



# TEA: Test-time Energy Adaptation

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Paper



Code



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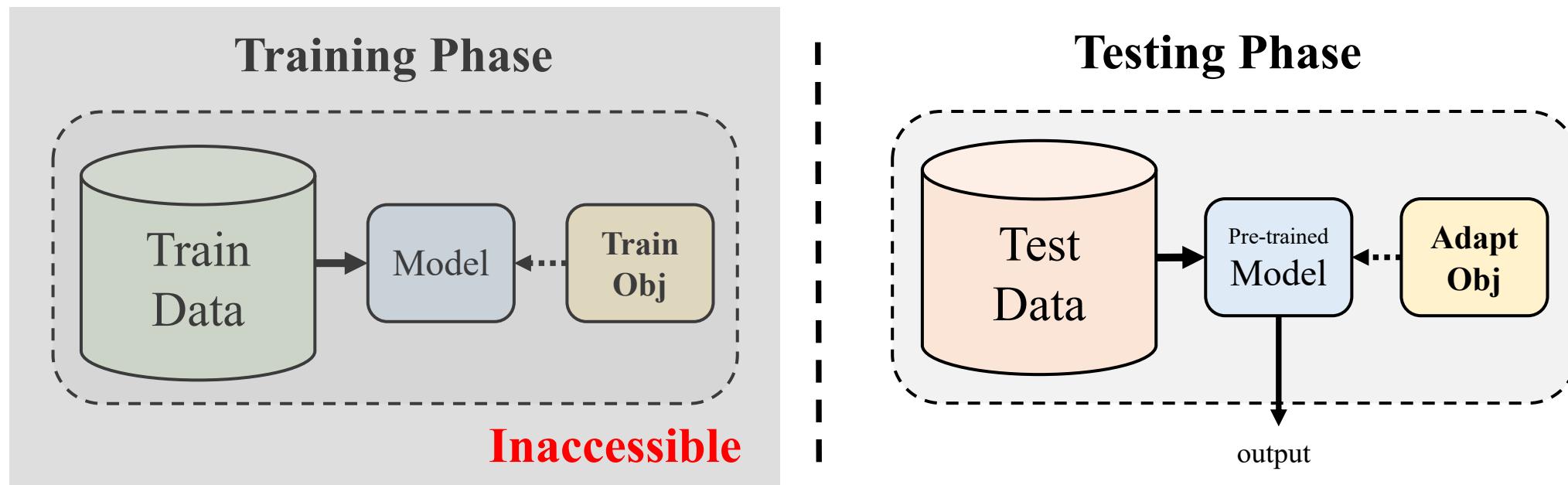
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- Motivation
- Method
- Experiments

# MOTIVATION

## Test-time Adaptation

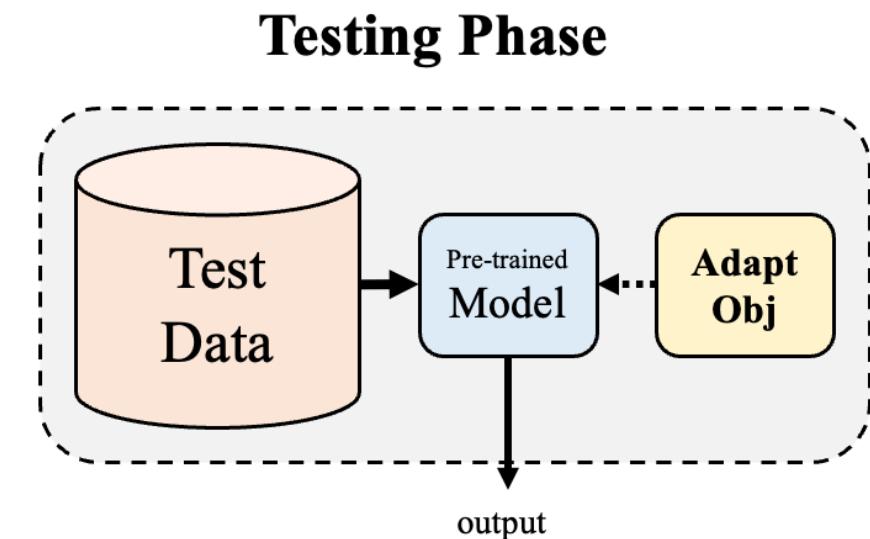
- Inaccessible training data and training procedure.
- Adapting a pre-trained model with test data.



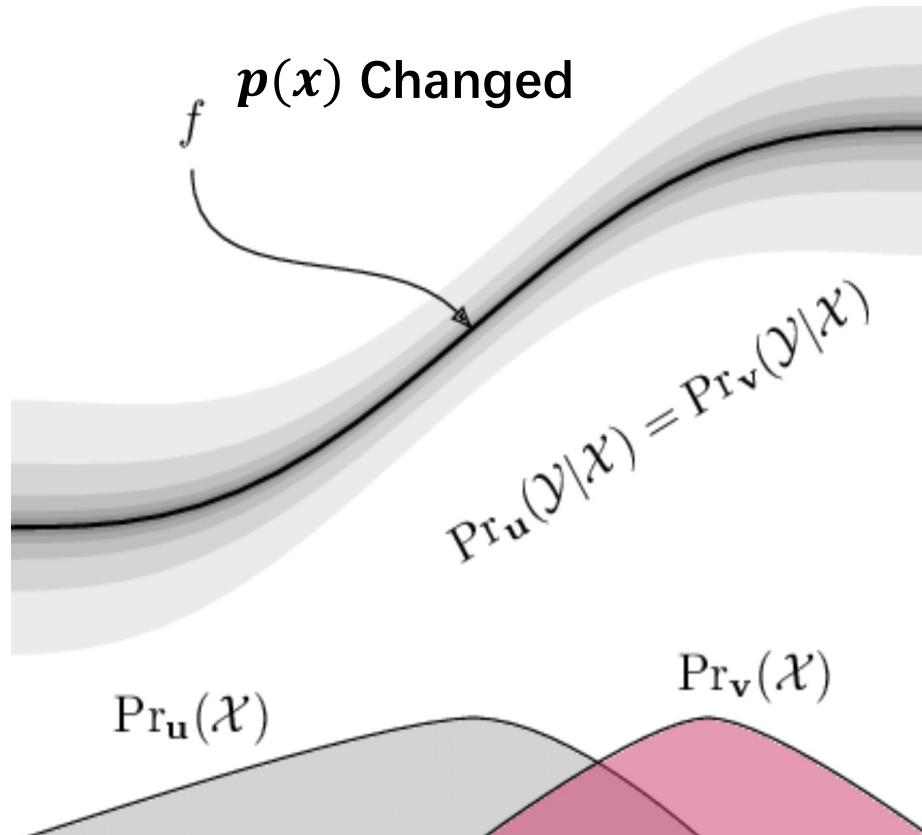
# MOTIVATION

## Related Work

- Entropy-based TTA
  - Minimize the prediction entropy.
  - TENT, ETA, EATA, SAR
- Pseudo-labeling-based TTA
  - Utilize test-time generated labels for updates.
  - PL, SHOT
- Consistency-based TTA
  - Constraint consistency across augmented samples.
  - MEMO, AdaContrast
- ....



# MOTIVATION



## Covariate Shift

- the decrease in generalization ability on test data with distribution shift can be attributed to the model's reliance on the marginal distribution of the training data
- They do not address the marginal distribution shift  $p(x)$ , impairing model calibration and introducing confirmation bias.

**How to perceive marginal distribution  $p(x)$ ?**

# MOTIVATION

## Energy Based Model

- **What is? A Non-normalized Probabilistic Model**

the energy function maps each sample into an energy that can be considered as an unnormalized probability, with lower scores indicating higher likelihoods

$$E_{\theta}(x) : R^D \rightarrow R$$

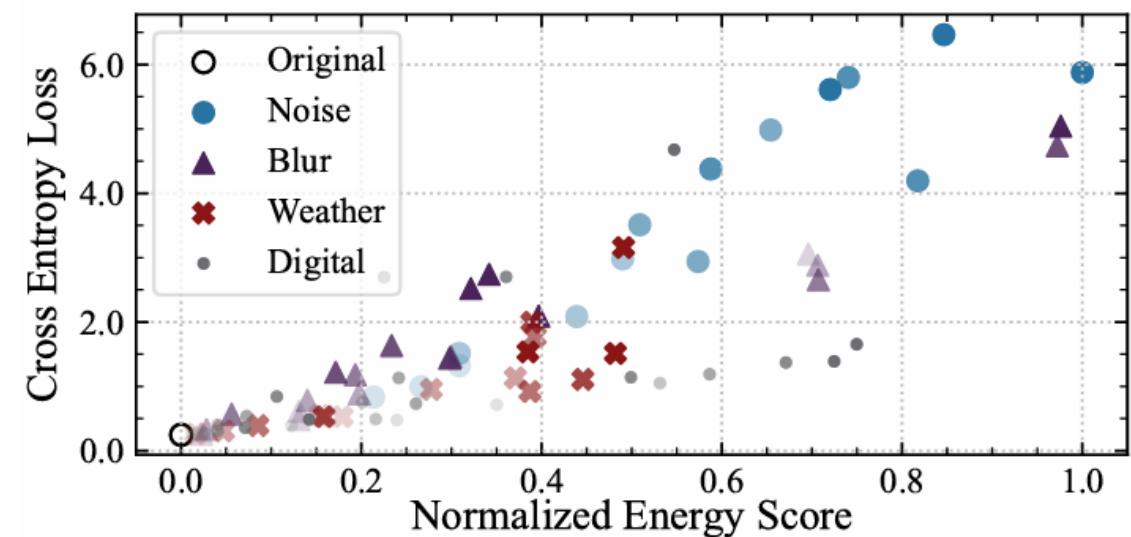
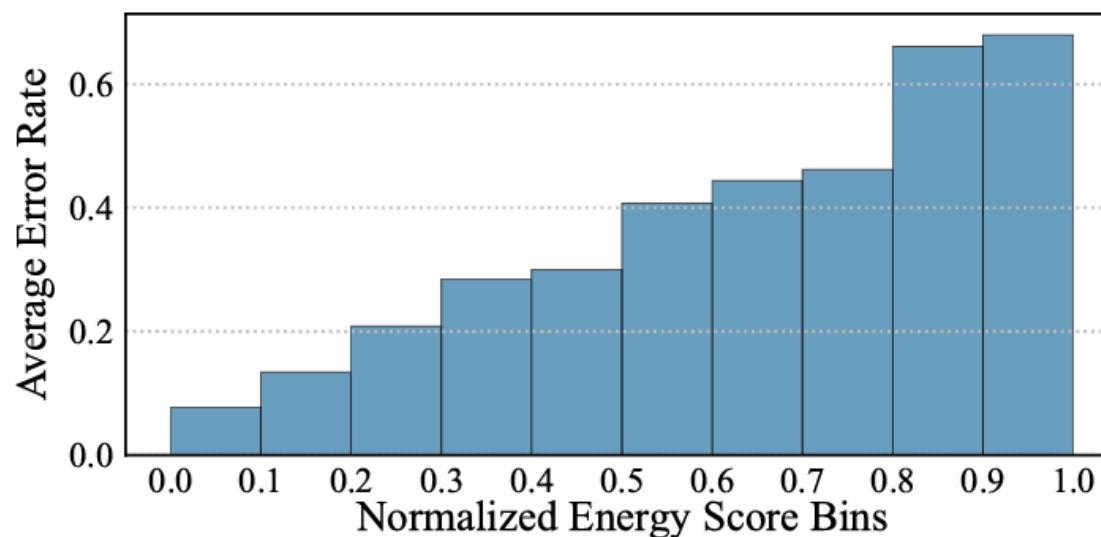
$$p_{\theta}(x) = \frac{\exp(-E_{\theta}(x))}{Z_{\theta}}$$

$$Z_{\theta} = \int \sum_y \exp(f_{\theta}(x)[y]) dx$$

# MOTIVATION

## How Energy related to Generalization

- Our Observation
  - Low energy = high probability, high performance
  - High energy = low probability, low performance



- Motivation
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# METHOD

## Overall idea

Enhancing the model's perception of test distribution from an energy-based perspective, involving two key steps:

- treating the Pretrained Classifier as the energy-based model
- optimizing it to perceive test data by decreasing the energy

## Notation

Labeled training data  $(x, y) \sim P_{\text{train}}(x, y)$

Inaccessible

Unlabeled test data  $x \sim P_{\text{test}}(x)$

Accessible

Pre-trained Classifier  $f_\theta: X \rightarrow Y$

Accessible

# METHOD

## Treating Classifier as EBM

**Pretrained Classifier**

introduce unknown  
normalizing constant  $Z_\theta$

marginalize out  $y$

substitute  $E_\theta$

**Energy Based Model**

$$p_\theta(y \mid \mathbf{x}) = \frac{\exp(f_\theta(\mathbf{x})[y])}{\sum_{y'} \exp(f_\theta(\mathbf{x})[y'])}$$

$$p_\theta(\mathbf{x}, y) = \frac{\exp(f_\theta(\mathbf{x})[y])}{Z_\theta}$$

$$p_\theta(\mathbf{x}) = \sum_y p_\theta(\mathbf{x}, y) = \frac{\sum_y \exp(f_\theta(\mathbf{x})[y])}{Z_\theta}$$

$$p_\theta(\mathbf{x}) = \frac{\exp(-E_\theta(\mathbf{x}))}{Z_\theta}$$

$$E_\theta(\mathbf{x}) = -\log \sum_y \exp(f_\theta(\mathbf{x})[y])$$

A Pre-Trained Classifier can be reinterpret as an Energy Based Model

# METHOD

## Inject Test Distribution into Classifier

Our Objective:

Test Data

$$\max p_{\theta}(\mathbf{x}_{\text{test}})$$

Classifier's Inherent Distribution

Modeling Test Distribution under Pre-trained Classifier

$$p_{\theta}(\mathbf{x}_{\text{test}}) = \frac{\exp(-E_{\theta}(\mathbf{x}_{\text{test}}))}{Z_{\theta}}$$

$$Z_{\theta} = \int \sum_y \exp(f_{\theta}(\mathbf{x})[y]) d\mathbf{x}$$

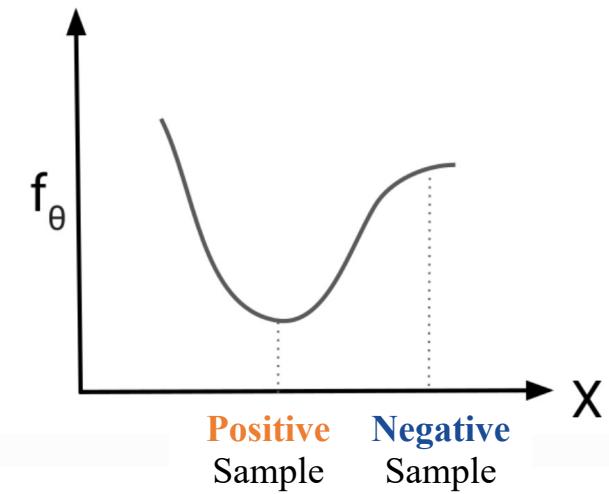
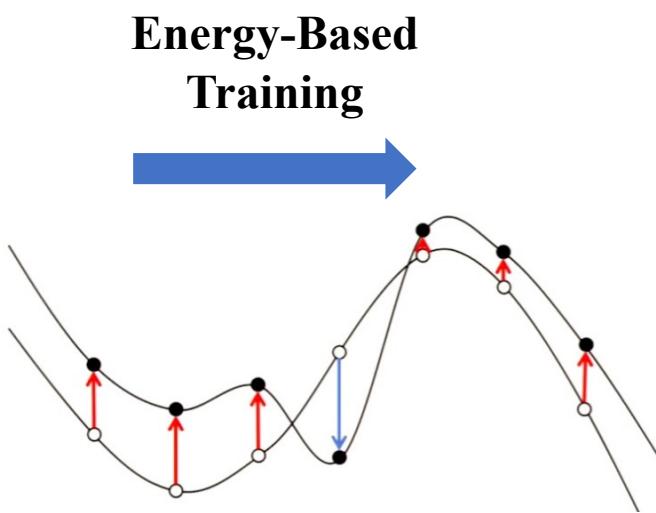
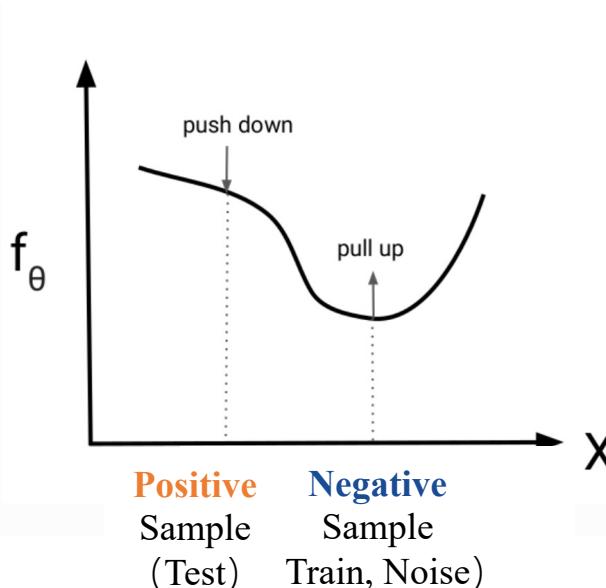
Computing Z requires integrating all x, How to Optimize?

# METHOD

## Inject Test Distribution into Classifier

### Contrastive Divergence

$$\frac{\partial \log p_\theta(\mathbf{x}_{\text{test}})}{\partial \theta} = \mathbb{E}_{\tilde{\mathbf{x}} \sim p_\theta} \left[ \frac{\partial E_\theta(\tilde{\mathbf{x}})}{\partial \theta} \right] - \frac{\partial E_\theta(\mathbf{x}_{\text{test}})}{\partial \theta}$$



# METHOD

## Inject Test Distribution into Classifier

Test Distribution Injection:

$$\max_{\theta} p_{\theta}(\mathbf{x}_{\text{test}})$$

Test Data  
Classifier's Inherent Distribution

Contrastive Divergence

$$\frac{\partial \log p_{\theta}(\mathbf{x}_{\text{test}})}{\partial \theta} = \mathbb{E}_{\tilde{\mathbf{x}} \sim p_{\theta}} \left[ \frac{\partial E_{\theta}(\tilde{\mathbf{x}})}{\partial \theta} \right] - \frac{\partial E_{\theta}(\mathbf{x}_{\text{test}})}{\partial \theta}$$



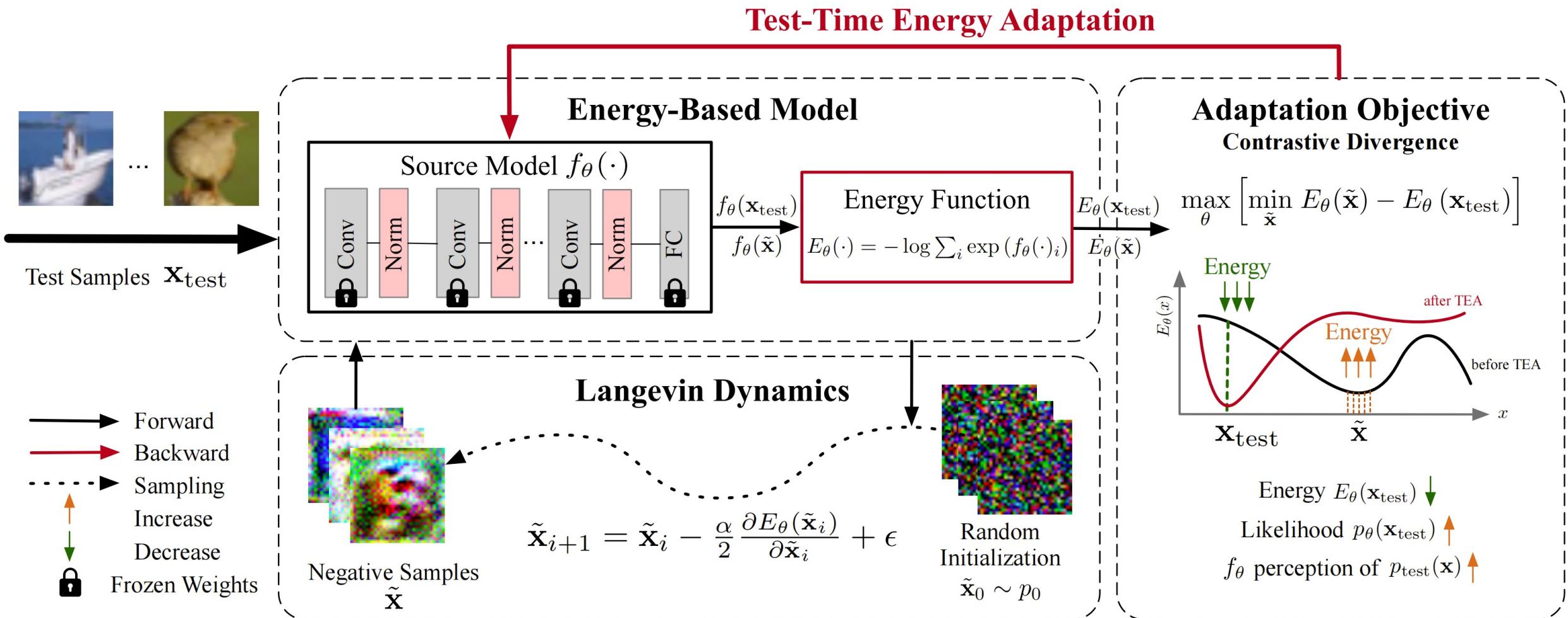
Stochastic Gradient Langevin Dynamics

$$\tilde{\mathbf{x}}_{t+1} = \mathbf{x}_t - \frac{\alpha}{2} \frac{\partial E_{\theta}(\tilde{\mathbf{x}}_t)}{\partial \tilde{\mathbf{x}}_t} + \sqrt{\alpha} \epsilon, \quad \epsilon \sim \mathcal{N}(\mathbf{0}, \mathbf{I}),$$

Overall Objective

$$\max p_{\theta}(\mathbf{x}_{\text{test}}) = \max_{\theta} [\min_{\tilde{\mathbf{x}}} E_{\theta}(\tilde{\mathbf{x}}) - E_{\theta}(\mathbf{x}_{\text{test}})]$$

# METHOD



- Motivation
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# EXPERIMENTS

## Experimental Settings

- **Datasets**
  - 15 shift corruption distributions by **CIFAR-10(C)**, **CIFAR-100(C)**, and **Tiny-ImageNet(C)**.
  - 4 domains in the PCAS dataset: **Photo**, **Art**, **Cartoon**, and **Sketch**.
- **Baselines**
  - Without TTA: **Source**
  - Norm Based TTA: **BN DUA**
  - Pseudo Label Based TTA: **PL**, **SHOT**
  - Entropy Based TTA: **TENT**, **ETA**, **EATA**, **SAR**
- **Metrics**
  - **Accuracy** on clean data.
  - **Average Accuracy** and **mCE** across all severity levels and at the severest level.

# EXPERIMENTS

## Image Corruption Scenario Performance

Table 1. Comparisons of TEA and baselines for image corruption on CIFAR-10(C), CIFAR-100(C), and Tiny-ImageNet(C) using WRN-28-10 with BatchNorm. Accuracy and mCE are evaluated at the most severe level and across all levels with asterisk (\*) indicating the results are taken from the original paper [56]. The best adaptation results are highlighted in **boldface**.

WRN-28-10 BatchNorm	CIFAR-10(C)					CIFAR-100(C)					Tiny-ImageNet(C)					
	Clean	Corr Severity 5	Corr Severity 1-5	Clean	Corr Severity 5	Corr Severity 1-5	Clean	Corr Severity 5	Corr Severity 1-5	Clean	Corr Severity 5	Corr Severity 1-5	Clean	Corr Severity 5	Corr Severity 1-5	
	Acc (↑)	Acc (↑)	mCE (↓)	Acc (↑)	Acc (↑)	mCE (↓)	Acc (↑)	Acc (↑)	mCE (↓)	Acc (↑)	Acc (↑)	mCE (↓)	Acc (↑)	Acc (↑)	mCE (↓)	
Source	94.77	56.47	100.00	73.45	100.00	81.79	35.39	100.00	52.12	100.00	63.19	21.21	100.00	34.13	100.00	
Norm	BN [52]	93.97	79.56	52.65	85.63	60.00	80.83	60.06	63.54	68.11	69.42	45.04	27.74	93.42	34.27	100.96
	DUA* [41]	-	80.10	50.78	-	-	-	-	-	-	-	-	-	-	-	
Pseudo	PL [34]	93.75	51.42	106.98	72.62	99.37	80.52	53.40	72.12	64.53	75.29	47.84	28.26	91.22	39.83	91.67
	SHOT [36]	93.25	74.77	63.19	82.35	72.61	80.52	56.53	68.01	66.00	73.28	47.95	29.14	90.16	<b>40.01</b>	<b>91.41</b>
Entropy	TENT [60]	93.66	81.41	48.13	86.75	56.17	80.14	63.09	59.42	69.47	67.80	39.54	26.31	95.52	32.03	104.49
	ETA [45]	93.96	79.58	52.64	85.63	59.99	80.65	59.82	64.52	67.17	72.40	43.20	27.28	94.12	33.46	102.25
	EATA [45]	93.96	79.59	52.62	85.64	59.98	80.68	60.24	63.75	67.48	71.66	43.42	27.28	94.09	33.47	102.24
	SAR [46]	93.97	79.77	51.94	85.83	58.97	80.84	62.95	59.37	70.01	65.99	41.58	28.21	92.82	34.60	100.47
Energy	TEA	<b>94.09</b>	<b>83.34</b>	<b>43.69</b>	<b>87.88</b>	<b>52.00</b>	<b>80.88</b>	<b>65.10</b>	<b>56.18</b>	<b>71.22</b>	<b>63.74</b>	<b>51.65</b>	<b>31.67</b>	<b>87.99</b>	39.96	92.12

Figure: Adaptation performance under image corruption scenarios using BatchNorm

# EXPERIMENTS

## Image Corruption Scenario Performance

Table 2. Comparisons for image corruption on CIFAR-10(C), CIFAR-100(C), and Tiny-ImageNet(C) using ResNet-50 with GroupNorm across all severity levels. Best results are in **boldface**.

ResNet50		CIFAR-10(C)		CIFAR-100(C)		Tiny-ImageNet(C)	
	GroupNorm	Acc (↑)	mCE (↓)	Acc (↑)	mCE (↓)	Acc (↑)	mCE (↓)
	Source	78.71	100.00	54.98	100.00	26.64	100.00
Pseudo	PL	79.43	94.76	56.68	96.02	26.60	99.92
	SHOT	81.98	86.65	58.31	93.45	29.11	96.73
Entropy	TENT	77.29	102.88	56.34	96.88	26.65	99.94
	ETA	78.68	100.09	56.72	96.37	29.25	96.42
	EATA	78.70	100.02	56.76	96.28	29.25	96.42
	SAR	78.78	99.65	55.28	99.33	27.05	99.41
Energy	TEA	<b>83.05</b>	<b>79.09</b>	<b>59.67</b>	<b>89.32</b>	<b>30.41</b>	<b>94.81</b>

Figure: Adaptation performance under image corruption scenarios using GroupNorm

# EXPERIMENTS

## Domain Generalization Scenario Performance

Table 3. Single source domain generalization comparisons on PACS datasets using ResNet-18 with BatchNorm in terms of Accuracy. The best adaptation results are highlighted in **boldface**.

Source Domain	Method	Target Domain				Avg
		Photo	Art	Cartoon	Sketch	
Photo	Source	-	26.76	22.40	16.62	21.93
	BN	-	26.66	27.94	15.96	23.52
	TENT	-	26.95	29.86	17.54	24.78
	EATA	-	26.66	28.11	15.98	23.59
	SAR	-	26.71	28.41	15.98	23.70
	SHOT	-	26.61	29.86	20.92	25.80
Art	TEA	-	<b>28.81</b>	<b>33.62</b>	<b>20.49</b>	<b>27.64</b>
	Source	49.04	-	36.43	24.48	36.65
	BN	46.65	-	28.28	22.73	32.55
	TENT	50.78	-	30.12	24.61	35.17
	EATA	46.83	-	29.31	23.42	33.19
	SAR	47.90	-	33.02	26.27	35.73
Cartoon	SHOT	50.24	-	34.30	<b>29.37</b>	37.97
	TEA	<b>56.29</b>	-	<b>38.57</b>	28.71	<b>41.19</b>

Source Domain	Method	Target Domain				Avg
		Photo	Art	Cartoon	Sketch	
Cartoon	Source	42.69	29.79	-	29.47	33.98
	BN	28.68	25.15	-	20.87	24.90
	TENT	30.96	23.34	-	22.65	25.65
	EATA	28.80	25.10	-	<b>25.04</b>	26.31
	SAR	29.70	25.78	-	21.51	25.66
	SHOT	<b>37.72</b>	22.66	-	23.14	27.84
Sketch	TEA	36.05	<b>31.44</b>	-	22.88	<b>30.12</b>
	Source	19.94	18.70	32.21	-	23.62
	BN	13.47	17.14	29.86	-	20.16
	TENT	13.53	17.38	29.52	-	20.14
	EATA	13.17	17.33	30.08	-	20.19
	SAR	13.29	18.80	29.95	-	20.68
TEA	SHOT	<b>19.76</b>	18.75	30.46	-	22.99
	TEA	19.64	<b>21.24</b>	<b>33.19</b>	-	<b>24.69</b>

Figure: Adaptation performance under domain generalization scenarios

# EXPERIMENTS

## Energy Reduction & Generalizability Enhancement

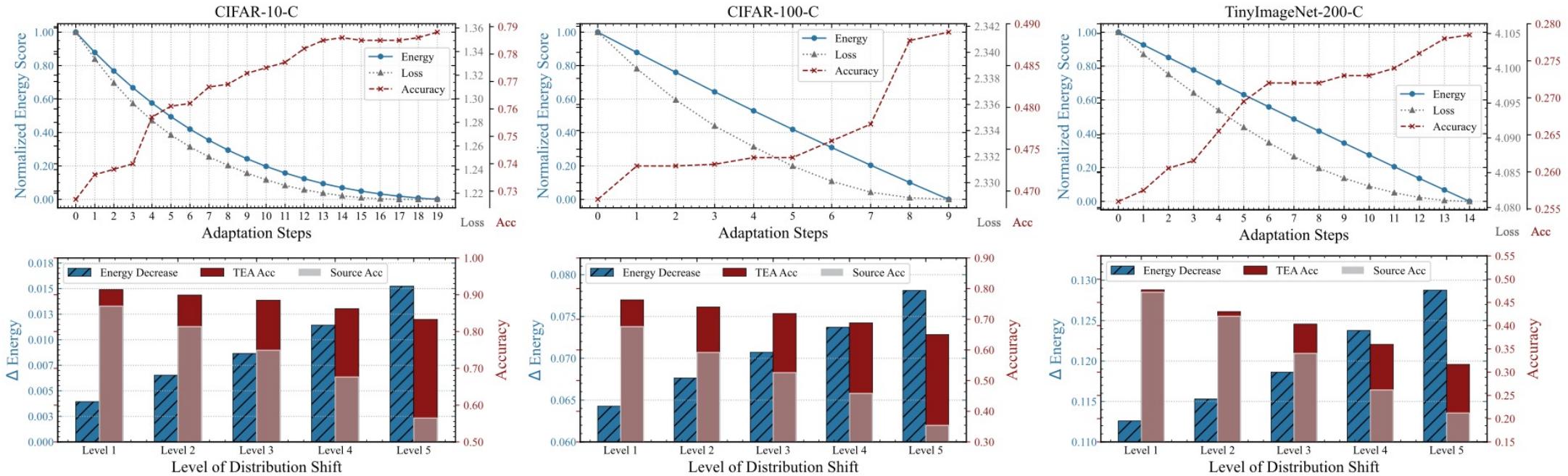


Figure 3. This illustration captures the energy reduction and generalizability enhancement achieved by TEA across CIFAR-10-C, CIFAR-100-C, and TinyImageNet-200-C, displayed from left to right. The **upper** set of graphs trace the evolution of energy score, corresponding loss and accuracy in response to incrementally increasing TEA adaptation steps. The **lower** set uncovers the extent of energy reduction and the consequent performance improvement before and after executing TEA adaptation, under different levels of distribution shift.

Figure: Relation between energy reduction and generalizability enhancement

# EXPERIMENTS

## Distribution Perception and Generation

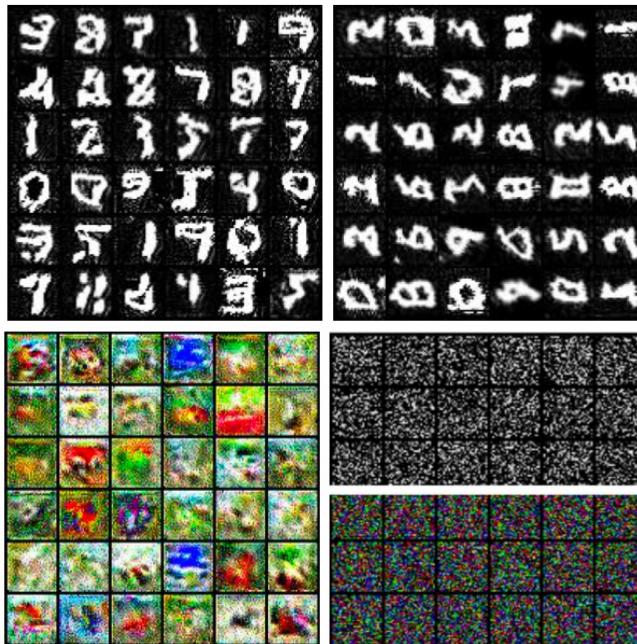


Figure 4. Test distribution perception visualization for identical training and testing distributions on MNIST and CIFAR-10.

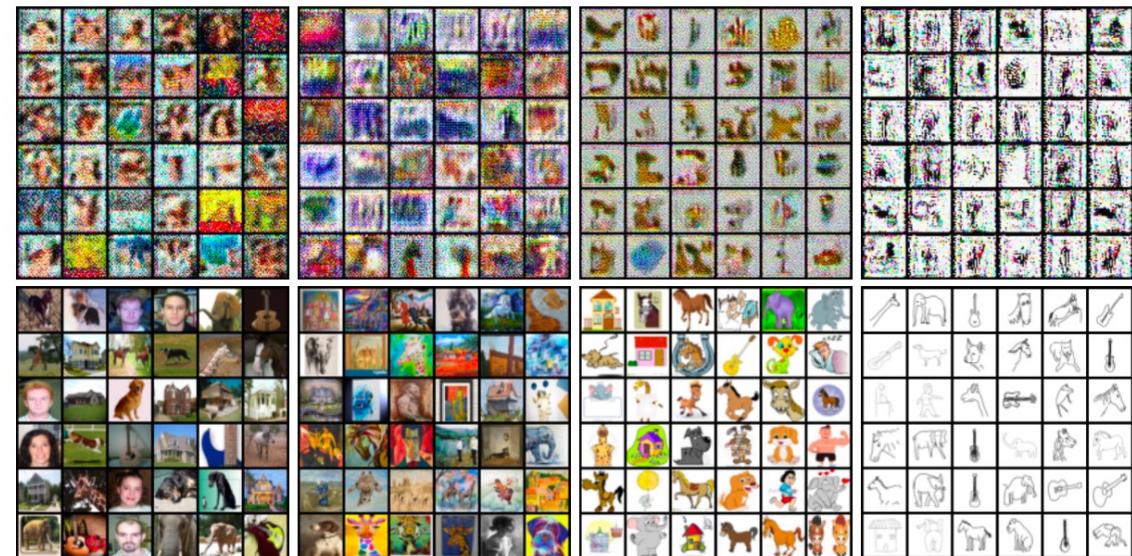


Figure 5. Test distribution perception visualization (**upper**) and real samples (**lower**) on shifted distribution: A model trained on PACS-A dataset then individually tested with TEA adaptation across PACS-P, PACS-A, PACS-C, PACS-S datasets.

Figure: TEA's Distribution Perception and Generation

# EXPERIMENTS

## Distribution Perception and Generation

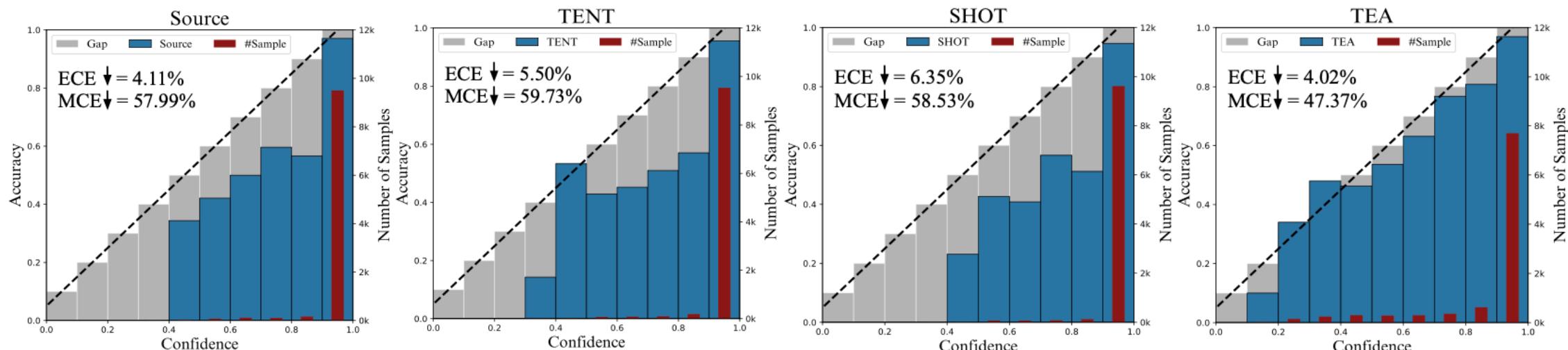


Figure 6. Calibration comparison between TEA and baselines on CIFAR-10 dataset. In an ideal scenario for optimal calibration, blue bars should align with the diagonal line, and a smaller grey gap area is preferred. Quantitative measures are provided via ECE and MCE metrics, where lower values indicate better calibration.

Figure: TEA's Improvements in Confidence Calibration



Thanks for all the authors of this paper:



**Yige Yuan**

- Generalization
- Trustworthy AI



**Bingbing Xu**

- Graph Neural Networks
- Network Embedding



**Liang Hou**

- Generative Adversarial Nets
- Generative Models



**Fei Sun**

- Recommender Systems
- Natural Language Processing



**Huawei Shen**

- Network Data Mining
- Social Network Analysis
- Graph Neural Networks



**Xueqi Cheng**

- Network Data Science
- Social Computing
- Information Retrieval



# Thank you for your attention!

Paper



Code



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