

5.

Proof: any integer is one of the forms  $3x$ ,  $3x+1$ ,  $3x+2$  for an integer  $x$

We will show that the statement holds when integer  $n$  is any of above forms.

If  $n=3x$  for an integer  $x$ , since  $x$  is an integer,  $n$  is divisible by 3

If  $n=3x+1$ ,  $n+2=3x+3=3(x+1)$ , so  $n+2$  is divisible by 3

If  $n=3x+2$ ,  $n+4=3x+6=3(x+2)$ , so  $n+4$  is divisible by 3

So, look at all the forms of  $n$ , at least one of the integers  $n$ ,  $n + 2$ ,  $n + 4$  is divisible by 3. The statement has been proved.