

False.

Proof:

Assume that  $(\exists m \in \mathbb{N})(\exists n \in \mathbb{N})(3m + 5n = 12)$

We have  $m = \frac{12}{3} - \frac{5n}{3} = 4 - \frac{5n}{3}$

Since  $n$  is a natural number,  $m$  is a natural number,  $n, m$  are both non-negative,

so  $m = 4 - \frac{5n}{3}$  can not hold,

i.e., we can not find a natural number  $n$  that satisfy  $m = 4 - \frac{5n}{3}$ .

We have a contradiction. So the original statement is false.