

3. True.

Proof: For any integer  $n$ ,  $n$  is either an odd or an even number. We will show that the statement holds for both (i.e., holds when  $n$  is odd or  $n$  is even).

If  $n$  is an odd number,  $n^2$  is odd,  $n^2+n$  is even, so  $n^2+n+1$  is odd.

If  $n$  is an even number,  $n^2$  is even,  $n^2+n$  is even, so  $n^2+n+1$  is odd.

So for any integer  $n$ ,  $n^2+n+1$  is odd. The statement has been proved.