

## ECO 102: Topics in Economics

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### TD 1 (part 2): Maximisation and the social multiplier

In this TD we will a review maximisation technique (the Lagrangian method) and apply it in the context of the social multiplier effect.

#### Exercise

1. Review the Lagrangian method to solve for constrained optimization problems (we will see this together in class).
2. Apply the Lagrangian method to solve for the following problem:  
Maximize  $f = x^{1/2}y^{1/2}$  subject to  $ax + cy = b$   
Obtain first order conditions,  $x^*$ ,  $y^*$  and  $\lambda^*$
3. Apply the Lagrangian method to the social multiplier effect seen in class (slide 11 of lecture 1). Show that:
  - (a)  $U_x = pU_y$
  - (b)  $\frac{dX}{dS} > 0 \Leftrightarrow U_{xs} > pU_{ys}$
4. (Extra) Interpret the lagrange multiplier  $\lambda$  in the general case seen in question 1.
5. (Extra) Derive second-order conditions for constrained maximisation in the general case seen in question 1.