Assignment #A: Graph starts

Updated 1830 GMT+8 Apr 22, 2025

2025 spring, Complied by袁奕 2400010766 数院

说明:

1. 解题与记录:

对于每一个题目,请提供其解题思路(可选),并附上使用Python或C++编写的源代码(确保已在OpenJudge,Codeforces,LeetCode等平台上获得Accepted)。请将这些信息连同显示"Accepted"的截图一起填写到下方的作业模板中。(推荐使用Typora https://typoraio.c 进行编辑,当然你也可以选择Word。)无论题目是否已通过,请标明每个题目大致花费的时间。

- 2. **提交安排**: 提交时,请首先上传PDF格式的文件,并将.md或.doc格式的文件作为附件上传至右侧的"作业评论"区。确保你的Canvas账户有一个清晰可见的头像,提交的文件为PDF格式,并且"作业评论"区包含上传的.md或.doc附件。
- 3. **延迟提交**:如果你预计无法在截止日期前提交作业,请提前告知具体原因。这有助于我们了解情况并可能为你提供适当的延期或其他帮助。

请按照上述指导认真准备和提交作业,以保证顺利完成课程要求。

1. 题目

M19943:图的拉普拉斯矩阵

OOP, implementation, http://cs101.openjudge.cn/practice/19943/

要求创建Graph, Vertex两个类,建图实现。

思路:

```
class Vertex:
        def __init__(self, key):
 2
 3
            self.key = key
 4
            self.neighbour = set()
 5
   class Graph:
 6
 7
        def __init__(self):
8
            self.vertices = {}
9
        def add_edge(self, start, end):
10
            if start not in self.vertices:
11
                self.vertices[start] = Vertex(start)
12
            if end not in self.vertices:
                self.vertices[end] = Vertex(end)
13
            self.vertices[start].neighbour.add(end)
14
15
            self.vertices[end].neighbour.add(start)
```

```
16
17
    graph = Graph()
18
    n, m = map(int, input().split())
19
    for i in range(m):
20
21
        a, b = map(int, input().split())
22
        graph.add_edge(a, b)
23
    for i in range(n):
24
25
        res = [0] * n
        for j in range(n):
26
27
            if i == j:
                 res[j] = len(graph.vertices.get(i, Vertex(i)).neighbour)
28
29
            elif j in graph.vertices.get(i, Vertex(i)).neighbour:
30
                 res[j] = -1
        print(*res, sep=" ")
31
```

#48997382提交状态

查看 提交 统计 提问

基本信息

状态: Accepted

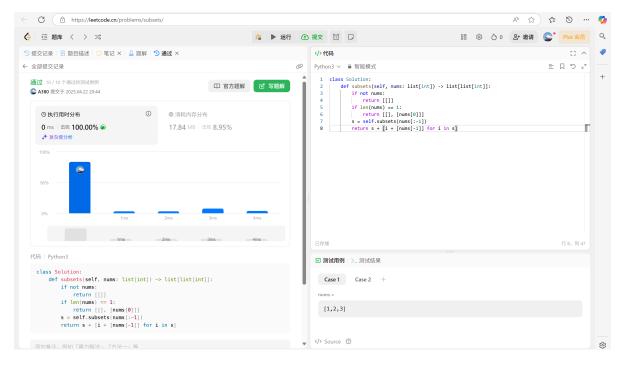
```
源代码
                                                                                 #: 48997382
                                                                                题目: 19943
 class Vertex:
                                                                              提交人: 24n2400010766
     def __init__(self, key):
                                                                                内存: 3664kB
         self.key = key
                                                                                时间: 25ms
        self.neighbour = set()
                                                                                语言: Python3
 class Graph:
                                                                            提交时间: 2025-04-23 22:08:19
     def __init__(self):
         self.vertices = {}
     def add_edge(self, start, end):
        if start not in self.vertices:
             self.vertices[start] = Vertex(start)
         if end not in self.vertices:
             self.vertices[end] = Vertex(end)
         self.vertices[start].neighbour.add(end)
         self.vertices[end].neighbour.add(start)
 graph = Graph()
 n, m = map(int, input().split())
 for i in range(m):
     a, b = map(int, input().split())
     graph.add_edge(a, b)
 for i in range (n):
     res = [0] * n
     for j in range(n):
             res[j] = len(graph.vertices.get(i, Vertex(i)).neighbour)
         elif j in graph.vertices.get(i, Vertex(i)).neighbour:
            res[j] =
     print(*res, sep=" ")
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                                                                                               English 帮助 关于
```

LC78.子集

backtracking, https://leetcode.cn/problems/subsets/

思路:

```
class Solution:
1
       def subsets(self, nums: list[int]) -> list[list[int]]:
2
3
           if not nums:
4
                return [[]]
           if len(nums) == 1:
5
               return [[], [nums[0]]]
6
7
           s = self.subsets(nums[:-1])
8
            return s + [i + [nums[-1]] for i in s]
```

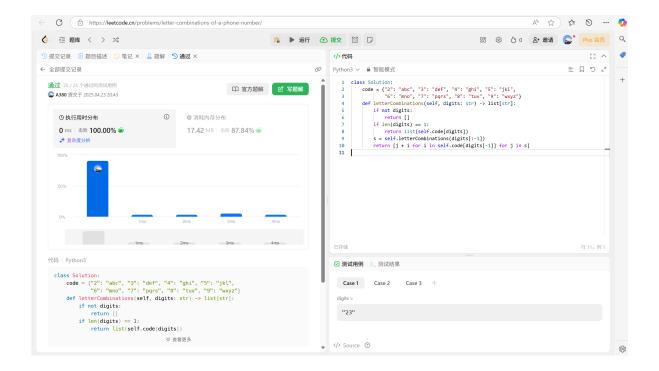


LC17.电话号码的字母组合

 $hash\ table,\ backtracking,\ \underline{https://leetcode.cn/problems/letter-combinations-of-a-phone-number/$

思路:

```
class Solution:
 1
        code = {"2": "abc", "3": "def", "4": "ghi", "5": "jkl",
 2
                "6": "mno", "7": "pqrs", "8": "tuv", "9": "wxyz"}
 3
        def letterCombinations(self, digits: str) -> list[str]:
 4
            if not digits:
 5
 6
                return []
 7
            if len(digits) == 1:
                return list(self.code[digits])
 8
 9
            s = self.letterCombinations(digits[:-1])
10
            return [j + i for i in self.code[digits[-1]] for j in s]
```



M04089:电话号码

trie, http://cs101.openjudge.cn/practice/04089/

思路:

```
1
    class TreeNode:
 2
        def __init__(self, val):
 3
            self.val = val
            self.children = dict()
 4
 5
    def build(s : str):
 6
 7
        curr = root
 8
        isSame = True
9
        for c in s:
            if c in curr.children:
10
                curr = curr.children[c]
11
12
            else:
                 curr.children[c] = TreeNode(c)
13
                 curr = curr.children[c]
14
15
                 isSame = False
16
        return isSame
17
    T = int(input())
18
19
    for _ in range(T):
20
        root = TreeNode(None)
21
        n = int(input())
22
        read = []
23
        for _ in range(n):
24
            read.append(input())
25
        read = sorted(read, key=len, reverse=True)
```

```
26
        havePrint = False
27
        for i in range(n):
28
            if build(read[i]):
29
                 print("NO")
                 havePrint = True
30
31
                 break
32
        if not havePrint:
33
            print("YES")
```

#48987253提交状态

查看 提交 统计 提问

状态: Accepted

```
基本信息
源代码
                                                                                #: 48987253
                                                                               题目: 04089
                                                                             提交人: 24n2400010766
    def __init__(self, val):
                                                                              内存: 26604kB
         self.val = val
        self.children = dict()
                                                                               时间: 350ms
                                                                               语言: Pvthon3
 def build(s : str):
                                                                           提交时间: 2025-04-22 21:17:19
    curr = root
     isSame = True
     for c in s:
        if c in curr.children:
            curr = curr.children[c]
         else:
            curr.children[c] = TreeNode(c)
            curr = curr.children[c]
            isSame = False
    return isSame
 T = int(input())
 for _ in range(T):
    root = TreeNode(None)
    n = int(input())
     read = []
    read.append(input())
     read = sorted(read, key=len, reverse=True)
     havePrint = False
     for i in range(n):
         if build(read[i]):
            print("NO")
            havePrint = True
            break
     if not havePrint:
        print("YES")
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                                                                                              English 帮助 关于
```

T28046:词梯

bfs, http://cs101.openjudge.cn/practice/28046/

思路: 两两逐位比较是 $O(n^2k)$ 复杂度, 会超时. 于是类似筛法, 用 buckets 存储.

```
1
    from collections import deque
2
3
    class Vertex:
        def __init__(self, key):
4
5
            self.key = key
6
            self.neighbour = set()
7
8
    class Graph:
9
        def __init__(self):
            self.vertices = {}
10
```

```
11
        def add_edge(self, start : str, end : str):
12
            if start not in self.vertices:
13
                 self.vertices[start] = Vertex(start)
14
            if end not in self.vertices:
                 self.vertices[end] = Vertex(end)
15
16
            self.vertices[start].neighbour.add(end)
17
    graph = Graph()
18
    n = int(input())
19
20
    buckets = {}
    for _ in range(n):
21
        word = input()
22
23
        for i, _ in enumerate(word):
24
            bucket = f"{word[:i]}_{word[i + 1:]}"
25
            buckets.setdefault(bucket, set()).add(word)
26
    for similar_words in buckets.values():
27
28
        for word1 in similar_words:
29
             for word2 in similar_words - {word1}:
                 graph.add_edge(word1, word2)
30
31
32
    start, end = input().split()
33
34
    def main():
35
        que = deque([(graph.vertices.get(start, Vertex(start)), [start])])
36
        visited = {start}
        while que:
37
38
            last, path = que.popleft()
39
            if last.key == end:
40
                return path
            for next in last.neighbour:
41
42
                 if next not in visited:
43
                     que.append((graph.vertices[next], path + [next]))
44
                     visited.add(next)
45
        return
46
47
    res = main()
    print(*res, sep=" ") if res else print("NO")
48
```

#48997799提交状态 查看 提交 统计 提问

基本信息

状态: Accepted

```
源代码
                                                                                   # 48997799
                                                                                  题目: 28046
 from collections import deque
                                                                                提交人: 24n2400010766
                                                                                 内存: 11296kB
 class Vertex:
                                                                                 时间: 77ms
     def __init__(self, key):
         \overline{\text{self.key}} = \text{key}
                                                                                 语言: Python3
         self.neighbour = set()
                                                                              提交时间: 2025-04-24 09:07:02
 class Graph:
     def __init__(self):
         self.vertices = {}
     def add edge(self, start : str, end : str):
        if start not in self.vertices:
            self.vertices[start] = Vertex(start)
         if end not in self.vertices:
            self.vertices[end] = Vertex(end)
         self.vertices[start].neighbour.add(end)
 graph = Graph()
 n = int(input())
 buckets = {}
 for _ in range(n):
     word = input()
     for i, _ in enumerate(word):
        bucket = f"{word[:i]}_{word[i + 1:]}"
         buckets.setdefault(bucket, set()).add(word)
 for similar_words in buckets.values():
     for word1 in similar words:
         for word2 in similar words - {word1}:
             graph.add edge (word1, word2)
 start, end = input().split()
 def main():
     que = deque([(graph.vertices.get(start, Vertex(start)), [start])])
     visited = {start}
     while que:
         last, path = que.popleft()
         if last.key == end:
             return path
         for next in last.neighbour:
             if next not in visited:
                que.append((graph.vertices[next], path + [next]))
                 visited.add(next)
     return
 res = main()
 print(*res, sep=" ") if res else print("NO")
```

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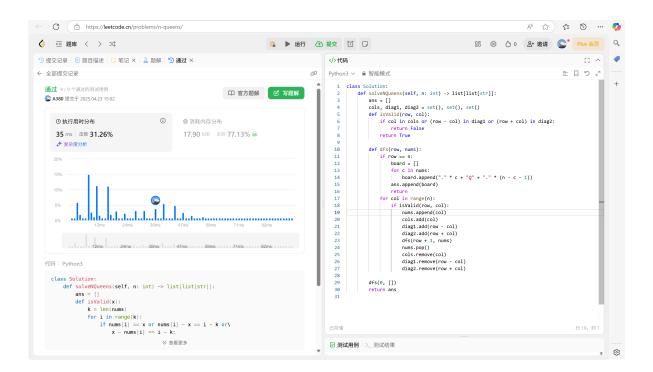
T51.N皇后

backtracking, https://leetcode.cn/problems/n-queens/

思路:

```
1
    class Solution:
2
        def solveNQueens(self, n: int) -> list[list[str]]:
3
             ans = []
4
             def isValid(x):
5
                  k = len(nums)
6
                  for i in range(k):
7
                      if nums[i] == x \text{ or } nums[i] - x == i - k \text{ or} \setminus
8
                           x - nums[i] == i - k:
9
                           return False
```

```
10
                 return True
11
            nums = []
12
            def dfs():
13
                 if len(nums) == n:
                     ans.append(["." * i + "Q" + "." * (n - i - 1) for i in
14
    nums])
15
                     return
16
                 for x in range(n):
                     if isValid(x):
17
18
                         nums.append(x)
19
                         dfs()
20
                         nums.pop()
            dfs()
21
22
             return ans
```



2. 学习总结和收获

学习了 dict.get() 和 dict.setdefault() 方法. 更安全, 不会有 KeyError 报错.

LeetCode 链表和二叉树还差5题, 周末做完

| 链表 | |
|-----------------------------------|----|
| ⊘ 相交链表 | 简单 |
| ⊘ 反转链表 | 简单 |
| ⊘ 回文链表 | 简单 |
| ◇ 环形链表 | 简单 |
| | 中等 |
| ◇ 合并两个有序链表 | 简单 |
| ○ 两数相加 | 中等 |
| | 中等 |
| | 中等 |
| | 困难 |
| ○ 随机链表的复制 | 中等 |
| ◇ 排序链表 | 中等 |
| ○ 合并 K 个升序链表 | 困难 |
| ○ LRU 缓存 | 中等 |
| 二叉树 | |
| ○ 二叉树的中序遍历 | 简单 |
| ◇ 二叉树的最大深度 | 简单 |
| ⊘ 翻转二叉树 | 简单 |
| ⊘ 对称二叉树 | 简单 |
| ○ 二叉树的直径 | 简单 |
| ○ 二叉树的层序遍历 | 中等 |
| 将有序数组转换为二叉搜索树 | 简单 |
| ◎ 验证二叉搜索树 | 中等 |
| ○ 二叉搜索树中第 K 小的元素 | 中等 |
| ○ 二叉树的右视图 | 中等 |
| ○ 二叉树展开为链表 | 中等 |
| 从前序与中序遍历序列构造二叉树 | 中等 |
| ○ 路径总和 III | 中等 |
| | |
| ○ 二叉树的最近公共祖先 | 中等 |