

6.

Proof:

Proof by contradiction.

Assume there are at least one prime triple expect for 3,5,7

i.e., exists prime number $n > 3$, that n , $n+2$, $n+4$ are prime number

Since any natural number is even or odd, if n is even or odd, $n+2$, $n+4$ are even or odd

When n is even, then n can be written as the form $2x$, $x \in \mathbb{N}$, and $x > 1$

If $n=2x$, then $n+2=2x+2=2(x+1)$, $n+4=2x+4=2(x+2)$. So $n+2$ and $n+4$ can be divided by 2, which is a contradiction.

When n is odd, then n can be written as the form $3x$, $3x+2$, $3x+4$, here $n > 1$ and n is odd.

if n is the form of $3x$, n is divisible by 3, so n is not a prime. Contradiction.

If n is the form of $3x+2$, $n+4=3x+6=3(x+2)$, which is divisible by 3, so $n+4$ is not a prime. Contradiction.

If n is the form of $3x+4$, $n+2=3x+6=3(x+2)$, which is divisible by 3, so $n+2$ is not a prime. Contradiction.

So we have proved that when n is even or odd, n , $n+2$, $n+4$ can not be prime number if $n > 3$. The statement has been proved.