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滑动窗口, 双指针

滑动窗口：

[3. 无重复字符的最长子串 - 力扣 \(LeetCode\)](#)

```
1 class Solution(object):
2     def lengthOfLongestSubstring(self, s):
3         if not s: return 0
4         left = 0
5         MAX = 1
6         pos_val = {}
7         for right, c in enumerate(s):
8             if s[right] in pos_val and pos_val[s[right]] >= left:
9                 left = pos_val[s[right]] + 1
10            pos_val[s[right]] = right # pos_val : left ~ right
11            if right - left + 1 > MAX:
12                MAX = right - left + 1
13        return MAX
```

双指针：

[11. 盛最多水的容器 - 力扣 \(LeetCode\)](#)

```
1 class Solution(object):
2     def maxArea(self, height):
3         left, right = 0, len(height) - 1
4         MAX = 0
5         while left <= right:
6             if height[left] <= height[right]:
7                 MAX = max(MAX, (right - left) * height[left])
8                 left += 1
9             else:
10                MAX = max(MAX, (right - left) * height[right])
11                right -= 1
12        return MAX
```

快慢指针 (Floyd's Tortoise and Hare Algorithm)

求链表中点, 判断链表是否有圈

单调栈：

[739. 每日温度 - 力扣 \(LeetCode\)](#)

```
1 class Solution(object):
2     def dailyTemperatures(self, temperatures):
3         st = []
4         res = [0] * len(temperatures)
5         for i, t in enumerate(temperatures):
6             if not st:
7                 st.append(i)
8             else:
9                 while st and temperatures[st[-1]] < t:
```

```

10         res[st[-1]] = i - st[-1]
11         st.pop()
12         st.append(i)
13     return res

```

84. 柱状图中最大的矩形 - 力扣 (LeetCode)

Key : 如何遍历?

Solution : 例如 [3, 1, 4, 1, 5, 9, 2, 6]

[3] => [1] => [1, 4] => [1] => [1, 5] => [1, 5, 9] => [1, 2] => [1, 2, 6]

其中红色的一步, 每次枚举最右侧是 9 的矩形 ([9], [5, 9]) (不会枚举 [1, 5, 9], 因为 [4, 9, 2, ...] 之后会枚举到的)

其中在 height 末尾加 0 是为了保证最后把 [1, 2, 6] 完整的枚举一遍 ([6], [2, 6], [1, 5, 9, 2, 6])

```

1 class Solution(object):
2     def largestRectangleArea(self, heights):
3         heights.append(0)
4         st = []
5         MAX = 0
6         for i in range(len(heights)):
7             while st and heights[st[-1]] > heights[i]:
8                 h = heights[st.pop()]
9                 w = i if not st else i - st[-1] - 1
10                MAX = max(MAX, h * w)
11            st.append(i)
12        return MAX

```

85. 最大矩形 - 力扣 (LeetCode)

```

1 class Solution(object):
2     def maximalColumn(self, col):
3         col.append(0)
4         st = []
5         MAX = 0
6         for i, x in enumerate(col):
7             while st and col[st[-1]] > x:
8                 if len(st) >= 2:
9                     MAX = max(MAX, col[st[-1]] * (i - st[-2] - 1))
10                else:
11                    MAX = max(MAX, col[st[-1]] * i)
12            st.pop()
13            st.append(i)
14        return MAX
15    def maximalRectangle(self, matrix):
16        m, n = len(matrix), len(matrix[0])
17        pre = [0] * n
18        MAX = 0
19        for i in range(m):
20            for j in range(n):
21                pre[j] = pre[j] + 1 if matrix[i][j] == "1" else 0
22            MAX = max(MAX, self.maximalColumn(pre.copy()))
23        return MAX

```

单调队列：

[239. 滑动窗口最大值 - 力扣 \(LeetCode\)](#)

```
1 from collections import deque
2
3 class Solution(object):
4     def maxSlidingWindow(self, nums, k):
5         dq = deque([])
6         res = []
7         for i, x in enumerate(nums):
8             while dq and dq[0] <= i - k:
9                 dq.popleft()
10            while dq and nums[dq[-1]] <= x:
11                dq.pop()
12            dq.append(i)
13            if i >= k - 1:
14                res.append(nums[dq[0]])
15        return res
```

Stack

[中序表达式转后序表达式](#)

以下是 Shunting Yard 算法的基本步骤：

1. 初始化运算符栈和输出栈为空.
2. 从左到右遍历中缀表达式的每个符号.
 - 如果是操作数(数字), 则将其添加到输出栈.
 - 如果是左括号, 则将其推入运算符栈.
 - 如果是运算符:
 - 如果运算符的优先级大于运算符栈顶的运算符, 或者运算符栈顶是左括号, 则将当前运算符推入运算符栈.
 - 否则, 将运算符栈顶的运算符弹出并添加到输出栈中, 直到满足上述条件(或者运算符栈为空).
 - 将当前运算符推入运算符栈.
 - 如果是右括号, 则将运算符栈顶的运算符弹出并添加到输出栈中, 直到遇到左括号. 将左括号弹出但不添加到输出栈中.
3. 如果还有剩余的运算符在运算符栈中, 将它们依次弹出并添加到输出栈中.
4. 输出栈中的元素就是转换后的后缀表达式.

```
1 opr_pri = {"+" : 1, "-" : 1, "*" : 2, "/" : 2, "(" : 3, ")" : 3}
2
3 def find_num(s : str, i : int) -> int:
4     # e.g. find_num("1.0+2.5", 0) = 3
5     while i < len(s) and s[i] not in opr_pri:
6         i += 1
7     return i
8
9 def trans() -> list:
```

```

10     s, i = input(), 0
11     res, opr_st = [], []
12     while i < len(s):
13         if s[i] in opr_pri:
14             if s[i] == "(":
15                 opr_st.append(s[i])
16             elif s[i] == ")":
17                 while opr_st and opr_st[-1] != "(":
18                     res.append(opr_st.pop())
19                 opr_st.pop()
20             else:
21                 while opr_st and opr_st[-1] != "(" and opr_pri[s[i]] <=
opr_pri[opr_st[-1]]:
22                     res.append(opr_st.pop())
23                 opr_st.append(s[i])
24                 i += 1
25             else:
26                 j = find_num(s, i)
27                 res.append(s[i : j])
28                 i = j
29         while opr_st:
30             res.append(opr_st.pop())
31     return res
32
33 n = int(input())
34
35 for _ in range(n):
36     print(*trans(), sep = " ")

```

排序

Merge Sort, [OpenJudge - 07622:求排列的逆序数](#)

```

1  def merge_count(arr1, arr2):
2      cnt, j = 0, 0
3      for x in arr1:
4          while j < len(arr2) and arr2[j] < x:
5              j += 1
6          cnt += j
7      res, i, j = [], 0, 0
8      while i < len(arr1) and j < len(arr2):
9          if arr1[i] < arr2[j]:
10             res.append(arr1[i]); i += 1
11          else:
12             res.append(arr2[j]); j += 1
13      return res + arr1[i:] + arr2[j:], cnt
14
15 def sortArray(nums):
16     if not nums or len(nums) == 1:
17         return nums, 0
18     mid = len(nums) // 2
19     arr1, sum1 = sortArray(nums[:mid])
20     arr2, sum2 = sortArray(nums[mid:])
21     arr, cnt = merge_count(arr1, arr2)
22     return arr, sum1 + sum2 + cnt

```

Linked List

引用与赋值

```
1  # 定义链表节点类
2  class ListNode:
3      def __init__(self, val, next = None):
4          self.val = val
5          self.next = next
6      def __str__(self):
7          return f"ListNode({self.val} -> {self.next.val})"
8
9  d = ListNode(4)
10 c = ListNode(3, d)
11 b = ListNode(2, c)
12 a = ListNode(1, b)
```

1.

```
1  # Example 1 : `prev` 和 `curr` 指向相同的节点, 修改 `prev` 后 `curr` 不受影响
2  prev = a
3  curr = prev
4  prev = b
5  print(curr == a, a) # output : True ListNode(1 -> 2)
```

2.

```
1  # Example 2 : `curr` 指向 `a.next` (i.e. `b`), 修改 `prev` 后 `curr` 不受影响
2  prev = a
3  curr = prev.next
4  prev = c
5  print(curr == b, b) # output : True ListNode(2 -> 3)
```

3.

```
1  # Example 3 : `curr` 指向 `a`, 修改 `a.val`, `curr.val` 也受影响
2  curr = a
3  a.val = 0
4  print(curr) # output : ListNode(0 -> 2)
```

4.

```
1  # Example 4 : `prev` 和 `curr` 指向相同对象 `a`, 修改 `prev.val`, `curr.val` 也受影响
2  prev = a
3  curr = a
4  prev.val = 0
5  print(curr) # output : ListNode(0 -> 2)
```

5.

```
1  # Example 5 : `curr` 指向 `a`, 修改 `a.next`, `curr.next` 也受影响
2  prev = a
3  curr = prev
4  prev.next = c
5  print(curr) # output : ListNode(0 -> 3)
```

引用变更不会同步, 赋值变更 (`prev.next = ...` 或者 `prev.val = ...`) 会同步

[206. 反转链表 - 力扣 \(LeetCode\)](#)

```
1 class ListNode:
2     def __init__(self, val, next=None):
3         self.val = val
4         self.next = next
5
6 class Solution(object):
7     def reverseList(self, head):
8         pre = None
9         curr = head
10        while curr:
11            curr_next = curr.next
12            curr.next = pre
13            pre = curr
14            curr = curr_next
15        return pre
```

Tree

```
1 class Tree():
2     def __init__(self, val = 0, left = None, right = None):
3         self.val = val
4         self.left = left
5         self.right = right
```

手搓Heapq

此略

并查集 Disjoint Set

[OpenJudge - 02524:宗教信仰](#)

```
1 def find(x):
2     if parent[x] != x:
3         parent[x] = find(parent[x])
4     return parent[x]
5
6 def union(x, y):
7     x = find(x)
8     y = find(y)
9     parent[x] = y
10
11 case = 0
12 while True:
13     case += 1
14     n, m = map(int, input().split())
15     if n == 0:
16         break
17     parent = [i for i in range(n + 1)]
18     for _ in range(m):
19         x, y = map(int, input().split())
```

```

20         union(x, y)
21     for i in range(1, n + 1):
22         find(i)
23     parent_set = set(parent)
24     print(f"Case {case}: {len(parent_set) - 1}")

```

Graph

拓扑排序 (可用于判断有向图中有无环)

Kahn, 时间复杂度 $O(V + E)$

```

1  def topological_sort(graph : Dict[str : List[str]]):
2      in_degree = defaultdict(int)
3      res, que = [], deque()
4      for u in graph:
5          for v in graph[u]:
6              in_degree[v] += 1
7      for u in graph:
8          if in_degree[u] == 0:
9              que.append(u)
10     while que:
11         u = que.popleft()
12         res.append(u)
13         for v in graph[u]:
14             in_degree[v] -= 1
15             if in_degree[v] == 0:
16                 que.append(v)
17     if len(res) == len(graph):
18         return res
19     else:
20         return None # have a cycle

```

最短路径

- Dijkstra

key: 每个点一进一出, 但要求图无负权边

- Bellman-Ford $O(VE)$

```

1  def bellman_ford(graph, v, source):
2      dist = [float('inf')] * v # 初始化距离
3      dist[source] = 0
4      for _ in range(v - 1): # 松弛 v-1 次
5          for u, v, w in graph:
6              if dist[u] != float('inf') and dist[u] + w < dist[v]:
7                  dist[v] = dist[u] + w
8      for u, v, w in graph: # 检测负权环
9          if dist[u] != float('inf') and dist[u] + w < dist[v]:
10             print("图中存在负权环")
11             return None
12     return dist
13
14 edges = [(0, 1, 5), (0, 2, 4), (1, 3, 3), (2, 1, 6), (3, 2, -2)] # 图是边

```

列表, 每条边是 (起点, 终点, 权重)


```

15 V, source = 4, 0 # V 总点数, source 起点
16 print(bellman_ford(edges, V, source))

```

- SPFA

```

1  from collections import deque
2
3  def spfa(adj, V, source):
4      dist = [float('inf')] * V # 初始化距离
5      dist[source] = 0
6      in_queue = [False] * V # 初始化入队状态
7      in_queue[source] = True
8      count = [0] * V # 初始化松弛次数
9      queue = deque([source])
10     while queue:
11         u = queue.popleft()
12         in_queue[u] = False # in_queue 相当于存储 set(queue)
13         for v, w in adj[u]:
14             if dist[u] + w < dist[v]:
15                 dist[v] = dist[u] + w
16                 if in_queue[v] == False:
17                     queue.append(v)
18                     in_queue[v] = True
19                     count[v] += 1
20                     if count[v] > V:
21                         print("图中存在负权环")
22                         return None
23     return dist
24
25 adj = [(1, 5), (2, 4)], [(3, 3)], [(1, 6)], [(2, -2)]] # 图的邻接表表示
26 V, source = 4, 0 # V 总点数, source 起点
27 print(spfa(adj, V, source))

```

- Floyd-Warshall $O(V^3)$

```

1  def floyd_warshall(graph : Dict):
2      n = len(graph)
3      dist = [[float('inf')] * n for _ in range(n)]
4      for i in range(n):
5          for j in range(n):
6              if i == j:
7                  dist[i][j] = 0
8              elif j in graph[i]:
9                  dist[i][j] = graph[i][j]
10     for k in range(n):
11         for i in range(n):
12             for j in range(n):
13                 dist[i][j] = min(dist[i][j], dist[i][k] + dist[k][j])
14     return dist

```

最小生成树

- Prim, $O(V^2)$, 适用于稠密图

不断往MST中添加Vertex (greedy思想, 选距离 现有MST 权值最小的Vertex)

```
1 def prim(n, matrix : List[List[int]]):
2     MST, low = set(), [float("inf")] * n # low[k] 表示当前 MST 距离 k 点的
    最小权值.
3     low[0], tot = 0, 0
4     for _ in range(n):
5         new, MIN = 0, float("inf")
6         for i, dis in enumerate(low):
7             if i not in MST and dis < MIN:
8                 new, MIN = i, dis
9         MST.add(new)
10        tot += MIN
11        for i in range(n):
12            if i not in MST:
13                low[i] = min(low[i], matrix[i][new]) # 更新新版 MST 距离 k
    点的最小权值.
14    return tot
```

- ```
1 class DisjointSet:
2 def __init__(self, num_vertices):
3 self.parent = list(range(num_vertices))
4 self.rank = [0] * num_vertices
5 def find(self, x):
6 if self.parent[x] != x:
7 self.parent[x] = self.find(self.parent[x])
8 return self.parent[x]
9 def union(self, x, y):
10 root_x = self.find(x)
11 root_y = self.find(y)
12 if root_x != root_y:
13 if self.rank[root_x] < self.rank[root_y]:
14 self.parent[root_x] = root_y
15 elif self.rank[root_x] > self.rank[root_y]:
16 self.parent[root_y] = root_x
17 else:
18 self.parent[root_x] = root_y
19 self.rank[root_y] += 1
20
21 def kruskal(graph):
22 num_vertices = len(graph)
23 edges = [] # 构建边集
24 for i in range(num_vertices):
25 for j in range(i + 1, num_vertices):
26 if graph[i][j] != 0:
27 edges.append((i, j, graph[i][j]))
28 edges.sort(key=lambda x: x[2]) # 按照权重排序
29 disjoint_set = DisjointSet(num_vertices) # 初始化并查集
30 minimum_spanning_tree = [] # 构建最小生成树的边集
31 for edge in edges:
32 u, v, weight = edge
```

```
33 if disjoint_set.find(u) != disjoint_set.find(v):
34 disjoint_set.union(u, v)
35 minimum_spanning_tree.append((u, v, weight))
36 return minimum_spanning_tree
```

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强连通 **sorry**