}ml^2-\frac{1}{4}ml^2=\frac{1}{12}ml^2$$

19

- (a) 2.0 ms
- (b) The time interval is too short.
- (c) The moment of inertia is much too small, by one to two orders of magnitude. A torque of  $500~N\cdot m$  is reasonable.

20

- (a) 17,500 rpm
- (b) This angular velocity is very high for a disk of this size and mass. The radial acceleration at the edge of the disk is > 50,000 gs.
- (c) Flywheel mass and radius should both be much greater, allowing for a lower spin rate (angular velocity).

21

- (a) 185 J
- (b) 0.0785 rev
- (c) W = 9.81 N

23

- (a)  $2.57 \times 10^{29} \text{ J}$
- (b)  $KE_{rot} = 2.65 \times 10^{33} J$

25

$$KE_{rot} = 434 J$$

27

- (a) 128 rad/s
- (b) 19.9 m

29

- (a)  $10.4 \text{ rad/s}^2$
- (b) net W = 6.11 J

34

- (a) 1.49 kJ
- (b)  $2.52 \times 10^4$  N

36

- (a)  $2.66 \times 10^{40} \text{ kg} \cdot \text{m}^2/\text{s}$
- (b)  $7.07 \times 10^{33} \text{ kg} \cdot \text{m}^2/\text{s}$

The angular momentum of the Earth in its orbit around the Sun is  $3.77 \times 10^6$  times larger than the angular momentum of the Earth around its axis.

38

$$22.5 \text{ kg} \cdot \text{m}^2/\text{s}$$

40

25.3 rpm

43

(a) 0.156 rad/s

1606 Answer Key

- (b)  $1.17 \times 10^{-2} \,\mathrm{J}$
- (c)  $0.188 \text{ kg} \cdot \text{m/s}$

45

- (a) 3.13 rad/s
- (b) Initial KE = 438 J, final KE = 438 J

47

- (a) 1.70 rad/s
- (b) Initial KE = 22.5 J, final KE = 2.04 J
- (c)  $1.50 \text{ kg} \cdot \text{m/s}$

48

- (a)  $5.64 \times 10^{33} \text{ kg} \cdot \text{m}^2/\text{s}$
- (b)  $1.39 \times 10^{22} \text{ N} \cdot \text{m}$
- (c)  $2.17 \times 10^{15}$  N

### **Test Prep for AP® Courses**

1

(b)

3

(d) 5

(d)

You are given a thin rod of length 1.0 m and mass 2.0 kg, a small lead weight of 0.50 kg, and a not-so-small lead weight of 1.0 kg. The rod has three holes, one in each end and one through the middle, which may either hold a pivot point or one of the small lead weights.

7

(a)

9

(c)

44

(a) 13

(a)

**15** 

(b) **17** 

(c)

19

(b) 21

(b)

23

(c) **25** 

(d) 27

A door on hinges is a rotational system. When you push or pull on the door handle, the angular momentum of the system changes. If a weight is hung on the door handle, then pushing on the door with the same force will cause a different increase in angular momentum. If you push or pull near the hinges with the same force, the resulting angular momentum of the system will also be different.

29

Since the globe is stationary to start with,

1607

 $\tau = \frac{\Delta L}{\Delta t}$ 

Answer Key

 $\tau \cdot \Delta t = \Delta L$ 

By substituting,

120 N•m • 1.2 s = 144 N•m•s. The angular momentum of the globe after 1.2 s is 144 N•m•s.

# Rotational of ation Problems Solved.

b/we have to see how many nev. letimo i ma beseach second, me use the overge w = wg+w; just the V

-> = 16 Aad/A

= 2.5 5 nev/A -> 2.5 5.2 = 2.5 5.0.4 = 1 nev

7/4D+= DW = 32 = 45.1A

6/ 10 = 32 = 16 100/A

W = 2. Tracour/s -> 2. Tr. 45. += 116, 100

Material

25/WE= 2 MU2 -> WE 1 - 2 I W2 W= - 20 = 41. 7 Nod/A

1d Eno+= 434J

Test Prep: W-DO & W-DO 11 +5 PASSON W= = =0 [6] 3/L= AMU -5E 7/00 if A increases in w 50 does & [0] 2/w= D8 8= [e] 13/ Y = DL = 2C = 7.1 N.M D HAREST NAME & 13/ ED A (ERE) B 10 c-23/1= DL 17 -> 7/ DL = (21. 2) D+ [] 25/21

Rotational Motion.