

# UNIVERSITY OF MIAMI

Department of Electrical and Computer Engineering  
EEN 203

Name: \_\_\_\_\_  
Section: \_\_\_\_\_  
Date: \_\_\_\_\_

## EXPERIMENT 5

### LOWPASS AND HIGHPASS FILTERS

Frequency Response of R-C circuits: Bode Diagrams

**PURPOSE:** The purpose of this experiment is to introduce the student to two practical frequency discriminating circuits: the *lowpass* and the *highpass* filters. The lowpass filter lets pass frequencies below a certain cutoff  $\omega_c$  and rejects frequencies above it. The highpass filter performs the opposite task. The frequency band where signals pass through a filter is known as the *passband* and the region where they are attenuated or stopped is called the *stopband*. Since filters are not ideal, it takes a certain band for their gain to go from maximum to a level that can be considered negligible. This band is known as the *transition band*. Filters usually have relatively flat gains in the passband and decrease asymptotically at slopes of  $\pm 20n$  dB/decade where  $n$  is the order of the filter. The frequency at which the gain is down by  $\sqrt{2}$  from the maximum value is called the 3 dB point. For a lowpass filter, the 3 dB point is the same as the bandwidth. The bandwidth of a highpass filter is ideally infinite.

### Equipment

- 1 Frequency Generator
- 1 DVM (Multimeter)
- Resistors, Capacitors, and Inductors

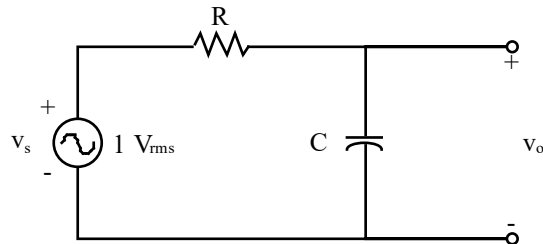
### Preliminary Work

- a) Derive the exact equation for  $V_o/V_s$  for the circuit of Fig. 5.1 and find an expression for the cutoff frequency  $\omega_c$ . Using semilog paper, plot the frequency response (magnitude vs. frequency) of the filter up to  $10f_c$  using the specified component values. Plot the horizontal axis for frequency on a logarithmic scale and the vertical axis for magnitude  $|V_o/V_s|$  (dB), on a linear scale.
- b) Repeat part (a) for the circuit of Fig. 5.2.

## Experimental Procedure

### I. The LowPass Filter:

- a) Set up the circuit shown in Fig. 5.1. Use  $R = 2.2 \text{ k}\Omega$ ,  $C = 0.047 \text{ }\mu\text{F}$ , and adjust the frequency generator's amplitude to  $1 \text{ V}_{\text{rms}}$ . Notice that the D.V.M. reading is in rms and must be used to get the proper reading.



**Figure 5.1** First order lowpass filter.

- b) Vary the frequency of the signal generator according to the values given in Table 5.1. Record the output voltage,  $V_o$ . Make sure  $V_s$  is  $1 \text{ V}_{\text{rms}}$  before **each** reading.

$f(\text{Hz})$	$V_o(\text{V})$	$V_o/V_s(\text{V})$	$ V_o/V_s (\text{dB})$
100			
200			
300			
500			
700			
800			
900			
1 k			
1.5 k			
2 k			
3 k			
5 k			
7 k			
10 k			
20 k			
30 k			
50 k			
70 k			
100 k			

**Table 5.1** Frequency Response data for circuit of Fig. 5.1.

c) Plot the graph of  $|V_o/V_s|$  (dB) vs.  $f$  (Hz) on the **same** graph you obtained in your preliminary work.

d) From the graph, find the cutoff frequency,  $f_c$  of the filter. This is the 3 dB point.

$$f_{c, \text{experimental}} = \underline{\hspace{2cm}}$$

e) Calculate  $f_c$  from  $\omega_c = \frac{1}{RC} = 2\pi f_c$ .

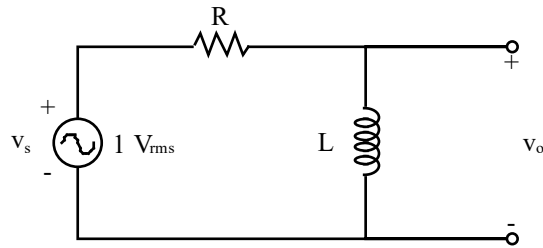
$$f_{c, \text{calculated}} = \underline{\hspace{2cm}}$$

f) Calculate the % error.

$$\% \text{ error } f_c = \underline{\hspace{2cm}}$$

## II. The HighPass Filter:

- a) Set up the circuit shown in Fig. 5.2. Choose  $R = 1\text{ k}\Omega$ ,  $L = 22\text{ mH}$ , and adjust the frequency generator's amplitude to  $1\text{ V}_{\text{rms}}$ .



**Figure 5.2** First order highpass filter.

- b) Vary the frequency of the signal generator according to the values given in Table 5.2. Record the output voltage,  $V_o$ . Make sure  $V_s$  is  $1\text{ V}_{\text{rms}}$  before **each** reading.

$f\text{ (Hz)}$	$V_o\text{ (V)}$	$V_o/V_s\text{ (V)}$	$ V_o/V_s \text{ (dB)}$
100			
200			
300			
500			
700			
800			
900			
1 k			
1.5 k			
2 k			
3 k			
5 k			
7 k			
10 k			
20 k			
30 k			
50 k			
70 k			
100 k			

**Table 5.2** Frequency Response data for circuit of Fig. 5.2.

- c) Plot the graph of  $|V_o/V_s|\text{ (dB)}$  vs.  $f\text{ (Hz)}$  on the **same** graph you obtained in your preliminary work.

d) From the graph, find the cutoff frequency,  $f_c$  of the filter. This is the 3 dB point.

$$f_{c, \text{ experimental}} = \underline{\hspace{2cm}}$$

e) Calculate  $f_c$  from  $\omega_c = \frac{R}{L} = 2\pi f_c$ .

$$f_{c, \text{ calculated}} = \underline{\hspace{2cm}}$$

f) Calculate the % error.

$$\% \text{ error } f_c = \underline{\hspace{2cm}}$$

### ***Discussion of Results***

---

a) Find the slope of the Bode plots of each filter and calculate the errors as compared with the theoretical value of  $\pm 20$  dB/decade.

b) Draw the circuit diagram of

- (i) A simple lowpass filter (LPF) using an inductor and a resistor only.
- (ii) A simple highpass filter (HPF) using a capacitor and a resistor only.

Indicate where the input and outputs are taken from.

c) Sketch the frequency response of a bandpass filter (BPF) and a bandstop filter (BSF).

d) Discuss the applications of filter circuits. Particularly in the following situations. Indicate the type of filter used in each case.

- (i) Power supply smoothing.
- (ii) DC blocking of audio inputs to speakers.
- (iii) Radio tuning.
- (iv) Cross-over networks in 3-way speaker systems.

e) Write a conclusion.